

Therefore

$$\frac{dV}{dt} = - \frac{B^2}{m} \frac{b^2}{c^2} \frac{V}{R}$$

b)

$$\begin{cases} \frac{dV}{dt} = - \frac{V}{\tau} \\ V(0) = V_0 \\ \tau \equiv \frac{mc^2 R}{B^2 b^2} \end{cases}$$

$$V(t) = V_0 e^{-t/\tau}$$

c)

$$\Delta X_{TOT} = \int_0^{\infty} V(t) dt = \left[-V_0 \tau e^{-t/\tau} \right]_0^{\infty} = V_0 \tau = \frac{V_0 mc^2 R}{B^2 b^2}$$

d)

The energy dissipated in the resistor is

$$\begin{aligned} W &= \int_0^{\infty} I^2(t) R dt = \int_0^{\infty} \frac{B^2 b^2}{c^2 R} V^2(t) dt = \\ &= \frac{B^2 b^2}{c^2 R} \left[-V_0^2 \frac{\tau}{2} e^{-2t/\tau} \right]_0^{\infty} = \frac{B^2 b^2}{c^2 R} V_0^2 \frac{\tau}{2} = \frac{1}{2} m V_0^2 = K \end{aligned}$$

Energy is conserved ✓