



Faraday's law $\mathcal{E} = \oint \vec{E} \cdot d\vec{e} = -\frac{1}{C} \frac{\partial \Phi_B}{\partial t} = -\frac{1}{C} \frac{\partial}{\partial t} \int_S \vec{B} \cdot d\vec{a} \quad (1)$

• Ohm's law: $\mathcal{E} = I_{\text{ind}} R \quad (2)$

• $\Phi_B = \int_S \vec{B} \cdot d\vec{a} = B \int_S da = B z w \quad (3)$

$\vec{B} = B \hat{y}$
 $d\vec{a} = da \hat{y}$
 $\frac{\partial \Phi_B}{\partial t} = B w \frac{dz}{dt} = B w v(t) < 0$
 $v(t) < 0$

As the loop falls the magnetic flux decreases

• Substitute (2) + (3) in (1):

$$I_{\text{ind}} = -\frac{1}{R_C} B w v(t) > 0$$

The induced current flows counterclockwise, increasing the magnetic flux

• The force on the loop is:

$$\vec{F} = \vec{F}_{\text{ind}} + \vec{F}_g = m\vec{a}$$