

Therefore

$$\frac{dv}{dt} = - \frac{B^2 b^2}{m c^2} \frac{v}{R}$$

b)

$$\begin{cases} \frac{dv}{dt} = - \frac{v}{\tau} \\ v(0) = v_0 \\ \tau \equiv \frac{mc^2 R}{B^2 b^2} \end{cases}$$

$$v(t) = v_0 e^{-t/\tau}$$

c)

$$\Delta x_{TOT} = \int_0^{\infty} v(t) dt = \left[ -v_0 \tau e^{-t/\tau} \right]_0^{\infty} = v_0 \tau = \frac{v_0 mc^2 R}{B^2 b^2}$$

d) The energy dissipated in the resistor is

$$\begin{aligned} W &= \int_0^{\infty} I^2(t) R dt = \int_0^{\infty} \frac{B^2 b^2}{c^2 R} v^2(t) dt = \\ &= \frac{B^2 b^2}{c^2 R} \left[ -v_0^2 \frac{\tau}{2} e^{-2t/\tau} \right]_0^{\infty} = \frac{B^2 b^2}{c^2 R} v_0^2 \frac{\tau}{2} = \frac{1}{2} m v_0^2 = K \end{aligned}$$

Energy is conserved ✓