

# Jason Gross' Wishlist for Coq

POPL 2014 — Coq Users Meeting

# 1 Higher Inductive Types

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```
Inductive Interval :=  
| zero : Interval  
| one   : Interval  
| seg   : zero = one.
```

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Higher inductive types are useful for:

- Homotopy type theory (making basic spaces)
- Quotient types
- Formalizing version control systems (according to Dan Licata<sup>1</sup>)
- Proving functional extensionality

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<sup>1</sup>“Git as a HIT”,

<http://dlicata.web.wesleyan.edu/pubs/l13git/git.pdf>

# Higher Inductive Types

## Proving functional extensionality

```

Definition functional_extensionality A B f g
  (H :  $\forall x, f\ x = g\ x$ )  $\rightarrow f = g$ 
:= f_equal
  ( $\lambda i\ x \Rightarrow$ 
    match i return B with
    | zero  $\Rightarrow f\ x$ 
    | one   $\Rightarrow g\ x$ 
    | seg   $\Rightarrow H\ x$ 
  end)
seg.

```

# Higher Inductive Types

Proving functional extensionality

```

:= match seg in (_ = y)
  return ((λ x ⇒ f x)
          = (λ x ⇒ match y with
                    | zero ⇒ f x
                    | one  ⇒ g x
                    | seg  ⇒ H x
                    end))

with
  | eq_refl => eq_refl
end.

```

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Note that higher inductive types don't magically give you computational functional extensionality.

You must solve computational functional extensionality to implement computational higher inductive types.

The following features, which I want, are slated for Coq 8.5:  
 universe polymorphism parallel processing tactics in terms faster  
 sigma types and projections eta for records

The following are features that I want: a better story for  
 namespacing ([https://coq.inria.fr/bugs/show\\_bug.cgi?id=3171](https://coq.inria.fr/bugs/show_bug.cgi?id=3171))  
 irrelevant fields/a type of strict hProps/Coq\* built-in CoqMT  
 judgmental eta for the unit type a search that searches the entire  
 standard library, and not just currently [Require]d files a search  
 which is up to unification, rather than up to pattern matching  
 coercions which don't care about the uniform inheritance condition  
 (see also [https://coq.inria.fr/bugs/show\\_bug.cgi?id=3115](https://coq.inria.fr/bugs/show_bug.cgi?id=3115)) built-in  
 MTac or other monadic tactic language better handling of open  
 terms in ltac, and support for recursing under binders in tactics  
 (maybe fixed with new tactic engine? see also  
[https://coq.inria.fr/bugs/show\\_bug.cgi?id=3106](https://coq.inria.fr/bugs/show_bug.cgi?id=3106) and  
[https://coq.inria.fr/bugs/show\\_bug.cgi?id=3102](https://coq.inria.fr/bugs/show_bug.cgi?id=3102)) easier use of ML  
 plugins (I don't want to have to recompile them myself)