# Homework 2: Trees and Calibration

## Instructions

Please push the .ipynb, .py, and .pdf to Github Classroom prior to the deadline. Please include your UNI as well.

Make sure to use the dataset that we provide in CourseWorks/Classroom.

There are a lot of applied questions based on the code results. Please make sure to answer them all. These are primarily to test your understanding of the results your code generate (similar to any Data Science/ML case study interviews).

```
# This is formatted as code
```

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UNI: hj2602

# The Dataset

# Description

This data set contains details of ecommerce product shipment tracking and the target variable is a binary variable reflecting the fact whether the product reached on time or not.

```
In [1]:
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
```

```
import seaborn as sns
import time

In [2]:
import warnings
warnings.filterwarnings('ignore', category=DeprecationWarning)
```

# **Question 1: Decision Trees**

#### 1.1: Load the provided dataset

```
In [3]:
         df = pd.read csv("data.csv")
         df.head(
Out[3]:
            ID Warehouse_block Mode_of_Shipment Customer_care_calls Customer_rating Cost_of_the_Product Prior_purchases Product_importance
         0
                              D
                                              Flight
                                                                     4
                                                                                                        177
                                                                                                                                             lov
             2
                                              Flight
                                                                                                        216
                                                                                                                                            lov
          2
             3
                                             Flight
                                                                     2
                                                                                                        183
                              Α
                                                                                                                                            lov
                                             Flight
          3 4
                                                                                                        176
                                                                                                                                         mediun
                              С
                                                                     2
                                                                                      2
                                                                                                                          3
             5
                                              Flight
                                                                                                        184
                                                                                                                                         mediun
```

### 1.2: Are there any missing values in the dataset?

```
In [6]: ## YOUR CODE HERE
print(df.isnull().values.any())
False
```

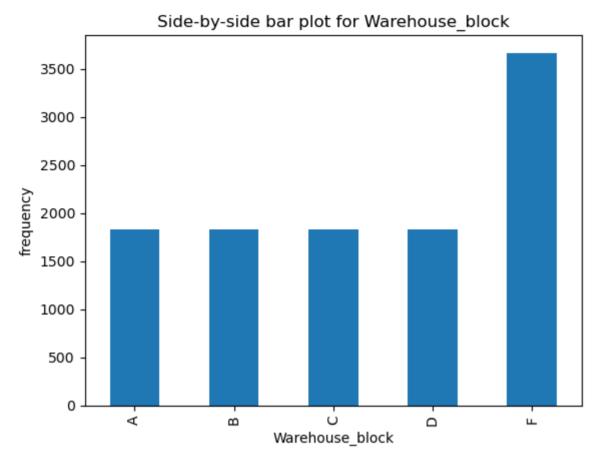
1.3: Plot side-by-side bars of class distribtuion for each category for the categorical feature and the target categories.

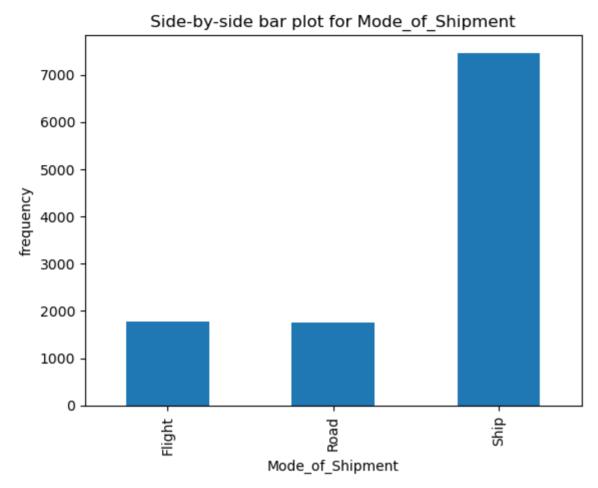
Out[8]:

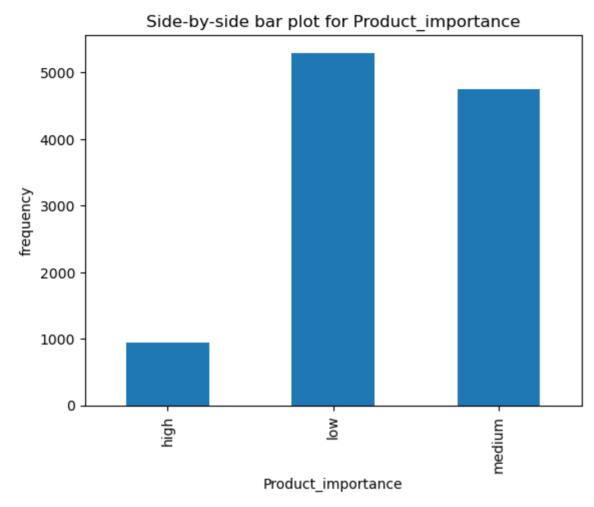
	Warehouse_block	Mode_of_Shipment	Product_importance	Gender
0	D	Flight	low	F
1	F	Flight	low	М
2	А	Flight	low	М
3	В	Flight	medium	М
4	С	Flight	medium	F
•••				•••
10994	А	Ship	medium	F
10995	В	Ship	medium	F
10996	С	Ship	low	F
10997	F	Ship	medium	М
10998	D	Ship	low	F

10999 rows × 4 columns

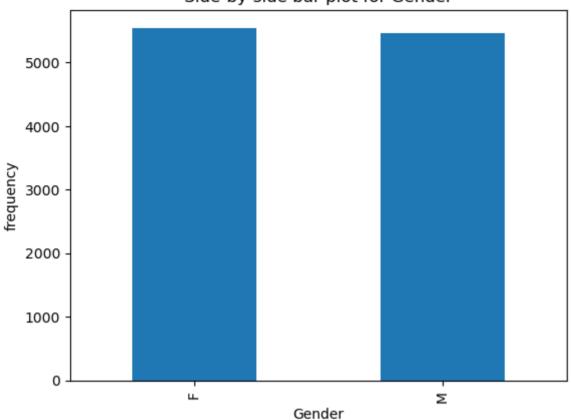
```
plt.figure()
cat_column_list = list(df_cat.columns)
for column in cat_column_list:
    df_cat[column].value_counts().sort_index().plot(kind='bar', xlabel=column, ylabel='frequency', title='Side-by-side bar plot for %s'%column)
    plt.show()
```





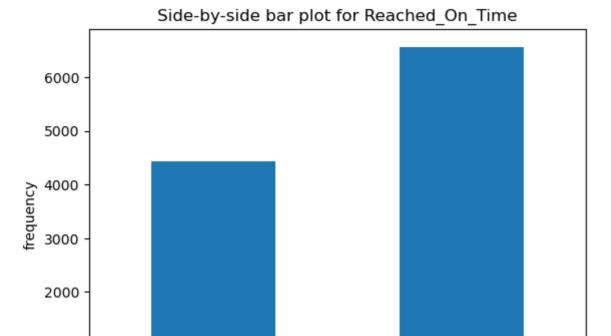


## Side-by-side bar plot for Gender



```
In [10]: plt.figure()
    df['Reached_On_Time'].value_counts().sort_index().plot(kind='bar', xlabel='Reached_On_Time', ylabel='frequency',
        title='Side-by-side bar plot for Reached_On_Time')
    plt.show()
```

1000



Reached\_On\_Time

1.4: Explain the distribution of the target variable and the dataset.

0

```
Out[12]: 1 0.596691
0 0.403309
Name: Reached_On_Time, dtype: float64
```

There is roughly 6:4 ratio of products that reached on time and products that did not reach on time. There is somewhat imbalance as within the dataset 60% has reached on time and the rest 40% has not reached on time.

1.5: Split the data into development and test datasets. Which splitting methodology did you choose and why?

Hint: Based on the distribution of the data, try to use the best splitting strategy.

```
In [16]:
         df.dtypes
Out[16]:
In [15]:
         num features = ['Customer care calls', 'Customer rating', 'Cost of the Product', 'Prior purchases',
         ohe_features = ['Warehouse_block', 'Mode_of_Shipment', 'Gender']
         te features = ['Product importance'
In [12]:
         #encoded cat df = pd.get dummies(df[ohe features + te features])
```

```
In [17]: ## YOUR CODE HERE
from sklearn.model_selection import train_test_split

X_dev, X_test, y_dev, y_test = train_test_split(df[te_features+ohe_features+num_features], df['Reached_On_Time'],

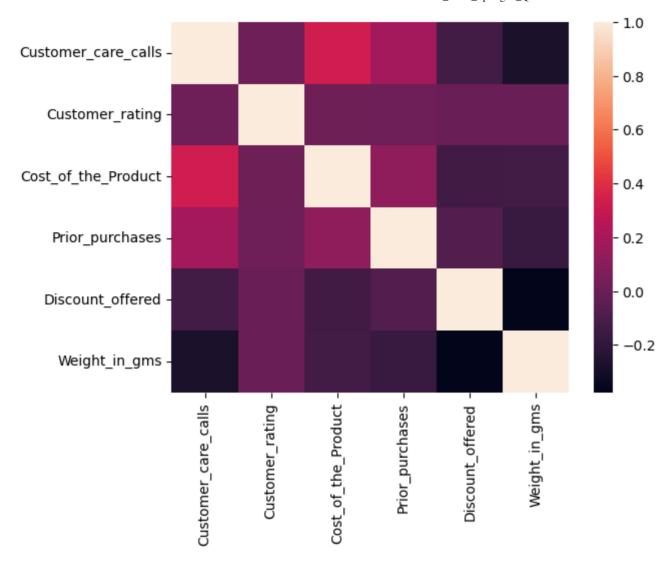
test_size=0.2, stratify=df['Reached_On_Time'], random_state=42)
```

Here we can use the stratifying splitting methodology as the dataset is imbalanced. We want to also have the development set and test set in good balance that represents the original data so the stratifying method is optimal.

1.6: Would you drop any column? Justify your reasoning.

Preprocess the data (Handle the Categorical Variable). Do we need to apply scaling? Briefly Justify

```
In [18]: corr_matrix = df[num_features+ohe_features+te_features].corr()
    plt.figure()
    sns.heatmap(corr_matrix)
    plt.show()
```



We don't want to drop any columns as the features do not have much correlation to each other. And yes we have to apply scaling for the categorical variables and the numerical variables as below.

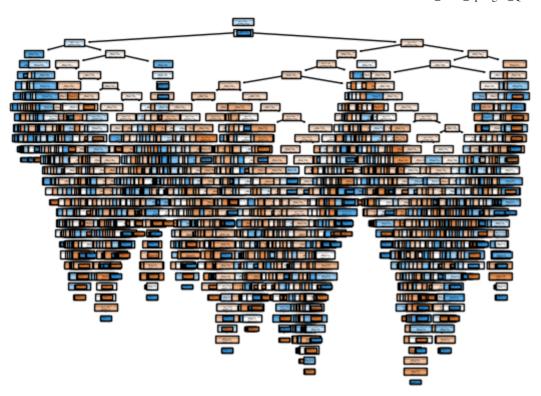
```
In [19]: ## YOUR CODE HERE
#pip install category_encoders
from sklearn.compose import make_column_transformer
```

1.7: Fit a Decision Tree on the development data until all leaves are pure. What is the performance of the tree on the development set and test set? Evaluate test and train accuracy on F-1 score and accuracy.

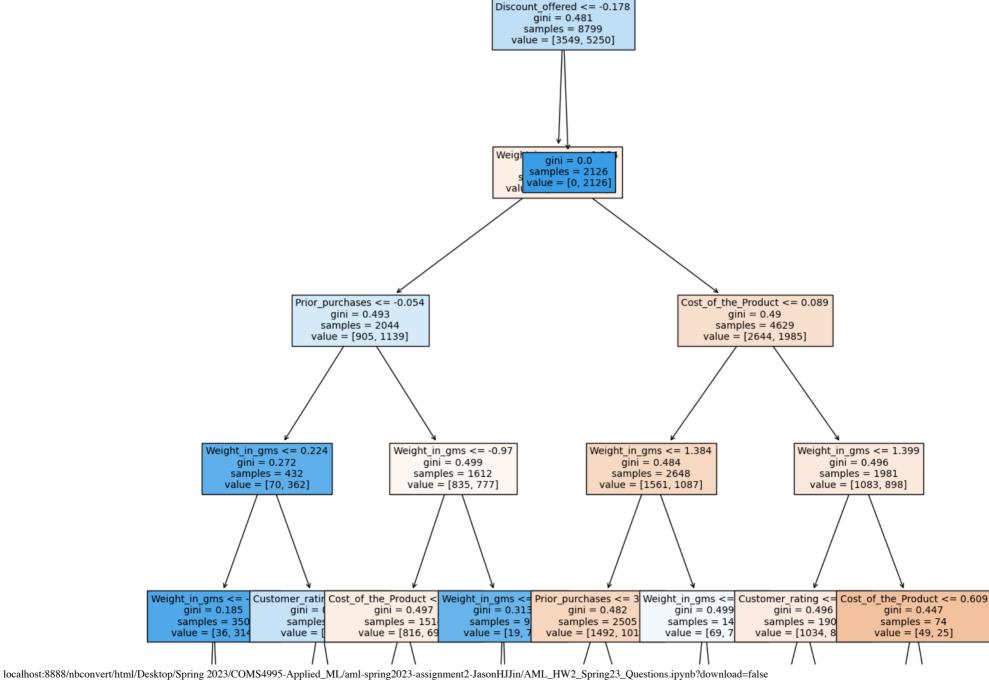
```
In [21]: ## YOUR CODE HERE
          rom sklearn.pipeline import make pipeline
          rom sklearn.model selection import GridSearchCV
          rom sklearn.tree import DecisionTreeClassifier, plot tree
         dtc = DecisionTreeClassifier(random state=0)
         pipe = make pipeline(preprocess, GridSearchCV(dtc
                                                       param grid={},
                                                       return train score="rue")
         pipe.fit(X dev, y dev)
         grid search results = pipe.named steps['gridsearchev']
         print(f"Best train score: ", grid search results.best score )
         print(f"Best train alpha: ", grid search results.best params )
         print(f"Test score:", pipe.score(X test, y test))
In [22]:
              sklearn.metrics import accuracy score, f1 score
         y pred = pipe.predict(X test)
```

```
print(f"Test accuracy: ",
                          accuracy score(y test, y pred))
print
                          f1 score(y test, y pred)
```

```
In [23]: ## YOUR CODE HERE
         best tree = grid search results.best estimator
         ohe feature names = preprocess.named transformers ['onehotencoder'].get_feature_names()
         te feature names = preprocess.named transformers ['targetencoder'].get feature names()
         feature names = num features + ohe feature names.tolist() + te feature names
         visual tree = plot tree(best tree, feature names=feature names, filled="rue)
         plt.show()
```



#### 1.8: Visualize the trained tree until the max\_depth 8.



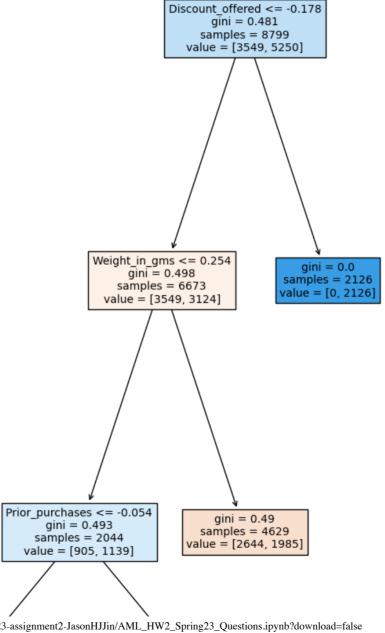
1.9: Prune the tree using one of the techniques discussed in class and evaluate the performance.

Print the optimal value of the tuned parameter.

```
Best train score: 0.6875789446483023

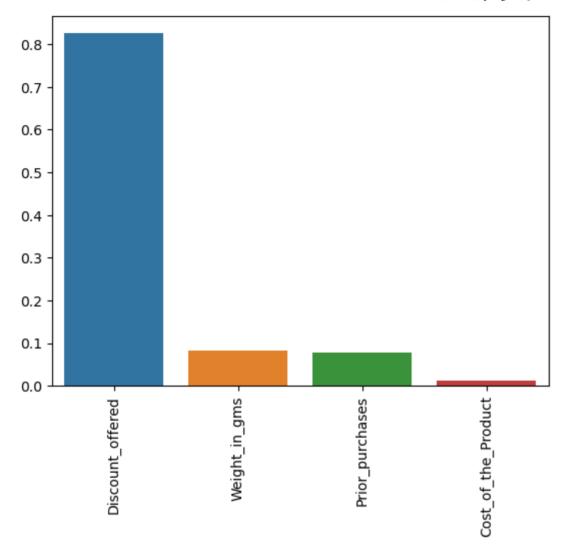
Best train alpha: {'ccp_alpha': 0.001}

Test score: 0.67772727272727
```



1.10: List the top 3 most important features for this trained tree? How would you justify these features being the most important?

```
In [27]: ## YOUR CODE HERE
         importance = best tree.feature importances
         indices = importance.argsort()[::-1]
         top 3 = indices[:3]
         print("Top 3 most important features:")
          or i in top 3:
             print(f"{feature names[i]}: {importance[i]}")
In [28]:
         feat imps = zip(feature names, best tree.feature importances )
         feats, imps = zip(*(sorted(list(filter(lambda x: x[1] != 0, feat imps)), key=lambda x:x[1], reverse=True)))
         ax = sns.barplot(list(feats), list(imps))
         ax.tick params(axis='x', rotation=90)
```



# **Question 2: Random Forests**

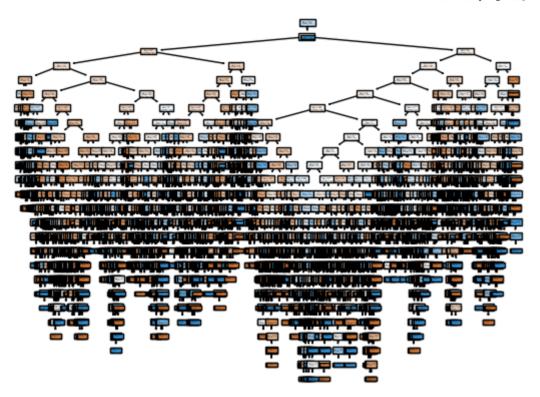
2.1: Train a Random Forest model on the development dataset using RandomForestClassifier class in sklearn. Use the default parameters. Evaluate the performance of the model on test dataset. Use accuracy and F1 score to evaluate. Does this perform better than Decision Tree on the test dataset (compare to results in Q 1.7)?

```
In [29]:
         ## YOUR CODE HERE
          rom sklearn.ensemble import RandomForestClassifier
         rfc = RandomForestClassifier(random state=0)
         param grid = {}
         pipe = make pipeline(preprocess, GridSearchCV(rfc
                                                       param grid = param grid
                                                       return train score="rue")
         pipe.fit(X dev, y dev)
         grid search results = pipe.named steps['gridsearchcv']
         print(f"Best train score: ", grid search results.best score )
         print(f"Best train alpha: ", grid search results.best params )
         print(f"Test score:", pipe.score(X test, y test))
In [32]:
         y pred = pipe.predict(X test)
         print(f"Test accuracy: ", accuracy score(y test, y pred))
         print(f"Test f-1 score: ", f1 score(y test, y pred)
```

Yes the model performs slightly better than Decision Tree model

2.2: Do all trees in the trained random forest model have pure leaves? How would you verify that all trees have pure leaves? Print the score (mean accuracy) values of your choosen method

```
In [33]: ## YOUR CODE HERE
draw_tree = plot_tree(grid_search_results.best_estimator_.estimators_[0], filled=True)
plt.show()
```



While it may require some additional time and effort to fully draw out the tree, it is ultimately the most reliable method for verifying the values at the terminal nodes and ensuring that all leaves are pure.

2.3: Assume you want to improve the performance of this model. Also, assume that you had to pick two hyperparameters that you could tune to improve its performance. Which hyperparameters would you choose and why?

# YOUR SOLUTION HERE

n\_estimators to help with the model's variance and improve its accuracy and max\_depth to find the right balance between bias and variance.

2.4: Now, assume you had to choose up to 5 different values (each) for these two hyperparameters. How would you choose these values that could potentially give you a performance lift?

```
Best train score: 0.6735996046307303

Best train alpha: {'max_depth': 10, 'n_estimators': 800}

Test score: 0.6740909090909091
```

2.5: Perform model selection using the chosen values for the hyperparameters. Use out-of-bag (OOB) error for finding the optimal hyperparameters. Report on the optimal hyperparameters. Estimate the performance of the optimal model (model trained with optimal hyperparameters) on train and test dataset? Has the performance improved over your plain-vanilla random forest model trained in Q2.1?

```
In [43]: ## YOUR CODE HERE

rfc = RandomForestClassifier(random_state=42, oob_score=True)
param_grid = {
        'n_estimators':[800],
        'max_depth':[10]
}
pipe = make_pipeline(preprocess, GridSearchCV(rfc,
```

```
Best train score: 0.6735996046307303

Best train alpha: {'max_depth': 10, 'n_estimators': 800}

OOB score: 0.6783725423343562

Test score: 0.6740909090909091
```

2.6: Can you find the top 3 most important features from the model trained in Q2.5? How do these features compare to the important features that you found from Q1.10? If they differ, which feature set makes more sense?

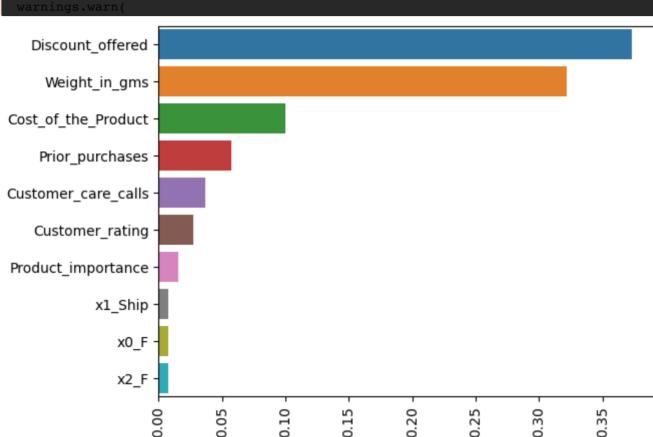
```
In [44]:
    ## YOUR CODE HERE
    best_trees = grid_search_results.best_estimator_
    importance = best_trees.feature_importances_
    indices = importance.argsort()[::-1]
    top_3 = indices[:3]
    print("Top 3 most important features:")
    ior i in top_3:
        print(f"{feature_names[i]}: {importance[i]}")

Top 3 most important features:
    Discount_offered: 0.3729356201082552
    Weight in gms: 0.32210718273031186
    cost of the Product: 0.0994972425536031

In [47]:
    rf = grid_search_results.best_estimator_
    feat imps = zip feature names_rf.feature importances_)
```

```
feats, imps = zip(*(sorted(list(filter(lambda x: x[1] != 0, feat_imps)), key=lambda x:x[1], reverse=True)))
ax = sns.barplot(list(imps[:10]), list(feats[:10]))
ax.tick_params(axis='x', rotation=90)
```

Users/jasonjin/opt/anaconda3/lib/python3.9/site-packages/seaborn/\_decorators.py:36: FutureWarning: Pass the following variables as keyword args: x, y. From version 0.12, the only valid positional argument will be `data`, and passing other arguments without an explicit keyword will result in an error or misinterpretation.



# **Question 3: Gradient Boosted Trees**

3.1: Choose three hyperparameters to tune HistGradientBoostingClassifier on the development dataset using 5-fold cross validation. For each hyperparameter, give it 3 potential values. Report on the time taken to do model selection for the model. Also,

report the performance of the test dataset from the optimal models.

```
In [48]:
         ## YOUR CODE HERE
           som sklearn.ensemble import HistGradientBoostingClassifier
         param grid = {
         hbgc = HistGradientBoostingClassifier(
         pipe = make pipeline(preprocess, GridSearchCV(hbgc
                                                       param grid=param grid,
                                                       return train score=True,
                                                       cv=5,
         pipe.fit(X dev, y dev)
         grid search results = pipe.named steps['gridsearchev']
         print(f"Best train score: ", grid search results.best score )
         print(f"Best train alpha: ", grid search results.best params )
         print(f"Test Score: ", pipe.score(X test, y test))
```

#### 3.2: Repeat 3.1 for XGBoost.

**Note**: For XGBoost, you **DO NOT NEED** to choose the same hyperparameters as HistGradientBoostingClassifier.

```
In [29]: #pip install xgboost
```

```
In [49]: ## YOUR CODE HERE
              xgboost import XGBClassifier
         pipe = make pipeline
             preprocess
             GridSearchCV
                 XGBClassifier(random state=42),
                 param grid=
                 cv=5,
                 return train score=True
         pipe.fit(X dev, y dev)
         grid search results = pipe.named steps['gridsearchov']
         print('Optimal hyperparameters:', grid search results.best params )
         print('Time taken:', grid search results.refit time )
         test score = pipe.score(X test, y test)
         print('Test score:', test_score)
```

```
Optimal hyperparameters: {'gamma': 0, 'learning_rate': 0.01, 'max_depth': 3, 'n_estimators': 100}
Time taken: 0.14075922966003418
Test score: 0.67727272727272
```

3.3: Compare the results on the test dataset of XGBoost and HistGradientBoostingClassifier. Which model do you prefer and why?

## YOUR CODE HERE

The XGBoost model has achieved a higher test score than the HistGradientBoostingClassifier model, which suggests that it may have better predictive accuracy on new data. Additionally, XGBoost is known for its scalability, which can result in faster performance of the boosting algorithm when dealing with large datasets.

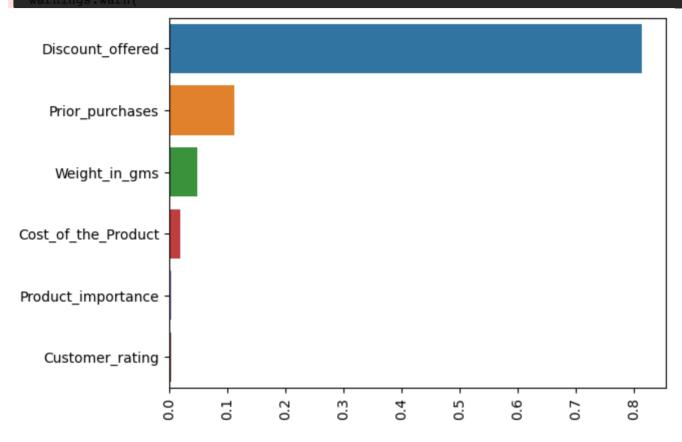
3.4: Can you list the top 3 important features from the trained XGBoost model? How do they differ from the features found from Random Forest and Decision Tree?

```
In [50]: ## YOUR CODE HERE
best_trees_xbg = grid_search_results.best_estimator_
importance = best_trees_xbg.feature_importances_
indices = importance.argsort()[::-1]
top_3 = indices[:3]
print("Top 3 most important features:")
for i in top_3:
    print(f"(feature_names(i)): (importance(i))")

Top 3 most important features:
Discount_offered: 0.8135257959365845
Prior_purchases: 0.11220099031925201
Weight_in_gms: 0.048295456916093826

In [51]: feat_imps = zip(feature_names, best_trees_xbg.feature_importances_)
feats, imps = zip(*(sorted(list filter(lambds x: x[1] != 0, feat_imps)), key=lambda x:x[1], reverse=lrue)))
ax = sns.barplot(list(imps[:10]), list(feats[:10]))
ax.tick_params(axis='x', rotation=00)
```

/Users/jasonjin/opt/anaconda3/lib/python3.9/site-packages/seaborn/\_decorators.py:36: FutureWarning: Pass the followin variables as keyword args: x, y. From version 0.12, the only valid positional argument will be `data`, and passing ot er arguments without an explicit keyword will result in an error or misinterpretation.



The top 3 important features from the trained models are the following:

XGBoost: Discount\_offered, Prior\_purchases, Weight\_in\_gms

 $Random\ Forest:\ Discount\_offered,\ Weight\_in\_gms,\ Cost\_of\_the\_Product$ 

Decision Tree: Discount\_offered, Weight\_in\_gms, Prior\_purchases

3.5: Can you choose the top 5 features (as given by feature importances from XGBoost) and repeat Q3.2? Does this model perform better than the one trained in Q3.2? Why or why not is the performance better?

```
In [52]: ## YOUR CODE HERE
         best trees xbg = grid search results.best estimator
         importance = best trees xbg.feature importances
         indices = importance.argsort()[::-1]
         top 5 = indices[:5]
          or i in top 5:
             print(f"{feature names[i]}")
In [53]: te_features_top = ['Product_importance']
         num features top = ['Discount offered', 'Prior purchases', 'Weight_in_gms', 'Cost_of_the_Product']
         preprocess = make column transformer
              (StandardScaler(), num features top),
              (TargetEncoder(handle_unknown='ignore'), te_features_top)
In [54]: pipe = make_pipeline
             preprocess
             GridSearchCV
                 XGBClassifier(random_state=42),
                 param grid=
                 cv=5,
```

```
return_train_score=True
)

# Fit the pipeline on the development dataset
pipe.fit(X_dev, y_dev)

# Get the grid search results
grid_search_results = pipe.named_steps['gridsearchev']

# Print the optimal hyperparameters
print('Optimal hyperparameters:', grid_search_results.best_params_)

# Print the time taken to do model selection
print('Time taken:', grid_search_results.refit_time_)

# Evaluate the performance of the pipeline on the test dataset
test_score = pipe.score(X_test, y_test)
print('Test_score:', test_score)
```

```
Optimal hyperparameters: {'gamma': 0, 'learning_rate': 0.01, 'max_depth': 3, 'n_estimators': 100}
Time taken: 0.11275982856750488
Test score: 0.67727272727272
```

## **Question 4: Calibration**

4.1: Estimate the brier score for the HistGradientBoosting model (trained with optimal hyperparameters from Q3.1) scored on the test dataset.

```
In [55]:
## YOUR CODE HERE
from sklearn.metrics import brier_score_loss
param_grid = {
        'max_depth':[3],
        'learning_rate':[0.1],
        'min_samples_leaf':[2]
}
hbgc = HistGradientBoostingClassifier()
```

Brier score: 0.32227272727272727

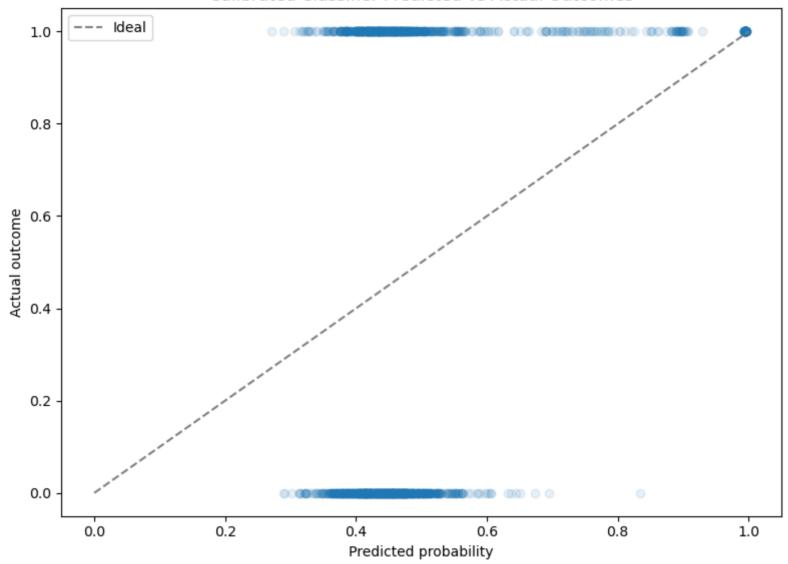
4.2: Calibrate the trained HistGradientBoosting model using Platt Scaling. Print the brier score after calibration and plot predicted v.s. actual on test datasets from the calibration method.

```
In [57]: ## YOUR CODE HERE
          rom sklearn.calibration import CalibratedClassifierCV
         platt scaled hbgc = CalibratedClassifierCV(hbgc, method='sigmoid', cv=5)
         platt_pipe = make_pipeline(preprocess, platt_scaled_hbgc)
         platt pipe.fit(X dev, y dev)
         platt y pred = platt pipe.predict(X test)
         print(f"After calibration, Brier score: {brier score loss(y test, platt y pred)}")
         plt.figure(figsize=(8, 6))
         plt.scatter(platt pipe.predict proba(X test)[:,1], y test, alpha=0.1)
```

```
plt.xlabel("Predicted probability")
plt.ylabel("Actual outcome")
plt.title("Calibrated Classifier Predicted vs Actual Outcomes")
plt.plot([0, 1], [0, 1], linestyle='--', color='gray', label='Ideal')
plt.legend()
plt.tight_layout()
plt.show()
```

After calibration, Brier score: 0.325

### Calibrated Classifier Predicted vs Actual Outcomes



4.3: Compare the brier scores from 4.1 and 4.2. Do the calibration methods help in having better predicted probabilities?

# YOUR CODE HERE

The improvement in Brier score is indicative of a reduction in the mean squared difference between the predicted probabilities and the observed outcomes. This means that the predicted probabilities have become more accurate, and the calibration methods have reduced the gap between the predicted probabilities and the actual outcomes. So brier score obtained in 4.2 using platt scaling suggests that the calibration method was particularly effective.