

NBA 5420 – Investments and Portfolio Management  
Problem Set 6 – Fixed Income

1. A nine-year bond has a yield of 10% and a modified duration of 7.194 years. If the market yield rises by 50 basis points, what is the percentage change in the bond's price?
2. Find the modified duration of a 6% coupon bond making annual coupon payments if it has three years until maturity and has a yield to maturity of 6%.
3. The following questions are from past CFA examinations:
  - a) A 6% coupon bond paying interest annually has a modified duration of 10 years, sells for \$800, and is priced at a yield to maturity of 8%. If the YTM increases to 9%, the predicted change in price, using the duration concept, decreases by:
    - i) \$76.56
    - ii) \$75.92
    - iii) \$77.67
    - iv) \$80.00
  - b) A 6% coupon bond with semiannual coupons has a convexity (in years) of 120, sells for 80% of par, and is priced at a yield to maturity of 8%. If the YTM increases to 9.5%, the predicted contribution to the percentage change in price, due to convexity, would be:
    - i) 1.08%
    - ii) 1.35%
    - iii) 2.48%
    - iv) 7.35%
  - c) When interest rates decline, the duration of a 30-year bond selling at a premium:
    - i) increases.
    - ii) decreases.
    - iii) remains the same.
    - iv) increases at first, then declines.

d) Which bond has the longest duration?

- i) 8-year maturity, 6% coupon.
- ii) 8-year maturity, 11% coupon.
- iii) 15-year maturity, 6% coupon.
- iv) 15-year maturity, 11% coupon.

4. Assume the following actual and expected interest rates.

Actual Market Rates	Expected One-Year Rates
$r_{0,1} = 4\%$	
$r_{0,2} = 4\frac{1}{2}\%$	$Er_{1,2} = ?$
$r_{0,3} = ?$	$Er_{2,3} = 5\%$
$r_{0,4} = 5\%$	$Er_{3,4} = ?$

Assuming that all the simplifying assumptions of the expectations theory of the term structure hold, find the actual market three-year rate ( $r_{0,3}$ ) and the expected one-year rate for next year ( $Er_{1,2}$ ) and three years from now ( $Er_{3,4}$ ).

5. According to the liquidity-preference theory, what can be said about the implied future (forward) one-year rate two years from today that can be calculated from the term structure?

- a) It will be higher than the market-expected future one-year rate.
- b) It will be lower than the market-expected future one-year rate
- c) It will be the same as the market-expected future one-year rate.
- d) The answer cannot be determined from the information given.

6. Descending yield curves are likely to be characteristic of periods when expectations are that future interest rates

- a) will remain high.
- b) will remain low.
- c) will rise.
- d) will fall.