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CS540

HW4

## Question 1

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1.

If  $h(B) \leq 1/2$  it will be considered admissible, because the distance between B and G is  $1/2$  and an admissible heuristic never over-estimates.

2.

a. Enqueue the start node A.

Dequeue A from OPEN and add to CLOSE

Get successors of A: B and C1

Add B and C1 to OPEN

End states:

OPEN: B, C1

$h(B) = 100m$ ,  $g(B) = 1/2$ ,  $f(B) = 100 + 1/2$

$h(C1) = 0$ ,  $g(C1) = 1$ ,  $f(C1) = 1$

Back Pointer B  $\rightarrow$  A and C1  $\rightarrow$  A

b. Dequeue C1 from OPEN

Add C1 to CLOSE

get successors of C1: C2

add C2 to OPEN

end states:

OPEN: C2 B

CLOSE: A, C1

$h(C2) = 0$ ,  $g(C2) = 1 + 1/2$ ,  $f(C2) = 1 + 1/2$

Back pointer: C2  $\rightarrow$  C1

c. Dequeue C2 from OPEN

Add C2 to CLOSE

get successors of C2: C3

add C3 to OPEN

end states:

OPEN: C3 B

CLOSE: A, C1, C2

$h(C3) = 0$ ,  $g(C3)=1+3/4$ ,  $f(C2) = 1+3/4$

Back Pointer: C3->C2

d. Dequeue C3 from OPEN

Add C3 to CLOSE

get successors of C3: C4

add C4 to OPEN

end states:

OPEN: C4 B

CLOSE: A, C1, C2, C3

$h(C4) = 0$ ,  $g(C4)=1+7/8$ ,  $f(C4) = 1+7/8$

Back Pointer: C4->C3

e. Dequeue C4 from OPEN

Add C4 to CLOSE

get successors of C4: C5

add C5 to OPEN

end states:

OPEN: C5 B

CLOSE: A, C1, C2, C3, C4

$h(C5) = 0$ ,  $g(C5)=1+15/16$ ,  $f(C6) = 1+15/16$

Back Pointer: C5->C4

**3.**

limit of  $f(C_i)$  when  $i$  approaches infinity equals  $1 + 1/2 + 1/4 + 1/8 + \dots = (1/2)/(1 - 1/2) + 1 = 2$

#### 4.

In a heuristic search, the search will only go through the point with the lowest  $h$  value in the OPEN list. Because 100 is always larger than  $1/2$ ,  $1/4$ ,  $1/8$ , etc, the search will never search any successors of  $B$ , where contains goal  $G$ , but only go through the branch contains  $C_1$ ,  $C_2$ ,  $C_3$ .... So it will never reach the goal  $G$ .

#### 5.

From the question 3 we've got  $f(C_i)$  will be 2 if  $i$  approaches infinity. So if we would like to search the successors of  $B$ , we need  $f(B) < 2$ . So  $h(B) < 2 - g(B)$ ,  $h(B) < 3/2$

Also to make it inadmissible, we need to have  $h(B) < 1/2$ , so  $1/2 < h(B) < 3/2$

#### 6.

From 5, we observe we can still get to  $G$  though  $h(B)$  is not admissible. So it is sufficient but not necessary.

## Question 2

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a. Current Point:  $x=2$ ,  $f(x) = 2$

Temperature:  $2(0.9)^1 = 1.8$

Random number is 3,  $f(3) = 1$ ;

$p = e^{-(|2-1|/1.8)} = 0.574$

Random successor is not better than current state  $x=2$ .

$p > z$ , so the  $x=3$  still accepted

b. CP:  $x = 3$ ,  $f(x) = 1$

T:  $2(0.9)^2 = 1.62$

$y = 1$ ,  $f(y) = 3$

// $p = e^{-(2/1.62)} = 0.291$

Probability of moving to successor is actually 1, because  $f(y) > f(x)$

c. CP:  $x = 1$ ,  $f(x) = 3$

T:  $2(0.9)^3 = 1.458$

$y = 1$ ,  $f(1)=3$

It is not better than current (equal)

$$p = e^{(0)} = 1$$

$1 > z$ , we will not choose it as successor. But actually this is the same state as current state.

d. CP:  $x = 1, f(x)=3$

$$T: 2(0.9)^4=1.312$$

$$y=4, f(4) = 0$$

$$p=e^{(-3/1.312)}=0.102$$

$p < z$ , so it will not be accepted.

e. CP:  $x=1, f(x) = 3$

$$T: 2(0.9)^5=1.181$$

$$y=2, f(y) = 2;$$

$$p = e^{(-1/1.181)} = 0.429$$

$p > z$ , successor will be accepted

f. CP:  $x = 2, f(x) = 2$

$$T: 2(0.9)^6 = 1.068$$

$$y=3, f(y) = 1$$

$$p = e^{(-1/1.068)} = 0.392$$

$p < z$ , it will not be accepted

g. CP:  $x=2, f(x) = 2$

$$T: 2(0.9)^7=0.957$$

$$y=4, f(y) = 0$$

$$p = e^{(-2/0.957)} = 0.124$$

$p < z$  it will not be accepted

h. CP:  $x= 2, f(x) =2$

$$T: 2(0.9)^8=0.861$$

$$y=3, f(y)=1$$

$$p=e^{(-1/0.861)} = 0.313$$

$p < z$ , it will not be accepted

## Question 3

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**1.**

There are  $n!$  states for  $n$  trees

**2.**

We will have  $n-1$  states for one neighborhood. According to 1, one neighborhood will cover  $(n-1)/n!$

**3.**

Using lines counter I found there are 112511 trees.

So there are 112511! States

**4.**

Starting from the office, going to every trees, and backing to office, the inspector has to travel  $n+1$  times of the distance of diameter.  $112512 \times 10 = 3 \text{ LD}$

**5.**

Similar to 4, inspector will travel 112512 times.  $112512 \times 0.01 = 1125.12 \text{ km}$

**6.**

25 mph = 40.23 kmph. Assume the inspector will work 24 hrs a day,  $24 \times 40.23 = 965.52 \text{ km}$ .

$965.52 \text{ km} < 1125.12 \text{ km}$ . So the inspector cannot finish the task even in the best situation. It is impossible to do that in one day.