```
In[*]:= ClearAll["Global`*"];
In[*]:= $Version
Out[*]= 12.3.0 for Mac OS X x86 (64-bit) (May 10, 2021)
In[*]:= SetDirectory[NotebookDirectory[]];
```

Crossed-polarization (CP) optical microscopy intensity calculation

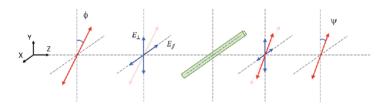
A. Input

B. Optical properties

C. Light properties after passing through a single CNC (add figure)

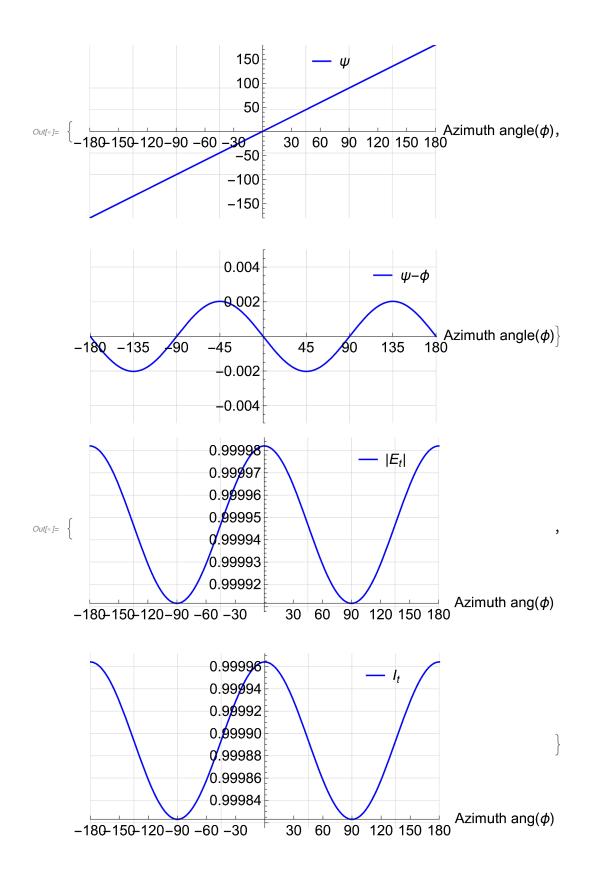
- Electric field, intensity and polarization angle as a function of the polarization angle with respect to the CNC angle

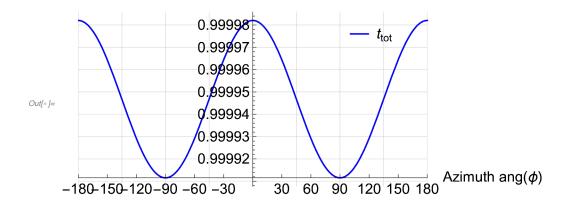
(* Supplementary Figure 8a *) Ep = E_{\parallel} , Es = E_{\perp}



```
In[•]:= (*E= ~0 *)
        \epsilon = 10^{-9};
        \theta = \epsilon (*deg*);
        (*Incident beam Ep0, Es0, Ip0, Is0*)
        Ep0[\phi_{-}] := 1 Sin[\phi * (\pi / 180)];
        Es0[\phi] := 1 Cos[\phi * (\pi / 180)];
        Ip0[\phi_{-}] := Ep0[\phi]^{2};
        Is0[\phi_{-}] := Es0[\phi]<sup>2</sup>;
         (* Output beam- Ep1, Es1, Ip1, Is1 after a single CNC *)
        Ep[\phi_{-}] := Ep0[\phi] * t123p[8]; (*[[8]] = 600nm *)
        Es[\phi] := Es0[\phi] * t123s[8]; (*[8]] = 600nm *)
        Ip[\phi_{-}] := Ep[\phi] * Conjugate[Ep[\phi]];
        Is [\phi_{-}] := Es[\phi] * Conjugate[Es[\phi]];
        (* Output beam- \psi, (\psi-\phi) (\phi dependence) *)
        \psi[\phi_{-}] := Piecewise[{}
               \left\{ \operatorname{ArcTan} \left[ \sqrt{\operatorname{Ep}[\phi] * \operatorname{Conjugate}[\operatorname{Ep}[\phi]]} \right/ \sqrt{\operatorname{Es}[\phi] * \operatorname{Conjugate}[\operatorname{Es}[\phi]]} \right] * \frac{180}{\pi} - 180, \right\}
                 \phi < -90,
               \left\{\operatorname{ArcTan}\left[\sqrt{\operatorname{Ep}[\phi]} * \operatorname{Conjugate}[\operatorname{Ep}[\phi]]\right] / - \sqrt{\operatorname{Es}[\phi]} * \operatorname{Conjugate}[\operatorname{Es}[\phi]]\right] * \frac{180}{-} + 180,
                 \phi > 90,
               \left\{\operatorname{ArcTan}\left[\sqrt{\operatorname{Ep}[\phi] * \operatorname{Conjugate}[\operatorname{Ep}[\phi]]} \middle/ \sqrt{\operatorname{Es}[\phi] * \operatorname{Conjugate}[\operatorname{Es}[\phi]]}\right] * \frac{180}{}, \phi > 0\right\},\right\}
               \left\{\operatorname{ArcTan}\left[\sqrt{\operatorname{Ep}[\phi] * \operatorname{Conjugate}[\operatorname{Ep}[\phi]]} \middle/ - \sqrt{\operatorname{Es}[\phi] * \operatorname{Conjugate}[\operatorname{Es}[\phi]]}\right] * \frac{180}{-}, \phi > -90\right\}
            \bigg\}\bigg](* \psi=\tan^{-1}[E_{\parallel}/E_{\perp}] - Equation 3 *)
        (*Output beam |Etot| and Itot*)
        \mathsf{Et}[\phi_{-}] := \sqrt{\mathsf{Ep}[\phi]} * \mathsf{Conjugate}[\mathsf{Ep}[\phi]] + \mathsf{Es}[\phi] * \mathsf{Conjugate}[\mathsf{Es}[\phi]] ;
        (* |E_{total}| = \sqrt{E_{\parallel} * E_{\parallel}^* + E_{\perp} * E_{\perp}^*} - Equation 4 *)
        It[\phi_{-}] := Et[\phi] * Conjugate[Et[\phi]];
         (*transmission coefficient*)
        tt[\phi_{-}] := Et[\phi] / 1;
```

```
In[*]:= (*check plots*)
     \{Plot[\psi[\phi], \{\phi, -180, 180\}, PlotRange \rightarrow \{\{-180, 180\}, \{-180, 180\}\}, \}
        Ticks → {Table[30 i, {i, -12, 12}], Automatic},
        GridLines \rightarrow {Table [45 i, {i, -4, 4}], {-90, -45, 45, 90}},
        PlotLegends \rightarrow Placed[{"\psi"}, {0.7, 0.9}], PlotStyle \rightarrow {Blue},
        AxesLabel \rightarrow {"Azimuth angle(\phi)", None}, ImageSize \rightarrow 500, AspectRatio \rightarrow 1 / 2,
        LabelStyle → {FontFamily → "Arial", FontSize → 15, Black}],
       Plot[\{\psi[\phi] - \phi\}, \{\phi, -180, 180\}, PlotRange \rightarrow \{\{-180, 180\}, \{-0.005, 0.005\}\},
        Ticks → {Table[45 i, {i, -12, 12}], Automatic},
        GridLines → {Table [45 i, {i, -12, 12}], Automatic},
        PlotLegends \rightarrow Placed[{"\psi-\phi"}, {0.9, 0.85}], PlotStyle \rightarrow {Blue},
        AxesLabel \rightarrow {"Azimuth angle(\phi)", None}, ImageSize \rightarrow 500, AspectRatio \rightarrow 1 / 2,
        LabelStyle → {FontFamily → "Arial", FontSize → 15, Black}]
        (* Supplementary Figure 8b *)
     }
     \{Plot[Et[\phi], \{\phi, -180, 180\}, PlotRange \rightarrow \{\{-180, 180\}, All\}, \}\}
        Ticks \rightarrow {Table[30 i, {i, -12, 12}], Automatic},
        GridLines → {Table[45 i, {i, -12, 12}], Automatic},
        PlotLegends \rightarrow Placed[{"|E<sub>t</sub>|"}, {0.84, 0.87}], PlotStyle \rightarrow {Blue},
        AxesLabel \rightarrow {" Azimuth ang(\phi)", None}, ImageSize \rightarrow 500, AspectRatio \rightarrow 1 / 2,
        LabelStyle → {FontFamily → "Arial", FontSize → 15, Black}]
        (* Supplementary Figure 8c *),
       Plot[It[\phi], \{\phi, -180, 180\}, PlotRange \rightarrow \{\{-180, 180\}, All\},
        Ticks → {Table[30 i, {i, -12, 12}], Automatic},
        GridLines → {Table[45 i, {i, -12, 12}], Automatic},
        PlotLegends \rightarrow Placed[{"I<sub>t</sub>"}, {0.84, 0.87}], PlotStyle \rightarrow {Blue},
        AxesLabel \rightarrow {" Azimuth ang(\phi)", None}, ImageSize \rightarrow 500, AspectRatio \rightarrow 1 / 2,
        LabelStyle → {FontFamily → "Arial", FontSize → 15, Black}]}
     Plot[tt[\phi], \{\phi, -180, 180\}, PlotRange \rightarrow \{\{-180, 180\}, All\},
      Ticks → {Table[30 i, {i, -12, 12}], Automatic},
      GridLines → {Table[45 i, {i, -12, 12}], Automatic},
      PlotLegends → Placed[{"t<sub>tot</sub>"}, {0.84, 0.87}], PlotStyle → {Blue},
      AxesLabel \rightarrow {" Azimuth ang(\phi)", None}, ImageSize \rightarrow 500, AspectRatio \rightarrow 1 / 2,
      LabelStyle → {FontFamily → "Arial", FontSize → 15, Black}]
```





D. 100 CNC angle generation for the five CMF organizations: crossedpolylamellate, random, helicoidal (10°), uniaxial, and biomodal.

E. Light properties after the 100 CNC organizations - Loop1 for each organization

```
n_{i}=\phi i=0; (* the initial polarization direction of the incident beam w.r.t. y-axis *)
    (*0 deg was chosen as an example - Supplementary Figure 8 *)
    \phi i = \phi i + \epsilon; (* \epsilon is a small number, 10^{-9} *)
```

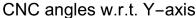
1) Cross-polylamellate

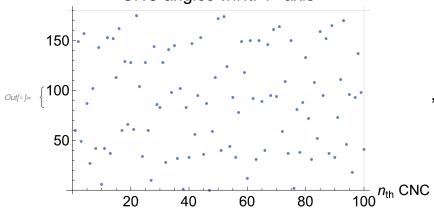
Storage

```
ln[\cdot]:= For[p = 1, p < n + 1, p++,
       \phibtn[p]] = \psiy[p]] - \phicl180Norm[p]]; (* convert axis: From y-axis to CNC normal *)
       \psires[[p]] = \psi[\phibtn[[p]]]; (* result of rotation in CNC normal axis*)
       \psi y [p + 1] = \psi res[p] + \phi cl180Norm[p];
        (* back to y-axis system*) (*F180 is for *)
       d\psi \llbracket p \rrbracket = \psi res \llbracket p \rrbracket - \phi btn \llbracket p \rrbracket; (* (\psi after - \psi before) in CNC axis *)
       \mathsf{ttot}[\![p]\!] = \mathsf{tt}[\phi \mathsf{btn}[\![p]\!]];
       Etot[p+1] = Etot[p] * ttot[p]; (* energy loss as passing through *)
       d\psi 2[p] = \psi y[p + 1] - \psi y[p];
        (* (ψafter - ψbefore) in CNC axis. How much rotation @ each CNC*)
     PI = \left( \text{Etot}[n+1] * Sin \left[ (\psi y[n+1] - \phi 1) * \frac{\pi}{180} \right] \right)^{2}; (* I = (|E_{total}| * sin \psi)^{2} - Equation 5 *)
```

Check plots and final intensity (Supplementary Figure 8e,f here)

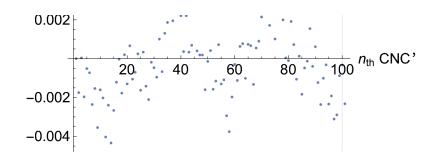
```
loge := {ListPlot[φcl180, ImageSize → 400, PlotRange → All, AxesLabel → {"nth CNC", None},
       LabelStyle → {FontFamily → "Arial", FontSize → 15, Black},
       GridLines → {\{100\}, \{180\}}, AxesOrigin → \{0, 0\},
       PlotLabel → "CNC angles w.r.t. Y-axis"] (* Supplementary Figure 8e *),
      ListPlot[ψy, ImageSize → 400, PlotRange → All,
       LabelStyle → {FontFamily → "Arial", FontSize → 15, Black},
       AxesLabel \rightarrow {"n<sub>th</sub> CNC", None}, PlotLabel \rightarrow "Pol. direction w.r.t. Y-axis",
       GridLines → {{100}, None}] (* Supplementary Figure 8f *),
      ListPlot[Etot, ImageSize → 400, PlotRange → All,
       LabelStyle → {FontFamily → "Arial", FontSize → 15, Black},
       AxesLabel \rightarrow {"nth CNC", None}, PlotLabel \rightarrow "|E<sub>total</sub>|", GridLines \rightarrow {{100}, None}],
      ListPlot[(d\psi), ImageSize \rightarrow 400, PlotRange \rightarrow All, LabelStyle \rightarrow
        {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"nth CNC", None},
       PlotLabel \rightarrow "Rotation (\psi - \psi_0)", GridLines \rightarrow {{100}, None}]}
     {ListPlot[φbtn, ImageSize → 400, LabelStyle →
        {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"n<sub>th</sub> CNC", None},
       PlotLabel → "Pol. direction w.r.t. CNC normal (before)",
       GridLines → {{100}, None}],
      ListPlot[\psi res, ImageSize → 400, LabelStyle →
        {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"n<sub>th</sub> CNC", None},
       PlotLabel → "Pol. direction w.r.t. CNC normal (after)",
       GridLines → {{100}, None}]}
    Print["E<sub>total</sub> after 100th CNC=", Etot[n + 1]]
    Print["Final intensity after the 2nd polarizer=", PI]
                  CNC angles w.r.t. Y-axis
```

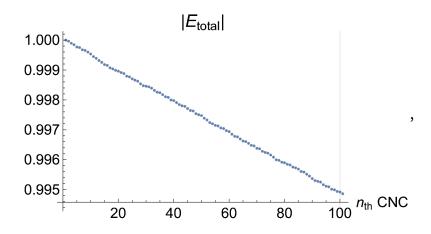


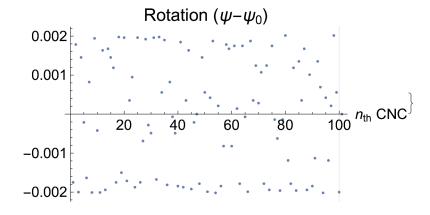


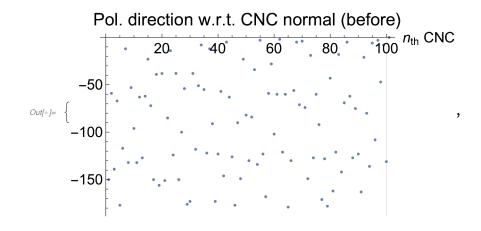
Pol. direction w.r.t. Y-axis

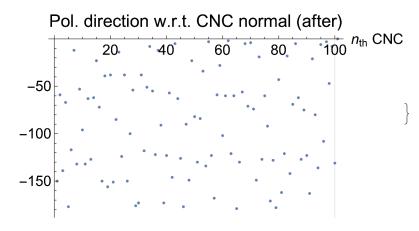












 E_{total} after 100th CNC=0.994861 + 0. i Final intensity after the 2nd polarizer=0.742347 + 0. i

Check numbers after each CNC

2) Random

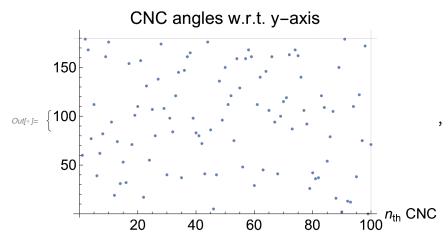
Storage

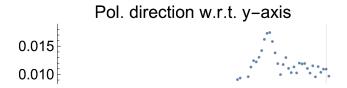
```
ln[\cdot]:= For[p = 1, p < n + 1, p++,
       \phibtn[p]] = \psiy[p]] - \phira180Norm[p]]; (* convert axis: From y-axis to CNC normal *)
       \psires[[p]] = \psi[\phibtn[[p]]]; (* result of rotation in CNC normal axis*)
       \psi y [p + 1] = \psi res [p] + \phi ra180Norm[p];
       (* back to y-axis system*) (*F180 is for *)
       d\psi[\![p]\!] = \psi res[\![p]\!] - \phi btn[\![p]\!]; (* (\psi after - \psi before) in CNC axis *)
       \mathsf{ttot}[\![p]\!] = \mathsf{tt}[\phi \mathsf{btn}[\![p]\!]];
       Etot[p+1] = Etot[p] * ttot[p]; (* energy loss as passing through *)
       d\psi 2[[p]] = \psi y[[p+1]] - \psi y[[p]];
       (* (\psiafter - \psibefore) in CNC axis. How much rotation @ each CNC*)
     PI = \left( \text{Etot}[n+1] * Sin \left[ (\psi y[n+1] - \phi 1) * \frac{\pi}{180} \right] \right)^{2}; (* I = (|E_{total}| * sin \psi)^{2} - Equation 5 *)
```

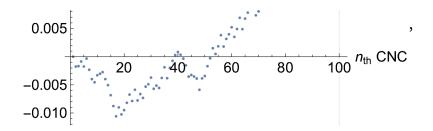
Check plots and final intensity

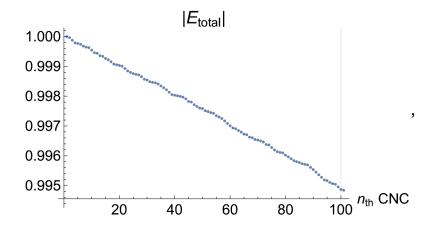
```
log_{ij} := \{ListPlot[\phi ra180, ImageSize \rightarrow 400, PlotRange \rightarrow All, AxesLabel \rightarrow \{"n_{th} CNC", None\}, \}
       LabelStyle → {FontFamily → "Arial", FontSize → 15, Black},
       GridLines → {\{100\}, \{180\}}, AxesOrigin → \{0, 0\},
       PlotLabel → "CNC angles w.r.t. y-axis"],
      ListPlot[\(\psi\)y, ImageSize \(\to \) 400, PlotRange \(\to \) All, LabelStyle \(\to \)
        {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"nth CNC", None},
       PlotLabel → "Pol. direction w.r.t. y-axis", GridLines → {{100}, None}],
      ListPlot[Etot, ImageSize → 400, PlotRange → All,
       LabelStyle → {FontFamily → "Arial", FontSize → 15, Black},
       AxesLabel → {"nth CNC", None}, PlotLabel → "|Etotal|", GridLines → {{100}, None}],
      ListPlot[(d\psi), ImageSize \rightarrow 400, PlotRange \rightarrow All, LabelStyle \rightarrow
        {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"n<sub>th</sub> CNC", None},
       PlotLabel → "Pol. rotation", GridLines → {{100}, None}]}
     {ListPlot[$\phi$btn, ImageSize $\to 400, LabelStyle $\to$
        {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"nth CNC", None},
       PlotLabel → "Pol. direction w.r.t. CNC normal (before)",
       GridLines \rightarrow {{100}, None}],
      ListPlot[\psi res, ImageSize → 400, LabelStyle →
        {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"nth CNC", None},
       PlotLabel → "Pol. direction w.r.t. CNC normal (after)",
       GridLines → {{100}, None}]}
```

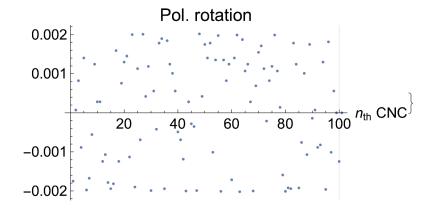
Print["E_{total} after 100th CNC=", Etot[n + 1]] Print["Final intensity after the 2nd polarizer=", PI]

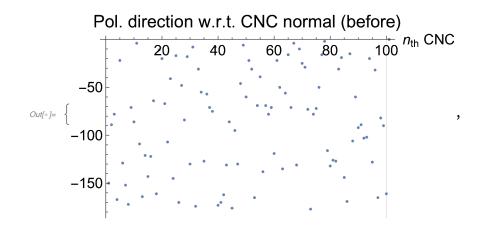


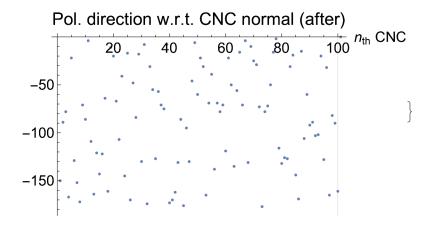












 E_{total} after 100th CNC=0.994844 + 0. i Final intensity after the 2nd polarizer=0.742141 + 0. i

Check numbers after each CNC

3) Helicoidal

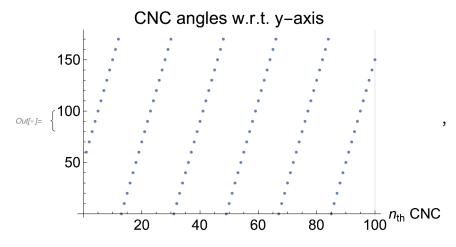
Storage

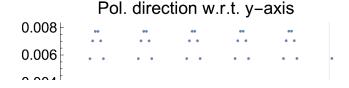
```
ln[\cdot]:= For[p = 1, p < n + 1, p++,
       \phibtn[p]] = \psiy[p]] - \phihe180Norm[p]]; (* convert axis: From y-axis to CNC normal *)
       \psires[[p]] = \psi[\phibtn[[p]]]; (* result of rotation in CNC normal axis*)
       \psi y [p + 1] = \psi res [p] + \phi he180Norm[p];
       (* back to y-axis system*) (*F180 is for *)
       d\psi[\![p]\!] = \psi res[\![p]\!] - \phi btn[\![p]\!]; (* (\psi after - \psi before) in CNC axis *)
       \mathsf{ttot}[\![p]\!] = \mathsf{tt}[\phi \mathsf{btn}[\![p]\!]];
       Etot[p+1] = Etot[p] * ttot[p]; (* energy loss as passing through *)
       d\psi 2[[p]] = \psi y[[p+1]] - \psi y[[p]];
       (* (\psiafter - \psibefore) in CNC axis. How much rotation @ each CNC*)
     PI = \left( \text{Etot}[n+1] * Sin \left[ (\psi y[n+1] - \phi 1) * \frac{\pi}{180} \right] \right)^{2}; (* I = (|E_{total}| * sin \psi)^{2} - Equation 5 *)
```

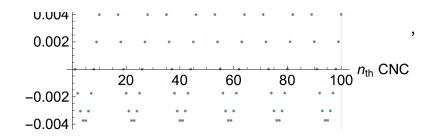
Check plots and final intensity

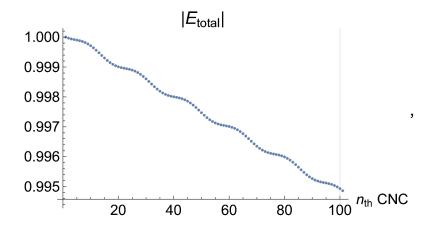
```
log_{ij} := \{ListPlot[\phi he180, ImageSize \rightarrow 400, PlotRange \rightarrow All, AxesLabel \rightarrow \{"n_{th} CNC", None\}, \}
       LabelStyle → {FontFamily → "Arial", FontSize → 15, Black},
       GridLines → {\{100\}, \{180\}}, AxesOrigin → \{0, 0\},
       PlotLabel → "CNC angles w.r.t. y-axis"],
      ListPlot[\(\psi\)y, ImageSize \(\to \) 400, PlotRange \(\to \) All, LabelStyle \(\to \)
        {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"nth CNC", None},
       PlotLabel → "Pol. direction w.r.t. y-axis", GridLines → {{100}, None}],
      ListPlot[Etot, ImageSize → 400, PlotRange → All,
       LabelStyle → {FontFamily → "Arial", FontSize → 15, Black},
       AxesLabel → {"nth CNC", None}, PlotLabel → "|Etotal|", GridLines → {{100}, None}],
      ListPlot[(d\psi), ImageSize \rightarrow 400, PlotRange \rightarrow All, LabelStyle \rightarrow
        {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"n<sub>th</sub> CNC", None},
       PlotLabel → "Pol. rotation", GridLines → {{100}, None}]}
     {ListPlot[$\phi$btn, ImageSize $\to 400, LabelStyle $\to$
        {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"nth CNC", None},
       PlotLabel → "Pol. direction w.r.t. CNC normal (before)",
       GridLines \rightarrow {{100}, None}],
      ListPlot[\psi res, ImageSize → 400, LabelStyle →
        {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"nth CNC", None},
       PlotLabel → "Pol. direction w.r.t. CNC normal (after)",
       GridLines → {{100}, None}]}
    Print["E<sub>total</sub> after 100th CNC=", Etot[n + 1]]
```

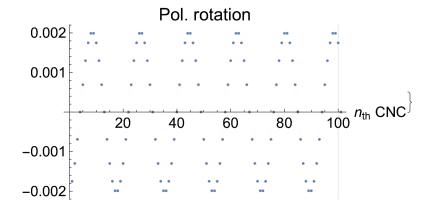
Print["Final intensity after the 2nd polarizer=", PI]

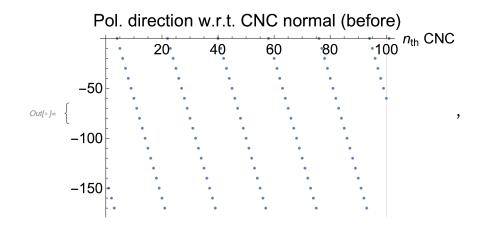


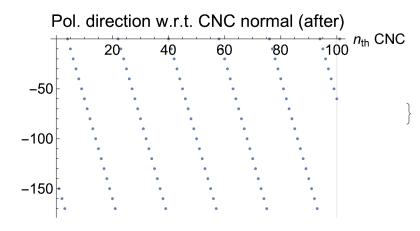












 E_{total} after 100th CNC=0.994863 + 0. i Final intensity after the 2nd polarizer=0.742228 + 0. i

Check numbers after each CNC

4) Uniaxial

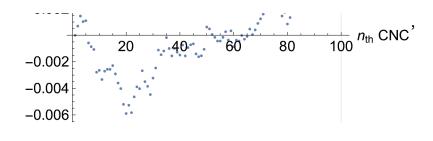
Storage

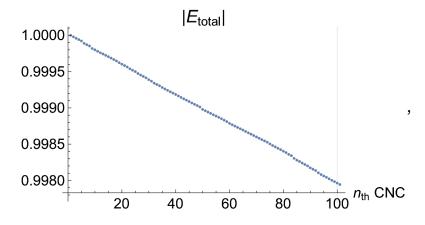
```
ln[\cdot]:= For[p = 1, p < n + 1, p++,
       \phibtn[p]] = \psiy[p]] - \phiun180Norm[p]]; (* convert axis: From y-axis to CNC normal *)
       \psires[[p]] = \psi[\phibtn[[p]]]; (* result of rotation in CNC normal axis*)
       \psi y [p + 1] = \psi res[p] + \phi un180Norm[p];
       (* back to y-axis system*) (*F180 is for *)
       d\psi[\![p]\!] = \psi res[\![p]\!] - \phi btn[\![p]\!]; (* (\psi after - \psi before) in CNC axis *)
       \mathsf{ttot}[\![p]\!] = \mathsf{tt}[\phi \mathsf{btn}[\![p]\!]];
       Etot[p+1] = Etot[p] * ttot[p]; (* energy loss as passing through *)
       d\psi 2[[p]] = \psi y[[p + 1]] - \psi y[[p]];
       (* (ψafter - ψbefore) in CNC axis. How much rotation @ each CNC*)
     ]
     PI = \left( \text{Etot}[n+1] * Sin \left[ (\psi y [n+1] - \phi 1) * \frac{\pi}{180} \right] \right)^{2}; \text{ (* } I = (|E_{total}| * sin \psi)^{2} - \text{Equation 5 *)}
```

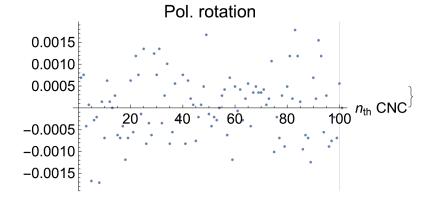
0.002

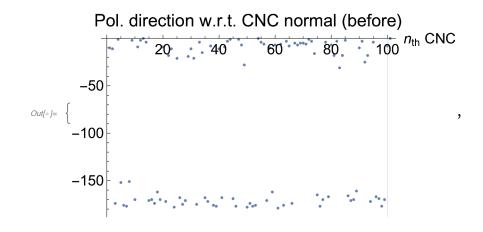
Check plots and final intensity

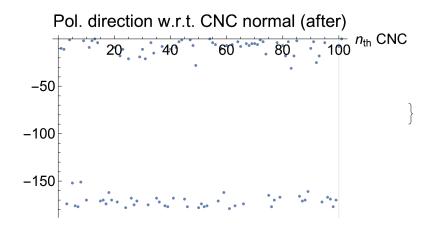
```
log_{ij} := \{ListPlot[\phiun180, ImageSize \rightarrow 400, PlotRange \rightarrow All, AxesLabel \rightarrow \{"n_{th} CNC", None\}, \}
       LabelStyle → {FontFamily → "Arial", FontSize → 15, Black},
       GridLines → {\{100\}, \{180\}}, AxesOrigin → \{0, 0\},
       PlotLabel → "CNC angles w.r.t. y-axis"],
      ListPlot[\(\psi\)y, ImageSize \(\to \) 400, PlotRange \(\to \) All, LabelStyle \(\to \)
        {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"nth CNC", None},
       PlotLabel → "Pol. direction w.r.t. y-axis", GridLines → {{100}, None}],
      ListPlot[Etot, ImageSize → 400, PlotRange → All,
       LabelStyle → {FontFamily → "Arial", FontSize → 15, Black},
       AxesLabel → {"nth CNC", None}, PlotLabel → "|Etotal|", GridLines → {{100}, None}],
      ListPlot[(d\psi), ImageSize \rightarrow 400, PlotRange \rightarrow All, LabelStyle \rightarrow
        {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"n<sub>th</sub> CNC", None},
       PlotLabel → "Pol. rotation", GridLines → {{100}, None}]}
     {ListPlot[$\phi$btn, ImageSize $\to 400, LabelStyle $\to$
        {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"nth CNC", None},
       PlotLabel → "Pol. direction w.r.t. CNC normal (before)",
       GridLines \rightarrow {{100}, None}],
      ListPlot[\psi res, ImageSize → 400, LabelStyle →
        {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"nth CNC", None},
       PlotLabel → "Pol. direction w.r.t. CNC normal (after)",
       GridLines → {{100}, None}]}
    Print["E<sub>total</sub> after 100th CNC=", Etot[n+1]]
    Print["Final intensity after the 2nd polarizer=", PI]
                  CNC angles w.r.t. v-axis
      120
      100
       40
       20
                                                      \frac{1}{100}n_{\text{th}} CNC
                  20
                           40
                                    60
                                              80
                   Pol. direction w.r.t. y-axis
       0.006
       0.004
```











 E_{total} after 100th CNC=0.997945 + 0. i Final intensity after the 2nd polarizer=0.746864 + 0. i

Check numbers after each CNC

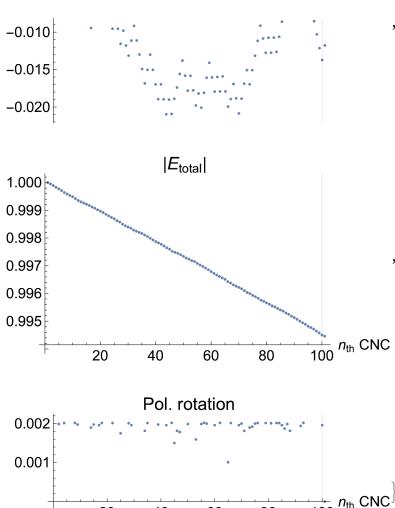
5) Bimodal

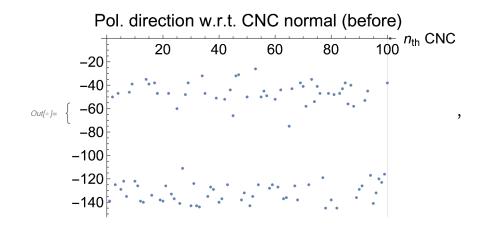
Storage

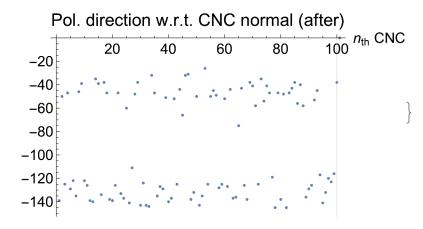
Check plots and final intensity

-0.005

```
In[*]:= {ListPlot[$\phi$bi180, ImageSize $\to 400, PlotRange $\to All, AxesLabel $\to \{\text{"nth CNC", None}\},
        LabelStyle → {FontFamily → "Arial", FontSize → 15, Black},
        GridLines → {\{100\}, \{180\}}, AxesOrigin → \{0, 0\},
        PlotLabel → "CNC angles w.r.t. y-axis"],
       ListPlot[\psiy, ImageSize \rightarrow 400, PlotRange \rightarrow All, LabelStyle \rightarrow
          {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"nth CNC", None},
        PlotLabel → "Pol. direction w.r.t. y-axis", GridLines → {{100}, None}],
       ListPlot[Etot, ImageSize → 400, PlotRange → All,
        LabelStyle → {FontFamily → "Arial", FontSize → 15, Black},
        AxesLabel → {"nth CNC", None}, PlotLabel → "|Etotal|", GridLines → {{100}, None}],
       ListPlot[(d\psi), ImageSize \rightarrow 400, PlotRange \rightarrow All, LabelStyle \rightarrow
          {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"n<sub>th</sub> CNC", None},
        PlotLabel → "Pol. rotation", GridLines → {{100}, None}]}
      {ListPlot[$\phi$btn, ImageSize $\rightarrow$ 400, LabelStyle $\rightarrow$
          {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"n<sub>th</sub> CNC", None},
        PlotLabel → "Pol. direction w.r.t. CNC normal (before)",
        GridLines \rightarrow {{100}, None}],
       ListPlot[ψres, ImageSize → 400, LabelStyle →
          {FontFamily → "Arial", FontSize → 15, Black}, AxesLabel → {"nth CNC", None},
        PlotLabel → "Pol. direction w.r.t. CNC normal (after)",
        GridLines \rightarrow {{100}, None}]}
      Print["E<sub>total</sub> after 100th CNC=", Etot[n + 1]]
      Print["Final intensity after the 2nd polarizer=", PI]
                   CNC angles w.r.t. y-axis
Out[•]= { 100
                                                        100 n<sub>th</sub> CNC
                   20
                             40
                                      60
                                               80
                    Pol. direction w.r.t. y-axis
                                                        100 n<sub>th</sub> CNC
                              40
                                       60
                                                80
```







 E_{total} after 100th CNC=0.994458 + 0. i

Final intensity after the 2nd polarizer=0.741886 + 0. i

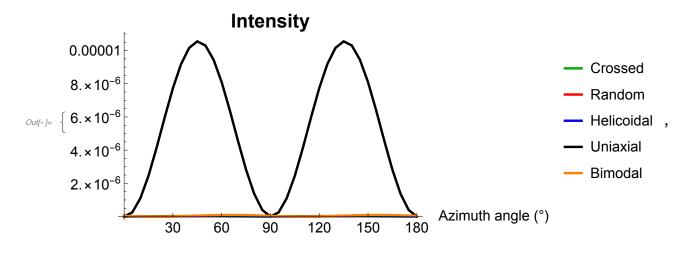
Check numbers after each CNC

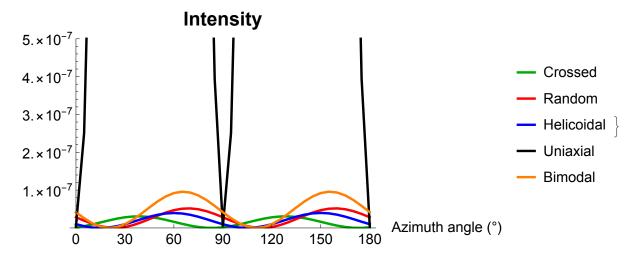
G. Final intensity as a function of the incident polarization angle

Note: the same calculation with various incident polarization angle (no explanation included). Data exportation included.

Plot check

```
In[*]:= (* Check plots *)
    {ListPlot[{clAng, raAng, heAng, unAng, biAng},
      PlotStyle → {{Darker[Green], Thickness[0.008]}, {Red, Thickness[0.008]}, {Blue,
          Thickness[0.008]}, {Black, Thickness[0.008]}, {Orange, Thickness[0.008]}},
      Ticks → {Table[30 i, {i, 0, 6}], Automatic}, PlotRange → All,
      ImageSize → 500, AxesLabel → {" Azimuth angle (°)", None},
      LabelStyle → {FontFamily → "Arial", FontSize → 15, Black},
      PlotLabel → Style["Intensity", 20, Black, Bold], Joined → True,
      PlotLegends → {"Crossed", "Random", "Helicoidal", "Uniaxial", "Bimodal"}],
     ListPlot[{clAng, raAng, heAng, unAng, biAng},
      PlotStyle → {{Darker[Green], Thickness[0.008]}, {Red, Thickness[0.008]}, {Blue,
          Thickness[0.008]}, {Black, Thickness[0.008]}, {Orange, Thickness[0.008]}},
      Ticks \rightarrow {Table[30 i, {i, 0, 6}], Automatic}, PlotRange \rightarrow {All, {0, 5 * 10<sup>-7</sup>}},
      ImageSize → 500, AxesLabel → {" Azimuth angle (°)", None},
      LabelStyle → {FontFamily → "Arial", FontSize → 15, Black},
      PlotLabel → Style["Intensity", 20, Black, Bold], Joined → True,
      PlotLegends → {"Crossed", "Random", "Helicoidal", "Uniaxial", "Bimodal"}]}
```





H. Data export

```
In[⊕]:= (* Combine generated data *)
    clAng2 = Transpose[clAng];
    raAng2 = Transpose[raAng];
    heAng2 = Transpose[heAng];
    unAng2 = Transpose[unAng];
    biAng2 = Transpose[biAng];
    b1 = {clAng2[[1]], clAng2[[2]], raAng2[[2]], heAng2[[2]], unAng2[[2]], biAng2[[2]]};
    b1 = Abs[b1];
    b1 = b1 // Transpose;
    b1 // MatrixForm;
    b1 = PrependTo[b1, {"wavenumber", "crossed-polylamellate",
         "random", "helicoidal10", "uniaxial", "bimodal"}];
     (* Data exportation *)
     name = CurrentValue[EvaluationNotebook[], {"NotebookFileName"}];
    name = StringDrop[name, -3];
    time = TextString[TimeObject[]];
    time2 = ToExpression["StringTake[time,2]"] <>
       ToString["."] <> ToExpression["StringTake[time, {4,5}]"] <>
       ToString["."] <> ToExpression["StringTake[time,-2]"]
    Export[NotebookDirectory[] <> ToExpression["name"] <>
        ToExpression["time2"] <> ToString["_"] <> "CRHUB.xlsx", b1];
Out[ \circ ] = 15.18.50
```