

```
(* Function: subset a b *)
```

```
let rec subset a b = match a with  
| [] -> true  
| h::t ->  
(match List.mem h b with  
| true -> subset t b  
| false -> false);;
```

```
(* Function: equal_sets a b *)
```

```
let equal_sets a b = match (subset a b, subset b a) with  
| (true, true) -> true  
| (_, _) -> false;;
```

```
(* Function: set_union a b *)
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```
let set_union a b = List.sort_uniq Pervasives.compare (List.append a b);;
```

```
(* Function: set_intersection a b *)
```

```
let rec intersect a b c = match a with  
| [] -> c  
| h::t ->  
(match List.mem h b with  
| true -> intersect t b (List.cons h c)  
| false -> intersect t b c);;
```

```
let set_intersection a b = List.sort_uniq Pervasives.compare (intersect a b []);;
```

```
(* Function: set_diff a b *)
```

```
let rec unintersect a b c = match a with  
| [] -> c  
| h::t ->  
(match List.mem h b with  
| true -> unintersect t b c  
| false -> unintersect t b (List.cons h c));;
```

```
let set_diff a b = List.sort_uniq Pervasives.compare (unintersect a b []);;
```

```
(* Function: computed_fixed_point eq f x *)
```

```
let rec computed_fixed_point eq f x =  
if eq x (f x) then x  
else computed_fixed_point eq f (f x);;
```

```
(* Function: filter_reachable g *)
```

```

type ('nonterminal, 'terminal) symbol =
  | N of 'nonterminal
  | T of 'terminal;;

let rec get_reachable_set sym fixed_rules rules reachable_set =
let rec process_rhs f_r aux_rhs aux_rset = match aux_rhs with
| [] -> aux_rset
| h::t ->
    (match h with
    | N element ->
        (match List.mem element aux_rset with
        | true -> process_rhs f_r t aux_rset
        | false -> process_rhs f_r t (get_reachable_set element f_r f_r (List.cons element aux_rset)))
    | T element -> process_rhs f_r t aux_rset)
in
match rules with
| [] -> reachable_set
| (lhs, rhs)::t ->
    if lhs = sym then
    get_reachable_set sym fixed_rules t (process_rhs fixed_rules rhs reachable_set)
    else
    get_reachable_set sym fixed_rules t reachable_set;;

let filtering rules reachable_set =
List.filter (fun rule -> List.mem (Pervasives.fst rule) reachable_set = true) rules;;

let filter_reachable g = match g with
| (start_symbol, rules) -> (start_symbol, filtering rules (get_reachable_set start_symbol rules rules [start_symbol]));;

```