1 Problem 1

$$(R-S)\cup(S-R)$$

A	В	С
7	5	3
1	4	3
6	7	9
1	4	4
8	3	2

Work:

A	В	С
7	5	3
2	1	2
1	4	3
5	8	7
6	7	9

A	В	С
2	1	2
1	4	4
8	3	2
5	8	7

$$R-S$$

A	В	С
7	5	3
1	4	3
6	7	9

$$S - R$$

A	В	С
1	4	4
8	3	2

2 Problem 2

 $\sigma_{R.L>S.M \land R.M < S.P}(R \times S)$

R.L	R.M	S.M	S.N	S.P
4	3	1	6	4
4	3	3	4	7
6	5	3	4	7
8	7	6	1	8

Work:

R

S

 $R \times S$

L	Μ		
4	3		
6	5		
8	7		

D				
M	N	Р		
6	1	8		
1	6	4		
2	5	1		
3	4	7		

R.L	R.M	S.M	S.N	S.P
4	3	6	1	8
4	3	1	6	4
4	3	2	5	1
4	3	3	4	7
6	5	6	1	8
6	5	1	6	4
6	5	2	5	1
6	5	3	4	7
8	7	6	1	8
8	7	1	6	4
8	7	2	5	1
8	7	3	4	7

3 Problem 3

- $\mathbf{a}) \left(\pi_{Student-name}(Student) \right) \left(\pi_{Student-name}(\sigma_{Course-name='Database\ Management\ Systems'}(Enrollment)) \right)$
- b) $\pi_{Student.Student-name}(\sigma_{Student.Department} <> Course.Department}(\sigma_{Student.Student-name} = Enrollment.Student-name}(Student \times (Enrollment \bowtie Course))))$
- c) $(\pi_{Course-name}(Course)) (\pi_{Course-name}(Enrollment))$
- d) $\pi_{Student.Department}(\sigma_{Student.Student-name=Enrollment.Student-name}(Student \times (\sigma_{Department='CS'}(Enrollment \bowtie Course))))$
- e) $\pi_{Department}(Student (\pi_{Student-name,Department}(Student \bowtie (\sigma_{Enrollment.Course-name} <> E2.Course-name) (\sigma_{Enrollment.Student-name} = E2.Student-name (Enrollment × \rho_{E2}(Enrollment)))))))$

Work:

a)

Use the *Enrollment* relation:

Enrollment

Select only the tuples that have the 'Database Management Systems' Course-name:

 $\sigma_{Course-name}$ ='Database Management Systems'(Enrollment)

Filter out the Course - name column, so that we only have the names of the students:

 $\pi_{Student-name}(\sigma_{Course-name='Database\ Management\ Systems'}(Enrollment))$

We want the names of all students who are not in 'Database Management Systems', so we use the *Student* relation:

Student

Filter out the *Department* column, so that we only have the names of the students:

 $\pi_{Student-name}(Student)$

We now use the difference operator to get the names of all the students in the *Student* relation that are not in the relation we have above, which are the names of all the student enrolled in 'Database Management Systems':

```
(\pi_{Student-name}(Student)) - (\pi_{Student-name}(\sigma_{Course-name}) - (\pi_{Student-name}(\sigma_{Course-name})))
```

b)

Use the *Enrollment* relation:

Enrollment

Natural join with the *Course* relation, so we get the courses students are enrolled in with the departments those courses belong to:

 $Enrollment \bowtie Course$

Cross product the *Student* relation and the relation above:

 $Student \times (Enrollment \bowtie Course)$

Select only the tuples with matching student names:

 $\sigma_{Student.Student-name=Enrollment.Student-name}(Student \times (Enrollment \bowtie Course))$

Select only the tuples with mismatched departments:

 $\sigma_{Student.Department} <> Course.Department (\sigma_{Student.Student-name} = Enrollment.Student-name (Student \times (Enrollment \times Course)))$

Filter out all columns except the students' names:

 $\pi_{Student.Student-name}(\sigma_{Student.Department} <> Course.Department}(\sigma_{Student.Student-name} = Enrollment.Student-name}(Student \times (Enrollment \bowtie Course))))$

c)

Use the Enrollment relation:

Enrollment

Filter out the Student - name column, so that we only have the names of the courses that have students enrolled:

```
\pi_{Course-name}(Enrollment)
```

We want the names of all courses which have no students enrolled, so we use the *Course* relation:

Course

Filter out the *Department* column, so that we only have the names of the courses:

```
\pi_{Course-name}(Course)
```

We now use the difference operator to get the names of all of the courses in the *Course* relation that are not in the relation we have above, which are names of all the courses with students enrolled:

```
(\pi_{Course-name}(Course)) - (\pi_{Course-name}(Enrollment))
```

d)

Use the *Enrollment* relation:

Enrollment

Natural join with the *Course* relation, so we get the courses students are enrolled in with the departments those courses belong to:

 $Enrollment \bowtie Course$

Select only the students who are taking courses that belong to the CS department:

```
\sigma_{Department='CS'}(Enrollment \bowtie Course)
```

We want the departments of all the students who are taking at least one class offered by the CS department, so we use the Student relation:

Student

We then cross product the *Student* relation and the relation we found above:

```
Student \times (\sigma_{Department='CS'}(Enrollment \bowtie Course))
```

Select only the tuples with a matching Student.Student-name and Enrollment.Student-name, so we only get the tuples of students in a CS course:

```
\sigma_{Student.Student-name} = Enrollment.Student-name (Student \times (\sigma_{Department='CS'}(Enrollment \bowtie Course)))
```

Filter out all other columns besides the students' departments:

```
\pi_{Student.Department}(\sigma_{Student.Student-name=Enrollment.Student-name}(Student \times (\sigma_{Department='CS'}(Enrollment \otimes Course))))
```

e)

Use the *Enrollment* relation:

Enrollment

We the self join the Enrollment relation:

 $Enrollment \times \rho_{E2}(Enrollment)$

Select the tuples with matching student names:

```
\sigma_{Enrollment.Student-name=E2.Student-name}(Enrollment \times \rho_{E2}(Enrollment))
```

Select the tuples with mismatched course names, as this means a student is enrolled in 2 or more courses:

```
\sigma_{Enrollment.Course-name} <> E2.Course-name (\sigma_{Enrollment.Student-name} = E2.Student-name (Enrollment \times \rho_{E2}(Enrollment)))
```

Natural join with the *Student* relation to concatenate a *Department* attribute for the students that are enrolled in 2 or more courses:

```
Student \bowtie (\sigma_{Enrollment.Course-name} <> E2.Course-name (\sigma_{Enrollment.Student-name} = E2.Student-name (Enrollment × \rho_{E2}(Enrollment))))
```

Natural join combined all 3 of the Student-name attributes into one, so now we remove the Course-name columns, so that our result has the same schema as the Student relation:

```
\pi_{Student-name,Department}(Student \bowtie (\sigma_{Enrollment.Course-name} <> E2.Course-name) (\sigma_{Enrollment.Student-name} = E2.Student-name (Enrollment × \rho_{E2}(Enrollment)))))
```

Now we find the difference between the Student relation and the result thus far to get the tuples of students who are not taking more than one class:

```
Student - (\pi_{Student-name, Department}(Student \bowtie (\sigma_{Enrollment.Course-name} <> E2.Course-name)))
```

 $\sigma_{Enrollment.Student-name=E2.Student-name}(Enrollment \times \rho_{E2}(Enrollment))))))$

Finally, we filter out the student names to get just the department names:

```
\pi_{Department}(Student - (\pi_{Student-name, Department}(Student \bowtie (\sigma_{Enrollment.Course-name} <> E2.Course-name) (\sigma_{Enrollment.Student-name} (Enrollment \times \rho_{E2}(Enrollment))))))))
```

4 Problem 4

A relational algebra expression to find the names of the lowest valued companies is:

```
\pi_{company-name}(Company-(\pi_{Company.company-name,Company.valuation}(\sigma_{Company.valuation})))))
```

Work:

First, we self join the *Company* relation:

 $Company \times \rho_{C2}(Company)$

Then, we select all of the tuples where Company.valuation > C2.valuation, to get the Company.company - name names that do not have the lowest valuation. This follows the logic that if a company has a valuation greater than at least one other company, then it does not have the lowest valuation:

```
\sigma_{Company.valuation} > C2.valuation (Company \times \rho_{C2}(Company))
```

We then filter out the C2 attributes, to get a schema that is the same as the Company relation:

 $\pi_{Company.company-name,Company.valuation}(\sigma_{Company.valuation} > C2.valuation(Company \times \rho_{C2}(Company)))$ We then find the difference between the Company relation and our result thus far to get the tuples of companies with the lowest valuation:

```
Company-(\pi_{Company.company-name,Company.valuation}(\sigma_{Company.valuation})))
 \times \rho_{C2}(Company))))
```

We then filter out the *valuation* attribute from the result to get just the names of the companies with the lowest valuation:

```
\pi_{company-name}(Company-(\pi_{Company.company-name,Company.valuation}(\sigma_{Company.valuation})))))
Company \times \rho_{C2}(Company)))))
```