

CS174A Lecture 11

Announcements & Reminders

- *Team project proposals due (final version): Nov 8*
- *Projects due: Dec 1*
- *Project presentations: Dec 3 and 5, in class*
- *Final exam: Dec 12*

TA Session This Friday

- *Team project proposals*

Last Lecture Recap

- ***Hidden Surface Removal***
 - Painter's algorithm
 - Z-buffer algorithm
 - Scanline z-buffer algorithm
 - Properties, advantages, disadvantages of each
 - Efficiency considerations

Next Up

- ***Lighting/Illumination Models***
 - Ambient
 - Diffuse
 - Specular
- ***Barycentric Coordinates, Trilinear Interpolations***
- ***Flat and Smooth Shading***
- ***Hidden Surface Removal***
 - 2-pass z-buffer algorithm (shadows)
 - Ray casting

Lighting/Illumination

- ***Geometric Properties***

- **Object:** position, orientation (normal)
- **Light:** position, direction, point vs. spot vs. area
- **Eye:** position, orientation

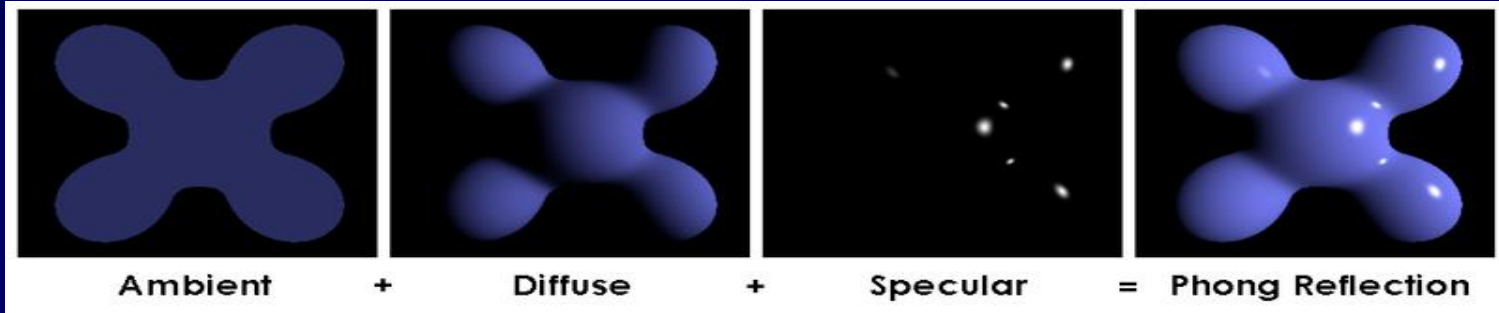
- ***Material Properties***

- **Object:** color, reflectivity, shininess, bumpiness, translucency
- **Light:** color
- **Eye:** filter, color blindness

Lighting/Illumination

- *Types of Lighting*

- Ambient
- Diffuse
- Specular



Ambient Lighting

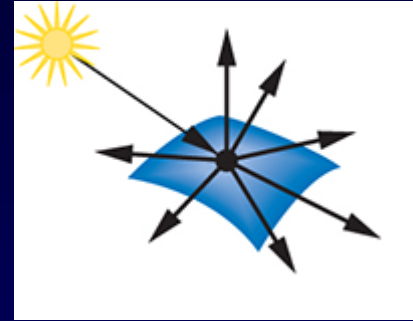
- *Properties*

- Background light
- Unrealistic
- Works as a good approximation of scattered light
- Does NOT depend on position/orientation of light, object or eye
- Only depends on object's material property
- k_a = ambient reflection coefficient, values [0..1], may be different for R, G, B
- I_a = intensity of ambient light source, values [0..1], different for R, G, B
- **Ambient light reflected off object = $k_a * I_a$**

Diffuse Lighting

- **Properties**

- Point light source
- Lambertian (of diffuse) reflection for dull, matte surfaces
- Surfaces look equally bright from all directions
- Reflect light **equally** in all directions
- Lambert's Law: *amount of light reflected from a differential unit area dA toward a viewer is \propto the cosine of the angle between the incident light and the normal (θ)*
- k_d = diffuse reflection coefficient, values $[0..1]$
- I_p = intensity of point light source, values $[0..1]$
- **Diffuse light reflected off object** = $k_d * I_p * \cos\theta = k_d * I_p * (N \cdot L)$



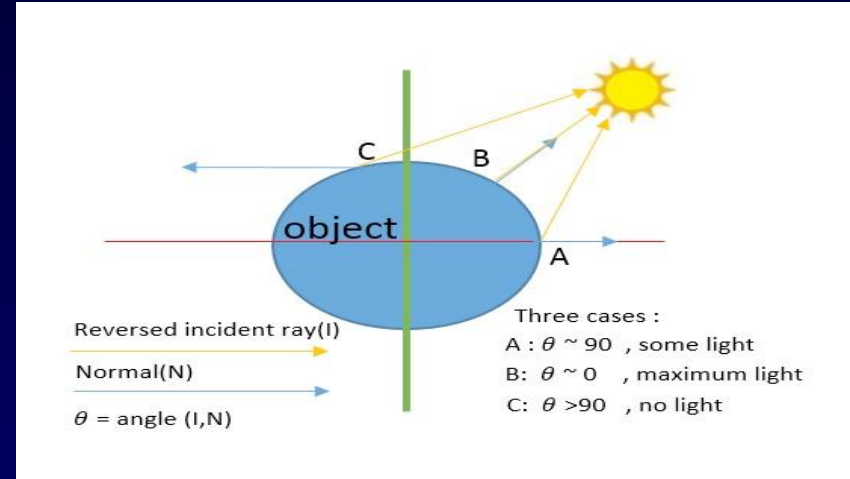
Diffuse Lighting (Contd.)

- **Incident angle θ**

- $\theta < 90^\circ \Rightarrow$ some light based on angle θ
- $\theta = 0^\circ \Rightarrow$ max light
- $\theta > 90^\circ \Rightarrow$ self occlusion

- **Directional light source**

- A light at sufficient distance from object (e.g., sun)
- L remains the same for entire scene
- N remains the same for entire polygon
- Therefore, $N \cdot L = \text{constant on poly}$; $L = \text{constant everywhere}$



- **Attenuated light source**

- Diffuse light reflected off object $= f_{\text{att}} * k_d * I_p * \cos\theta = f_{\text{att}} * k_d * I_p * (N \cdot L)$
- $f_{\text{att}} = \frac{1}{d_i^2}$ or $\frac{1}{c_1 + c_2 * d + c_3 * d^2}$; $f_{\text{att}} = \min(f_{\text{att}}, 1)$

Diffuse Lighting (Contd.)

- **Colored Light and Objects**

- Object's Diffuse Color ($O_{d\lambda}$): O_{dR}, O_{dG}, O_{dB}
- $I_{\lambda} = [k_a * I_{a\lambda} + f_{att} * k_d * I_{p\lambda} * (N \cdot L)] * O_{d\lambda}$

- **Atmospheric Attenuation or Blending**

- Depth cueing or fog (fog color = $I_{dc\lambda}$)
- $I'_{\lambda} = s_o * I_{\lambda} + (1 - s_o) * I_{dc\lambda}$
- $s_o = s_b$ when $z > z_b$
- $s_o = s_f$ when $z < z_f$
- $s_o = s_f + \frac{(s_b - s_f)}{(z_b - z_f)}(z - z_f)$

Specular Lighting

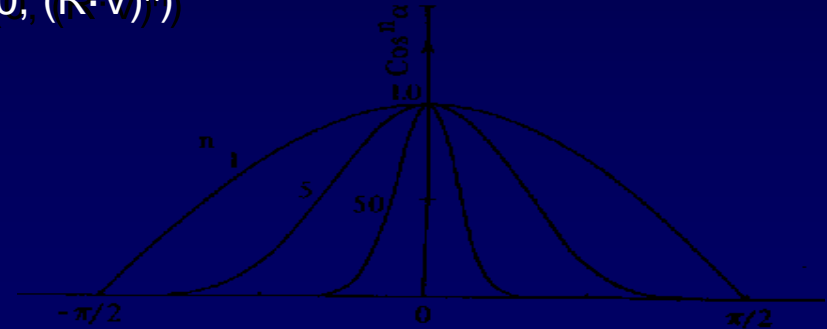
- *Properties*

- Shiny surfaces
- Color of light, not object
- Does depend on position of light, object and eye
- Light reflects **unequally** in different directions (e.g., perfect reflector: mirror)
- For non-perfect reflectors
- k_s = specular reflection coefficient, values $[0..1]$, may be different for R, G, B
- n = material's specular reflection exponent, values $[1..100s]$, perfect reflector $n = \infty$
- **Specular light reflected off object** = $f_{att} * k_s * I_p * \cos^n \alpha = f_{att} * k_s * I_p * (R \cdot V)^n$
- $I_\lambda = k_a * I_{a,\lambda} * O_{d,\lambda} + f_{att} * k_d * I_{p,\lambda} * (N \cdot L) * O_{d,\lambda} + f_{att} * k_s * I_{p,\lambda} * (R \cdot V)^n$

Specular Lighting (Contd.)

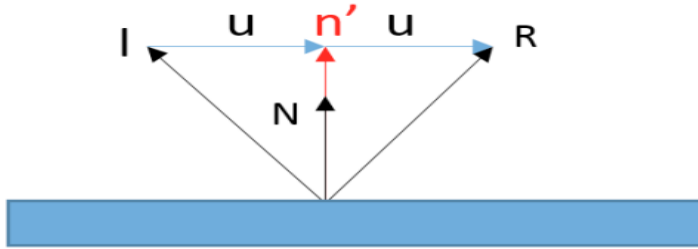
- **Specular Term: Smoothness Exponent Effect**

- Exponentiating a term that has values < 1 draws it closer to 0
- Higher exponent \Rightarrow smaller region where point light's reflection is considered aligned with the viewer \Rightarrow smaller shiny spot
- -ve values of $\cos\alpha$ is clamped to 0 = $\max(0, (R \cdot V)^n)$
- Max specular reflection when $\alpha = 0$

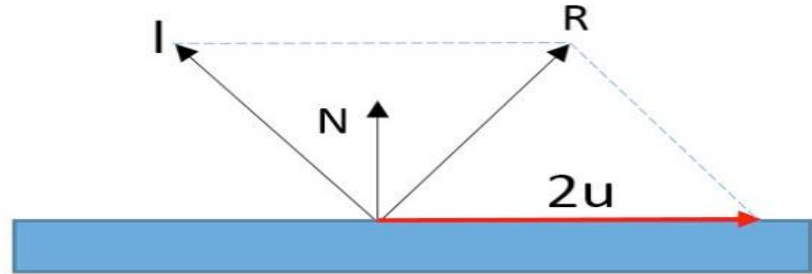


Specular Lighting (Contd.)

- *Calculating R Vector: reflection of point light source*



The $\vec{n'}$ is the projection of \vec{I} on \vec{N}
 $\vec{n'} = (\vec{N} \cdot \vec{I}) \vec{N}$, with $\|\vec{N}\|^2 = 1$
 $\vec{u} = \vec{n'} - \vec{I}$

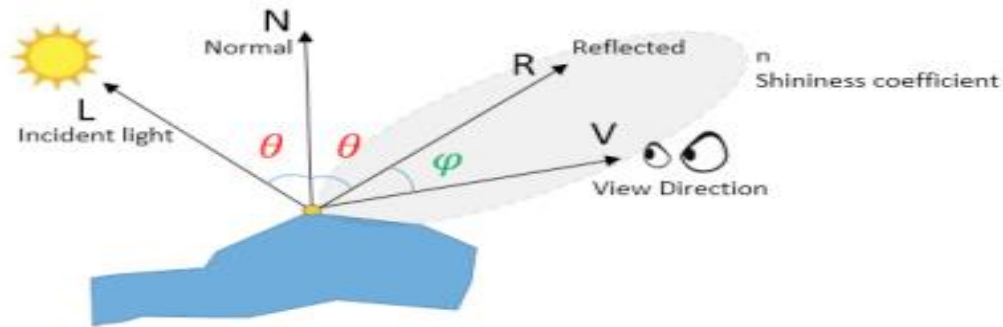


$$\vec{R} = \vec{I} + 2\vec{u} = \vec{I} + 2(\vec{n'} - \vec{I})$$
$$\vec{R} = 2(\vec{N} \cdot \vec{I}) \vec{N} - \vec{I}$$

Specular Lighting (Contd.)

- ***Halfway Vector: Alternate Formulation of $R \cdot V$***
 - Halfway vector (H) between L and V = $\text{normalize}(L + V)$
 - Replace $(R \cdot V)^n$ with $(H \cdot N)^n$

Final Light Equation



$I = \text{emissive} + \text{ambient} + \text{diffuse} + \text{specular}$

$\text{emissive} = k_e$

$\text{ambient} = k_a * \text{ambientColor}$

$\text{diffuse} = k_d * \text{lightColor} * \cos(\theta)$
 $= k_d * \text{lightColor} * \max(0, N \cdot L)$

$\text{specular} = k_s * \text{lightColor} * \cos(\phi)^n$
 $= k_s * \text{lightColor} * \max(0, R \cdot V)^n$

Lighting: Misc Improvements

- ***Spot Lights***
 - Smooth spot silhouette
- ***Multiple Light Sources***
 - Sum the light terms over all light sources
- ***Clamping***
 - $x = \max(0, x)$ and $\min(x, 1)$
 - $x = \text{normalize}(x)$ wrt to max value of color in entire image
- ***Fast Alternative to Phong Illumination***
 - $t = R \cdot V$ or $H \cdot N$
 - Instead of t^n , do $\frac{t}{n - nt + t}$