

# Data Structure

## BIT

---

```
1 // start from 1
2 #include <bits/stdc++.h>
3 using namespace std;
4 using ll = long long;
5 const ll MAXN = 100005;
6 ll tree[MAXN];
7 ll lowbit(int x) { return (x) & (-x); };
8 void Update(int i, ll x) {
9     // increase
10    for (int pos = i; pos <= MAXN; pos += lowbit(pos)) {
11        tree[pos] += x;
12    }
13 }
14 ll PrefixQuery(int n) {
15     ll ret = 0;
16     for (int pos = n; pos; pos -= lowbit(pos)) {
17         ret += tree[pos];
18     }
19     return ret;
20 }
21 ll RangeQuery(int ql, int qr) { return PrefixQuery(qr) - PrefixQuery(ql - 1); }
22 int main() {
23     int a[10] = {-1, 4, 2, 1, 5, 6, 7, 2, 1, 4};
24     for (int i = 1; i <= 9; i++) {
25         Update(i, a[i]);
26     }
27     for (int i = 1; i <= 9; i++) {
28         cout << PrefixQuery(i) << endl;
29     }
30     return 0;
31 }
32
```

## Mono Queue

---

```
1 #include <bits/stdc++.h>
2 // monotonic descending queue, segMax at front
3 using namespace std;
4
5 void getSegMax(vector<int>& v, int k, vector<int>& ans) {
6     deque<int> que;
7     int n = v.size();
8     for (int i = 0; i + 1 < k; ++i) {
```

```

9     while (!que.empty() && v[que.back()] <= v[i]) que.pop_back();
10    que.push_back(i);
11  }
12  for (int i = k - 1; i < n; ++i) {
13    while (!que.empty() && v[que.back()] <= v[i]) que.pop_back();
14    que.push_back(i);
15    while (que.front() <= i - k) que.pop_front();
16    ans.push_back(v[que.front()]);
17  }
18 }
19 void getSegMin(vector<int>& v, int k, vector<int>& ans) {
20   deque<int> que;
21   int n = v.size();
22   for (int i = 0; i + 1 < k; ++i) {
23     while (!que.empty() && v[que.back()] >= v[i]) que.pop_back();
24     que.push_back(i);
25   }
26   for (int i = k - 1; i < n; ++i) {
27     while (!que.empty() && v[que.back()] >= v[i]) que.pop_back();
28     que.push_back(i);
29     while (que.front() <= i - k) que.pop_front();
30     ans.push_back(v[que.front()]);
31   }
32 }
33 int main() {
34   vector<int> v = {2, 3, 1, 4, 5, 6, 7, 3};
35   vector<int> ans;
36   getSegMin(v, 3, ans);
37   for (auto itm: ans) {
38     cout << itm << " ";
39   }
40   return 0;
41 }

```

## Segment Tree Range

```

1  #include <iostream>
2  using namespace std;
3  using ll = long long;
4  const int MAXN = 200005;
5
6  struct Node {
7    // TODO modify to fit the need
8    ll l, r;
9    ll ans, mulv, addv;
10   Node() {}
11 };
12 Node tree[MAXN << 2];
13 ll n, m, q, rawValues[MAXN];
14
15 void MergeNode(Node &f, const Node &lc, const Node &rc) {
16   // TODO VARY based on different problems
17   f.ans = (lc.ans + rc.ans) % m;
18   f.addv = 0;
19   f.mulv = 1;
20 }
21 void NodeAdd(int k, ll addv) {
22

```

```

23 }
24 void NodeMul(int k, ll mulv) {
25
26 }
27 void SpreadTag(Node &f, Node &sn) {
28     // TODO VARY based on different problems
29     ll addv = f.addv, mulv = f.mulv;
30     sn.ans = (sn.ans * mulv % m + (sn.r - sn.l + 1) % m * addv % m) % m;
31     sn.mulv = sn.mulv * mulv % m;
32     sn.addv = (sn.addv * mulv % m + addv) % m;
33 }
34 void PushUp(int k) { // up a level
35     MergeNode(tree[k], tree[k << 1], tree[k << 1 | 1]);
36 }
37 void PushDown(int k) { // push the lazy tag down a level
38     if (!(tree[k].addv == 0 && tree[k].mulv == 1)) {
39         SpreadTag(tree[k], tree[k << 1]);
40         SpreadTag(tree[k], tree[k << 1 | 1]);
41         // TODO reset father's lazy tag
42         tree[k].addv = 0;
43         tree[k].mulv = 1;
44     }
45 }
46 void BuildTree(int k, int l, int r) {
47     // prepare the nodes
48     tree[k].l = l;
49     tree[k].r = r;
50     if (l == r) {
51         // TODO VARY based on different problems
52         tree[k].ans = rawValues[l];
53         tree[k].addv = 0;
54         tree[k].mulv = 1;
55     } else {
56         int mid = l + (r - l) / 2;
57         BuildTree(k << 1, l, mid);
58         BuildTree(k << 1 | 1, mid + 1, r);
59         PushUp(k);
60     }
61 }
62 void UpdateSegMul(int k, int l, int r, ll mulv) {
63     if (l <= tree[k].l && tree[k].r <= r) {
64         // TODO VARY based on problems
65         // record the operation for query with smaller range
66         tree[k].ans = tree[k].ans * mulv % m;
67         tree[k].mulv = tree[k].mulv * mulv % m;
68         tree[k].addv = tree[k].addv * mulv % m;
69     } else {
70         PushDown(k);
71         int mid = tree[k].l + (tree[k].r - tree[k].l) / 2;
72         if (mid >= l) // separated update
73             UpdateSegMul(k << 1, l, r, mulv);
74         if (mid < r) UpdateSegMul(k << 1 | 1, l, r, mulv);
75         PushUp(k);
76     }
77 }
78 void UpdateSegAdd(int k, int l, int r, ll addv) {
79     if (l <= tree[k].l && tree[k].r <= r) {
80         // TODO VARY based on problems
81         tree[k].ans = (tree[k].ans + addv * (tree[k].r - tree[k].l + 1) % m) % m;
82         tree[k].addv = (tree[k].addv + addv) % m;
83     } else {

```

```

84     PushDown(k);
85     int mid = tree[k].l + (tree[k].r - tree[k].l) / 2;
86     if (mid >= 1) // separated update
87         UpdateSegAdd(k << 1, 1, r, addv);
88     if (mid < r) UpdateSegAdd(k << 1 | 1, 1, r, addv);
89     PushUp(k);
90 }
91 }
92 void UpdateDot(int k, int pos, ll val) {
93     if (tree[k].l == tree[k].r) {
94         // TODO VARY based on problems
95         // tree[k].sum = val;
96     } else {
97         PushDown(k);
98         int mid = tree[k].l + (tree[k].r - tree[k].l) / 2;
99         if (pos <= mid) // separated update
100             UpdateDot(k << 1, pos, val);
101         else
102             UpdateDot(k << 1 | 1, pos, val);
103         PushUp(k);
104     }
105 }
106 Node Query(int k, int ql, int qr) {
107     if (tree[k].l >= ql && tree[k].r <= qr) return tree[k];
108     // when not single, push down firstly, then do the query
109     PushDown(k);
110     int mid = tree[k].l + (tree[k].r - tree[k].l) / 2;
111     Node resL, resR, retVal;
112     bool hasL = false, hasR = false;
113     if (ql <= mid) {
114         hasL = true;
115         resL = Query(k << 1, ql, qr);
116     }
117     if (mid < qr) {
118         hasR = true;
119         resR = Query(k << 1 | 1, ql, qr);
120     }
121     if (hasL && hasR)
122         MergeNode(retVal, resL, resR);
123     else if (hasL)
124         retVal = resL;
125     else if (hasR)
126         retVal = resR;
127     return retVal;
128 }
129 int main() {
130     ios::sync_with_stdio(false);
131     cin >> n >> q >> m;
132     for (int i = 1; i <= n; i++) cin >> rawValues[i];
133     ///////////////////////////////////////////////////
134     BuildTree(1, 1, n);
135     ///////////////////////////////////////////////////
136     int t, l, r, v;
137     while (q--) {
138         cin >> t >> l >> r;
139         if (t == 3) {
140             cout << Query(1, l, r).ans << "\n";
141         } else if (t == 1) {
142             cin >> v;
143             UpdateSegMul(1, l, r, v);
144         } else if (t == 2) {

```

```

145     cin >> v;
146     UpdateSegAdd(1, l, r, v);
147 }
148 }
149 return 0;
150 }

```

## Union Set

```

1  #include <iostream>
2  using namespace std;
3  const int MAXN = 100005;
4  int father[MAXN];
5  int trank[MAXN];
6
7  void Init(int n) {
8      for (int i = 0; i < n; ++i) {
9          father[i] = i;
10         trank[i] = 0;
11     }
12 }
13 int Find(int x) {
14     if (father[x] == x) {
15         return x;
16     }
17     return father[x] = Find(father[x]);
18 }
19 void Unite(int x, int y) {
20     x = Find(x);
21     y = Find(y);
22     if (x == y) {
23         return;
24     }
25     if (trank[x] < trank[y]) {
26         father[x] = y;
27     } else {
28         father[y] = x;
29         if (trank[x] == trank[y]) {
30             trank[x]++;
31         }
32     }
33 }
34 bool inSame(int x, int y) { return Find(x) == Find(y); }

```

# Geometry

```
1 int sgn (double x) { // sign of a double
2     if (fabs(x) < eps) return 0;
3     else if (x < 0) return -1;
4     else return 1;
5 }
```

## 3D Sphere

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 const double PI = acos(-1.0);
4 struct Sphere {
5     double x, y, z, r;
6     Sphere() {}
7     Sphere(double x, double y, double z, double r) : x(x), y(y), z(z), r(r) {}
8 };
9 double IntersectionVolume(Sphere o, Sphere t) {
10     // basic formula:  $V = (3 * r - h) * h * h * PI / 3$ 
11     // calculated from spinning surface calculus
12     if (o.r < t.r) swap(o, t);
13     double dis = sqrt((o.x - t.x) * (o.x - t.x) + (o.y - t.y) * (o.y - t.y) +
14                       (o.z - t.z) * (o.z - t.z));
15     if (dis <= o.r - t.r) { // completely in
16         return 4.0 / 3 * PI * t.r * t.r * t.r;
17     } else if (dis <= o.r) { // center of the smaller sphere in bigger sphere
18         //  $\cos A = (b^2 + c^2 - a^2) / 2bc$ 
19         double angleb = acos((t.r * t.r + dis * dis - o.r * o.r) / (2 * t.r * dis));
20         double anglea = PI - angleb;
21         double l = t.r * cos(anglea);
22         double H = o.r - l - dis;
23         double h = t.r - l;
24         return 4.0 / 3 * PI * t.r * t.r * t.r - PI / 3 * (3 * t.r - h) * h * h +
25                PI / 3 * (3 * o.r - H) * H * H;
26     } else if (dis < o.r + t.r) { // normal intersection
27         double angler = acos((t.r * t.r + dis * dis - o.r * o.r) / (2 * t.r * dis));
28         double angleR = acos((o.r * o.r + dis * dis - t.r * t.r) / (2 * o.r * dis));
29         double H = o.r - o.r * cos(angleR);
30         double h = t.r - t.r * cos(angler);
31         return PI / 3 * (3 * t.r - h) * h * h + PI / 3 * (3 * o.r - H) * H * H;
32     } else {
33         return 0;
34     }
35 }
36 double IntersectionSurface(Sphere &o, Sphere &t) {
37     // basic formula:  $S = 2 * PI * r * h$ 
38     if (o.r < t.r) swap(o, t);
39     double dis = sqrt((o.x - t.x) * (o.x - t.x) + (o.y - t.y) * (o.y - t.y) +
```

```

40         (o.z - t.z) * (o.z - t.z));
41     if (dis <= o.r - t.r) { // completely in
42         return 4 * PI * t.r * t.r;
43     } else if (dis <= o.r) { // center of the smaller sphere in bigger sphere
44         double angleb = acos((t.r * t.r + dis * dis - o.r * o.r) / (2 * t.r * dis));
45         double anglea = PI - angleb;
46         double l = t.r * cos(anglea);
47         double H = o.r - l - dis;
48         double h = t.r - l;
49         return 4 * PI * t.r * t.r - 2 * PI * t.r * h + 2 * PI * o.r * H;
50     } else if (dis < o.r + t.r) { // normal intersection
51         double angler = acos((t.r * t.r + dis * dis - o.r * o.r) / (2 * t.r * dis));
52         double angleR = acos((o.r * o.r + dis * dis - t.r * t.r) / (2 * o.r * dis));
53         double H = o.r - o.r * cos(angleR);
54         double h = t.r - t.r * cos(angler);
55         return 2 * PI * t.r * h + 2 * PI * o.r * H;
56     } else {
57         return 0;
58     }
59 }
60 int main() {
61     Sphere A, B;
62     cin >> A.x >> A.y >> A.z >> A.r;
63     cin >> B.x >> B.y >> B.z >> B.r;
64     cout << fixed << setprecision(10) << 4*PI*(A.r*A.r+B.r*B.r) - IntersectionSurface(A, B) << endl;
65     return 0;
66 }

```

## 2D Vector

```

1  /**
2   * structs of
3   * point, vector, segment
4   * and some operator overloads
5   */
6  // whether a seg AB intersects with a circle O?
7  // see the endpoints' tangent point (P, Q) angle
8  // angles: AOP + BOQ < AOB <==> intersect
9  #include <bits/stdc++.h>
10 using namespace std;
11 using ll = long long;
12 ll MOD = 1e9 + 7;
13 ll QpowMod(ll bse, ll pwr) {
14     ll ret = 1;
15     while (pwr) {
16         if (pwr & 1) ret = ret * bse % MOD;
17         bse = bse * bse % MOD;
18         pwr >>= 1;
19     }
20     return ret;
21 }
22 struct Point2 {
23     ll x, y;
24     Point2() : x(0), y(0) {}
25     Point2(ll _x, ll _y) : x(_x), y(_y) {}
26     ll Norm2() { return 1ll * x * x + 1ll * y * y; }
27     double Norm() { return sqrt(Norm2()); }
28     Point2 operator+(const Point2 &po) {

```

```

29     return Point2(x + po.x, y + po.y);
30 }
31 Point2 operator-(const Point2 &po) {
32     // note the direction
33     return Point2(x - po.x, y - po.y);
34 }
35 bool operator==(const Point2 &po) {
36     return x == po.x && y == po.y;
37 }
38 };
39 typedef Point2 Vector2;
40 struct Segment2 {
41     Point2 s, e;
42     Segment2() {}
43     Segment2(Point2 _s, Point2 _e) : s(_s), e(_e) {}
44 };
45 ll MulCross(const Point2 &p1, const Point2 &p2) {
46     return p1.x * p2.y - p1.y * p2.x;
47 }
48 ll MulDot(const Point2 &p1, const Point2 &p2) {
49     return p1.x * p2.x + p1.y * p2.y;
50 }
51 double DisPointToSeg(Point2 p, Point2 s1, Point2 s2) {
52     Point2 v1 = p - s1, v2 = s2 - s1;
53     if (MulDot(v2, v1) < 0 || MulDot(v2, v1) > v2.Norm2())
54         return min(1.0 * (p - s1).Norm(), 1.0 * (p - s2).Norm());
55     return abs(1.0 * MulCross(v2, v1) / v2.Norm());
56 }
57 int Dis2PointToSeg_INT(Point2 p, Point2 s1, Point2 s2) {
58     // square of distance between two points
59     Point2 v = p - s1, u = s2 - s1;
60     if (MulDot(u, v) < 0 || MulDot(u, v) > u.Norm2())
61         return min((p - s1).Norm2(), (p - s2).Norm2()) % MOD;
62     return ((MulCross(v, u) % MOD) * (MulCross(v, u) % MOD)) % MOD *
63         QpowMod(u.Norm2() % MOD, MOD - 2) % MOD;
64 }
65 int main() { return 0; }

```

## 3D Vector

```

1  #include <bits/stdc++.h>
2  using namespace std;
3  using ll = long long;
4  ll MOD = 1e9 + 7;
5  struct Point3 {
6      ll x, y, z;
7      Point3() : x(0), y(0), z(0) {}
8      Point3(ll _x, ll _y, ll _z) : x(_x), y(_y), z(_z) {}
9      ll Norm2() { return x * x + y * y + z * z; }
10     double Norm() { return sqrt(Norm2()); }
11     Point3 operator+(const Point3 &po) {
12         return Point3(x + po.x, y + po.y, z + po.z);
13     }
14     Point3 operator-(const Point3 &po) {
15         return Point3(x - po.x, y - po.y, z - po.z);

```



```

16     }
17     bool operator==(const Point3 &po) {
18         return x == po.x && y == po.y && z == po.z;
19     }
20 };
21 typedef Point3 Vector3;
22 struct Segment3 {
23     Point3 s, e;
24     Segment3() {}
25     Segment3(Point3 _s, Point3 _e): s(_s), e(_e) {}
26 };
27 ll MulDot(const Point3 &p1, const Point3 &p2) {
28     return p1.x * p2.x + p1.y * p2.y + p1.z * p2.z;
29 }
30 Point3 MulCross(const Point3 &p1, const Point3 &p2) {
31     return Point3(p1.y * p2.z - p1.z * p2.y, p1.z * p2.x - p1.x * p2.z, p1.x * p2.y - p1.y * p2.x);
32 }
33 int main() {
34     Point3 a{0, 0, 1}, b{1, 1, 1};
35     Point3 c = MulCross(a, b);
36     cout << c.Norm() << endl;
37     return 0;
38 }
39

```

# Math

$$C_n^m$$

---

```
1 #include <stdio.h>
2 using ll = long long;
3 const ll MN = 2000000;
4 const ll MOD = 1000000007;
5 int fac[MN + 5], inv[MN + 5];
6
7 ll qpowMod(ll bse, ll pwr) {
8     ll ret = 1;
9     while (pwr) {
10         if (pwr & 1) ret = ret * bse % MOD;
11         bse = bse * bse % MOD;
12         pwr >>= 1;
13     }
14     return ret;
15 }
16 void init() {
17     fac[0] = 1;
18     for (int i = 1; i <= MN; i++) fac[i] = 1ll * fac[i - 1] * i % MOD;
19     inv[MN] = qpowMod(fac[MN], MOD - 2);
20     for (int i = MN - 1; i >= 0; i--) inv[i] = 1ll * inv[i + 1] * (i + 1) % MOD;
21 }
22 int C(int n, int m) {
23     if (m > n) return 0;
24     return 1ll * fac[n] * inv[m] % MOD * inv[n - m] % MOD;
25 }
26 int main() {
27     init();
28     printf("%d\n", C(5, 3));
29     return 0;
30 }
```

## Euler Primers

---

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 using ll = long long;
4 const int MAXN = 1e6 + 5;
5 const int MOD = 1e9 + 7;
6 // priority_queue<ll, vector<ll>, greater<ll>> minor_que;
7
8 int prime[MAXN];
9 bool vis[MAXN];
10 int cnt = 0;
11 ll maxv = -1;
12 void EulerPrime(int n) {
13     for (int i = 2; i <= n; ++i) {
```

```

14     if (vis[i] == 0) {
15         prime[cnt++] = i;
16         vis[i] = 1;
17     }
18     for (int j = 0; i * prime[j] <= n; ++j) {
19         vis[i * prime[j]] = 1;
20         if (i % prime[j] == 0) break; // key of O(n)
21     }
22 }
23 }
24 int main() {
25     EulerPrime(100);
26     for (int i = 0; i < cnt; ++i) printf("%d ", prime[i]);
27     printf("\n");
28     return 0;
29 }

```

## Josephus Ring

```

1  // n - 1 规模时留下的最后一人，与 n 规模的相差了一个偏移量 k。J_{n, k} = (J_{n - 1, k} + k) mod n。 (从 0
   编号，下同，答案加一个偏移即可)
2  #include <cstdio>
3  long long josephus(int n, int k) {
4      if (n == 1)
5          return 0;
6      else
7          return (josephus(n - 1, k) + k) % n;
8  }
9  int main(void) {
10     long long n, k;
11     scanf("%lld %lld", &n, &k);
12
13     printf("%lld\n", 1 + josephus(n, k));
14     return 0;
15 }
16 // total n, k-th out, find the m-th out, start from 1
17 void solve(int casei) {
18     cout << "Case #" << casei << ": ";
19     long long ans = (K - 1) % (N - M + 1);
20     if (K == 1) {
21         cout << M << endl;
22         return;
23     }
24     for (ll i = N - M + 2; i <= N; i++) {
25         ans = (ans + K) % i; // normal iteration
26         // jump forward
27         ll rem = (i - ans - 1) / K;
28         rem = min(rem, N - i); // limit the times of jump
29         i += rem; // jump
30         ans += rem * K;
31     }
32     cout << ans + 1 << endl;
33 }

```

## Matrix Inverse Element

Inverse element of 2x2 matrix  $\begin{pmatrix} a & b \\ c & d \end{pmatrix}$  is  $\begin{pmatrix} d & -b \\ -c & a \end{pmatrix} / (ad - bc)$ .

## Matrix Power

```
1  #include <bits/stdc++.h>
2  #define inf 0x3f3f3f3f
3  using namespace std;
4  typedef long long ll;
5  const int N = 205, mod = 998244353, MS = 205;
6  struct Mat {
7      ll a[MS][MS];
8      ll n, m;
9      Mat(int n = 0, int m = 0) : n(n), m(m) { memset(a, 0, sizeof(a)); }
10     Mat operator*(const Mat& B) const {
11         Mat C(n, B.m);
12         for (int i = 1; i <= n; i++)
13             for (int j = 1; j <= B.m; j++)
14                 for (int k = 1; k <= m; k++)
15                     C.a[i][j] = (C.a[i][j] + a[i][k] * B.a[k][j]) % mod;
16         return C;
17     }
18 };
19 Mat qpow(Mat a, int n) {
20     Mat ans(a.n, a.n);
21     for (int i = 1; i <= a.n; i++) ans.a[i][i] = 1;
22     for (; n; n >>= 1, a = a * a)
23         if (n & 1) ans = ans * a;
24     return ans;
25 }
26 int main() {
27     ll n;
28     cin >> n;
29     string s;
30     cin >> s;
31     ll now = stol(s);
32     Mat A(100, 100);
33     A = qpow(A, n);
34
35     Mat B(100, 100);
36     B.a[1][1] = 1;
37     B = B * A;
38     cout << B.a[1][now];
39 }
```

## Quick Power

```
1  #include <cstdio>
2  // a^(-1) mod p => a^(p - 2) mod p
3  // n * n * (n + 1) * (n + 1) / 4 = \sum_{1}^{n} i^3
4  // n * (n + 1) * (2n + 1) / 6 = \sum_{1}^{n} i^2
5  using ll = long long;
```

```
6  ll MOD = 1e9+7;
7  ll QpowMod(ll bse, ll pwr) {
8      ll ret = 1;
9      while (pwr) {
10         if (pwr & 1) ret = ret * bse % MOD;
11         bse = bse * bse % MOD;
12         pwr >>= 1;
13     }
14     return ret;
15 }
16 int main() {
17     printf("%lld", QpowMod(2, 199) * 6 % MOD);
18     return 0;
19 }
```

# Graph

## SCC kosaraju

```
1  #include <cstdio>
2  #include <stack>
3  using namespace std;
4  stack<int> stk;
5  // adjacent matrix
6  int mp[10][10];
7  // reversed graph
8  int mpt[10][10];
9  int vst[10];
10 int clr[10];
11 int vn, en;
12 void dfs1(int s) {
13     if (vst[s] == 1) return;
14     vst[s] = 1;
15     // dfs routine
16     for (int i = 1; i <= vn; ++i) {
17         if (mp[s][i] < 0x3f3f3f3f) {
18             dfs1(i);
19         }
20     }
21     // push
22     stk.push(s);
23 }
24 void dfs2(int s, int cnt) {
25     if (vst[s] == 0) return;
26     clr[s] = cnt;
27     vst[s] = 0;
28     for (int i = 1; i <= vn; ++i) {
29         if (mpt[s][i] < 0x3f3f3f3f) {
30             dfs2(i, cnt);
31         }
32     }
33 }
34 void init() {
35     for (int i = 1; i <= vn; ++i) {
36         for (int j = 1; j <= vn; ++j) {
37             mp[i][j] = mp[j][i] = 0x3f3f3f3f;
38             mpt[i][j] = mpt[j][i] = 0x3f3f3f3f;
39         }
40         mpt[i][i] = mp[i][i] = 0;
41     }
42 }
43 void SCC_kor() {
44     for (int i = 1; i <= vn; ++i) {
45         if (vst[i] == 0) dfs1(i);
46     }
47     int cnt = 1;
48     while (!stk.empty()) {
49         int s = stk.top();
50         stk.pop();
```

```

51     if (vst[s] == 0) continue;
52     dfs2(s, cnt++);
53 }
54 // vertexes with same value in clr[] is in one SCC
55 for (int i = 1; i <= vn; ++i) {
56     printf("%d ", clr[i]);
57 }
58 printf("\n");
59 }
60 int main() {
61     scanf("%d %d", &vn, &en);
62     init();
63     for (int i = 1; i <= en; ++i) {
64         int fr, to;
65         scanf("%d %d", &fr, &to);
66         mp[fr][to] = 1;
67         mpt[to][fr] = 1;
68     }
69     SCC_kor();
70     return 0;
71 }

```

## SCC tarjan

```

1  #include <bits/stdc++.h>
2  using namespace std;
3  int n, m;
4  struct node {
5      vector<int> nxt;
6  } g[100000];
7  int dfn[100000], low[100000], d[100000], col[100000], cnt[100000], stk[100000];
8  int vis[100000];
9  int top, deep, colour;
10 void tarjan(int u) {
11     dfn[u] = low[u] = ++deep;
12     stk[top++] = u;
13     vis[u] = 1;
14     for (int i = 0; i < g[u].nxt.size(); i++) {
15         int v = g[u].nxt[i];
16         if (!vis[v]) {
17             tarjan(v);
18             low[u] = min(low[v], low[u]);
19         } else {
20             low[u] = min(low[v], low[u]);
21         }
22     }
23     if (dfn[u] == low[u]) {
24         int node;
25         colour++;
26         while (node != u) {
27             node = stk[top - 1];
28             top--;
29             col[node] = colour;
30         }
31     }
32 }

```

# String

## KMP

---

```
1  int nxt[100005];
2  char t[100005];
3  void getNext() {
4      nxt[0] = -1;
5      int k = -1, j = 0;
6      while (t[j] != '\0') {
7          if (k == -1 || t[k] == t[j]) {
8              nxt[++j] = ++k;
9          } else {
10             k = nxt[k];
11         }
12     }
13 }
```

## Manacher

---

```
1  // find the palindrome in O(n)
2  #include <bits/stdc++.h>
3  using namespace std;
4  char s[100005];
5  int ps = 0;
6  int p[100005], ctr, maxr, mirr;
7  void solve() {
8      ctr = maxr = 0;
9      for (int i = 0; i < ps; ++i) {
10         mirr = 2 * ctr - i;
11         if (i < maxr) {
12             p[i] = min(maxr - i, p[mirr]);
13         } else {
14             p[i] = 0;
15         }
16         while (s[i - 1 - p[i]] == s[i + 1 + p[i]]) {
17             p[i]++;
18         }
19         if (p[i] + i > maxr) {
20             ctr = i;
21             maxr = p[i] + i;
22         }
23     }
24     int maxi = 0;
25     for (int i = 0; i < ps; ++i) {
26         maxi = p[maxi] < p[i] ? i : maxi;
27     }
28     printf("%d\n", p[maxi]);
29     for (int i = maxi - p[maxi]; i <= maxi + p[maxi]; ++i) {
30         if (s[i] != '#') {
```



```
31     printf("%c", s[i]);
32 }
33 }
34 printf("\n");
35 }
36 int main() {
37     int Case = 1;
38     while (Case--) {
39         char c = getchar();
40         s[ps++] = '#';
41         while (c != '\n') {
42             s[ps++] = c;
43             s[ps++] = '#';
44             c = getchar();
45         }
46         solve();
47     }
48     return 0;
49 }
```

# Misc

## fastIO

```
1 namespace GTI
2 {
3     char gc(void)
4     {
5         const int S=1<<17;
6         static char buf[S],*s=buf,*t=buf;
7         if (s==t) t=buf+fread(s=buf,1,S,stdin);
8         if (s==t) return EOF;
9         return *s++;
10    }
11    int gti(void)
12    {
13        int a=0,b=1,c=gc();
14        for (;!isdigit(c);c=gc()) b^=(c=='-');
15        for (;isdigit(c);c=gc()) a=a*10+c-'0';
16        return b?a:-a;
17    }
18 };
19
```

## Discretization

```
1 namespace GTI
2 {
3     char gc(void)
4     {
5         const int S=1<<17;
6         static char buf[S],*s=buf,*t=buf;
7         if (s==t) t=buf+fread(s=buf,1,S,stdin);
8         if (s==t) return EOF;
9         return *s++;
10    }
11    int gti(void)
12    {
13        int a=0,b=1,c=gc();
14        for (;!isdigit(c);c=gc()) b^=(c=='-');
15        for (;isdigit(c);c=gc()) a=a*10+c-'0';
16        return b?a:-a;
17    }
18 };
```

## Inverse Pair Merge Sort

```
1  using ll = long long;
2  ll MAXN = 2e5 + 5;
3  ll n, q[MAXN], tmp[MAXN];
4  // [l, r]
5  ll merge_sort(int l, int r) {
6      if (l >= r) return 0;
7      ll mid = (l + r) >> 1;
8      ll res = merge_sort(l, mid) + merge_sort(mid + 1, r);
9
10     ll k = 0, i = l, j = mid + 1;
11     while (i <= mid && j <= r) {
12         if (q[i] <= q[j])
13             tmp[k++] = q[i++];
14         else {
15             tmp[k++] = q[j++];
16             res += mid - i + 1;
17         }
18     }
19     while (i <= mid) tmp[k++] = q[i++];
20     while (j <= r) tmp[k++] = q[j++];
21     for (ll i = l, j = 0; i <= r; i++, j++) q[i] = tmp[j];
22     return res;
23 }
```

## Modui

```
1  /**
2   * Modui range number of distinct values
3   */
4  #include <bits/stdc++.h>
5  using namespace std;
6  #define endl "\n";
7  #define IOS_ONLY \
8   ios::sync_with_stdio(false); \
9   cin.tie(0); \
10  cout.tie(0);
11  const int MAXN = 30005, MAXQ = 200005, MAXM = 1000005;
12  int sq;
13  struct Query {
14      int ql, qr, id;
15      bool operator<(const Query &o) const {
16          // sqrt(n) partitions, assign sq with sqrt(n) first
17          if (ql / sq != o.ql / sq) return ql < o.ql;
18          if (ql / sq & 1) return qr < o.qr; // order by parity
19          return qr > o.qr;
20      }
21  } Q[MAXQ];
22  int A[MAXN], ans[MAXQ], Cnt[MAXM], cur, pl = 1, pr = 0, n;
23  inline void add(int pos) {
24      if (Cnt[A[pos]] == 0) cur++;
25      Cnt[A[pos]]++;
26  }
```

```

27 inline void del(int pos) {
28     Cnt[A[pos]]--;
29     if (Cnt[A[pos]] == 0) cur--;
30 }
31 int main() {
32     IOS_ONLY
33     cin >> n;
34     sq = sqrt(n);
35     for (int i = 1; i <= n; ++i) cin >> A[i];
36     int q;
37     cin >> q;
38     for (int i = 0; i < q; ++i) { // offline query
39         cin >> Q[i].ql >> Q[i].qr;
40         Q[i].id = i;
41     }
42     sort(Q, Q + q); // sort, KEY of modui
43     for (int i = 0; i < q; ++i) {
44         while (pl > Q[i].ql) add(--pl);
45         while (pr < Q[i].qr) add(++pr);
46         while (pl < Q[i].ql) del(pl++);
47         while (pr > Q[i].qr) del(pr--);
48         ans[Q[i].id] = cur; // store the rasult
49     }
50     for (int i = 0; i < q; ++i) cout << ans[i] << endl;
51     return 0;
52 }

```