

**1. Load resistance:**

$$R_L = \frac{V_0}{I_0} = 2\Omega$$

2.

**2. state space model:**

$$i(t) = i_1(t) + i_2(t), \quad V_c(t) + R_c i_1(t) = R_L i_2(t), \quad \text{Therefore} \quad i_1(t) = \frac{R_L i(t) - V_c(t)}{R_c + R_L}$$

$$\begin{aligned} L \frac{di(t)}{dt} &= -\frac{R_c R_L}{R_c + R_L} i(t) - \frac{R_L}{R_c + R_L} V_c(t) + V_{in}(t) \\ C \frac{dV_c(t)}{dt} &= \frac{R_L}{R_c + R_L} i(t) - \frac{1}{R_c + R_L} V_c(t) \end{aligned}$$

q(t)=1: Switch on

$$\begin{aligned} L \frac{di(t)}{dt} &= -\frac{R_c R_L}{R_c + R_L} i(t) - \frac{R_L}{R_c + R_L} V_c(t) \\ C \frac{dV_c(t)}{dt} &= \frac{R_L}{R_c + R_L} i(t) - \frac{1}{R_c + R_L} V_c(t) \end{aligned}$$

q(t)=0: Switch off

The derivation equation is:

$$\begin{aligned} \frac{di(t)}{dt} &= \frac{1}{L} d(t) \left[ -\frac{R_c R_L}{R_c + R_L} i(t) - \frac{R_L}{R_c + R_L} V_c(t) + V_{in}(t) \right] + \frac{1}{L} (1-d(t)) \left[ -\frac{R_c R_L}{R_c + R_L} i(t) - \frac{R_L}{R_c + R_L} V_c(t) \right] \\ \frac{dV_c(t)}{dt} &= \frac{R_L}{C(R_c + R_L)} i(t) - \frac{1}{C(R_c + R_L)} V_c(t) \end{aligned}$$

transfer into state-space mode is:

$$\begin{pmatrix} \frac{di(t)}{dt} \\ \frac{dV_c(t)}{dt} \end{pmatrix} = \begin{pmatrix} -\frac{R_c R_L}{L(R_c + R_L)} & -\frac{R_L}{L(R_c + R_L)} \\ \frac{R_L}{C(R_c + R_L)} & -\frac{1}{C(R_c + R_L)} \end{pmatrix} \begin{pmatrix} i(t) \\ V_c(t) \end{pmatrix} + \begin{pmatrix} \frac{d(t)}{L} \\ 0 \end{pmatrix} V_{in}(t)$$

$$V_0(t) = R_L i_2(t) = \frac{R_c R_L}{R_c + R_L} i(t) + \frac{R_L}{R_c + R_L} V_c(t) = \left( \frac{R_c R_L}{R_c + R_L}, \frac{R_L}{R_c + R_L} \right) \begin{pmatrix} \frac{di(t)}{dt} \\ \frac{dV_c(t)}{dt} \end{pmatrix}$$

**3. Steady-state Values:**

Let the nominal signals be:  $V_{in}(t) = V_{in}$ ;  $d(t) = D$

Let the right-hand sides of the state equations equal to 0. Then solve for  $i = L$ ,  $V_c = V$ .

Together, these values will be the nominal signals.

$$\frac{D}{L} \left[ -\frac{R_c R_L}{R_c + R_L} I - \frac{R_L}{R_c + R_L} V + V_{in} \right] + \frac{(1-D)}{L} \left[ -\frac{R_c R_L}{R_c + R_L} I - \frac{R_L}{R_c + R_L} V \right] = 0$$

$$\frac{R_L}{C(R_c + R_L)} I - \frac{1}{C(R_c + R_L)} V = 0$$

Steady state value is  $I = \frac{(R_c + R_L) D V_{in}}{R_L (R_c + R_L)}$ ,  $V = \frac{(R_c + R_L) D R_L V_{in}}{R_L (R_c + R_L)}$

#### 4. Linearized System around the nominal signal:

$$\begin{pmatrix} I \\ V \end{pmatrix} = \begin{pmatrix} -\frac{R_c R_L}{L(R_c + R_L)} & -\frac{R_L}{L(R_c + R_L)} \\ \frac{R_L}{C(R_c + R_L)} & -\frac{1}{C(R_c + R_L)} \end{pmatrix} \begin{pmatrix} I \\ V \end{pmatrix} + \begin{pmatrix} \frac{1}{L} \\ 0 \end{pmatrix} V_{in}$$

$$\begin{pmatrix} I \\ V \end{pmatrix} = \begin{pmatrix} -\frac{R_c R_L}{L(R_c + R_L)} & -\frac{R_L}{L(R_c + R_L)} \\ \frac{R_L}{C(R_c + R_L)} & -\frac{1}{C(R_c + R_L)} \end{pmatrix} \begin{pmatrix} I \\ V \end{pmatrix} + \begin{pmatrix} 0 \\ 0 \end{pmatrix} V_{in}$$

$$A_1 = A_2 = \begin{pmatrix} -\frac{R_c R_L}{L(R_c + R_L)} & -\frac{R_L}{L(R_c + R_L)} \\ \frac{R_L}{C(R_c + R_L)} & -\frac{1}{C(R_c + R_L)} \end{pmatrix}; B_1 = \begin{pmatrix} \frac{1}{L} \\ 0 \end{pmatrix}; B_2 = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

$$A = D A_1 + (1-D) A_2 = A_1 = \begin{pmatrix} -\frac{R_c R_L}{L(R_c + R_L)} & -\frac{R_L}{L(R_c + R_L)} \\ \frac{R_L}{C(R_c + R_L)} & -\frac{1}{C(R_c + R_L)} \end{pmatrix}$$

$$B = (A_1 - A_2) x_0 + (B_1 - B_2) V_{in} = B_1 V_{in} = \begin{pmatrix} \frac{V_{in}}{L} \\ 0 \end{pmatrix}$$

Local Linearization:  $\tilde{x}(t) = x(t) - x_0$ , where  $\tilde{i}(t) = i(t) - I$ ;  $\tilde{V}_c(t) = V_c(t) - V$

$$\frac{d\tilde{x}(t)}{dt} = A\tilde{x}(t) + B\tilde{d}(t) = \begin{pmatrix} -\frac{R_c R_L}{L(R_c + R_L)} & -\frac{R_L}{L(R_c + R_L)} \\ \frac{R_L}{C(R_c + R_L)} & -\frac{1}{C(R_c + R_L)} \end{pmatrix} \tilde{x}(t) + \begin{pmatrix} \frac{V_{in}}{L} \\ 0 \end{pmatrix} \tilde{d}(t)$$

## 5. Transfer Function:

$$Z(s) = Ls + \frac{R_L(R_c + \frac{1}{Cs})}{R_L + R_c + \frac{1}{Cs}} = Ls + \frac{R_L(R_c Cs + 1)}{(R_L + R_c)Cs + 1} = \frac{Ls[(R_L + R_c)Cs + 1] + R_L(R_c Cs + 1)}{(R_L + R_c)Cs + 1}$$

$$P(s) = \frac{1}{Z(s)} \times \frac{R_L(R_c Cs + 1)}{(R_L + R_c)Cs + 1} = \frac{R_L R_c Cs + R_L}{(R_L + R_c)CLs^2 + (L + R_L R_c C)s + R_L}$$

The transfer function :  $\frac{V_0(s)}{D(s)} = \frac{R_L R_c Cs + R_L}{(R_L + R_c)CLs^2 + (L + R_L R_c C)s + R_L}$

$$= \frac{1 \times 10^{-4} s + 2}{1.005 \times 10^{-6} s^2 + 2 \times 10^{-4} s + 2}$$

## 6. What should be $V_{set}$ :

To derive the competitor value that make  $V_{OUT}=12V$ ,  $I_{OUT}=6A$ , while  $V_{SET}$  is the reference value to compare with inductor current,  $I_{OUT}=6A$   $R_t=0.2\Omega$  therefore  $V_{SET}=1.2V$ .

## 7. System analyses:

Following in the report.

## Design Project 2, ECE5330/EVE5430/AET5330

Course Number: ECE 5330/EVE 5430/AET 5330

Title: Modeling and Control of Power Electronics and Electric Vehicle  
Powertrains

Instructor: Le Yi Wang, Professor

Student Name: Zhenyu Qu

Student ID: 004298218

I have not received, nor have I given, any help and assistance on this project.

Signature:

Date: