CSC 122 001 Computer Science II
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Documentation for Two-Child Tree Node Removal from a Binary Tree.

The following documentation is for this snippet:

```
// Move to right subtree.
attachPoint = tree->right;

// Locate the smallest node in the right subtree
// by moving as far to the left as possible.
while (attachPoint->left != nullptr)
    attachPoint = attachPoint->left;

// Attach the left subtree of the original tree
// as the left subtree of the smallest node
// in the right subtree.
attachPoint->left = tree->left;

// Replace the original tree with its right subtree.
tree = tree->right;
```

For the full source, see class IntBinaryTree implementation from text

The removal of tree node with two children from a binary tree is done as follows:

- 1. The pointer, attachPoint, finds the leftmost node of the right subtree of the node to be deleted.
- 2. The left subtree of the node to be deleted is attached to the leftmost node of right subtree.
- 3. The node to be deleted is replaced by its right subtree.
- 4. The node to be deleted is deleted from memory.

The following code is given to see this in action:

```
#include <iostream>
#include "IntBinaryTree.h"
using namespace std;

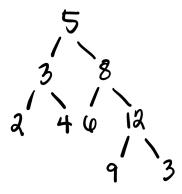
int main()
{
    IntBinaryTree tree;

    cout << "Inserting the numbers 5 8 3 12 9.\n";
    tree.insert(5);
    tree.insert(8);
    tree.insert(3);
    tree.insert(12);
    tree.insert(9);
    cout << "Inserting additional numbers, 2 4 6 13, to create two-children nodes.\n";
    // Adding the following numbers to create nodes with two children.
    // Nodes with two children are: 5, 3, 8, 12.</pre>
```

```
tree.insert(2);
    tree.insert(4);
    tree.insert(6);
    tree.insert(13);
    cout << "\nHere are the values in the tree:\n";</pre>
    tree.showInOrder();
    cout << "\nHere are the values in pre-order: \n";</pre>
    tree.showPreOrder();
    cout << "\n\nThe delete method has been altered to show \n";</pre>
    cout << "that the method is deleting a node with two children. \n";
    cout << "\nDeleting 8...\n";</pre>
    tree.remove(8);
    cout << "\nDeleting 12...\n";</pre>
    tree.remove(12);
    cout << "\nDeleting 3... \n";</pre>
    tree.remove(3);
    cout << "\nNow, here are the nodes:\n";</pre>
    tree.showInOrder();
    cout << "\nNow, here are the values in pre-order: \n";</pre>
    tree.showPreOrder();
    return 0;
}
The screenshot of runtime is as follows:
 Inserting the numbers 5 8 3 12 9.
 Inserting additional numbers, 2 4 6 13, to create two-children nodes.
 Here are the values in the tree:
 2 3 4 5 6 8 9 12 13
 Here are the values in pre-order:
 5 3 2 4 8 6 12 9 13
 The delete method has been altered to show
 that the method is deleting a node with two children.
 Deleting 8...
 Deleting a node with two children...
 Deleting 12...
 Deleting a node with two children...
 Deleting 3...
 Deleting a node with two children...
 Now, here are the nodes:
 2 4 5 6 9 13
 Now, here are the values in pre-order:
```

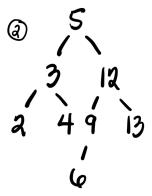
5 4 2 13 9 6

The binary tree after all the insertions should have the following structure:



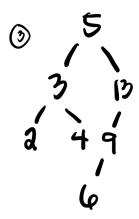
After the first removal of the node 8, the right subtree with node 12 at the head gets promoted and the left subtree with node 6 is attached to node 9.

The new structure is as follows:



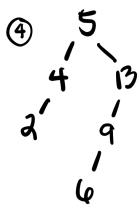
After the second removal (node 12), node 13 gets promoted and the left subtree with node 9 at the head gets attached as the left subtree of node 13.

The new structure is as follows:



After the last removal (node 3), node 4 gets promoted and node 2 gets attached as the left subtree of node 4.

The new structure is as follows:



This matches the pre-order display of the tree after the last three removals.