

# Natural Language Processing with Deep Learning

CS224N/Ling284



John Hewitt

Analysis and Interpretability of Neural NLP



# Course Logistics

## Final Project Report

- Due Saturday, March 14 at 11:59 PM PST
  - 1 late day: Sunday, March 15 at 11:59 PM PST
  - 2 late days: Monday, March 16 at 11:59 PM PST
  - 3 late days: Tuesday, March 17 at **4:30 PM PST**

## Final Project Poster

- Zoom 3-minute poster presentations with 2 TAs and a cohort of ~14 other teams
  - Monday, March 16 at 5PM - 7PM PST
  - Monday, March 16 at 7.30PM - 9:30PM PST
  - Tuesday, March 17 at 9AM - 11AM PST
- Fill out the form on Piazza with your time preferences

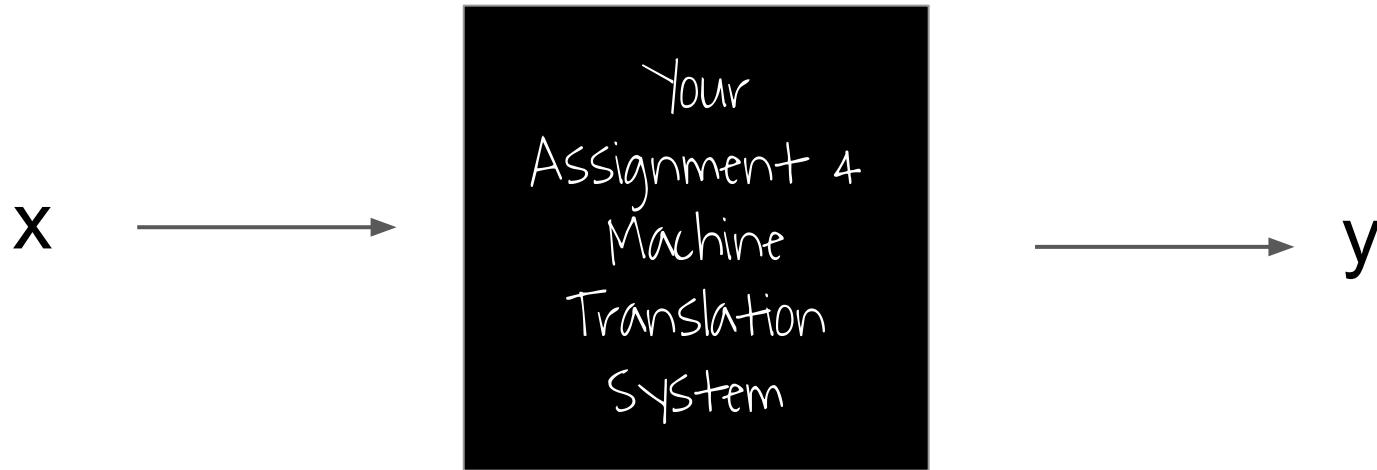


# Lecture Outline

## Lecture 20: Analysis and Interpretability of Neural NLP

- 1. Motivation: what are our models doing? (10 mins)**
2. Neural networks as linguistic test subjects (10 mins)
3. Careful ablation studies and architecture modifications (5 mins)
4. Analysis of inherently interpretable architectures (5 mins)
5. Playing the adversary: breaking NLP models (5 mins)
6. Analyzing representations using supervised methods (35 mins)
7. Aggregating analysis insights across studies (10 mins)

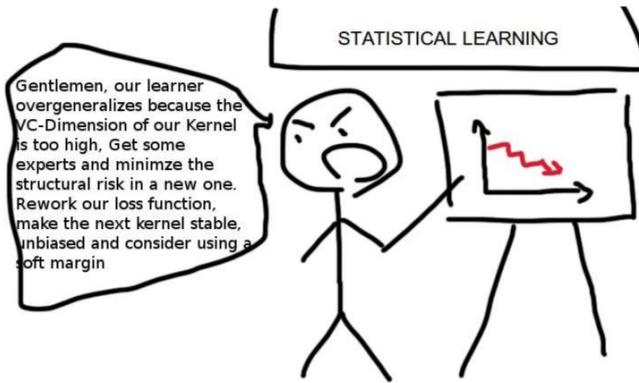
# Motivation: what are our models doing?



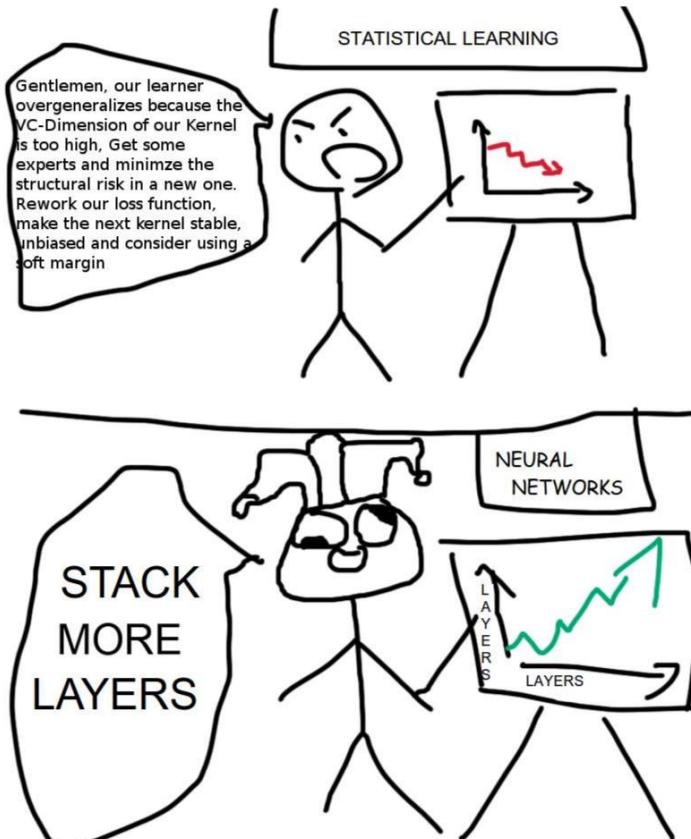
*Fig 1: A black box*

It is not clear what *functions* our algorithms learn, and their complexity precludes exact understanding

# Motivation: how do we make models better?

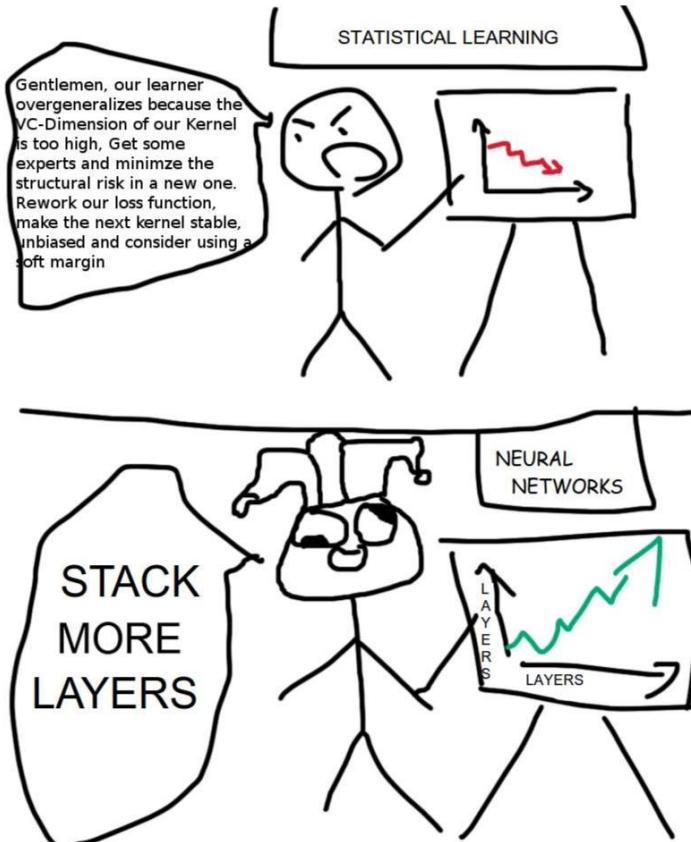


# Motivation: how do we make models better?



[Reddit; source unknown]

# Motivation: how do we make models better?



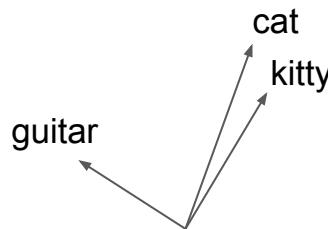
[Reddit; source unknown]



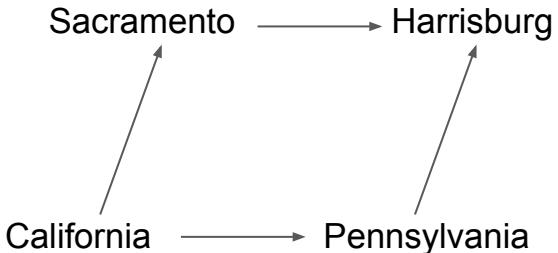
# What we've seen: simple analyses of word2vec

**Bold type: Math property**

*Italic type: interpretation*



We interpret **cosine similarity**  
as *semantic similarity*

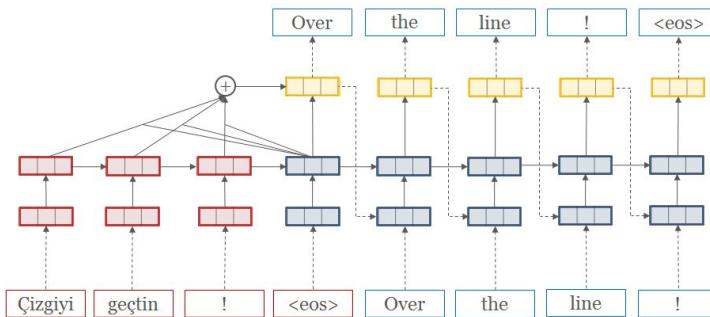


Some *relationships* are encoded  
as **vector differences**

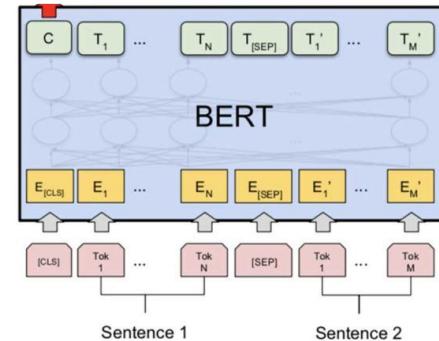
Knowing what *properties* word embeddings have: useful for practitioners!  
Knowing that word embeddings encode *undesirable social biases*: useful  
for everyone!

# Neural networks are worthy subjects of study

## Machine Translation



## Language Modeling



## Question Answering

The first recorded travels by Europeans to China and back date from this time. The most famous traveler of the period was the Venetian Marco Polo, whose account of his trip to "Cambaluc," the capital of the Great Khan, and of life there astounded the people of Europe. The account of his travels, *Il milione* (or, *The Million*, known in English as the *Travels of Marco Polo*), appeared about the year 1299. Some argue over the accuracy of Marco Polo's accounts due to the lack of mentioning the Great Wall of China, tea houses, which would have been a prominent sight since Europeans had yet to adopt a tea culture, as well the practice of foot binding by the women in capital of the Great Khan. Some suggest that Marco Polo acquired much of his knowledge **through contact with Persian traders** since many of the places he named were in Persian.

How did some suspect that Polo learned about China instead of by actually visiting it?

**Answer:** **through contact with Persian traders**

It's wild that any of our models work at all

- Their behavior is an emergent property of *data* and our *design decisions*
- Accuracy on a held out test set is not sufficient to fully characterize them



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# Neural networks as linguistic test subjects



# Neural networks as linguistic test subjects

*Humans*

# Neural networks as linguistic test subjects

## Humans

How do we understand language behavior in **humans**?

One method: *minimal pairs*. *What sounds “okay” to a speaker?*

The chef who made the pizzas **is** ← “Acceptable”

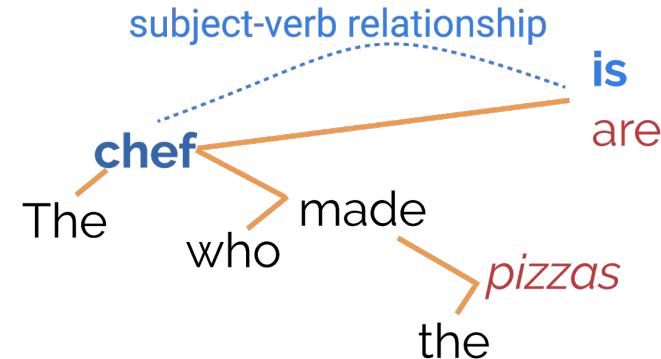
\*The chef who made the pizzas **are** ← “Unacceptable”

Idea: English present-tense verbs *agree in number* with their subject.

The **chef** who made the **pizzas** **is**  
are

agree in number

subject-verb relationship  
The **chef** **is**  
who made **pizzas**  
the



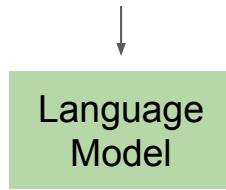
The diagram illustrates the subject-verb agreement in the sentence "The chef who made the pizzas is". It shows the words "The", "chef", "who", "made", "the", and "pizzas" arranged in a tree-like structure. A solid orange line connects "chef" to "made", and another solid orange line connects "pizzas" to "is". Dotted blue lines connect "The", "who", and "the" to their respective words ("chef", "made", and "pizzas"). The word "is" is written in blue, while "are" is written in red, corresponding to the two versions of the sentence shown above.

# Neural networks as linguistic test subjects

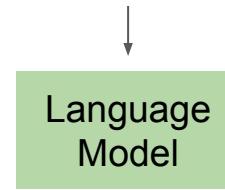
How do we understand language behavior in **language models**?

One method: *minimal pairs. Is the acceptable sentence higher-probability?*

The chef who made the pizzas is



The chef who made the pizzas are



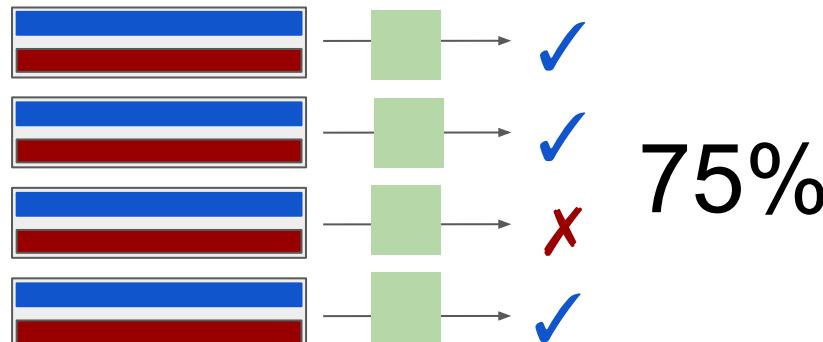
$$0.0001 > 0.00000001$$

**Premise:** A language model should assign higher probability to the acceptable sentence in any minimal pair.

# Neural networks as linguistic test subjects

Steps to conduct a *minimal pairs* test on a language model:

1. Gather or construct a test set of minimal pairs which require specific aspects of understanding to distinguish.
2. Run your language model on the pairs, and report percent of pairs the model predicts as desired.



# Neural networks as linguistic test subjects

Example: Do LMs show Subject-Verb number agreement across attractors?

The chef who made the pizzas and talked to the customers is

<i>subject</i>	<i>attractor</i>	<i>attractor verb</i>
----------------	------------------	-----------------------

	<b>n=0</b>	<b>n=1</b>	<b>n=2</b>	<b>n=3</b>	<b>n=4</b>
Random	50.0	50.0	50.0	50.0	50.0
Majority	32.0	32.0	32.0	32.0	32.0
LSTM, H=50 <sup>†</sup>	6.8	32.6	≈50	≈65	≈70
Our LSTM, H=50	2.4	8.0	15.7	26.1	34.65
Our LSTM, H=150	1.5	4.5	9.0	14.3	17.6
Our LSTM, H=250	1.4	3.3	5.9	<b>9.7</b>	13.9
Our LSTM, H=350	<b>1.3</b>	<b>3.0</b>	<b>5.7</b>	<b>9.7</b>	<b>13.8</b>
1B Word LSTM (repl)	2.8	8.0	14.0	21.8	20.0
Char LSTM	<b>1.2</b>	5.5	11.8	20.4	27.8

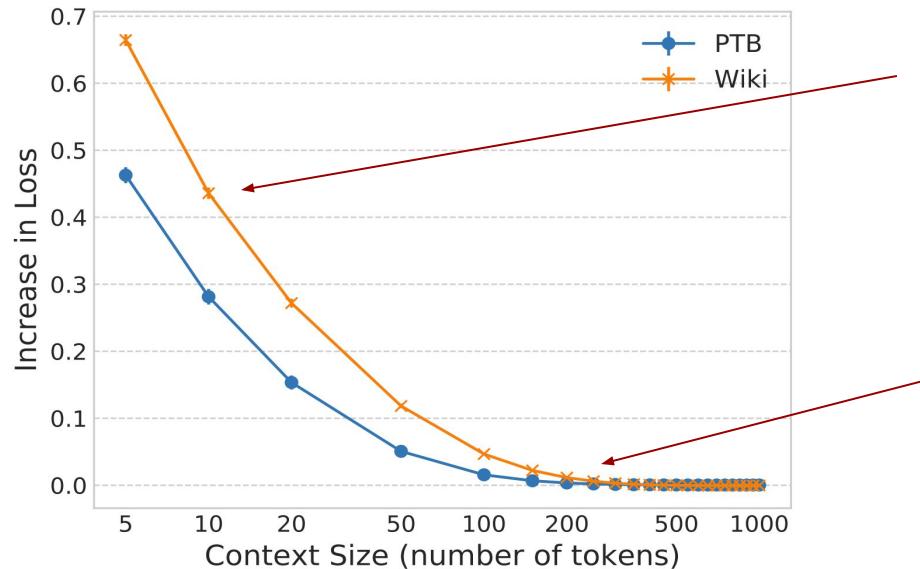
# of attractors between subject and verb

Error rate on a large corpus of minimal pairs

LMs do *really* well!?

# Neural networks as linguistic test subjects

Method: Modify the test set to remove long contexts, or replace them with longer words. Evaluate whether the LM perplexity changes.



Only giving the LM 10 words of context at test time makes the test error go up.

Only giving the LM 250 words of context *doesn't change its loss*, so it's not using contexts longer than 250 words much.



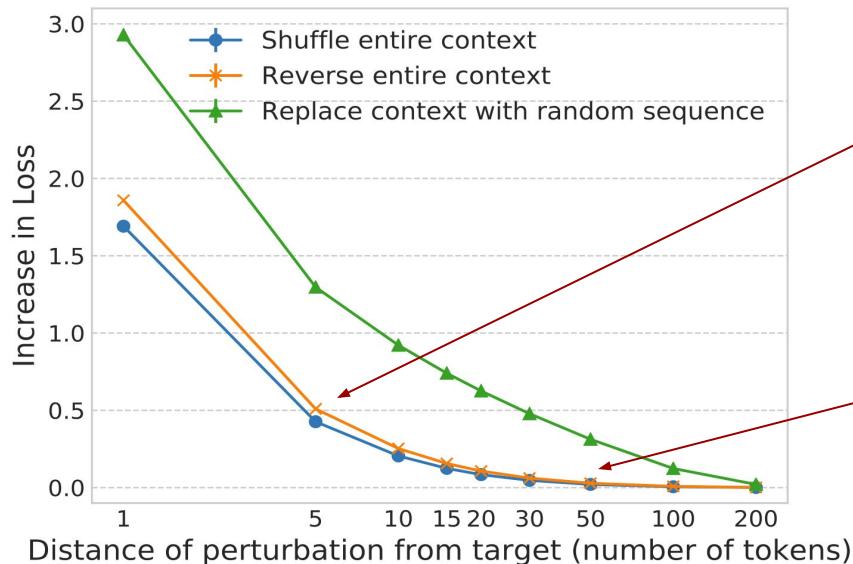
# Neural networks as linguistic test subjects

Question: How does an LSTM language model use its long-distance contexts?

Method: Modify the test set to remove long contexts, or replace them with longer words. Evaluate whether the LM perplexity changes.

# Neural networks as linguistic test subjects

Method: Modify the test set to remove long contexts, or replace them with longer words. Evaluate whether the LM perplexity changes.



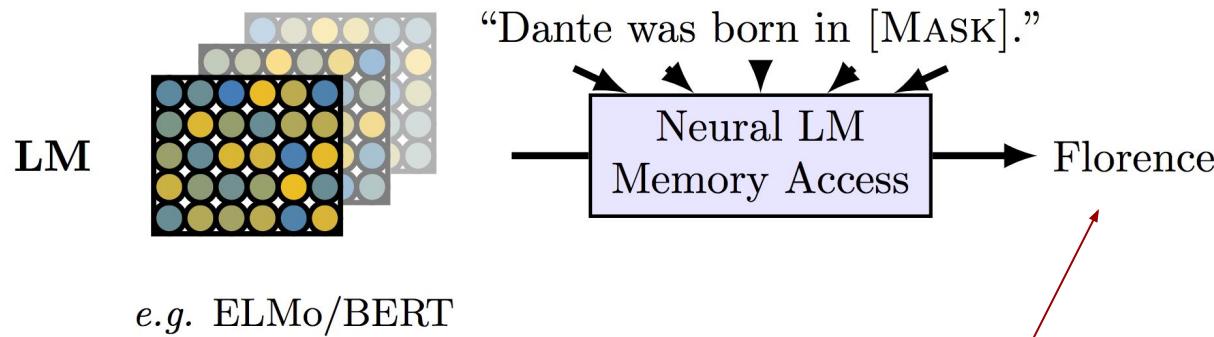
Shuffling the order of the context further than 5 words away increases loss, so the LM cares about word order past 5 words.

Shuffling the word order of the context further than 50 words away *doesn't* increase loss, so the LM treats words 50-250 effectively as a bag-of-words.

# Neural networks as linguistic test subjects

Question: Do LMs memorize factual relations?

Method:



Check if most likely word under the LM is a correct answer.

**Eval:** % of these relations for which this holds.

# Neural networks as linguistic test subjects

Question: Do LMs memorize factual relations?

Evaluation:

Baseline: Return word that shows up most with the subject (Dante) and the relation (born in)

BERT-base and BERT-large: memorize a surprising number of facts

Corpus	Relation	Statistics		Baselines		KB		LM					
		#Facts	#Rel	Freq	DrQA	RE <sub>n</sub>	RE <sub>o</sub>	Fs	Txl	Eb	E5B	Bb	Bl
Google-RE	birth-place	2937	1	4.6	-	3.5	13.8	4.4	2.7	5.5	7.5	14.9	<b>16.1</b>
	birth-date	1825	1	1.9	-	0.0	<b>1.9</b>	0.3	1.1	0.1	0.1	1.5	1.4
	death-place	765	1	6.8	-	0.1	7.2	3.0	0.9	0.3	1.3	13.1	<b>14.0</b>
	Total	5527	3	4.4	-	1.2	7.6	2.6	1.6	2.0	3.0	9.8	<b>10.5</b>



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1. Motivation: what are our models doing?
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# Viewing model studies as network analysis

Question: What is necessary, or even *good*, about my network design?

Method: Make targeted model changes; observe validation accuracy

Ex: The Transformer interleaves *self-attention* with *feed-forward* layers





# Viewing model studies as network analysis

Question: What is necessary, or even good, about my network design?

Method: Make targeted model changes; observe validation accuracy

Ex: The Transformer interleaves *self-attention* with *feed-forward* layers

But what if we re-ordered them?

ssssssssfsfsfsfsfsfsfsfsfffffff → **17.96 PPL**  
*(Better!)*

## Bunch of self-attention

## Bunch of feed-forward

[Press et al., 2019]



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# Analysis of “interpretable” architectures

Some architectures have components that lend themselves to inspection

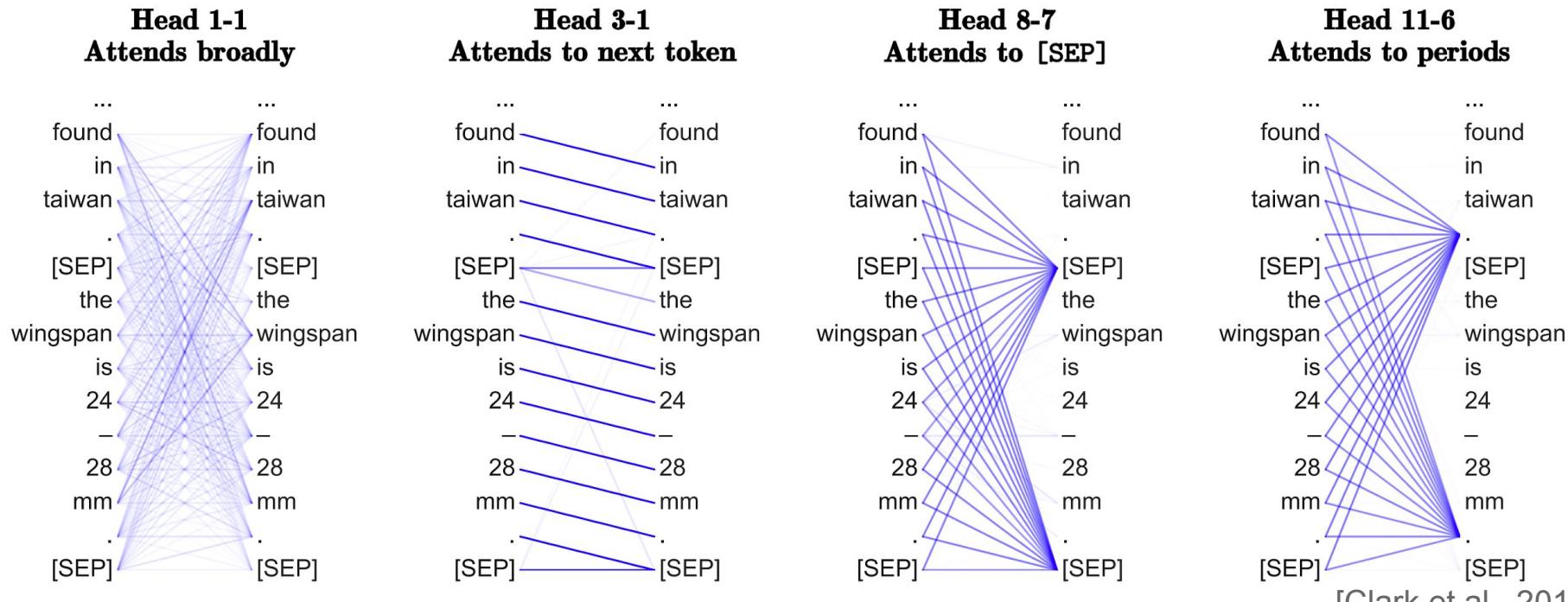
Example: Try to characterize each attention head of BERT.



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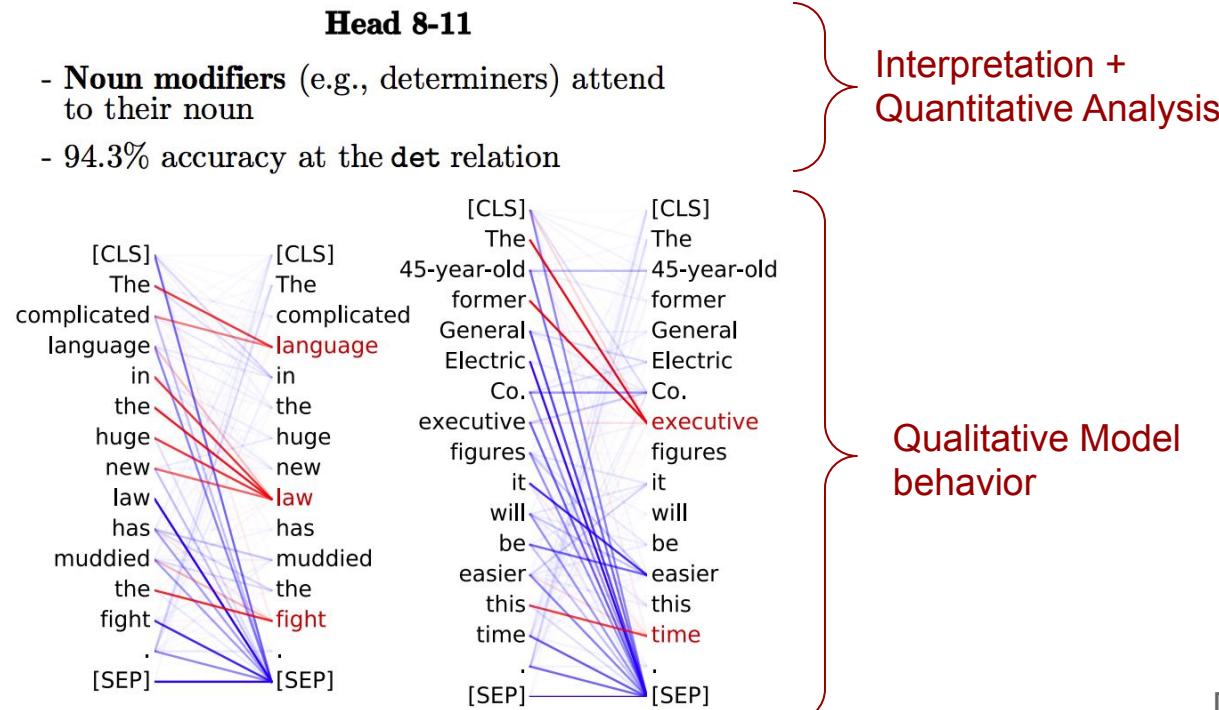
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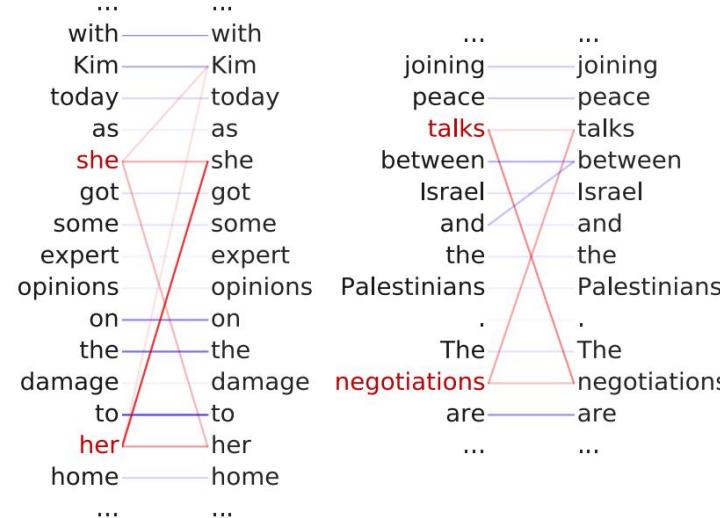
# Analysis of “interpretable” architectures

Some architectures have components that lend themselves to inspection

Example: Try to characterize each attention head of BERT.

## Head 5-4

- **Coreferent** mentions attend to their antecedents
- 65.1% accuracy at linking the head of a coreferent mention to the head of an antecedent



Interpretation +  
Quantitative Analysis

Qualitative Model  
behavior

# Understanding representations by inspection

Are individual hidden units in recurrent neural networks interpretable?

Cell sensitive to position in line:

The sole importance of the crossing of the Berezina lies in the fact  
that it plainly and indubitably proved the fallacy of all the plans for  
cutting off the enemy's retreat and the soundness of the only possible  
line of action--the one Kutuzov and the general mass of the army  
demanded--namely, simply to follow the enemy up. The French crowd fled  
at a continually increasing speed and all its energy was directed to  
reaching its goal. It fled like a wounded animal and it was impossible  
to block its path. This was shown not so much by the arrangements it  
made for crossing as by what took place at the bridges. When the bridges  
broke down, unarmed soldiers, people from Moscow and women with children  
who were with the French transport, all--carried on by vis inertiae--  
pressed forward into boats and into the ice-covered water and did not,  
surrender.



# Understanding representations by inspection

Are individual hidden units in recurrent neural networks interpretable?

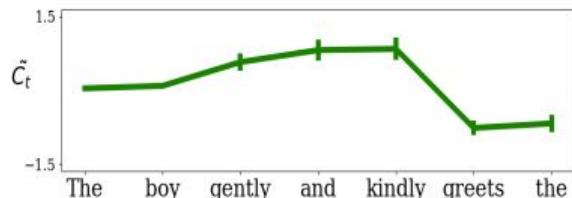
Cell that turns on inside quotes:

"You mean to imply that I have nothing to eat out of.... On the contrary, I can supply you with everything even if you want to give dinner parties," warmly replied Chichagov, who tried by every word he spoke to prove his own rectitude and therefore imagined Kutuzov to be animated by the same desire.

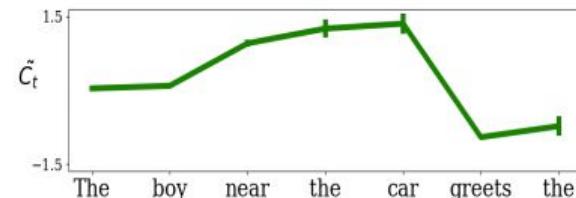
Kutuzov, shrugging his shoulders, replied with his subtle penetrating smile: "I meant merely to say what I said."

# Understanding representations by inspection

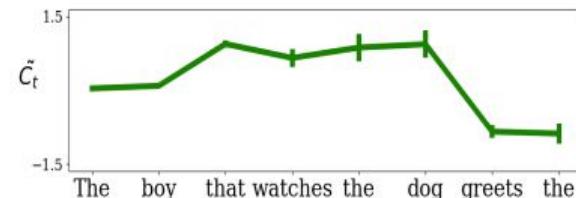
Are individual hidden units in recurrent neural networks interpretable?



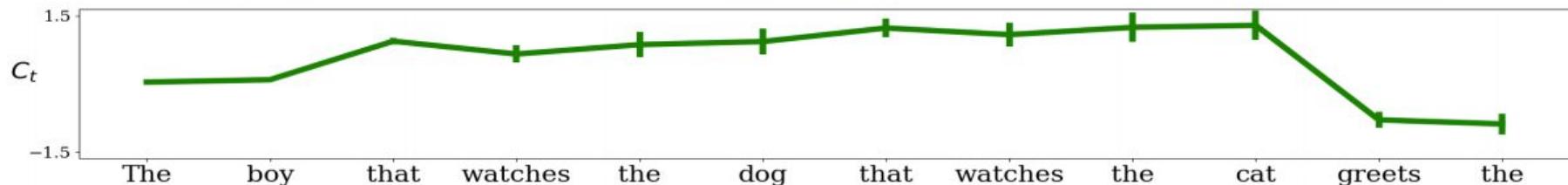
(a) 2Adv



(b) nounPP



(c) subject relative



Interpretation: this LSTM cell unit fires approximately between a subject and its verb



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# Understanding models by breaking them

Question: Are our models robust to innocuous changes in their input?  
By robust, in this case we mean their outputs do not change.

**Article:** Super Bowl 50

**Paragraph:** *"Peyton Manning became the first quarterback ever to lead two different teams to multiple Super Bowls. He is also the oldest quarterback ever to play in a Super Bowl at age 39. The past record was held by John Elway, who led the Broncos to victory in Super Bowl XXXIII at age 38 and is currently Denver's Executive Vice President of Football Operations and General Manager."*

The performance of this QA model on this input looks good!

**Question:** *"What is the name of the quarterback who was 38 in Super Bowl XXXIII?"*

**Original Prediction:** John Elway



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**Question:** *"What is the name of the quarterback who was 38 in Super Bowl XXXIII?"*

**Original Prediction:** *John Elway*

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This sentence is irrelevant;  
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**Question:** *"What is the name of the quarterback who was 38 in Super Bowl XXXIII?"*

**Original Prediction:** John Elway

**Prediction under adversary:** Jeff Dean

The performance of this QA model on this input looks good!

This sentence is irrelevant;  
adding it does not change the answer.

But it changes the model's prediction :(

Interpretation: model is not really working



# Understanding models by breaking them

Question: Are our models robust to innocuous changes in their input?

In the United States especially, several high-profile cases such as Debra LaFave, Pamela Rogers, and Mary Kay Letourneau have caused increased scrutiny on teacher misconduct.

(a) Input Paragraph

The performance of this QA model on this input looks good!

**Q:** What has been the result of this publicity?

**A:** increased scrutiny on teacher misconduct

(b) Original Question and Answer

# Understanding models by breaking them

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In the United States especially, several high-profile cases such as Debra LaFave, Pamela Rogers, and Mary Kay Letourneau have caused increased scrutiny on teacher misconduct.

(a) Input Paragraph

**Q:** What has been the result of this publicity?

**A:** increased scrutiny on teacher misconduct

(b) Original Question and Answer

**Q:** What haL been the result of this publicity?

**A:** teacher misconduct

(c) Adversarial Q & A (Ebrahimi et al., 2018)

The performance of this QA model on this input looks good!

This typo is annoying, but a reasonable language learner would be robust to it.

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(c) Adversarial Q & A (Ebrahimi et al., 2018)

**Q:** What's been the result of this publicity?

**A:** teacher misconduct

(d) Semantically Equivalent Adversary

The performance of this QA model on this input looks good!

This typo is annoying, but a reasonable language learner would be robust to it.

Changing *what has* to *what's* should never change the answer!



# Understanding models by breaking them

Question: Are our models robust to typos or noise in their input?



# Understanding models by breaking them

Question: Are ~~our~~ *my* models robust to typos or noise in their input?

*Humans*



# Understanding models by breaking them

Question: Are our models robust to typos or noise in their input?

Humans

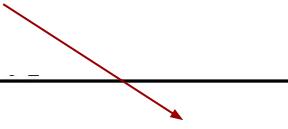
“Aoccdrnig to a rscheearch at Cmabrigde Uinervtisy, it deosn’t mttaer in waht oredr the ltteers in a wrod are, the olny iprmoetnt tihng is taht the frist and lsat ltteer be at the rghit pclae.”

Just 1 data point/meme, but interpretation: humans are!

# Understanding models by breaking them

Question: Are our models robust to typos or noise in their input?

BLEU on clean text



Vanilla		
French	charCNN	42.54
German	charCNN	34.79
	char2char	29.97
	Nematus	34.22
Czech	charCNN	25.99
	char2char	25.71
	Nematus	29.65

# Understanding models by breaking them

Question: Are our models robust to typos or noise in their input?

		Synthetic					
		Vanilla	Swap	Mid	Rand	Key	Nat
French	charCNN	42.54	10.52	9.71	1.71	8.26	17.42
German	charCNN	34.79	9.25	8.37	1.02	6.40	14.02
	char2char	29.97	5.68	5.46	0.28	2.96	12.68
	Nematus	34.22	3.39	5.16	0.29	0.61	10.68
Czech	charCNN	25.99	6.56	6.67	1.50	7.13	10.20
	char2char	25.71	3.90	4.24	0.25	2.88	11.42
	Nematus	29.65	2.94	4.09	0.66	1.41	11.88

BLEU on clean text

BLEU on data with  
noise like we just saw

BLEU on data with natural  
noise (real misspellings, +)



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# Understanding representations by probing

Hypothesis:

Neural models, especially large ones like BERT, perform well without any explicit linguistic supervision in part because they learn similar notions themselves.

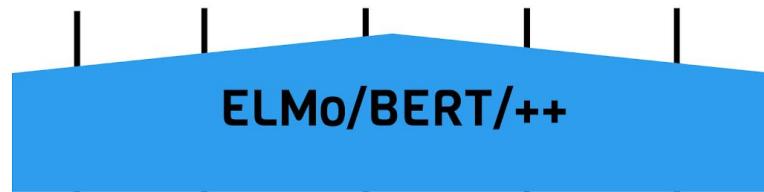
Question:

Do neural networks' internal representations encode linguistic notions of structure, like *parts-of-speech*, *dependency trees*, *named entities*?

# Probing: supervised analysis of representations

*Does my network make task (e.g., part-of-speech) labels accessible?*

The chef made five pizzas

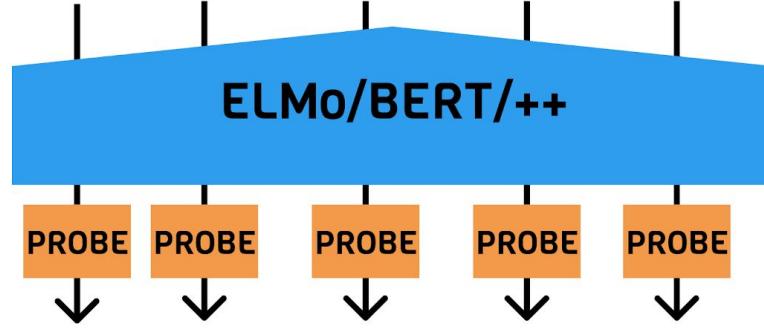


# Probing: supervised analysis of representations

*Does my network make task (e.g., part-of-speech) labels accessible?*

**Choose** a function family  
to decode the task. (e.g., linear)

The chef made five pizzas

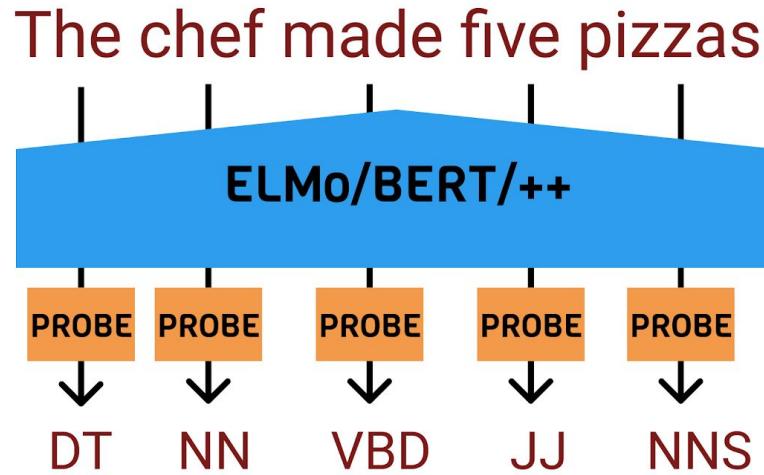


# Probing: supervised analysis of representations

*Does my network make task (e.g., part-of-speech) labels accessible?*

**Choose** a function family  
to decode the task. (e.g., linear)

**Train** a function  
representations --> task



# Probing: supervised analysis of representations

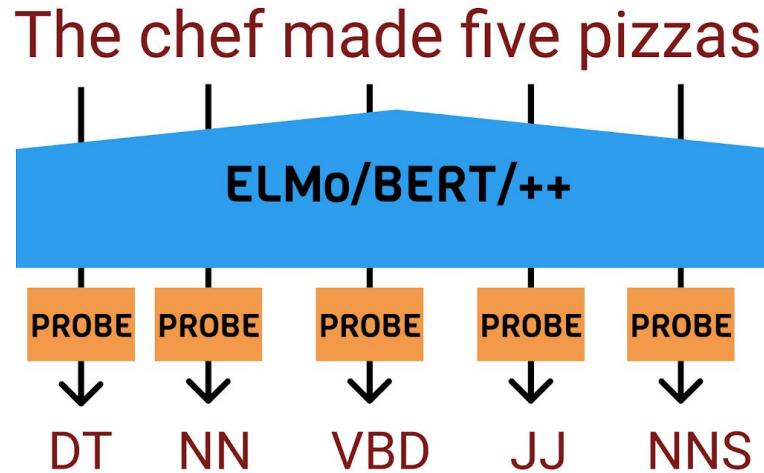
*Does my network make task (e.g., part-of-speech) labels accessible?*

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representations --> task

**Interpret** accuracy  
on held-out data

(Don't fine-tune the model while doing this!)



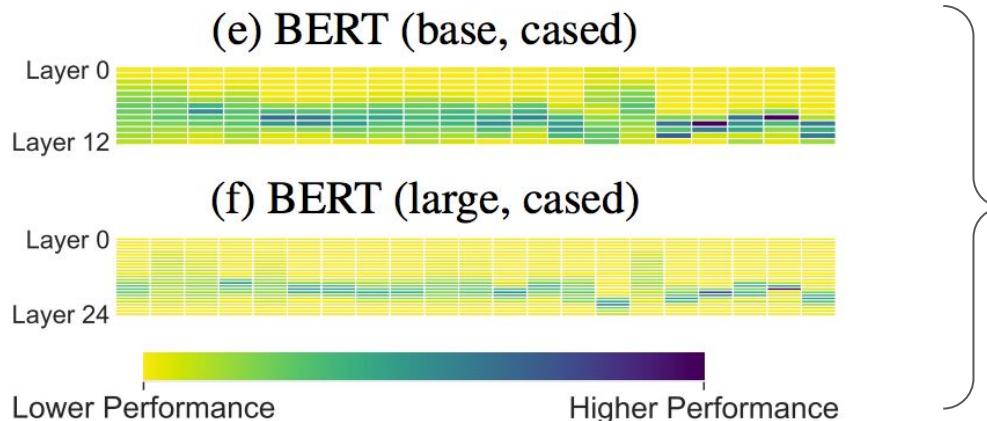
# Understanding representations by probing

Pretrained Representation	POS								Supersense ID		
	Avg.	CCG	PTB	EWT	Chunk	NER	ST	GED	PS-Role	PS-Fxn	EF
BERT (base, cased) best layer	84.09	93.67	96.95	95.21	92.64	82.71	93.72	43.30	<b>79.61</b>	87.94	75.11
BERT (large, cased) best layer	<b>85.07</b>	<b>94.28</b>	96.73	<b>95.80</b>	<b>93.64</b>	<b>84.44</b>	93.83	<b>46.46</b>	79.17	<b>90.13</b>	<b>76.25</b>
GloVe (840B.300d)	59.94	71.58	90.49	83.93	62.28	53.22	80.92	14.94	40.79	51.54	49.70
Previous state of the art (without pretraining)	83.44	94.7	97.96	95.82	95.77	91.38	95.15	39.83	66.89	78.29	77.10

Interpretation 1: BERT's representations, when used as features for a linear classifier, lead to high accuracy on linguistic tasks; this is evidence that BERT makes these properties linearly accessible.

Interpretation 2: BERT-large seems to perform better than BERT-base, indicating that it may learn better representations of linguistic properties.

# Understanding representations by probing

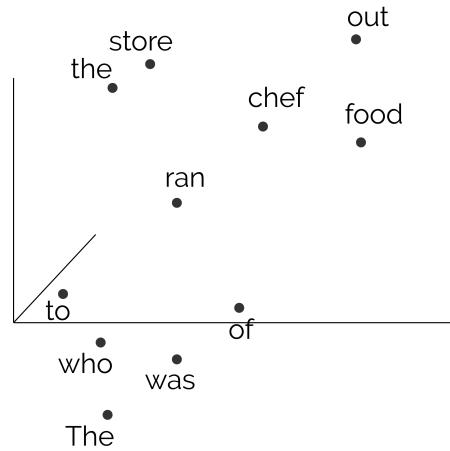


Interpretation: BERT makes linguistic properties most accessible in middle layers

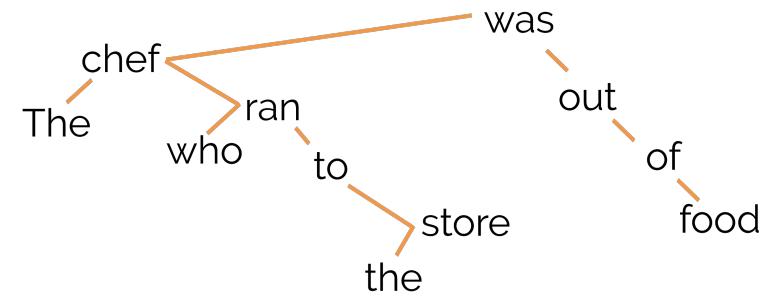
Figure 3: A visualization of layerwise patterns in task performance. Each column represents a probing task, and each row represents a contextualizer layer.

# Understanding representations by probing

Question: Can we ask questions about *structure* in neural representations?



*A neural (vector) representation*

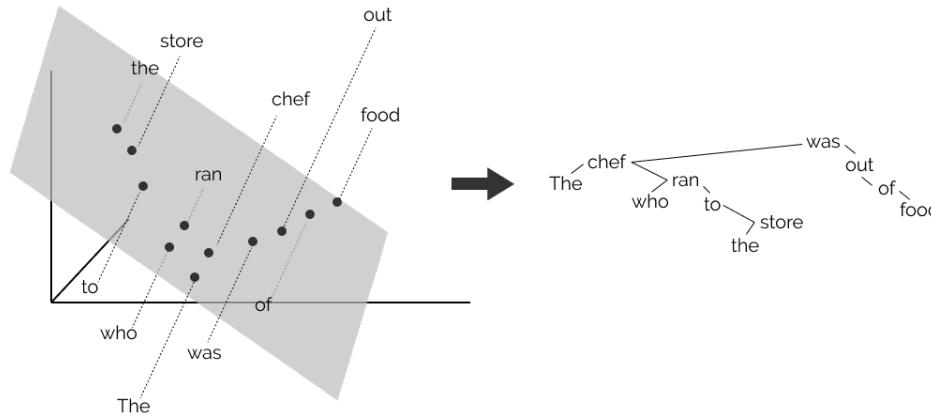


*A structured linguistic representation*

# Understanding representations by probing

Let's walk through a whole analysis paper, step-by-step

## A Structural Probe for Finding Syntax in Word Representations



## ***This work's questions!***

Do *ELMo* and *BERT* encode English dependency trees in their *contextual* representations?

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Do *ELMo* and *BERT* encode English dependency trees in their *contextual* representations?

How do we ask whether vector representations encode trees?

## *This work's questions!*

**tl;dr answers**

Do *ELMo* and *BERT* encode English dependency trees in their *contextual* representations?

How do we ask whether vector representations encode trees?

By **structural probes**: look at the geometry! A hypothesis for syntax in word representations.

## *This work's questions!*

**tl;dr answers**

Do *ELMo* and *BERT* encode English dependency trees in their *contextual* representations?

We provide evidence for yes, *approximately*!

How do we ask whether vector representations encode trees?

By **structural probes**: look at the geometry! A hypothesis for syntax in word representations.

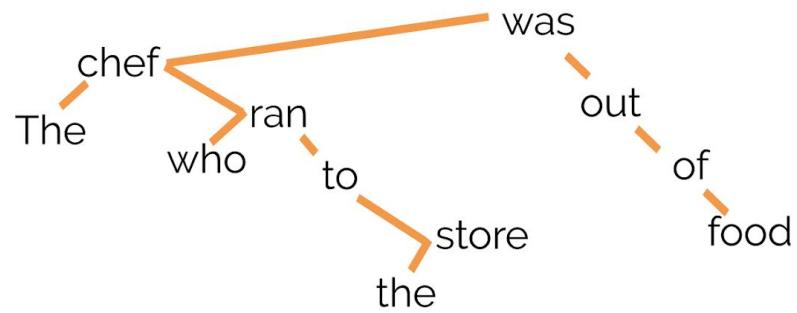
## *Outline*

1. *connecting* **vector spaces** and **trees**
2. The **structural probe** method
3. Results and pictures and fun

# Are vector spaces and trees reconcilable?

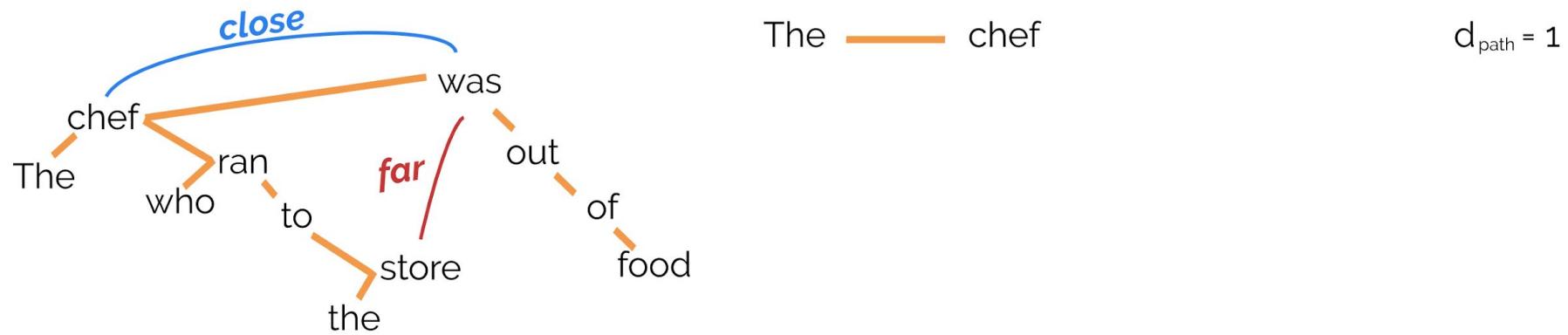
Are **vector space representations** in NLP reconcilable with the **discrete (syntactic) tree** structures hypothesized in language?

The	[.4 -.2 .3]	chef	[.1 .9 -.2]	who	[.3 -.4 .2]	ran	[.7 -.4 0]	to	[.4 0 -.5]	the	[.1 -.6 .2]	store	[.3 .1 -.6]	was	[.1 .9 -.8]	out	[.3 .1 .8]	of	[-.8 .3 -.6]	food	[0 .7 -.9]
-----	-------------------	------	-------------------	-----	-------------------	-----	------------------	----	------------------	-----	-------------------	-------	-------------------	-----	-------------------	-----	------------------	----	--------------------	------	------------------



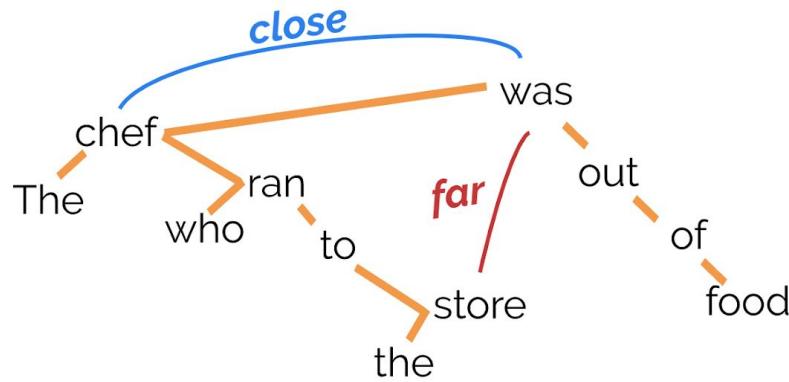
# Distance metrics unify trees and vectors

An **undirected tree** defines a **distance metric** on pairs of words, the path metric:  
the number of edges in the path between the words.



# Distance metrics unify trees and vectors

An **undirected tree** defines a **distance metric** on pairs of words, the path metric:  
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The ——— chef

...

chef ——— ran

chef ——— was

...

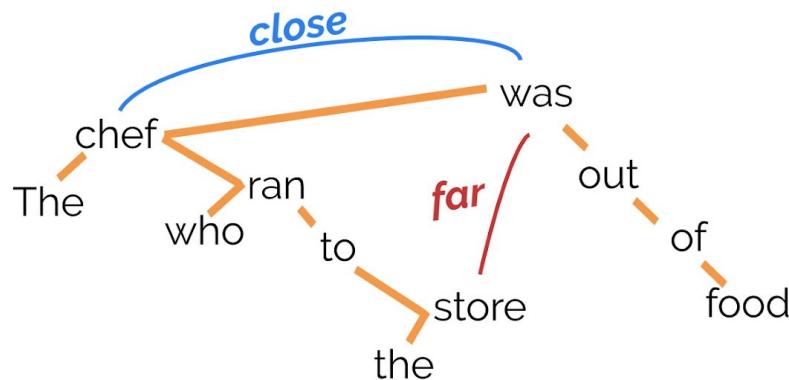
$$d_{\text{path}} = 1$$

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# Distance metrics unify trees and vectors

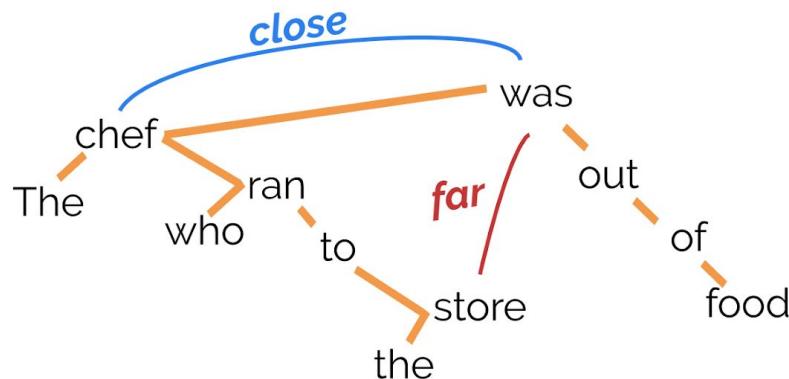
An **undirected tree** defines a **distance metric** on pairs of words, the path metric:  
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The	—	chef	$d_{\text{path}} = 1$
...			
chef	—	ran	$d_{\text{path}} = 1$
chef	—	was	$d_{\text{path}} = 1$
...			
was	—	—	$d_{\text{path}} = 4$
	—	—	
	—	—	
	—	store	

# Distance metrics unify trees and vectors

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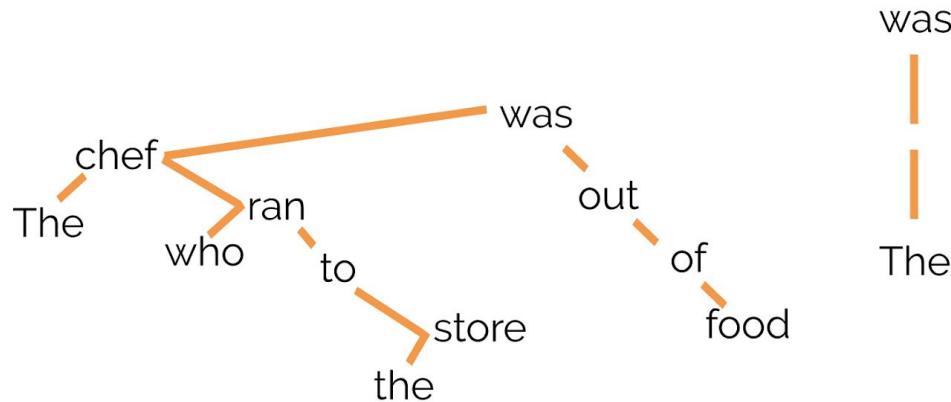


The	—	chef	$d_{\text{path}} = 1$
...			
chef	—	ran	$d_{\text{path}} = 1$
chef	—	was	$d_{\text{path}} = 1$
...			
was	—	—	$d_{\text{path}} = 4$
	—	—	
	—	—	
	—	store	

*The edges of the tree can be recovered by looking at all distance=1 pairs.*

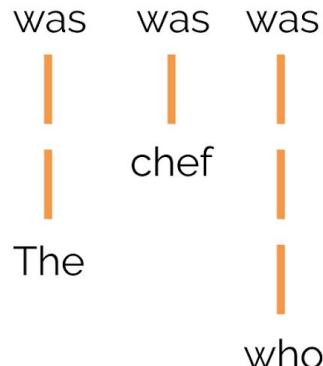
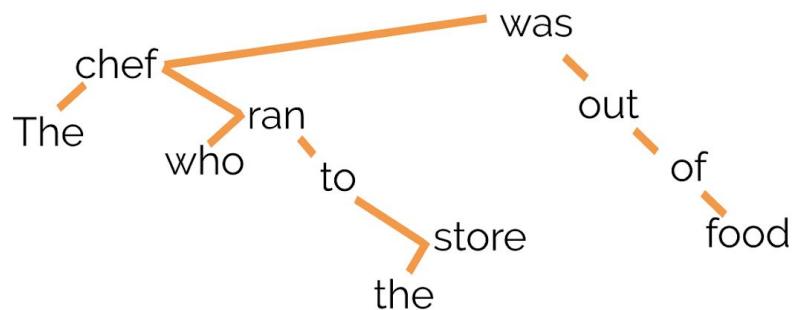
# Norms unify edge directions and vectors

A **rooted tree** defines a **norm** on the words, the parse depth:  
the number of edges from each word to ROOT.



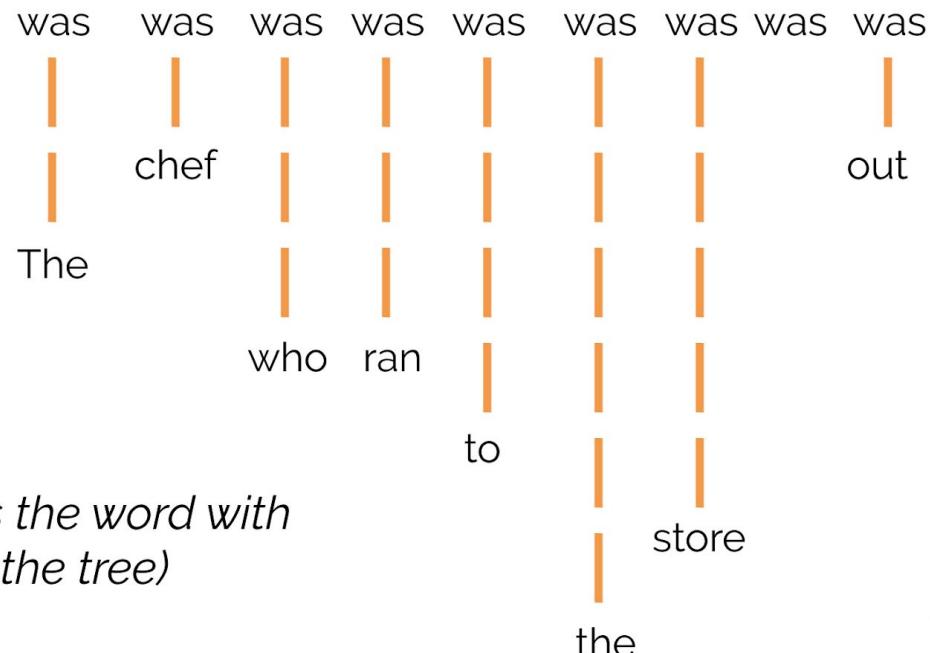
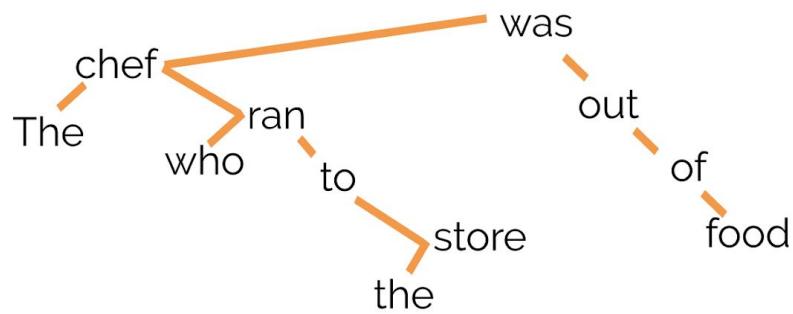
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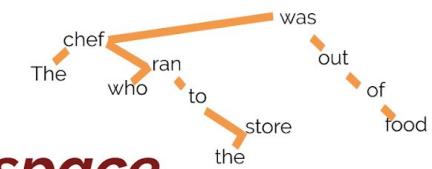
Norms unify edge directions and vectors

A **rooted tree** defines a **norm** on the words, the parse depth:  
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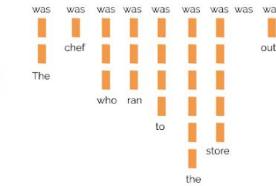


*Each edge is directed towards the word with greater norm (deeper in the tree)*

# *summary*



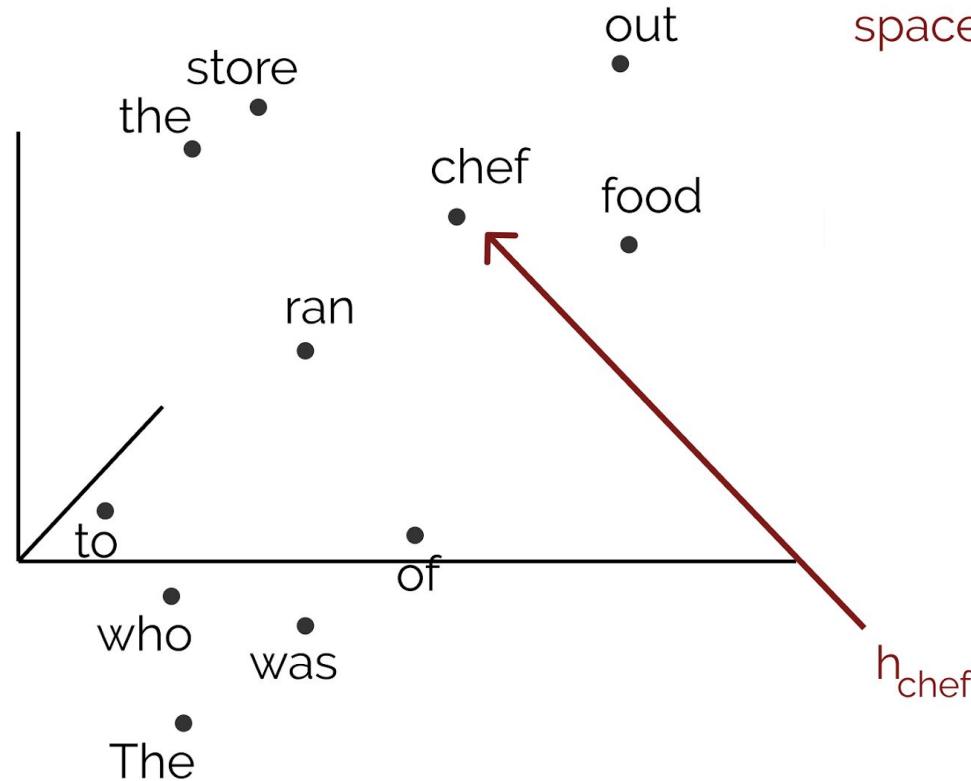
*distance unifies undirected trees and vector space*



*norm unifies edge directions and vector space*

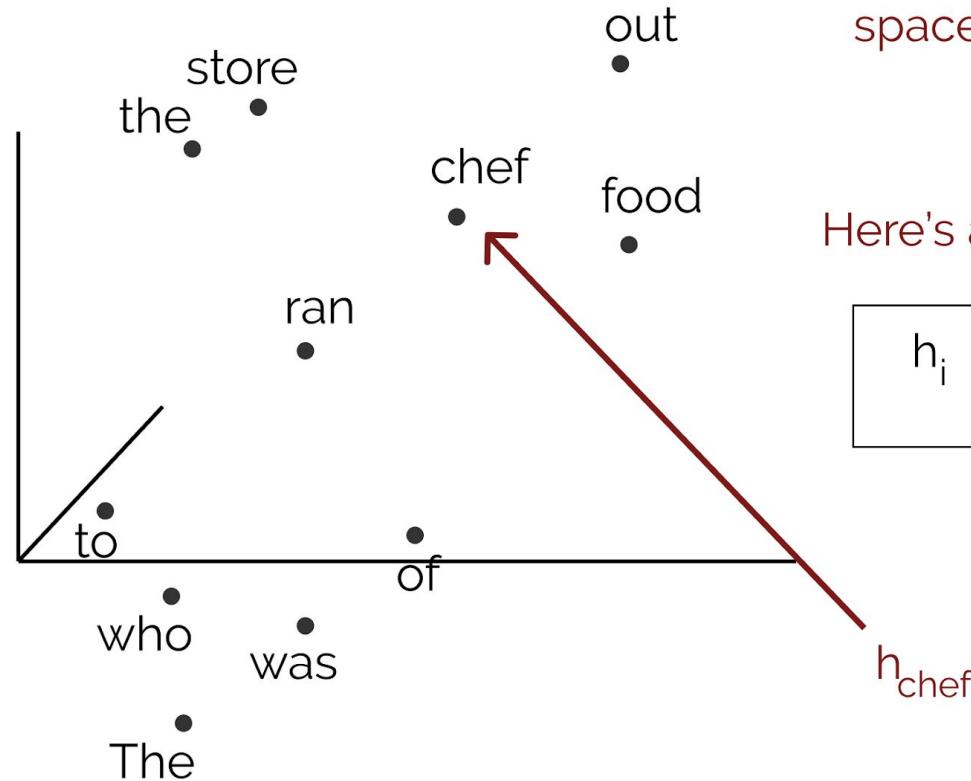
# The *structural probe* method

# Finding trees in vector spaces



We can look for trees in the vector space by looking for their **distances** and **norms** in the space.

# Finding trees in vector spaces

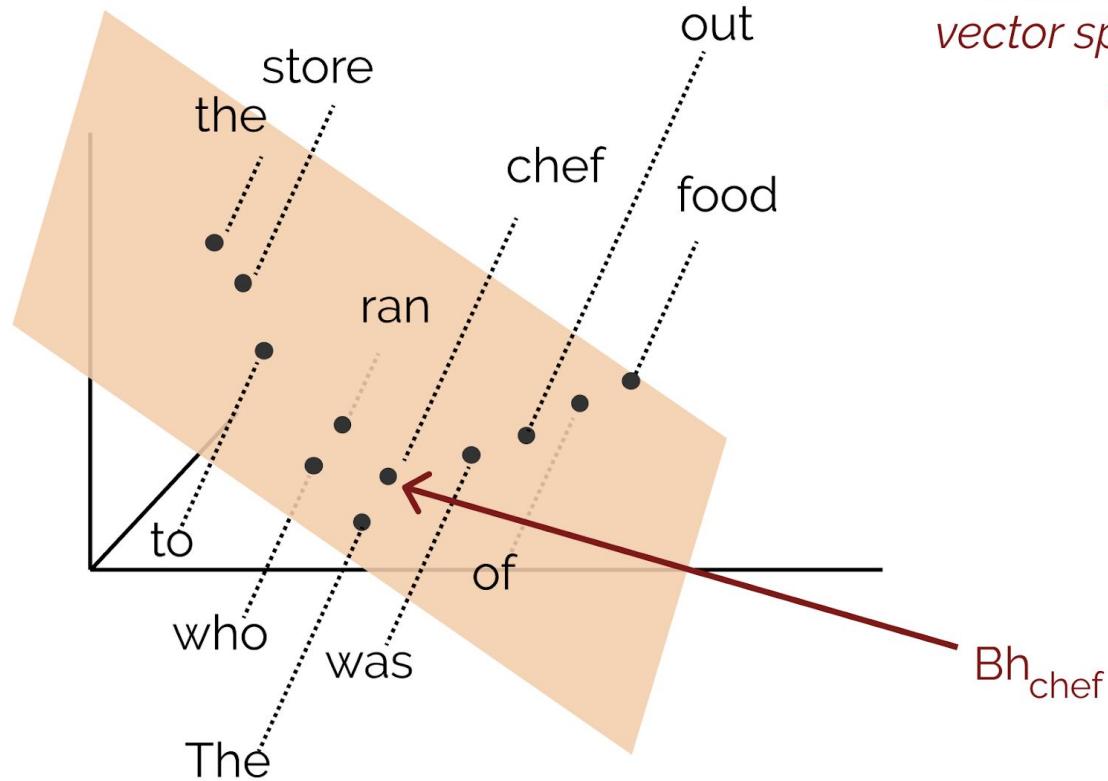


We can look for trees in the vector space by looking for their **distances** and **norms** in the space.

Here's a sentence embedded by a NN!

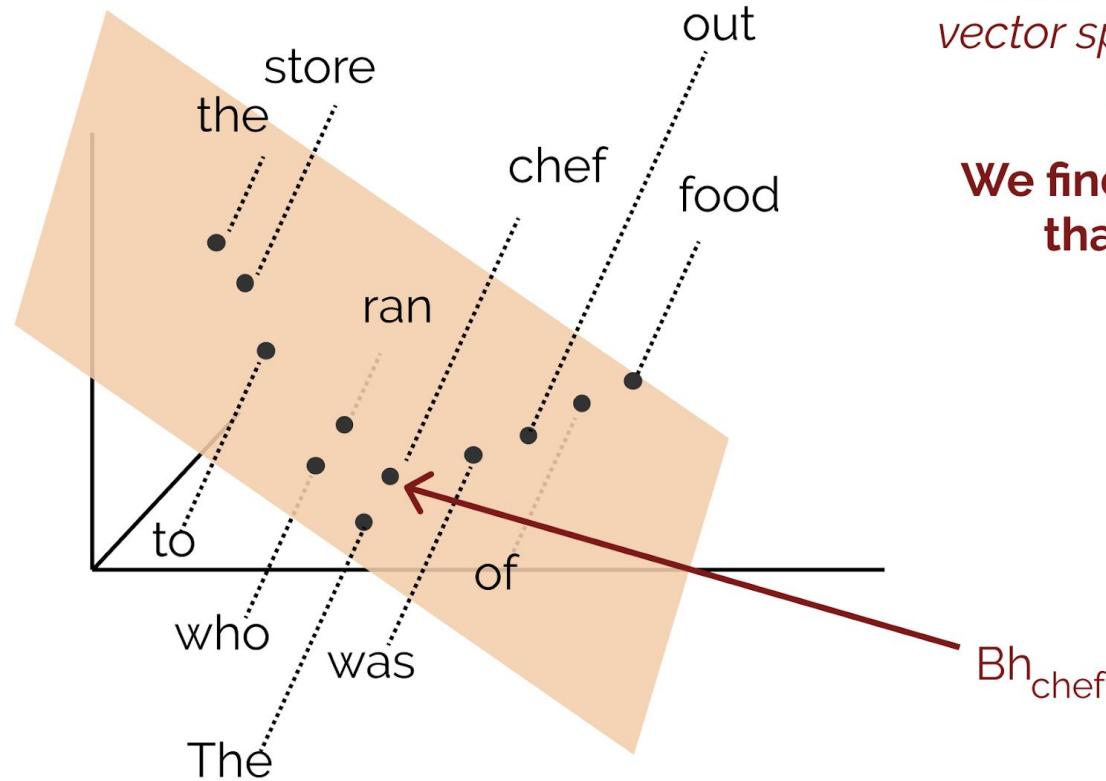
$h_i, h_j$ : vector representation of words  $i$  and  $j$ .

# Finding trees in vector spaces



*We don't expect all dimensions of the vector space to encode syntax -- NNs have a lot to encode!*

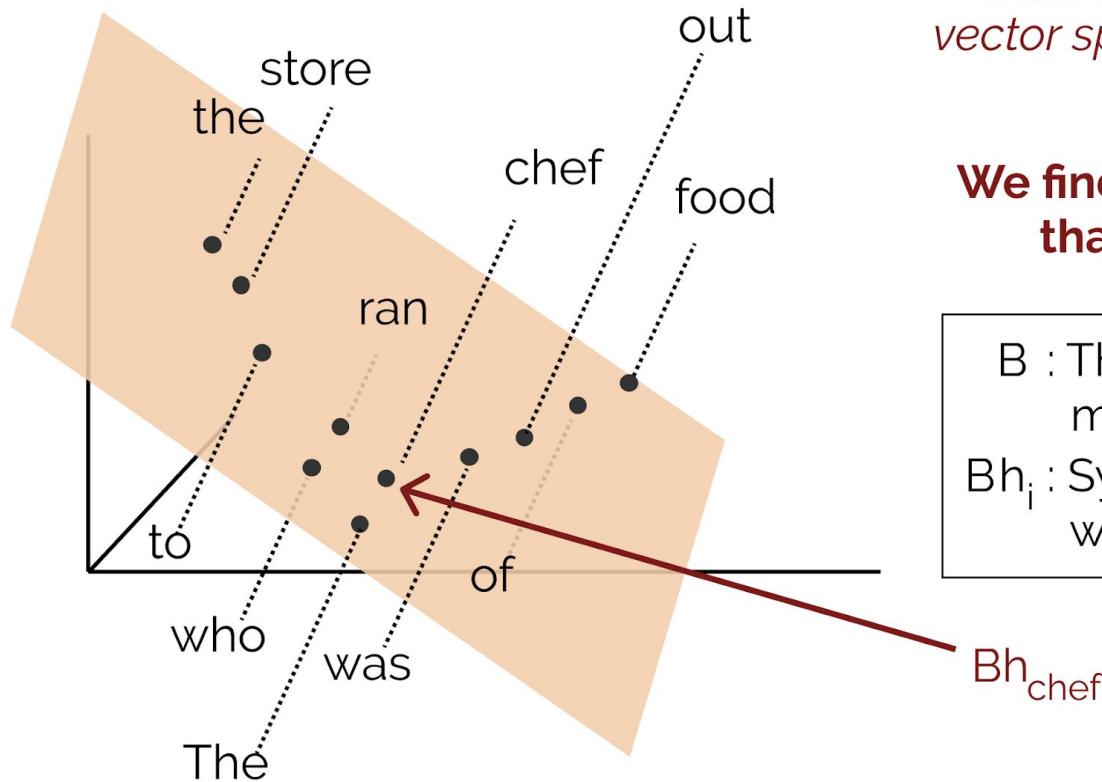
# Finding trees in vector spaces



We don't expect all dimensions of the vector space to encode syntax -- NNs have a lot to encode!

We find the linear transformation that encodes syntax best.

# Finding trees in vector spaces



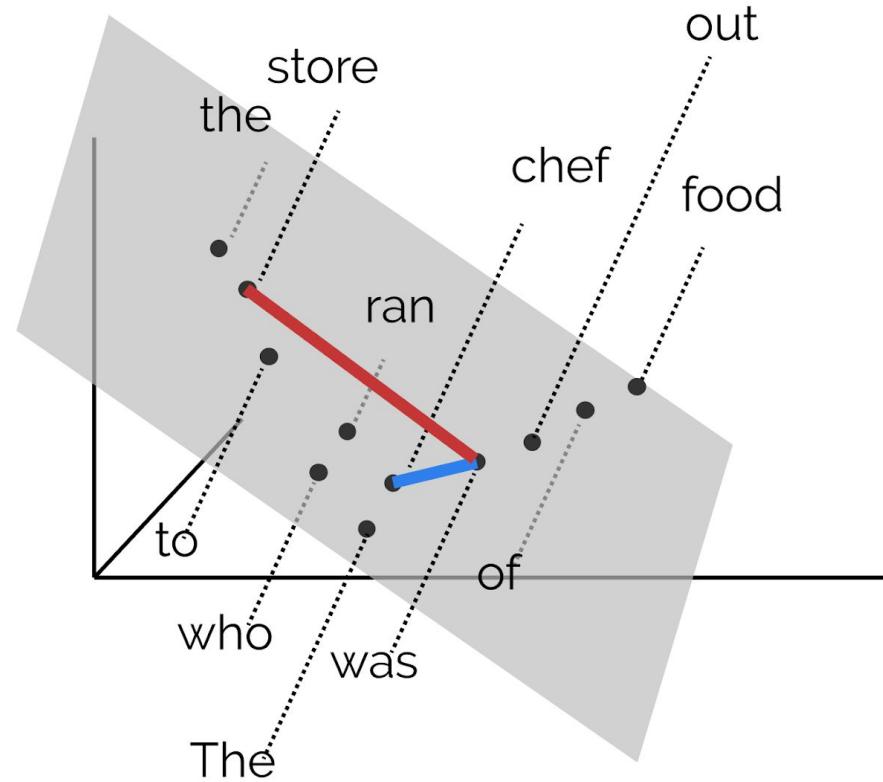
We don't expect all dimensions of the vector space to encode syntax -- NNs have a lot to encode!

We find the linear transformation that encodes syntax best.

$B$  : The syntax transformation matrix

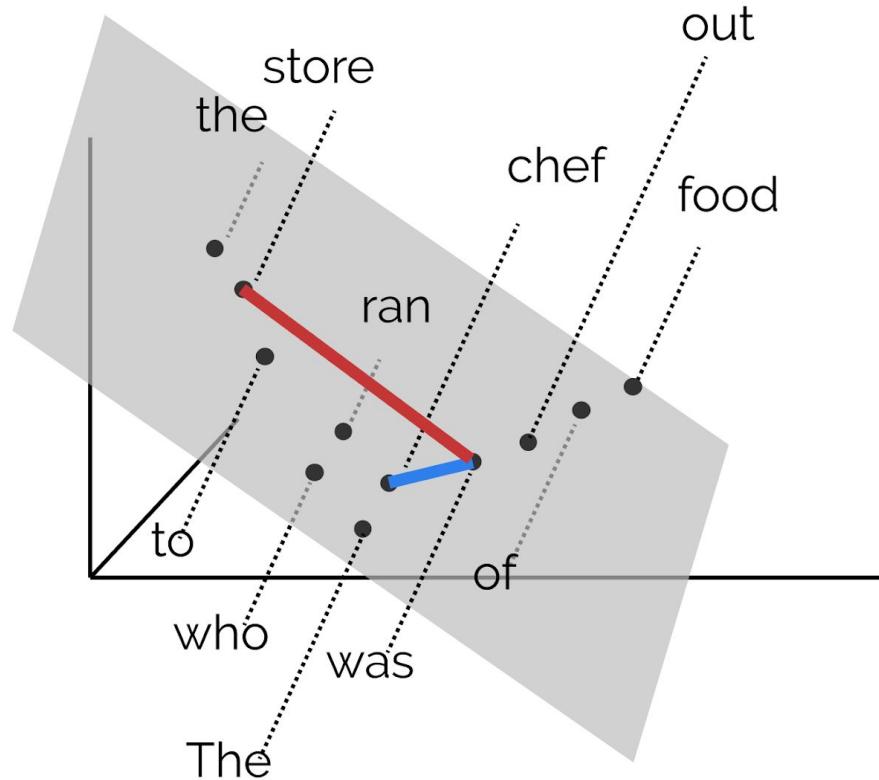
$Bh_i$  : Syntax-transformed vector word representation

# Finding trees in vector spaces



*In the transformed space,  
(squared) L2 distance  
approximates tree distance.*

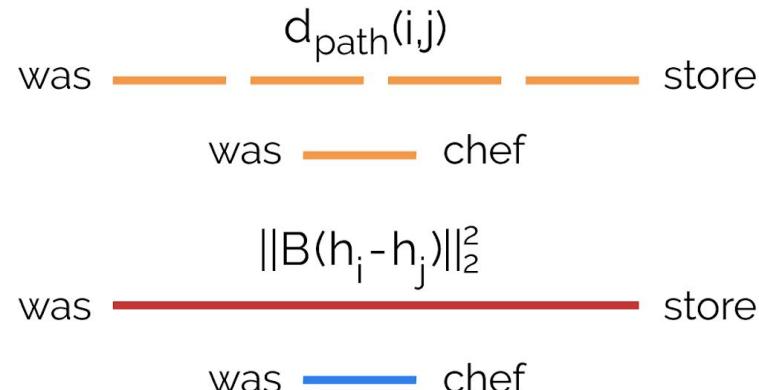
# Finding trees in vector spaces



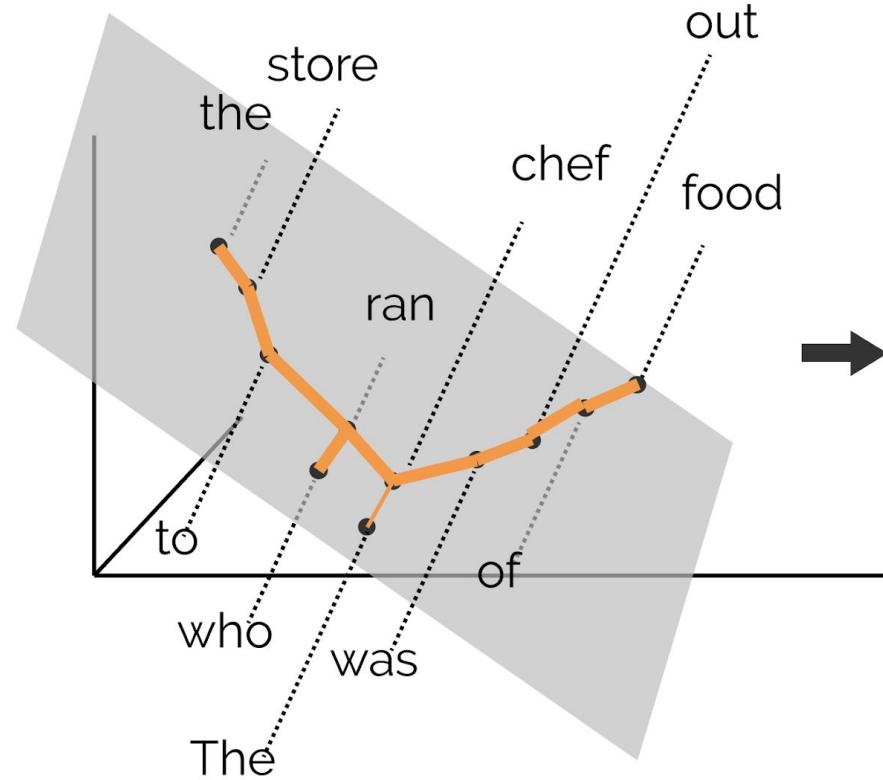
*In the transformed space,  
(squared) L2 distance  
approximates tree distance.*

$d_{\text{path}}(i,j)$  : Tree path distance

$\|B(h_i - h_j)\|_2^2$  : Squared Vector space  
distance ( $\|h_i - h_j\|_B^2$ )

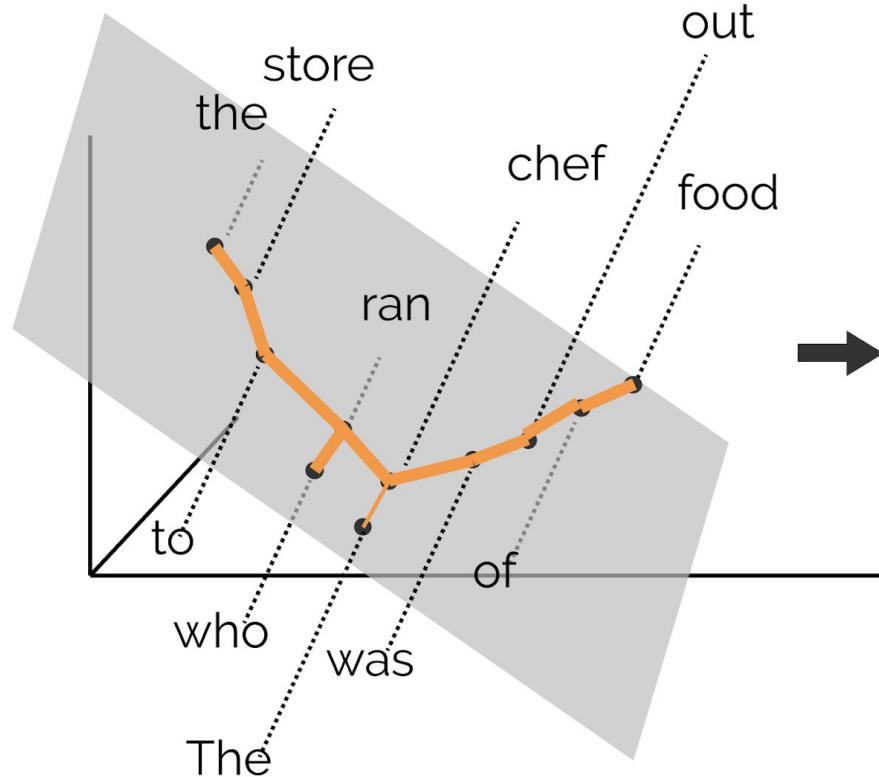


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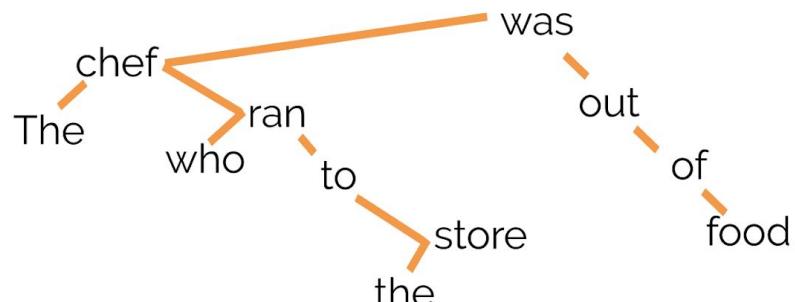


*With this property, a minimum spanning tree in the vector space distance recovers the tree.*

# Finding trees in vector spaces

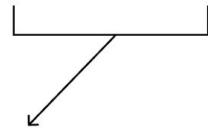


*With this property, a minimum spanning tree in the vector space distance recovers the tree.*

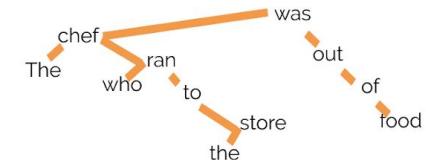


Does BERT encode undirected parse trees  
-> does there exist a *distance* transformation?

$$\arg \min_B$$



Find a single  
transformation  
 $B$

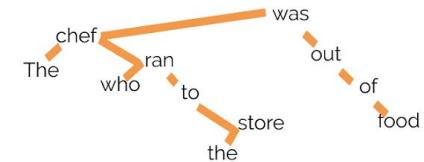


Does BERT encode undirected parse trees  
-> does there exist a *distance* transformation?

$$\arg \min_B \sum_{\ell \in \text{PTB}}$$

Find a single transformation  $B$

such that over all sentences in PTB training



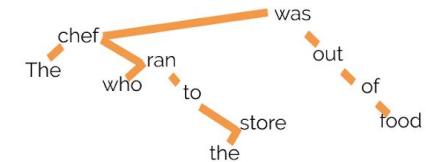
Does BERT encode undirected parse trees  
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$$\arg \min_B \sum_{\ell \in \text{PTB}} \sum_{i,j}$$

Find a single  
transformation  
 $B$

such that over all  
sentences in PTB  
training

Over all word  
pairs in each  
sentence



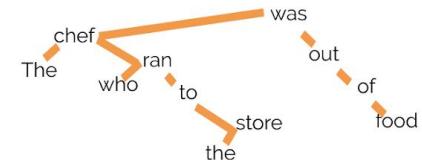
# Does BERT encode undirected parse trees -> does there exist a *distance* transformation?

$$\arg \min_B \sum_{\ell \in \text{PTB}} \sum_{i,j} |d_{\text{path}}^\ell(i,j) - \|B(h_i^\ell - h_j^\ell)\|_2^2|$$

Find a single transformation  $B$  such that over all sentences in PTB training

Over all word pairs in each sentence

The difference between **tree distance** and **squared vector distance** is *minimized*



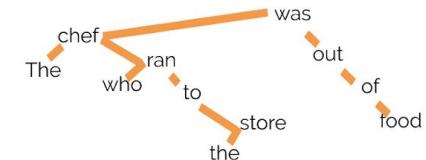
# Does BERT encode undirected parse trees -> does there exist a *distance* transformation?

$$\arg \min_B \sum_{\ell \in \text{PTB}} \frac{1}{|s^\ell|^2} \sum_{i,j} |d_{\text{path}}^\ell(i,j) - \|B(h_i^\ell - h_j^\ell)\|_2^2|$$

Find a single transformation  $B$  such that over all sentences in PTB training

Over all word pairs in each sentence

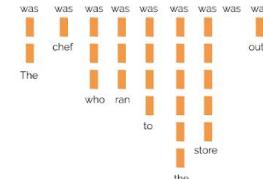
The difference between **tree distance** and **squared vector distance** is *minimized*



# Does BERT encode edge directions -> does there exist a *depth* transformation?

$$\arg \min_B \sum_{\ell \in \text{PTB}} \frac{1}{|s^\ell|}$$

Find a single transformation  $B$  such that over all sentences in PTB training



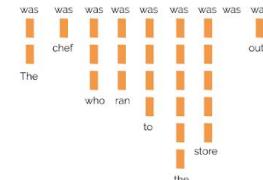
# Does BERT encode edge directions -> does there exist a *depth* transformation?

$$\arg \min_B \sum_{\ell \in \text{PTB}} \frac{1}{|s^\ell|} \sum_i$$

Find a single  
transformation  
 $B$

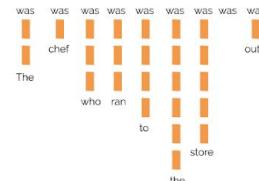
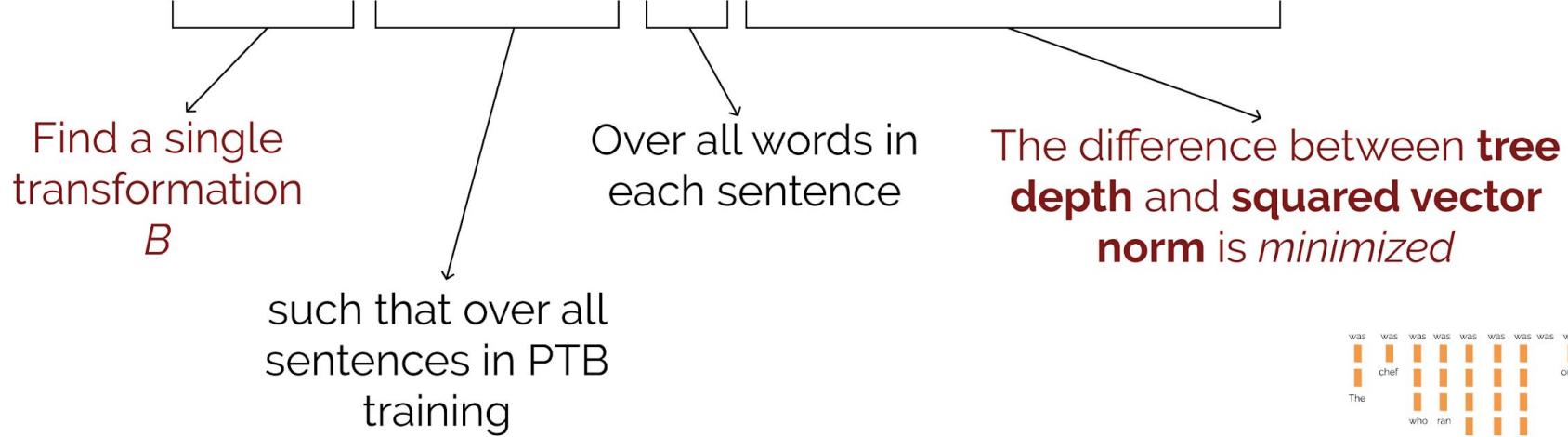
such that over all  
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# Does BERT encode edge directions -> does there exist a *depth* transformation?

$$\arg \min_B \sum_{\ell \in \text{PTB}} \frac{1}{|s^\ell|} \sum_i |\text{depth}^\ell(i) - \|Bh_i^\ell\|_2^2|$$



# *experiments & results*

Evaluating ELMo, BERT, and baselines

Training structural probes on PTB train, evaluating on test.

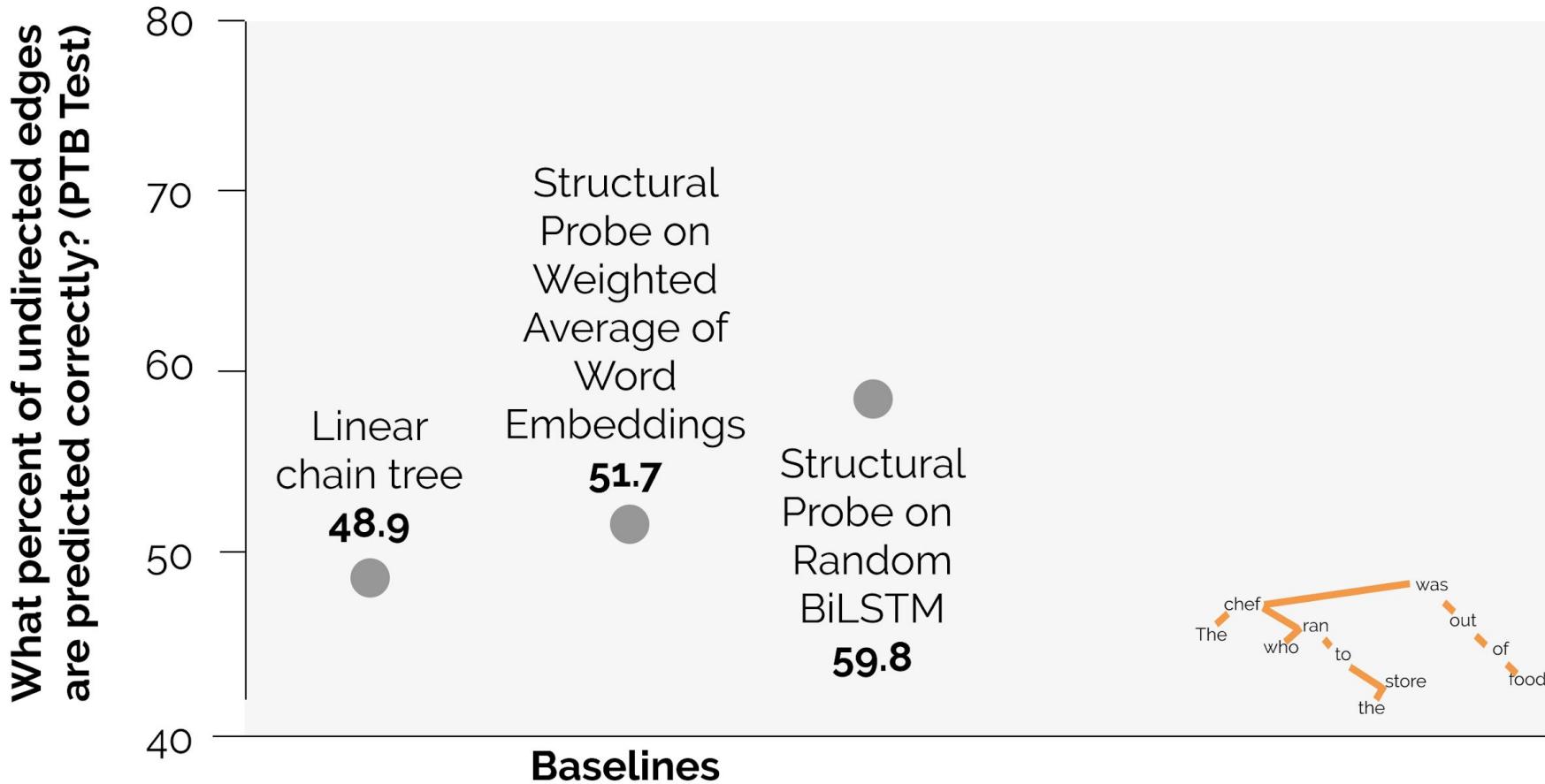
Evaluate by comparing structural probe minimum spanning trees to human-annotated parse trees.

Metrics:

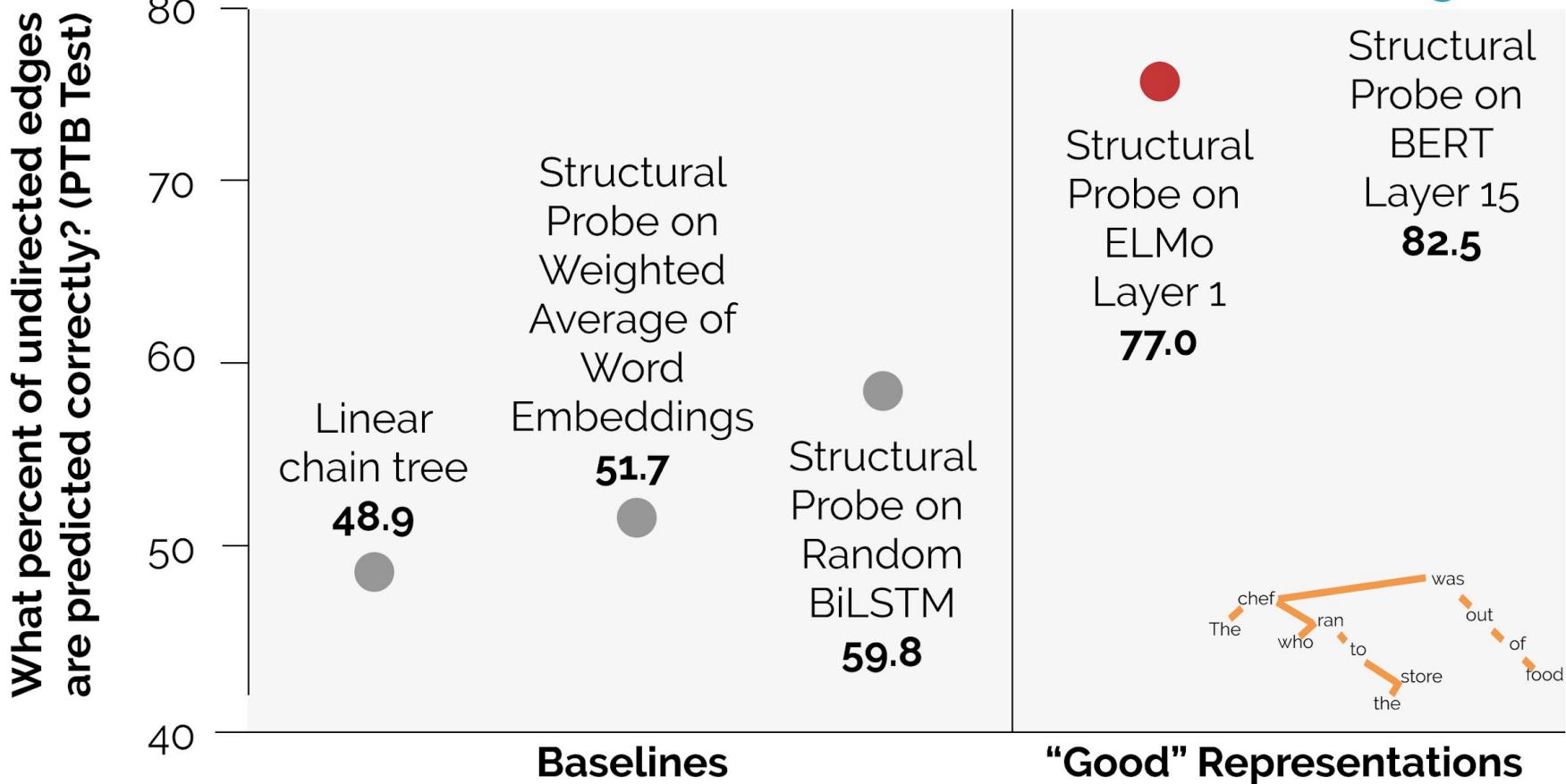
**Spearman correlation:** true vs predicted distances/depths

**UUAS:** Unlabeled Undirected Attachment Score,  
minimum spanning tree vs. gold tree

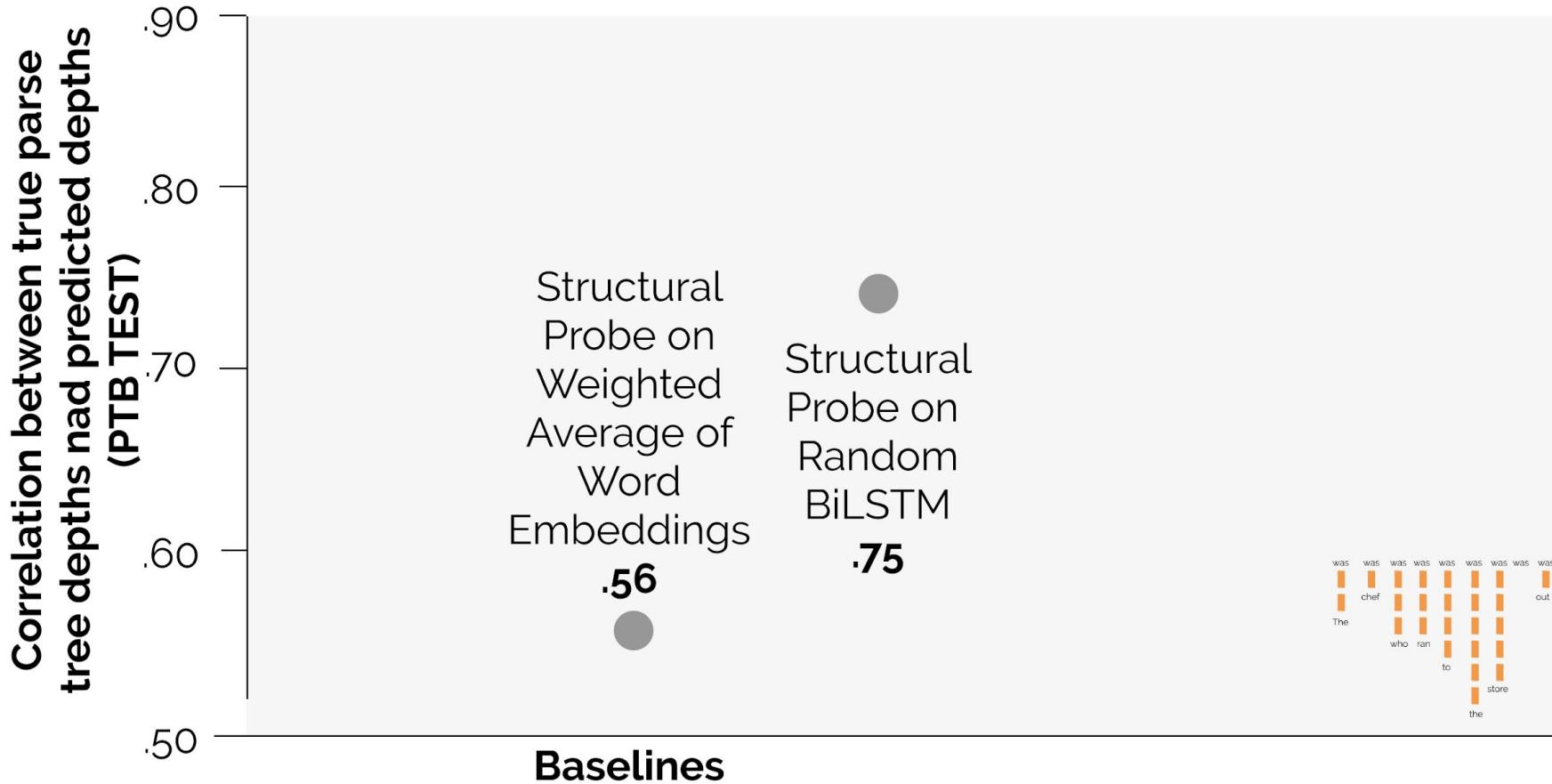
# Trees aren't well-encoded in baselines



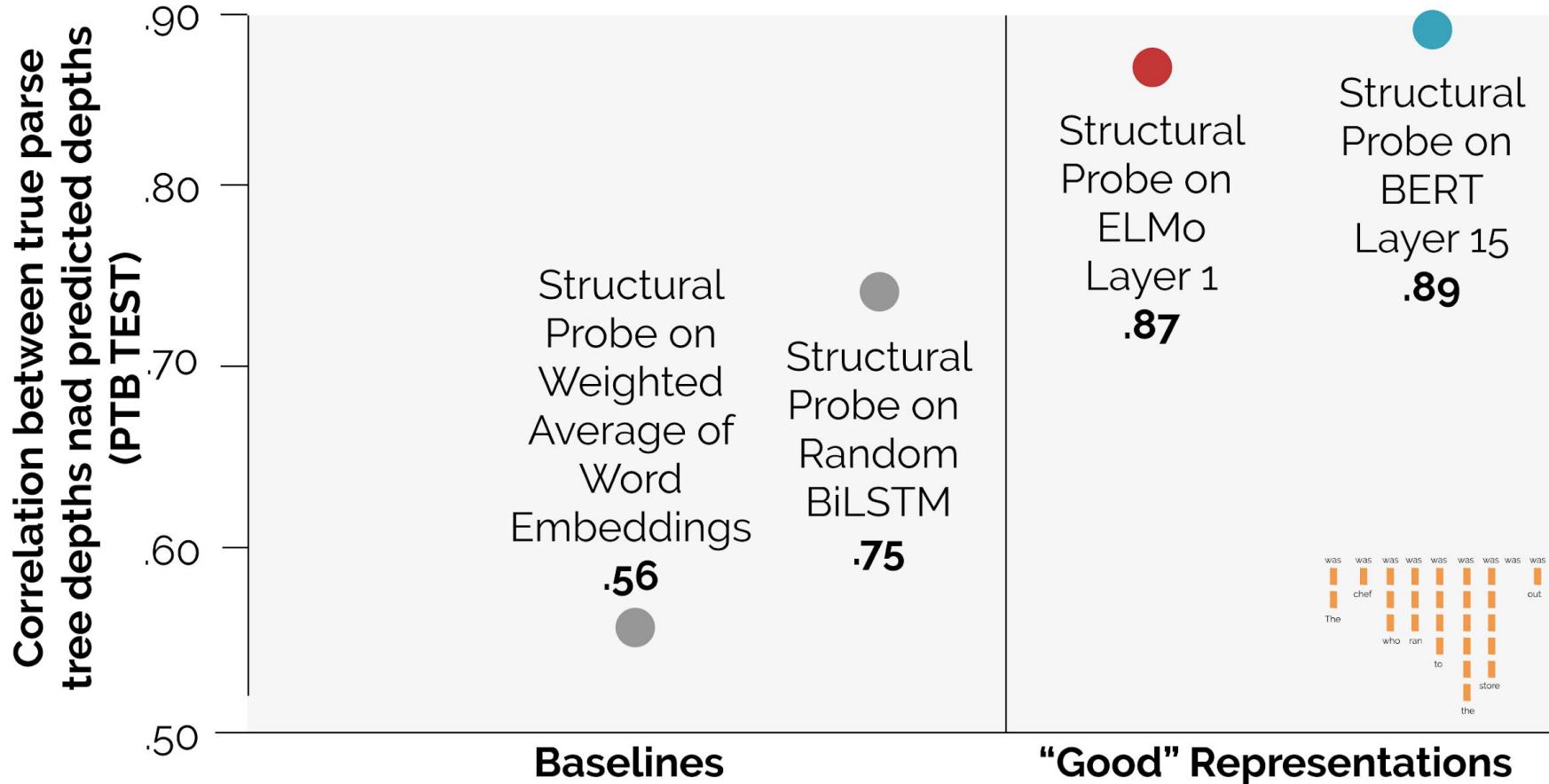
# But they are in trained representations!



# Tree depth isn't well-encoded in baselines



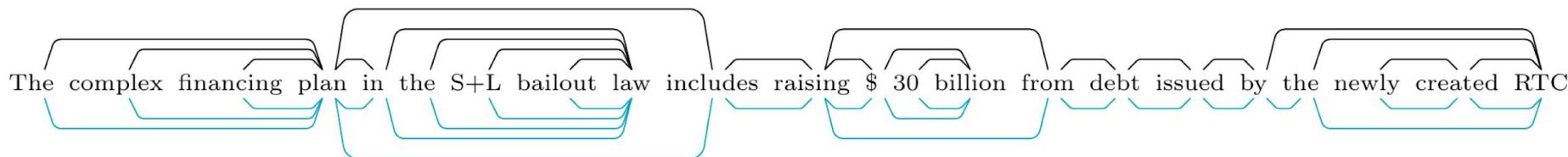
# But it is in trained representations!



# Trees from structural probe parse distances approximate parse trees pretty well!

**Black (above sentence): Human-annotated parse tree**

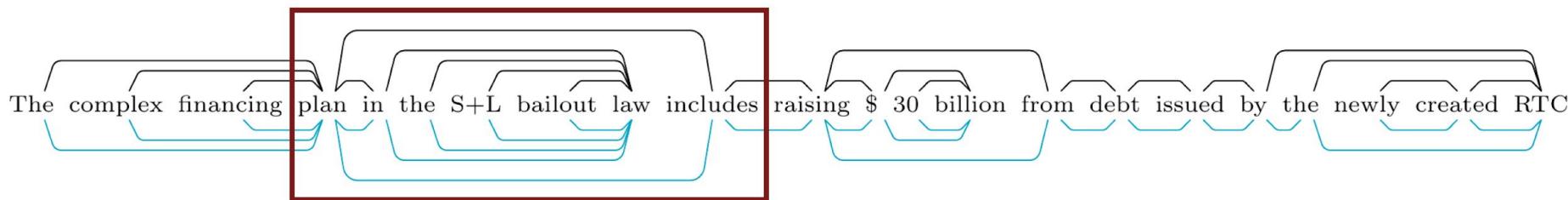
**Teal (below sentence): Minimum spanning tree, structural probe on BERT**



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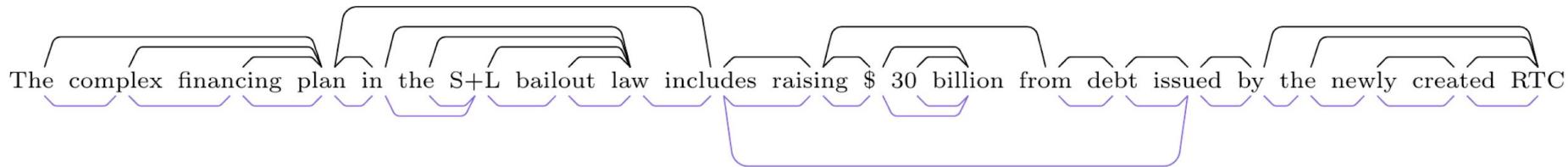
**Teal (below sentence): Minimum spanning tree, structural probe on BERT**



# Trees on baseline representations don't approximate gold trees well!

**Black (above sentence): Human-annotated parse tree**

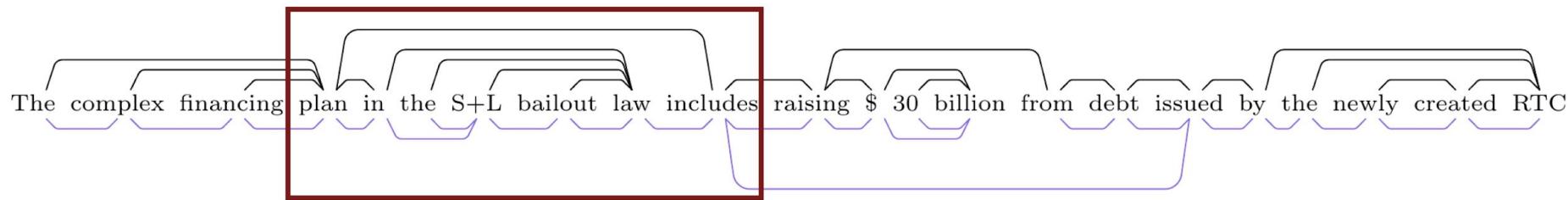
**Purple (below sentence): MST, structural probe on random-weights BiLSTM**



# Trees on baseline representations don't approximate gold trees well!

**Black (above sentence): Human-annotated parse tree**

**Purple (below sentence): MST, structural probe on random-weights BiLSTM**



# Predicted depths on BERT + ELMo reconstruct parse depths well!

grey circle: gold parse depth

red triangle: ELMo1 squared norm

blue square: BERT large 15 squared norm



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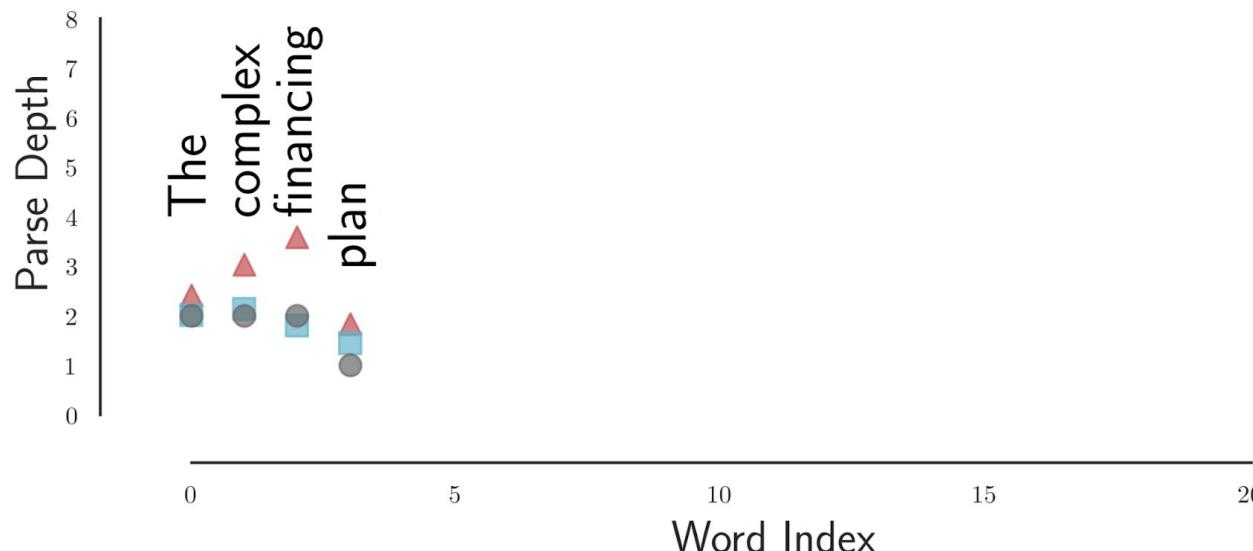


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blue square: BERT large 15 squared norm

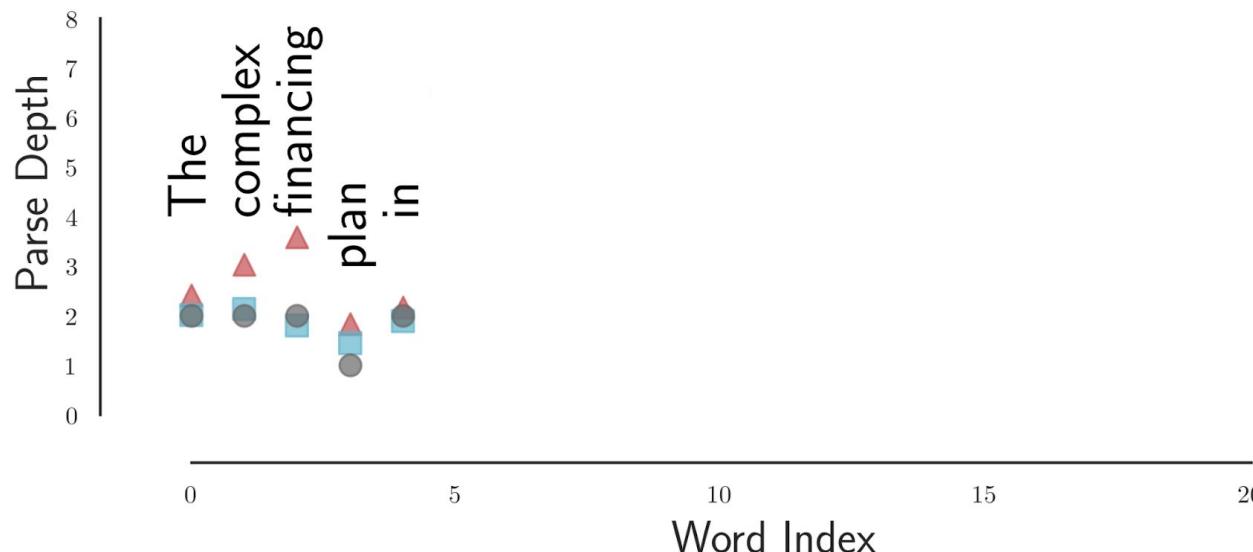


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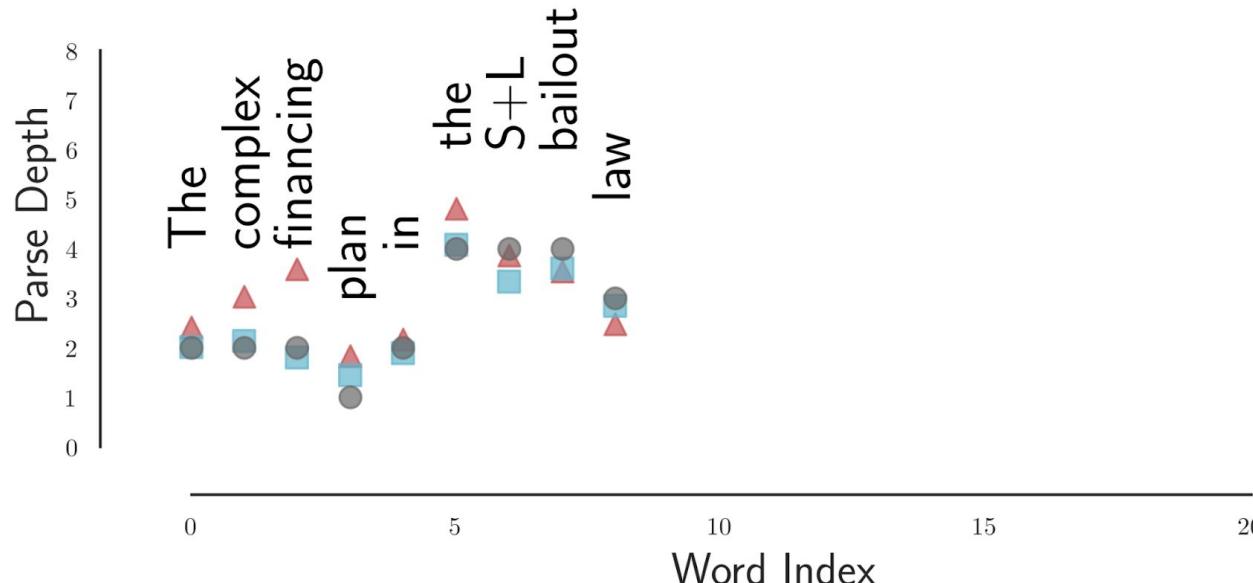


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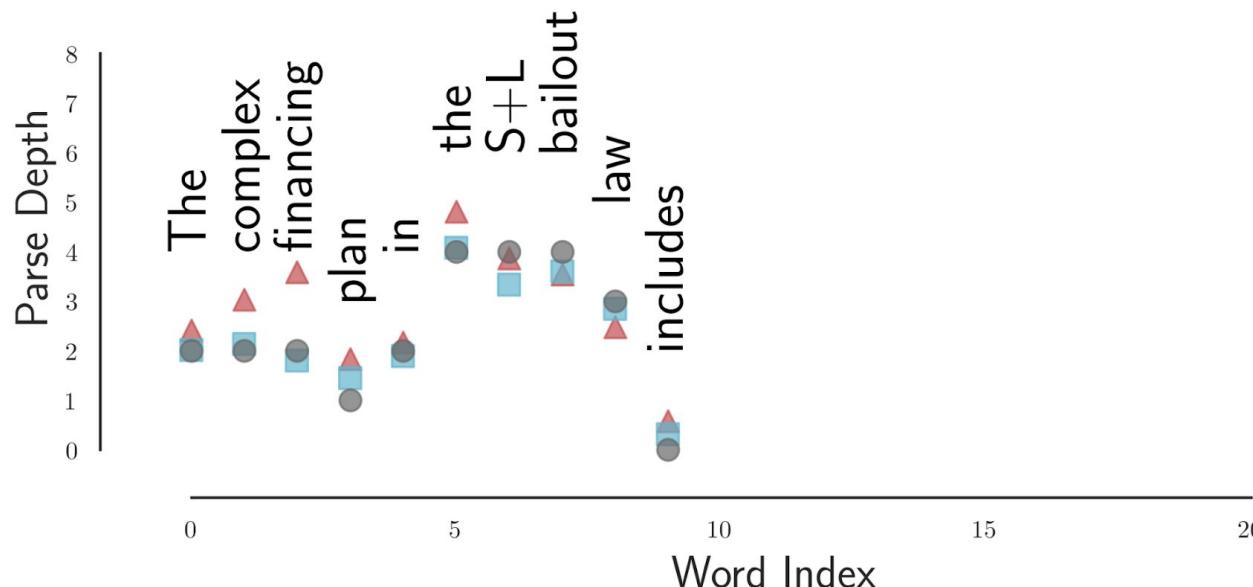


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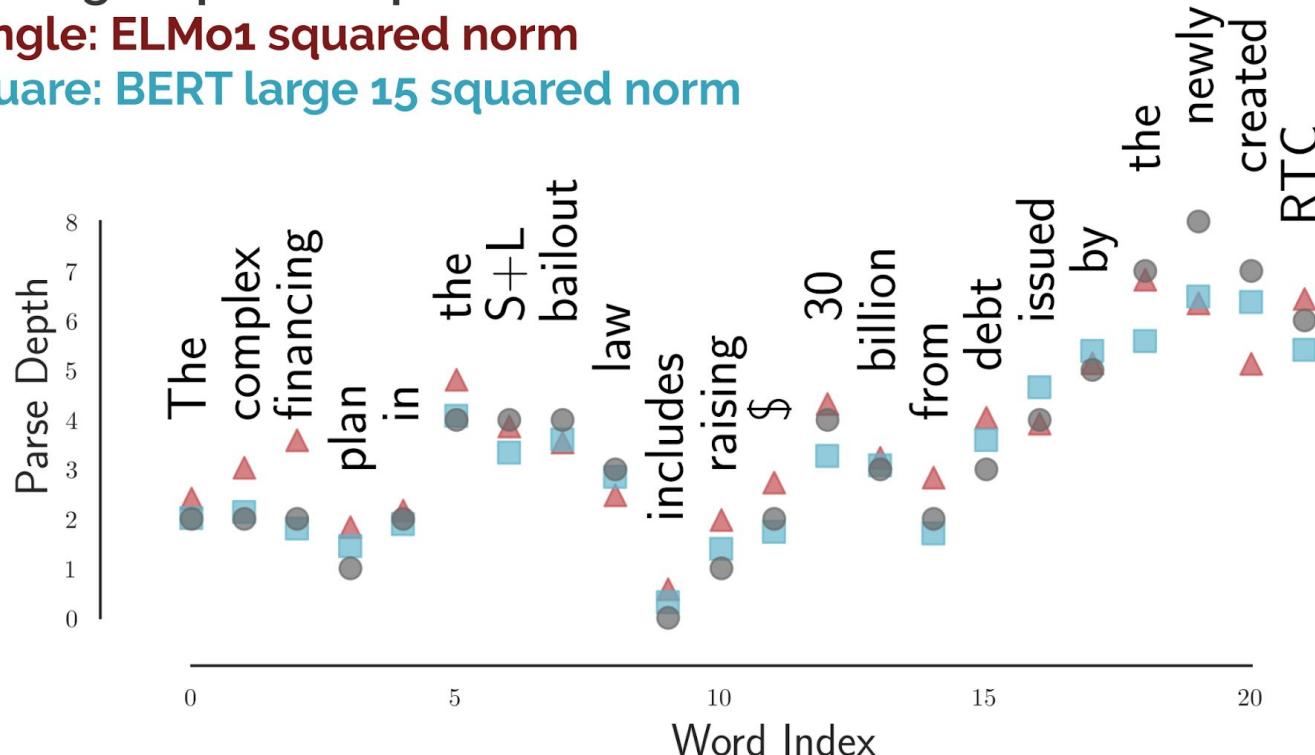


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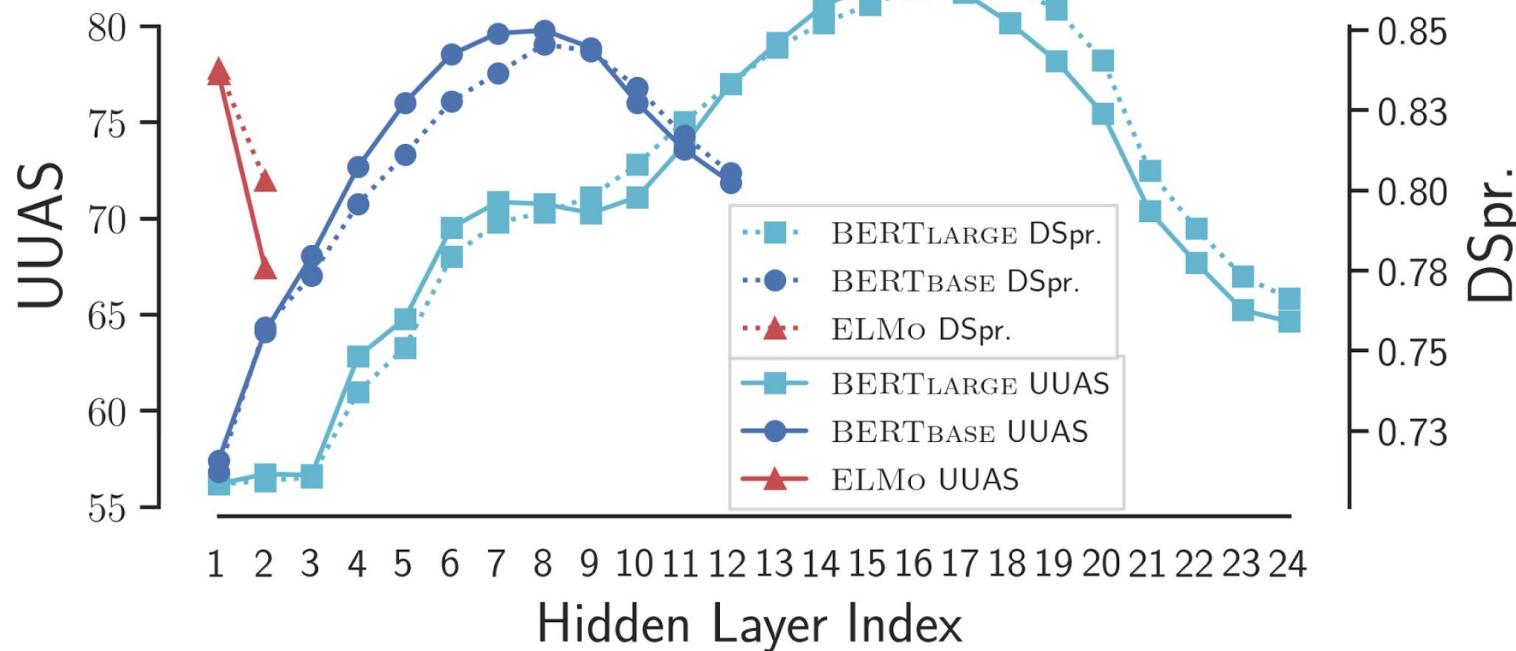
grey circle: gold parse depth

red triangle: ELMo1 squared norm

blue square: BERT large 15 squared norm



# Syntax geometry differs between layers





# More visualizations of structural probe

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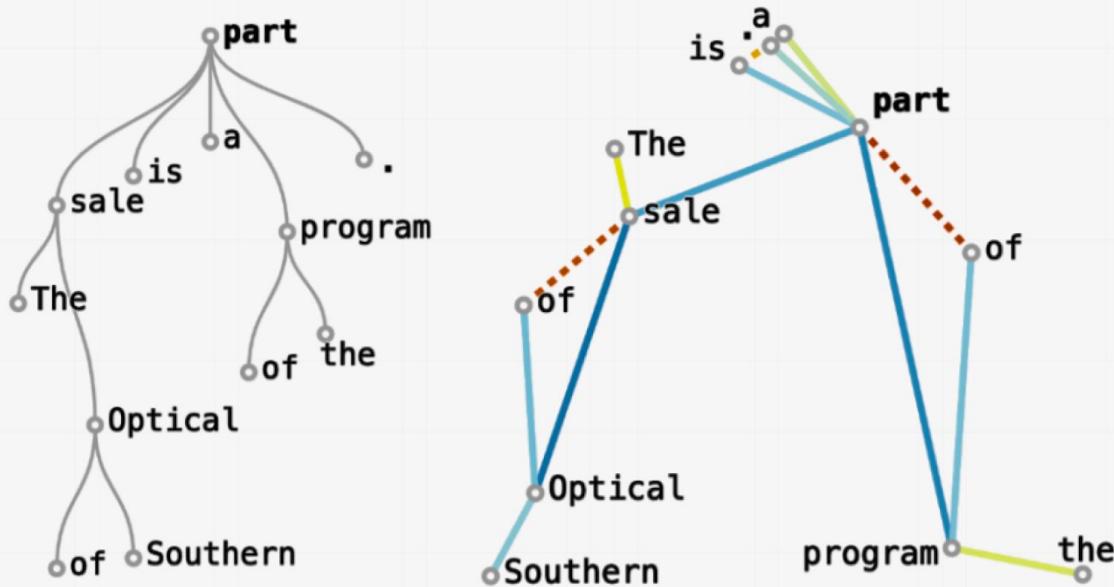
## Visualizing and Measuring the Geometry of BERT

---

Andy Coenen,\* Emily Reif,\* Ann Yuan\*  
Been Kim, Adam Pearce, Fernanda Viégas, Martin Wattenberg  
Google Brain  
Cambridge, MA

{andycoenen,ereif,annyuan,beenkim,adampearce,viegas,wattenberg}@google.com

“The sale of Southern Optical is a part of the program.”

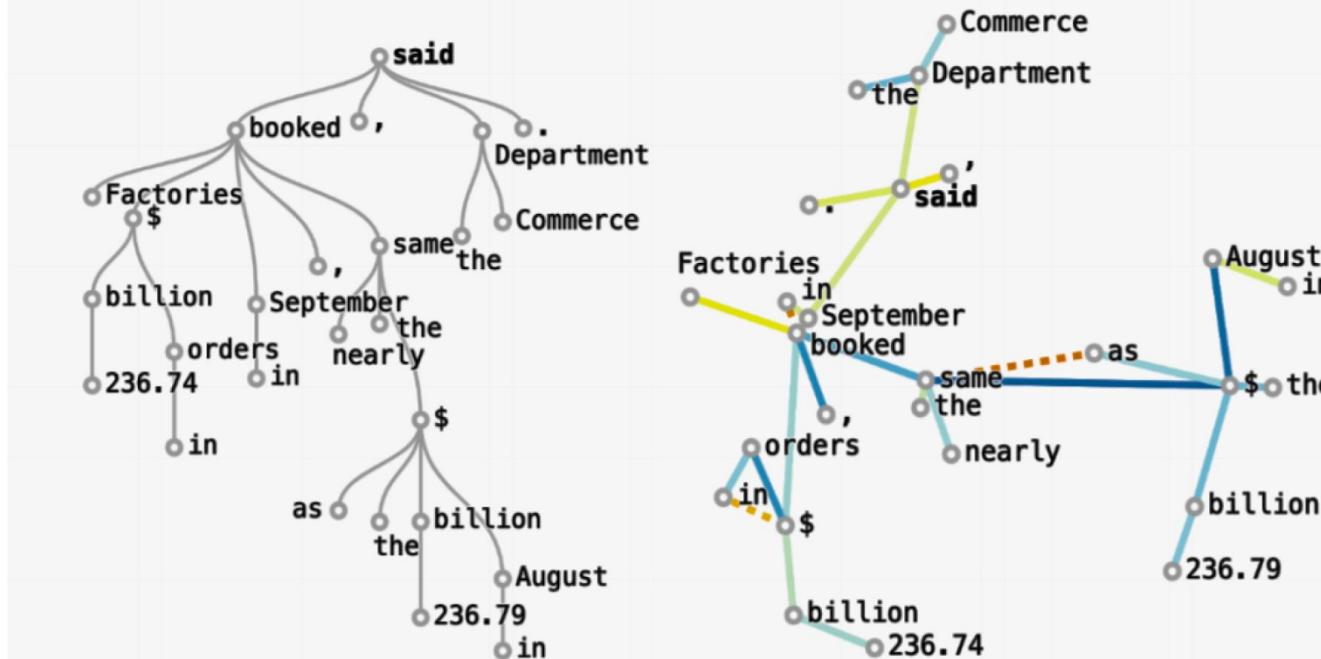


Ratio between  $d^2$  and tree distance



- Ground truth dependency
- - - No ground truth dependency,  $d^2 < 1.5$

"Factories booked \$236.74 billion in orders in September, nearly the same as the \$236.79 billion in August, the Commerce Department said."



Ratio between  $d^2$  and tree distance



— Ground truth dependency  
---- No ground truth dependency,  $d^2 < 1$



# Probing results can be hard to interpret

Supervised classifiers are powerful even when simple, and it can be unclear what you're learning about the representation itself.

You can learn good classifiers on top of lots of representations.  
How do we know what a probing accuracy means?



# Lecture Outline

## Lecture 20: Analysis and Interpretability of Neural NLP

1. Motivation: what are our models doing?
2. Neural networks as linguistic test subjects
3. Careful ablation studies and architecture modifications
4. Analysis of inherently interpretable architectures
5. Playing the adversary: breaking NLP models
6. Analyzing representations using supervised methods
7. **Aggregating analysis insights across studies**



# Aggregating analyses in surveys and toolkits

Each analysis paper asks a very specific question.

How do we ask, *what does the field currently know about BERT?*

Answer: meta-studies compiling results

## Analysis Methods in Neural Language Processing: A Survey

Yonatan Belinkov<sup>1,2</sup> and James Glass<sup>1</sup>

<sup>1</sup>MIT Computer Science and Artificial Intelligence Laboratory

<sup>2</sup>Harvard School of Engineering and Applied Sciences

Cambridge, MA, USA

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## A Primer in BERTology: What we know about how BERT works

Anna Rogers, Olga Kovaleva, Anna Rumshisky

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# Aggregating analyses in surveys and toolkits

How do we ask, *what can I easily find out about my model?*

Answer: interpretability toolkits!

**AllenNLP Interpret:**  
**A Framework for Explaining Predictions of NLP Models**

Eric Wallace<sup>1</sup>   Jens Tuyls<sup>2</sup>   Junlin Wang<sup>2</sup>   Sanjay Subramanian<sup>1</sup>  
Matt Gardner<sup>1</sup>   Sameer Singh<sup>2</sup>

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## Input Reduction



**Input Reduction** removes as many words from the input as possible without changing the model's prediction.

**Original Premise:** Two women are wandering along the shore drinking iced tea.

**Original Hypothesis:** Two women are sitting on a blanket near some rocks talking about politics

**Reduced Hypothesis:** politics



# Takeaways

Neural models are complex, fascinating objects that we don't currently understand, but we're making strides to understand them better!

A wide variety of analysis methods have been developed, for:

- Understanding a model's behavior on specific phenomena
- Understanding what a model learns about a topic or task
- Understanding what seemingly innocuous input changes make a model fail
- Many other things, with more coming every day!

These methods can be integrated into your future NLP projects!