#### Lecture 18: Mutable Trees

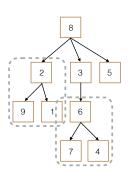
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#### **Announcements**

#### **Trees**

# **Terminology**

- Node: single unit containing an entry
- Root: top node
- Leaf: a node with no children
- Children: subtree with a parent



### **Tree Class**

```
class Tree:
    def __init__(self, entry, children=[]):
        for c in children:
            assert isinstance(c, Tree)
        self.entry = entry
        self.children = children

def is_leaf(self):
        return not self.children

>>> t = Tree(3, [Tree(2, [Tree(1)]), Tree(4)])
>>> t.entry
3
>>> t.children[0].entry
2
>>> t.children[1].is_leaf()
True
```

### Comparison to ADT

```
| def tree(entry, children=[]):
class Tree:
    return [entry, children]
          for c in children:
                                                   def entry(tree):
          assert isinstance(c, Tree)
self.entry = entry
                                                        return tree[0]
          self.children = children
                                                   def children(tree):
                                                        return tree[1]
>>> t_class = Tree(3, [Tree(2, ... [Tree(1)]), Tree(4)])
>>> t_adt = tree(3, [tree(2, ... [tree(1)]), tree(4)])
>>> t_class.entry == entry(t_adt)
                                                      2
>>> t_class.entry = 5
>>> entry(t_adt) = 5
SyntaxError: can't assign .
>>> t_class.entry == entry(t_adt)
False
```

### Map

- Want to apply a function fn to each element in the tree
- Main Ideas
  - Apply fn to current node (mutate tree)
  - Call map on children

### 

#### Existence

- Does the tree contain element **e**?
- Main Ideas
  - Check entry of current node
  - Otherwise, check
    - If no children to investigate, return False

```
class Tree:
    def __init__(self, entry, children=[]): ...

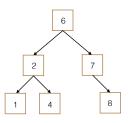
    def __contains__(self, e):
        if self.entry == e:
            return True
        for c in self.children:
            if e in c:
                 return True
        return True
        return False

>>> t = Tree(3, [Tree(2, [Tree(1)]), Tree(4)])
>>> 8 in t
False
>>> 2 in t
True
```

## **Binary Search Tree**

#### **Definition**

- Each node has at most 2 children, left and right
- Left child elements are all less than or equal to entry
- Right child elements are all greater than entry
- Left child and right child are also BSTs
- · Only contains numbers!



## **Binary Search Tree Class**

```
class BST:
    empty = ()
    def __init__(self, entry, left=empty, right=empty):
        assert left is BST.empty or isinstance(left, BST)
        assert right is BST.empty or isinstance(right, BST)

    self.entry = entry
    self.left, self.right = left, right

    if left is not BST.empty:
        assert left.max <= entry
    if right is not BST.empty:
        assert entry < right.min

@property
def max(self): ... # Returns the maximum element in the BST

@property
def min(self): ... # Returns the minimum element in the BST</pre>
```

#### Existence

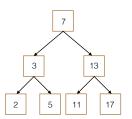
- Does the BST contain element e?
- Main Ideas
  - Check entry of current node
  - Otherwise, check left or right
    - If no children to investigate, return False

```
class BST:
    def __init__(self, entry,
        left=empty, right=empty): ...

def __contains__(self, e):
    if self.entry == e:
        return True
    elif e < self.entry and self.left
        is not BST.empty:
        return e in self.left
    elif e > self.entry and self.right
        is not BST.empty:
        return e in self.right
        return e in self.right
```

## **Runtime Comparison**

- Is there a difference in runtime when we check existence in a tree versus a BST?
- Runtime in terms of n, the number of nodes



## **Runtime Comparison**

```
class Tree:
    def __init__(self, entry, children=[]): ...
            _contains__(self, e):
         if self.entry == e:
         return True
for c in self.children:
              if e in c:
         return True return False
                                                       3
                                                                       13
>>> t = Tree(7, [Tree(3, [Tree(2), ... Tree(5)]), Tree(13,
                                                  2
                                                           5
                                                                  11
                                                                           17
         [Tree(11), Tree(17)])])
>>> 11 in t
                                                            \Theta(n)
```

### **Runtime Comparison**

```
class BST:

def __init__(self, entry, left=empty, right=empty): ...

def __contains__(self, e):
    if self.entry == e:
        return True
    elif e < self.entry and self.left
        is not BST.empty:
        return e in self.left
    elif e > self.entry and self.right
        is not BST.empty:
        return e in self.right
        is not BST.empty:
        return False

>>> bst = BST(7,
...
        BST(3, BST(2), BST(5)),
...
        BST(13, BST(11), BST(17)))
>>> 11 in bst
True
```

## Summary

- Trees created with a class are mutable!
- BSTs allow us to organize our data in left child and right child based on value
- BST allows for more efficient search
  - Θ(n) in regular tree
  - Θ(log n) in BST

