# **Topic2Vec: Learning Distributed Representations of Topics**

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### **Abstract**

Latent Dirichlet Allocation (LDA) mining thematic structure of documents plays an important role in nature language processing and machine learning areas. However, the probability distribution from LDA only describes the statistical relationship of occurrences in the corpus and usually in practice, probability is not the best choice for feature representations. Recently, embedding methods have been proposed to represent words and documents by learning essential concepts and representations, such as Word2Vec and Doc2Vec. The embedded representations have shown more effectiveness than LDA-style representations in many tasks. In this paper, we propose the Topic2Vec approach which can learn topic representations in the same semantic vector space with words, as an alternative to probability. The experimental results show that Topic2Vec achieves interesting and meaningful results.

#### 1 Introduction

Modeling text (words, topics and documents) is a key problem in nature language processing (NLP) and information retrieval (IR). The goal is to find short and essential descriptions which enable efficient processing of large systems and benefit basic tasks such as classification, clustering, summarization and estimation of similarity or relevance.

During the past decades, various models and solutions are proposed, such as Bag-of-Words (BOW) (Harris, 1954), *TF-IDF* (Salton and McGill, 1983), Latent Semantic Analysis (LSA) (Landauer et al., 1998) and Probabilistic Latent Semantic Analysis (PLSA) (Hofmann, 1999). But the best-known model is Latent Dirichlet Allocation (LDA) (Blei et al., 2003) which describes

the hierarchical relationships between words, topics and documents. In LDA, documents are represented as probability distributions over latent topics where each topic is characterized by a distribution over words. However, the probability distribution generated from LDA prefers to describe the statistical relationship of occurrences rather than real semantic information embedded in words, topics and documents. Also LDA will assign high probabilities to high frequency words and those words with low probabilities are hard to be chosen as representatives of topics. But in practice, low probability words sometimes distinguish topics better. For example, LDA will assign higher probability and choose "food" as representative other than "cheeseburger", "drug" other than "aricept" and "technology" other than "smartphone".

Recently, distributed representations with neural probabilistic language models (NPLMs) (Bengio et al., 2003) were proposed to represent words and documents as low-dimensional vectors in one semantic space, and achieved significant results in many NLP and ML tasks (Collobert and Weston, 2008; Mnih and Hinton, 2009; Mikolov et al., 2013a; Mnih and Kavukcuoglu, 2013; Huang et al., 2012; Le and Mikolov, 2014). In particular, Word2Vec proposed by Mikolov et al. (2013a) could automatically learn concepts and semantic-syntactic relationships between words like vec("Berlin") vec("Germany") = vec("Paris") - vec("France").Doc2Vec (Para2Vec) proposed by Le and Mikolov (2014) achieves state-of-the-art performance on sentiment analysis. Naturally, in this paper, we want to answer the question that, what will happen if we embed topics in the semantic vector space?

Following the ideas of previously proposed models for words and documents, we propose the model Topic2Vec as shown in Fig. 1. Based on the Word2Vec, we incorporates topics into the NPLM framework for learning distributed representations

of topics in the same semantic space with words. Furthermore, words and topics naturally can estimate similarity and relevance with each other such as using cosine function rather than using probability.

In the experiments, we evaluate two different topic representations including embedding of Topic2Vec and probability of LDA in two aspects: listed examples and t-SNE 2D embedding of nearest words for each topic. The experimental results show that our Topic2Vec achieves distinctive and meaningful results compared to LDA.

#### 2 Related Models

#### 2.1 Latent Dirichlet Allocation

Latent Dirichlet allocation (LDA) (Blei et al., 2003) is a probabilistic generative model that assumes each document is a mixture of latent topics, where each topic is a probability distribution over all words in vocabulary. Briefly, LDA generates a sequence of words as follows:

- For each of the N word  $w_n$  in document d:
  - Sample a topic  $z_n \sim \text{Multinomial}(\theta_d)$
  - Sample a word  $w_n \sim \text{Multinomial}(\phi_{z_n})$ .

By Gibbs Sampling  $^1$  estimation, we obtain document-topic probability matrix  $\Theta$  and topic-word probability matrix  $\Phi$ . For a new document of arbitrary length, we can infer its involved latent topics and meanwhile we will assign a topic label for each word in the document.

### 2.2 Word2Vec

Inspired by Neural Probabilistic Language Model (NPLM) (Bengio et al., 2003), Mikolov et al. (2013a) proposed Word2Vec including CBOW and Skip-gram for computing continuous vector representations of words from large data sets.

When training, given a word sequence  $D = \{w_1, ..., w_M\}$ , the learning objective functions are defined to maximize the following log-likelihoods, based on CBOW and Skip-gram, respectively.

$$\mathcal{L}_{CBOW}(D) = \frac{1}{M} \sum_{i=1}^{M} \log p(w_i | w_{cxt}), \quad \text{(1a)}$$

$$\mathcal{L}_{Skip-gram}(D) = \frac{1}{M} \sum_{i=1}^{M} \sum_{-k < c < k, c \neq 0} \log p(w_{i+c}|w_i).$$
 (1b)

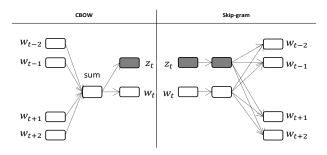


Figure 1: Learning architectures of Topic2Vec, where  $(w_{t-2}, w_{t-1}, w_{t+1}, w_{t+2})$  are context words and  $w_t$  is the current word paired with a topic  $z_t$ .

Here, in Equation (1a),  $w_{cxt}$  indicates the context of the current word  $w_i$ . In Equation (1b), k is the window size of context. For any variables  $w_j$  and  $w_i$ , the conditional probability  $p(w_j|w_i)$  is calculated using softmax function as follows,

$$p(w_j|w_i) = \frac{\exp(\mathbf{w_j} \cdot \mathbf{w_i})}{\sum_{w \in W} \exp(\mathbf{w} \cdot \mathbf{w_i})},$$
 (2)

where  $\mathbf{w}$ ,  $\mathbf{w_i}$  and  $\mathbf{w_j}$  are respectively the word representations of word w,  $w_i$  and  $w_j$ , W is the word vocabulary.

## 3 Topic2Vec

Inspired by word2vec, we incorporate topics and words into the NPLM. We propose Topic2Vec as shown in Fig. 1 for learning distributed topic representations together with word representations. Topic2Vec is also separated in CBOW and Skip-gram situations. For instance, given a word sequence  $(w_{t-2}, w_{t-1}, w_t, w_{t+1}, w_{t+2})$ , in which  $w_t$  is the current word assigned with topic  $z_t$  by LDA. The CBOW predicts the word  $w_t$  and topic  $z_t$  based on the surrounding words  $(w_{t-2}, w_{t-1}, w_{t+1}, w_{t+2})$ , while the Skip-gram predicts surrounding words  $(w_{t-2}, w_{t-1}, w_{t+1}, w_{t+2})$  given current  $w_t$  and  $z_t$ .

When training, given a word-topic sequence of a document  $D = \{w_1 : z_1, ..., w_M : z_M\}$ , where  $z_i$  is the word  $w_i$ 's topic inferred from LDA, the learning objective functions can be defined to maximize the following log-likelihoods, based on CBOW and Skip-gram, respectively.

$$\mathcal{L}_{CBOW}(D) = \frac{1}{M} \sum_{i=1}^{M} (\log p(w_i | w_{cxt}) + \log p(z_i | w_{cxt})),$$
(3a)

<sup>&</sup>lt;sup>1</sup>http://gibbslda.sourceforge.net/

	Topic_6		Topic_19		Topic_27		Topic_47	
	word	prob.	word	prob.	word	prob.	word	prob.
LDA	food	0.027	drug	0.031	medical	0.033	dog	0.011
	restaurant	0.008	drugs	0.019	hospital	0.024	garden	0.009
	eat	0.008	cancer	0.019	care	0.019	tree	0.009
	more	0.005	study	0.011	patients	0.018	dogs	0.009
	chicken	0.005	patients	0.011	doctors	0.016	plants	0.008
	cooking	0.005	treatment	0.009	health	0.013	trees	0.008
	eating	0.005	fda	0.009	doctor	0.009	animal	0.007
	one	0.005	heart	0.008	patient	0.009	plant	0.007
	good	0.005	risk	0.008	surgery	0.008	animals	0.006
	foods	0.005	more	0.007	center	0.008	Z00	0.006
Topic2Vec	word/topic	cos.	word/topic	cos.	word/topic	cos.	word/topic	cos.
	cheeseburgers	0.564	topic_62	0.618	topic_19	0.519	dogwood	0.498
	meatless	0.535	aricept	0.531	topic_62	0.478	dogwoods	0.494
	smoothies	0.534	topic_27	0.519	neonatal	0.466	topic_33	0.485
	topic_95	0.533	memantine	0.514	topic_13	0.457	bark	0.484
	meatloaf	0.530	enbrel	0.512	anesthesiologists	0.445	fescue	0.483
	tastier	0.530	gabapentin	0.511	anesthesia	0.439	aphids	0.478
	topic_52	0.527	colorectal	0.509	reconstructive	0.437	mulched	0.478
	cheeseburger	0.525	prilosec	0.507	comatose	0.437	azaleas	0.477
	concoctions	0.522	placebos	0.507	hysterectomy	0.433	shrub	0.475
	vegetarians	0.515	intravenously	0.504	ventilator	0.432	camellias	0.472
	Topic_53		Topic_67		Topic_79		Topic_93	
LDA	word	prob.	word	prob.	word	prob.	word	prob.
	government	0.022	www	0.028	computer	0.016	russia	0.028
	africa	0.015	com	0.023	technology	0.010	russian	0.027
	people	0.015	hotel	0.018	phone	0.009	putin	0.017
	african	0.011	travel	0.015	software	0.009	soviet	0.013
-5/1	country	0.009	trip	0.011	digital	0.008	moscow	0.012
	international	0.008	night	0.010	apple	0.008	president	0.010
	darfur	0.007	per	0.009	use	0.007	country	0.007
	sudan	0.007	day	0.008	system	0.006	former	0.007
	south	0.007	tour	0.008	microsoft	0.006	state	0.007
	human	0.007	cruise	0.007	up	0.006	union	0.006
	word/topic	cos.	word/topic	cos.	word/topic	cos.	word/topic	cos.
	mozambique	0.428	fairmont	0.569	wirelessly	0.584	topic_88	0.469
	uganda	0.423	motorcoach	0.553	handhelds	0.573	boris	0.435
	ghana	0.419	stateroom	0.547	desktops	0.572	leonid	0.411
			uniworld	0.540	pda	0.566	dmitry	0.404
	addis	0.417	u					
Topic2Vec	addis darfur	0.417 0.412	maarten	0.533	smartphone	0.566	vladimir	0.397
Topic2Vec				0.533 0.529	smartphone megabyte	0.566 0.562	vladimir mikhail	0.397 0.397
Topic2Vec	darfur	0.412	maarten					
Topic2Vec	darfur burundi	0.412 0.408	maarten tourcrafters	0.529	megabyte	0.562	mikhail	0.397
Topic2Vec	darfur burundi lanka	0.412 0.408 0.407	maarten tourcrafters wyndham	0.529 0.528	megabyte macbook	0.562 0.556	mikhail dmitri	0.397 0.396

Figure 2: Nearest words and topics for each topic. Words are listed with conditional probabilities in LDA while words and topics are listed with calculated cosine similarity in Topic2Vec.

$$\mathcal{L}_{Skip-gram}(D)$$

$$= \frac{1}{M} \sum_{i=1}^{M} \sum_{-k \le c \le k, c \ne 0} (\log p(w_{i+c}|w_i))^{(3b)} + \log p(w_{i+c}|z_i)).$$

Topic2Vec aims at learning topic representations along with word representations. Considering the simplicity and efficient solution, we just follow the optimization scheme that used in Word2Vec (Mikolov et al., 2013a). To approximately maximize the probability of the softmax, we use Negative Sampling without Hierarchical Softmax (Mikolov et al., 2013b). Stochastic gradient descent (SGD) and back-propagation algorithm are used to optimize our model. By the way, complexity of our Topic2Vec is linear with size of dataset, same with Word2Vec.

## 4 Experiments

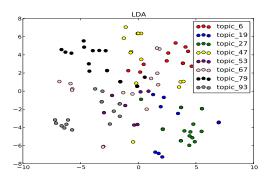
#### 4.1 Dataset

We use the English Gigaword Fifth Edition<sup>2</sup> as our training data for learning fundamental word and topic representations. We randomly extract part of documents and construct our training set described as follows: we chose 100,000 documents, where each consists of more than 1,000 characters from subfolder ltw\_eng (Los Angeles Times) containing 411,032 documents. Besides, we eliminate those words that occur less than 5 times and the stop words. In the end, training set contains about 42 million words and the vocabulary size is 102,644.

## 4.2 Evaluation Methods

In experiments, we run Topic2Vec in Skip-gram and learn topic representations together with word representations. And then we evaluate topic repre-

<sup>&</sup>lt;sup>2</sup>https://catalog.ldc.upenn.edu/LDC2011T07



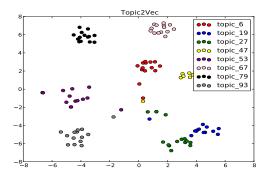


Figure 3: t-SNE 2D embedding of the nearest word representation for each topic in LDA (left) and Topic2Vec (right).

sentations via comparing Topic2Vec with LDA in two aspects: (1) we select most related topics or words conditioned on selected topics and (2) we embed these related words or topics in 2D space using t-SNE (Maaten et al., 2008). During the process, we cluster words into topics as follows:

- LDA: each topic is a probability distribution over words. We select the top N = 10 words with highest conditional probability.
- Topic2Vec: topics and words are equally represented as the low-dimensional vectors, we can immediately calculate the cosine similarity between words and topics. For each topic, we select higher similarity words.

### 4.3 Analysis of Results

Fig. 2 shows top 10 nearest words from LDA and Topic2Vec for eight typically selected topics, respectively. We now give more detailed analysis to understand the difference between them. As shown in Fig. 2, in Topic\_19, LDA returns the words like "drug", "drugs", "cancer" and "patients", while Topic2Vec returns "aricept", "memantine", "enbrel" and "gabapentin". In Topic\_27, LDA returns the words of "medical", "hospital", "care", "patients" and "doctors", while Topic2Vec returns "neonatal", "anesthesiologists", "anesthesia" and "comatose". We only know that Topic\_19 and Topic\_27 share the same topic about "patients" or "medical", but we can't get their further difference from the results of LDA. But from the result of Topic2Vec, we can easily discover that Topic\_19 focuses on a more specific topic about drugs ("aricept", "memantine", "enbrel" and "gabapentin"), while Topic\_27 focuses on another specific topic about treatment ("anesthesiologists", "anesthesia" and "comatose"), they are absolutely different. Obviously, Topic2Vec presents more distinguished results between two similar topics.

Fig. 3 shows the 2D embedding of the corresponding related words for each topic by using t-SNE. Obviously, Topic2Vec produces a better grouping and separation of the words in different topics. In contrast, LDA does not produce a well separated embedding, and words in different topics tend to mix together.

In summary, for each topic, words selected by Topic2Vec are more typical and representative compared to those returned by LDA. Eventually, Topic2Vec can better distinguish different topics.

### 5 Conclusions and Future Work

In this paper, via integrating NPLM, Word2Vec and LDA, we propose the Topic2Vec which successfully embeds latent topics in the same semantic vector space with words. In principle, our purpose clearly aims at learning new fashion topic representation by Topic2Vec. From the observation of experiments, Topic2Vec presents more distinguished results than LDA and we have the conclusion that Topic2Vec can model topics better.

But now, we just qualitatively evaluate the performance of Topic2Vec and LDA, we will quantitatively do more detailed analysis about their difference in the future. Besides, we have to run LDA firstly to assign a topic for each word in the corpus before Topic2Vec. We also will explore new independent topic models which can mine thematic structure of documents as LDA and learn inherent representations and model topics better as

Topic2Vec, simultaneously.

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