Rotational motion

All points move in circles about an axis within the body

Rigid body

A rigid body is an object with a definite shape that doesn't change

Torque(moment of a force)

It is the product of the force and the perpendicular distance between the line of action of the force and the rotational axis

- Newton's first law for rotational motion(rotational equilibrium)
  - An object continues to remain stationary or to move at a constant angular velocity unless an external torque acts on it
  - Condition of equilibrium: net force equals 0, net torque equals 0
- Moment of inertia

Inertia is a quantity that measures the resistance to change in rotational motion

Newton's second law for rotational motion

The net torque acting on a rigid body is the product of the moment of inertia and the angular acceleration

Center of mass

The point that moves as though the whole mass were concentrated there

- An external force applied at the center of mass causes linear but not angular acceleration
- If not applied at center of mass, there will be linear and rotational motion
- Rolling without slipping

The point of contact between the wheel and the floor is instantaneously at rest

Angular momentum

The angular momentum of an object is the product of the moment of inertia of this object and its angular velocity

- The net torque of an object is the rate of change of angular momentum of body
- Newton's third law of rotational motion

When object A applies a torque to object B, then the object will apply an equal and opposite torque to object A

Conservation of angular momentum

When the net torque on a system is zero, the total angular momentum of system remains constant

Kepler's first law of planetary motion

The path of each planet around the sun is an ellipse with the sun at on focus

Kepler's second law of planetary motion

A line joining a planet and the sun sweeps out equal areas in equal time

- 无普适性,严谨来说只适用于太阳系
- Kepler's third law of planetary motion

The square of a planet's orbital time period T, is proportional to the cube of its average orbital radius. R

Newton's universal law of gravitation

Every single point mass attracts every other point mass with a force that is directly proportional to the product of their masses and inversely proportional to the square of their separation

- Newton's law of gravitation
  - 1. Masses much smaller than their separation can be regarded as point mass
  - 2. 球体(密度均匀的)等同于中心的 point mass
- Gravitational field

A region of space where a mass experiences a force because of its mass

Gravitational field strength

Force per unit mass experienced by a test point mass placed in the field

- Gravitational potential energy
  - The work done against field in bringing the mass from infinity to the point
  - Why negative?
    - 1. Gravitational forces are attractive
    - 2. Work done against field is negative
- Gravitational potential
  - The work done per unit mass in bringing a small test mass from infinity to the point
  - If test mass move in the direction of field, work is done by the gravitational force, the gravitational potential decreases, and the gravitational potential energy decreases
  - Gravitational field strength is the negative of the rate of change of gravitational potential to the change in distance to the center of the planet
- Orbital motion: Ek, Ep, ET

$$E_k = \frac{GMm}{2r}$$

$$E_p = -\frac{GMm}{r}$$

$$E_T = -\frac{GMm}{2r}$$

Escape speed

The minimum speed needed to be able to escape completely from the gravitational field of the planet

Orbit and atmosphere

In the atmosphere of a planet, as the radius of orbital motion decreases, the speed of the satellite increases