## Batch Norm

CLASS torch.nn.BatchNorm2d(num\_features, eps=1e-05, momentum=0.1, affine=True, track\_running\_stats=True, device=None, dtype=None) [SOURCE]

Applies Batch Normalization over a 4D input (a mini-batch of 2D inputs with additional channel dimension) as described in the paper Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift.

$$y = rac{x - \mathrm{E}[x]}{\sqrt{\mathrm{Var}[x] + \epsilon}} * \gamma + eta$$

The mean and standard-deviation are calculated per-dimension over the mini-batches and  $\gamma$  and  $\beta$  are learnable parameter vectors of size C (where C is the input size). By default, the elements of  $\gamma$  are set to 1 and the elements of  $\beta$  are set to 0. The standard-deviation is calculated via the biased estimator, equivalent to torch.var(input, unbiased=False).

Also by default, during training this layer keeps running estimates of its computed mean and variance, which are then used for normalization during evaluation. The running estimates are kept with a default momentum of 0.1.

If track\_running\_stats is set to False, this layer then does not keep running estimates, and batch statistics are instead used during evaluation time as well.

## • NOTE

This momentum argument is different from one used in optimizer classes and the conventional notion of momentum. Mathematically, the update rule for running statistics here is  $\hat{x}_{\text{new}} = (1 - \text{momentum}) \times \hat{x} + \text{momentum} \times x_t$ , where  $\hat{x}$  is the estimated statistic and  $x_t$  is the new observed value.

Because the Batch Normalization is done over the C dimension, computing statistics on (N, H, W) slices, it's common terminology to call this Spatial Batch Normalization.



## Singular value decomposition

From Wikipedia, the free encyclopedia

In linear algebra, the **singular value decomposition** (SVD) is a factorization of a real or complex matrix. It generalizes the eigendecomposition of a square normal matrix with an orthonormal eigenbasis to any  $m \times n$  matrix. It is related to the polar decomposition.

Specifically, the singular value decomposition of an  $m \times n$  complex matrix  $\mathbf{M}$  is a factorization of the form  $\mathbf{M} = \mathbf{U} \mathbf{\Sigma} \mathbf{V}^*$ , where  $\mathbf{U}$  is an  $m \times m$  complex unitary matrix,  $\mathbf{\Sigma}$  is an  $m \times n$  rectangular diagonal matrix with non-negative real numbers on the diagonal, and  $\mathbf{V}$  is an  $n \times n$  complex unitary matrix. If  $\mathbf{M}$  is real,  $\mathbf{U}$  and  $\mathbf{V}$  can also be guaranteed to be real orthogonal matrices. In such contexts, the SVD is often denoted  $\mathbf{U} \mathbf{\Sigma} \mathbf{V}^T$ .

The diagonal entries  $\sigma_i = \Sigma_{ii}$  of  $\Sigma$  are uniquely determined by M and are known as the singular values of M. The number of non-zero singular values is equal to the rank of M. The columns of U and the columns of V are called left-singular vectors and right-singular vectors of M, respectively. They form two sets of orthonormal bases  $u_1, ..., u_m$  and  $v_1, ..., v_n$ , and the singular value decomposition can be written as v

$$\mathbf{M} = \sum_{i=1}^r \sigma_i \mathbf{u}_i \mathbf{v}_i^*$$
 , where  $r \leq \min\{m,n\}$  is the rank of  $\mathbf{M}$ .

The SVD is not unique. It is always possible to choose the decomposition so that the singular values  $\Sigma_{ii}$  are in descending order. In this case,  $\Sigma$  (but not U and V) is uniquely determined by M.

The term sometimes refers to the **compact SVD**, a similar decomposition  $\mathbf{M} = \mathbf{U} \mathbf{\Sigma} \mathbf{V}^*$  in which  $\mathbf{\Sigma}$  is square diagonal of size  $r \times r$ , where  $r \leq \min\{m,n\}$  is the rank of  $\mathbf{M}$ , and has only the non-zero singular values. In this variant,  $\mathbf{U}$  is an  $m \times r$  semi-unitary matrix and  $\mathbf{V}$  is an  $n \times r$  semi-unitary matrix, such that  $\mathbf{U}^*\mathbf{U} = \mathbf{V}^*\mathbf{V} = \mathbf{I}_r$ .

