

A1.1:

- (a) $f(-1) = -2$
- (b) $f(2) \approx 1.8$
- (c) $f(x) = 2$ at $x = 1$ and $x = -3$
- (d) $f(x) = 0$ at $x \approx -2.5$ and $x \approx 0.4$
- (e) The domain of f is $[-3, 3]$ and the range of f is $[-2, 3]$
- (f) f is increasing on $[-1, 3]$

A1.2:

- (a) $f(-4) = -2$ and $g(3) = 4$
- (b) $f(x) = g(x)$ at $x = -2$ and $x = 2$
- (c) $f(x) = -1$ at $x = -3$ and $x = 4$
- (d) f is decreasing on $[0, 4]$
- (e) The domain of f is $[-4, 4]$ and the range of f is $[-2, 3]$
- (f) The domain of g is $[-4, 3]$ and the range of g is $[0.5, 4]$

A1.3: The range of the vertical ground acceleration function is about $[-70, 120]$
 The range of the north-south ground acceleration function is about $[-300, 420]$
 The range of the east-west ground acceleration function is about $[-200, 200]$

A1.4: Skip

A1.5: Is not a function. Fails the vertical line test.

A1.6: Is a function. The domain is $[-2, 2]$ and the range is $[-1, 2]$

A1.7: Is a function. The domain is $[-3, 2]$ and the range is $[-3, -2) \cup [-1, 3]$

A1.8: Is not a function. Fails the vertical line test.

A1.9: Skip

A1.10: Skip

A1.11: Skip

A1.12: Skip

A1.13: Skip

A1.14: Skip

A1.15: Skip

A1.16: Skip

A1.17: Skip

A1.18: Skip

A1.19:

- $f(2) = 3(2)^2 - 2 + 2 = 3 \cdot 4 = 12$
- $f(-2) = 3(-2)^2 - (-2) + 2 = 3 \cdot 4 + 4 = 16$
- $f(a) = 3a^2 - a + 2$
- $f(-a) = 3(-a)^2 - (-a) + 2 = 3a^2 + a + 2$
- $f(a+1) = 3(a+1)^2 - (a+1) + 2 = 3(a^2 + 2a + 1) - a + 3 = 3a^2 + 5a + 6$
- $2f(a) = 2(3a^2 - a + 2) = 6a^2 - 2a + 4$
- $f(2a) = 3(2a)^2 - 2a + 2 = 3 \cdot 4a^2 - 2a + 2 = 12a^2 - 2a + 2$
- $f(a^2) = 3(a^2)^2 - 2a^2 + 2 = 3a^4 - 2a^2 + 2$
- $[f(a)]^2 = [3a^2 - a + 2]^2 = 9a^4 + a^2 + 4 - 3a^3 + 6a^2 - 2a = 9a^4 + 7a^2 - 3a^3 - 2a + 4$
- $f(a+h) = 3(a+h)^2 - (a+h) + 2 = 3(a^2 + 2ah + h^2) - a - h + 2 = 3a^2 - 2ah + h^2 - a - h + 2$

A1.20: Let $f(r) := V(r+1) - V(r)$

$$\begin{aligned}
 f(r) &= \frac{4}{3}\pi(r+1)^3 - \frac{4}{3}\pi r^3 \\
 &= \frac{4}{3}\pi\left((r+1)^3 - r^3\right) \\
 &= \frac{4}{3}\pi\left(r^3 + 3r^2 + 3r + 1 - r^3\right) \\
 &= \frac{4}{3}\pi\left(3r^2 + 3r + 1\right)
 \end{aligned}$$

A1.21:

$$\begin{aligned}
 f(2+h) &= (2+h) - (2+h)^2 \\
 &= 2+h-4+4h+h^2 \\
 &= h^2+5h-2
 \end{aligned}$$

$$\begin{aligned}
 f(x+h) &= (x+h) - (x+h)^2 \\
 &= x+h-x^2+2hx+h^2 \\
 &= h^2+h+2hx-x^2+x
 \end{aligned}$$

$$\begin{aligned}
 \frac{f(x+h)-f(x)}{h} &= \frac{(h^2+h+2hx-x^2+x)-(x-x^2)}{h} \\
 &= \frac{h^2+h+2hx}{h} \\
 &= h+1+2x
 \end{aligned}$$

A1.22:

$$\begin{aligned}
 f(2+h) &= \frac{2+h}{2+h+1} \\
 &= \frac{2+h}{3+h}
 \end{aligned}$$

$$f(x+h) = \frac{x+h}{x+h+1}$$

$$\begin{aligned} \frac{f(x+h) - f(x)}{h} &= \frac{\frac{x+h}{x+h+1} - \frac{x}{x+1}}{h} \\ &= h^{-1} \left(\frac{(x+h)(x+1)}{(x+h+1)(x+1)} - \frac{x(x+h+1)}{(x+h+1)(x+1)} \right) \\ &= h^{-1} \left(\frac{x^2 + hx + x + h - x^2 - hx - x}{x^2 + hx + x + x + h + 1} \right) \\ &= h^{-1} \left(\frac{h}{x^2 + hx + 2x + h + 1} \right) \\ &= \frac{1}{x^2 + 2x + hx + h + 1} \end{aligned}$$

A1.23: The domain of f is $\mathbb{R} - \{1/3\}$

A1.24: The domain of f is $\mathbb{R} - \{-2, -1\}$

A1.25: The domain of f is $[0, \infty)$

A1.26: The domain of g is $[0, 4]$

A1.27: The domain of h is all x for which $x^2 - 5x > 0$, so either $x < 0$ or $x > 5$. The domain is $(-\infty, 0) \cup (5, \infty)$

A1.28: The domain of this function is $[-2, 2]$, the range of this function is $[0, 2]$. I can't sketch it, but the graph is the upper half of a circle of radius 2 centered at the origin.

A1.29: Domain: \mathbb{R}

A1.30: Domain: \mathbb{R}

A1.31: Domain: \mathbb{R}

A1.32: Domain: $\mathbb{R} - \{2\}$

A1.33: Domain: $[5, \infty)$

A1.34: Domain: \mathbb{R}

A1.35: Domain: $\mathbb{R} - \{0\}$

A1.36: Domain: $\mathbb{R} - \{0\}$

A1.37: Domain: \mathbb{R}

A1.38: Domain: \mathbb{R}

A1.39: Domain: \mathbb{R}

A1.40: Domain: \mathbb{R}

A1.41: The slope is $(-6 - 1)/4 - (-2) = -7/6$. The domain is $[-2, 4]$. So

$$f(x) = -7/6(x+2) + 1 \quad -2 \leq x \leq 4$$

A1.42:

$$f(x) = -5/9(x+3) + 1 \quad -3 \leq x \leq 6$$

A1.43:

$$f(x) = -\sqrt{-x} + 1 \quad x \leq 0$$

A1.44:

$$f(x) = +\sqrt{(1 - (x - 1))^2}$$

A1.45:

$$f(x) = \begin{cases} x + 1 & -1 \leq x < 2 \\ -\frac{3}{2}(x - 2) & 2 \leq x \leq 4 \end{cases}$$

A1.46:

$$f(x) = \begin{cases} -2x + 2 & 0 \leq x < 1 \\ x - 1 & 1 \leq x \end{cases}$$

A1.47: Let l denote length and w denote width. Then a perimeter of 20 means

$$20 = 2l + 2w$$

The area of a rectangle is $A = lw$. We eliminate w by solving for w in the constraint above. We have that $w = (20 - 2l)/2 = 10 - l$. So our function is

$$f(l) = l(10 - l)$$

A1.48: Same as above, but solve for w using the area constraint: $w = 16/l$. Then

$$f(l) = 2l + 2\frac{16}{l} = 2l + \frac{32}{l}$$

A1.49: