VE414 Lecture 19

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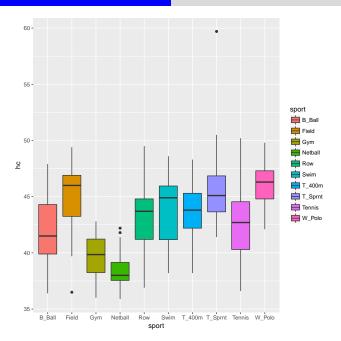
Let us consider the following dataset to illustrate how to use R to build BN

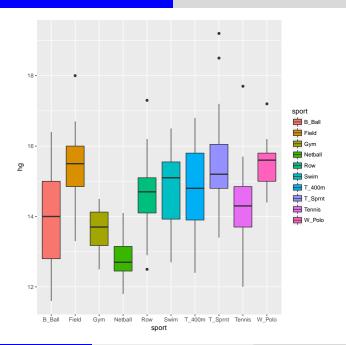
Red blood cell count rcc White blood cell count WCC Hematocrit hс Hemaglobin hg Plasma ferritins ferr bmi Body mass index pcBfat Percentage body fat 1 bm Lean body mass

ht Height wt Weight sex Gender

Sport Various types of sport that the athletes are in

- Suppose we are interested in how various characteristics of the blood varied with sport body size and sex of the athlete. It consists of 202 cases.
- We are particularly interested in hc and hg levels for various sports.





• To start with a simple network, we turn hc and hg into binary

```
> ais$high_hc = as.factor(ais$hc > median(ais$hc))
> ais$high_hg = as.factor(ais$hg > median(ais$hg))
```

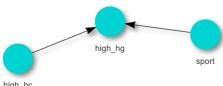
Defining the nodes

```
> structure = empty.graph(
    c("high_hc", "high_hg", "sport"))
```

Defining the links

```
> modelstring(structure) =
```

"[high_hc][sport][high_hg|sport:high_hc]"



Only the following three sports are included

```
> ais.sub = ais[
    ais$sport %in% c("Netball", "Tennis", "W_Polo"),
                c("high_hc", "high_hg", "sport")]
+
> head(ais.sub)
  high_hc high_hg sport
    FALSE
            FALSE Netball
36
37 FALSE FALSE Netball
38 FALSE FALSE Netball
39 FALSE FALSE Netball
40 FALSE FALSE Netball
41
    FALSE FALSE Netball
```

• Asking R to estimate conditional probabilities using frequentist's approach

```
> ais.sub$sport = factor(ais.sub$sport)
> bn.mod = bn.fit(structure,
                  method = "mle", data = ais.sub)
+
```

```
> cat("P(high hg) =",
      cpquery(bn.mod, (high_hg == "TRUE"), TRUE),
+
+ "\n")
P(high hg) = 0.2092
 cat("P(high hg | water polo and high hc) =",
+
      cpquery(bn.mod, (high_hg=="TRUE"),
              (sport == "W_Polo" &
+
                 high_hc == "TRUE")), "\n")
+
P(high hg \mid water polo and high hc) = 0.9292929
> cat("P(water polo | high hg and have high hc) =",
+
      cpquery(bn.mod, (sport == "W_Polo"),
              (high_hg == "TRUE" &
+
                 high_hc == "TRUE")), "\n")
+
P(water polo | high hg and have high hc) = 0.6507937
```

Now consider a hybrid Bayesian network, we use the original hc and hg.

```
> ais.sub = ais[
    ais$sport %in% c("Netball", "Tennis", "W_Polo"),
    c("hc", "hg", "sport")]
+
>
 ais.sub$sport = factor(ais.sub$sport)
>
> head(ais.sub)
    hс
        hg sport
36 42.2 13.6 Netball
37 38.0 12.7 Netball
38 37.5 12.3 Netball
```

39 37.7 12.3 Netball 40 38.7 12.8 Netball 41 36.6 11.8 Netball

- Defining the new nodes
 - > structure = empty.graph(c("hc", "hg", "sport"))
- Defining the links
 - > modelstring(structure) = "[hc][sport][hg|sport:hc]"
- The syntax for fitting is the same

```
> bn.mod = bn.fit(structure,
+ method = "mle", data = ais.sub)
```

Inference can be done using similar syntax

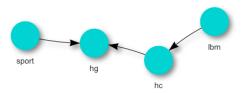
```
> cat("P(hg > 14 | water polo and high hc) =",
+ cpquery(bn.mod, (hg > 14),
+ (sport == "W_Polo" & hc > 42 )), "\n")
```

 $P(hg > 14 \mid water polo and high hc) = 0.9802891$

- Notice this BN corresponds to linear regression
 - > bn.mod

```
Parameters of node hg (conditional Gaussian distribution)
Conditional density: hg | hc + sport
Coefficients:
                   0
(Intercept) 1.5550754 -2.7611358 -0.1173597
            0.2929909 0.4019544 0.3398915
h c
> fit = lm(hg~sport*hc, data = ais.sub)
> summary(fit)
Call:
lm(formula = hg ~ sport * hc, data = ais.sub)
Coefficients:
             Estimate Std. Error t value Pr(>t)
(Intercept) 1.55508 1.43580 1.083 0.2845
sportTennis -4.31621 1.77311 -2.434 0.0190 *
sportW Polo -1.67244 2.29697 -0.728 0.4703
            0.29299 0.03732 7.851 5.68e-10 ***
sportTennis:hc 0.10896 0.04460 2.443
                                       0.0185 *
sportW Polo:hc 0.04690 0.05394 0.870 0.3892
```

Bayesian Network is a pathway to build more complicated models.



Defining the new nodes

```
> structure = empty.graph(
+ c("hc", "hg", "sport", "lbm"))
```

Defining the links

```
> modelstring(structure) =
+ "[lbm][hc|lbm][sport][hg|sport:hc]"
```

```
> ais.sub$sport = factor(ais.sub$sport)
> lbm.mod = bn.fit(structure, data = ais.sub)
> 1 bm.mod
 Parameters of node hg (conditional Gaussian distribution)
Conditional density: hg | hc + sport
Coefficients:
(Intercept) 1.5550754 -2.7611358 -0.1173597
            0.2929909 0.4019544 0.3398915
hс
> bn.mod
 Parameters of node hg (conditional Gaussian distribution)
Conditional density: hg | hc + sport
Coefficients:
                   0
(Intercept) 1.5550754 -2.7611358 -0.1173597
            0.2929909 0.4019544 0.3398915
hс
```

ais\$sport %in% c("Netball", "Tennis", "W_Polo"),

c("hc", "hg", "sport", "lbm")]

> ais.sub = ais[

Q: What is the difference?

We have the following without 1bm.

```
Parameters of node sport (multinomial distribution)

Conditional probability table:
Netball Tennis W_Polo
0.4509804 0.2156863 0.3333333
```

```
Parameters of node hc (Gaussian distribution)

Conditional density: hc

Coefficients:
(Intercept)

41.82353

Standard deviation of the residuals: 4.092363
```

With 1bm. we have

```
Parameters of node 1bm (Gaussian distribution)

Conditional density: 1bm

Coefficients:
(Intercept)
61.91667

Standard deviation of the residuals: 12.00722
```

The marginal probabilities of sport are the same

Parameters of node hc (Gaussian distribution)

```
Parameters of node sport (multinomial distribution)

Conditional probability table:
Netball Tennis W_Polo
0.4509804 0.2156863 0.3333333
```

• With 1bm, we have the following in addition to the above

 $P(hg > 14 \mid water polo and LBM > 65 kg) = 0.8199181$