

Oscillations élastiques forcées

Outils

* **Déphasage** : fonction sinusoïdale **synchrone**.

$$u_1(t) = 4 \sin(100\pi t)$$

$$u_2(t) = 3 \sin(100\pi t + \frac{\pi}{2})$$

isochrone et en même temps

$\Delta\varphi$ entre u_1 et u_2 : $\Delta\varphi = \varphi_1 - \varphi_2$
 $\Delta\varphi$ " u_2 et u_1 : $\Delta\varphi = \varphi_2 - \varphi_1$

$$\Delta\varphi = \varphi_2 - \varphi_1 = \frac{\pi}{2} \text{ rad} > 0$$

u_2 est en avance sur u_1 .

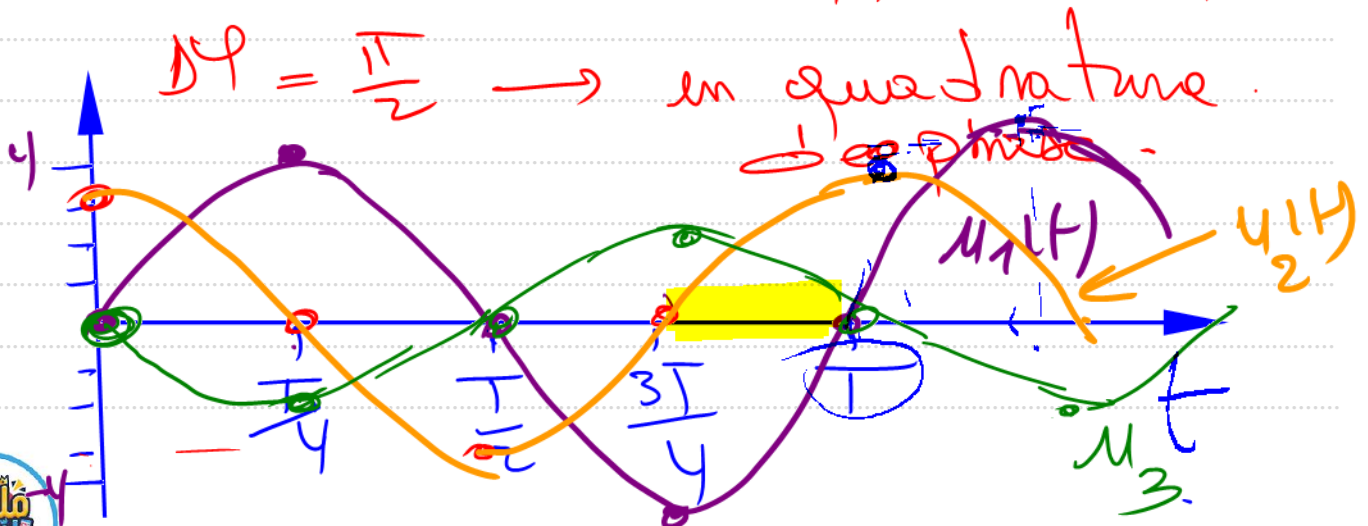
Si $\varphi_2 - \varphi_1 > 0 \rightarrow u_2$ en avance sur u_1 ,

si $\varphi_2 - \varphi_1 < 0 \rightarrow u_2$ en retard sur u_1 ,

$\Delta\varphi = 0 \rightarrow$ en phase

$\Delta\varphi = \pi \rightarrow$ en opposition de phase.

$\Delta\varphi = \frac{\pi}{2} \rightarrow$ en quadrature.



$$\sin t \quad u_2(t) = 2 \sin(100\pi t + \pi)$$

* Décalage Δt

Éap entre u_2 et u_1 $\Delta t = T/4$

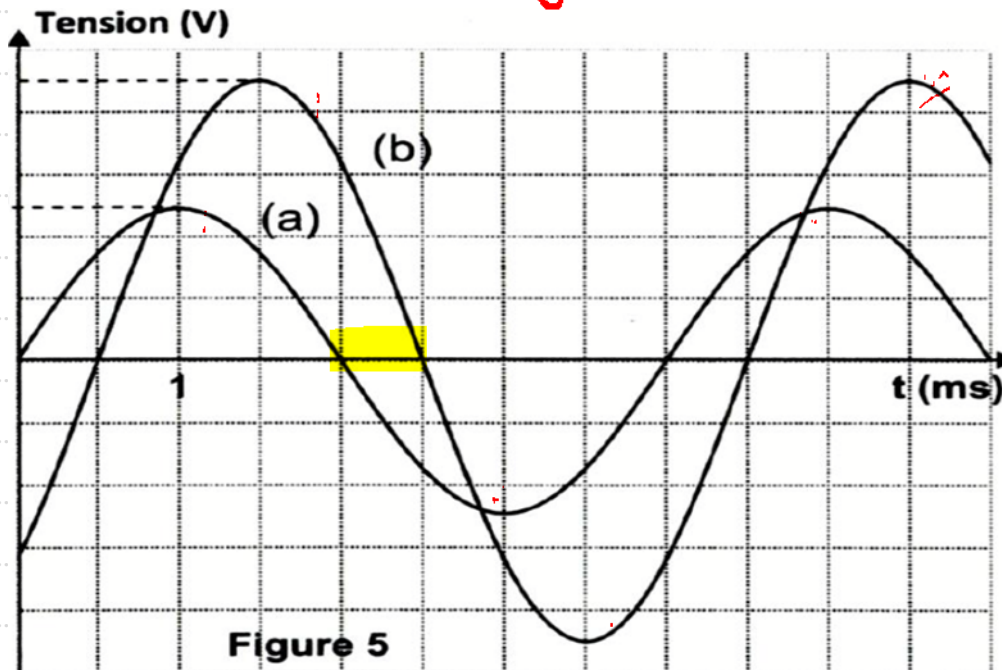
$$\text{Avec } \omega \cdot \Delta t = \frac{2\pi}{T} \cdot \frac{T}{4} = \frac{\pi}{2} \text{ rad}$$

$$= \varphi_2 - \varphi_1$$

Général

$$\odot |\varphi_2 - \varphi_1| = \frac{2\pi}{T} \cdot \Delta t \longrightarrow$$

$$\odot \longrightarrow \text{signe.}$$

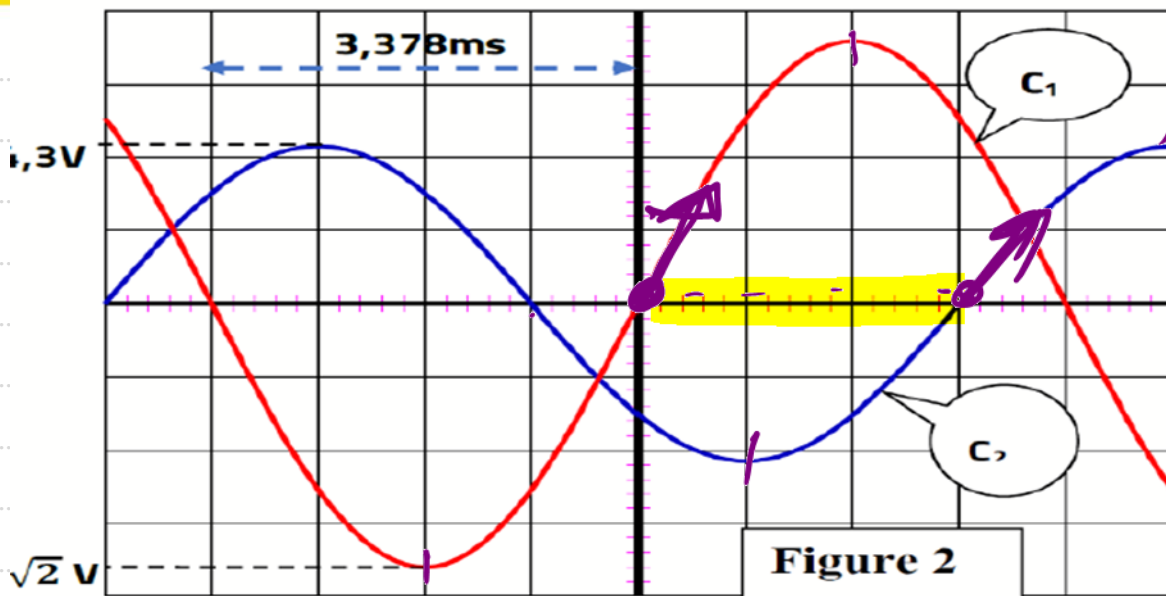


$\Delta t \rightarrow 1 \text{ Div}$
 $T \rightarrow 8 \text{ Div}$

$$|\varphi_b - \varphi_a| = \frac{2\pi}{T} \times \Delta t = \frac{2\pi}{T} \times \frac{T}{8} = \frac{\pi}{4} \text{ rad}$$

Or b en retard.

$$\varphi_b - \varphi_a = -\frac{\pi}{4} \text{ rad}$$



$$\varphi_1 - \varphi_2 = \frac{2\pi}{T} \times \frac{3T}{4} = \frac{3\pi}{2}$$

ou C_1 en avance sur C_2

$$\Rightarrow \varphi_1 - \varphi_2 = \frac{3\pi}{2} \text{ rad}$$

construction ~~de~~ Fresnel.

Problématique : Matz

$$u_1 = U_{1m} \sin(\omega t + \varphi_1) \quad u_2 = U_{2m} \sin(\omega t + \varphi_2)$$

⊙ si $U_{1m} = U_{2m}$

$$u(t) = u_1(t) + u_2(t) = U_m [\sin(a) + \sin(b)]$$

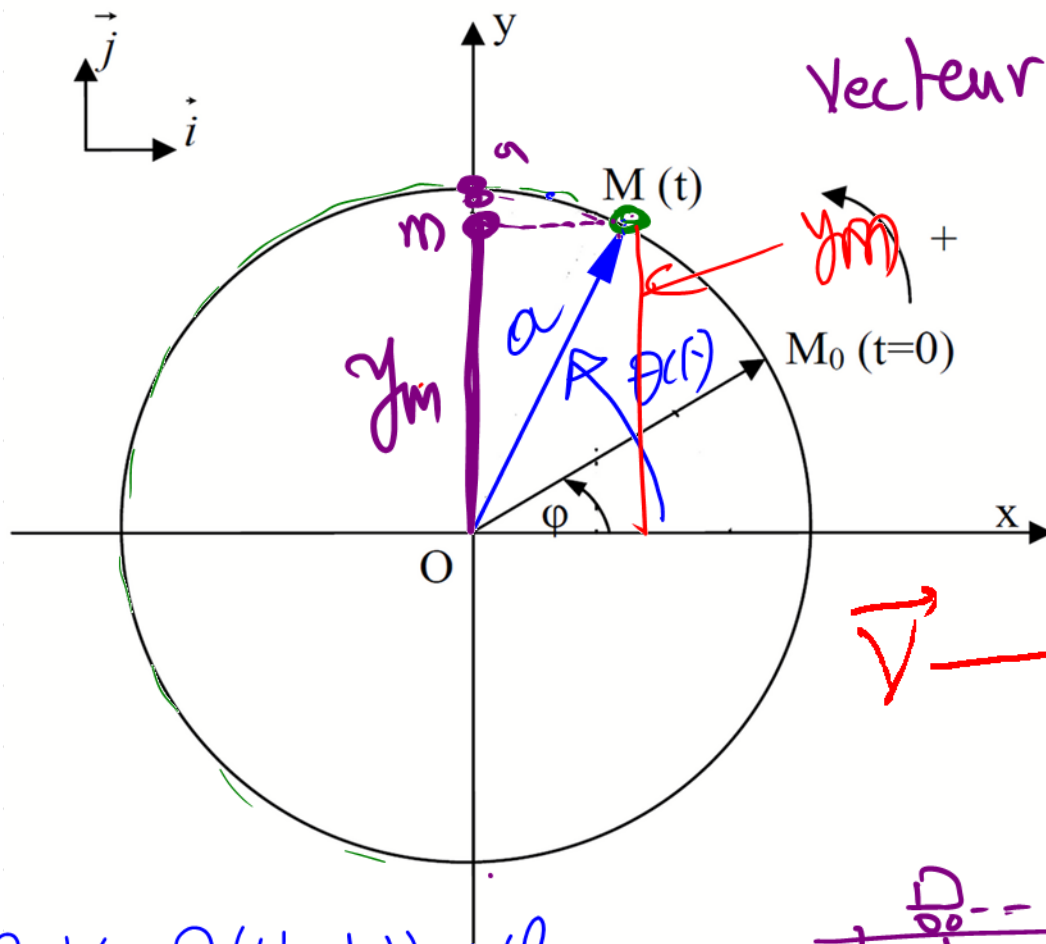
th $\sin a + \sin b = 2 \cos\left(\frac{a-b}{2}\right) \cdot \sin\left(\frac{a+b}{2}\right)$

$$\rightarrow u(t) = 2 \cos\left(\frac{\varphi_1 - \varphi_2}{2}\right) U_m \sin\left(\omega t + \frac{\varphi_1 + \varphi_2}{2}\right)$$

$$u(t) = U_m \sin(\omega t + \varphi)$$

$$\odot \delta: U_{1m} \rightarrow U_{2m}$$

$$u(t) = u_1(t) + u_2(t) = L_m \sin(\omega t + \varphi)$$



Vecteur tournant

$$\vec{v} \rightarrow \frac{d\vec{r}}{dt}$$

$$m \text{ R.P. } v = r\dot{\theta} = v_0$$

$$x(t) = v_0 t + x_0$$

C.U. $\theta(t) = \omega t + \varphi$

$$\frac{y_m}{a} = \sin(\theta(t))$$

$$y_m = a \sin(\omega t + \varphi)$$

$$\vec{v} \rightarrow \frac{d}{dt} (a \sin(\omega t + \varphi))$$

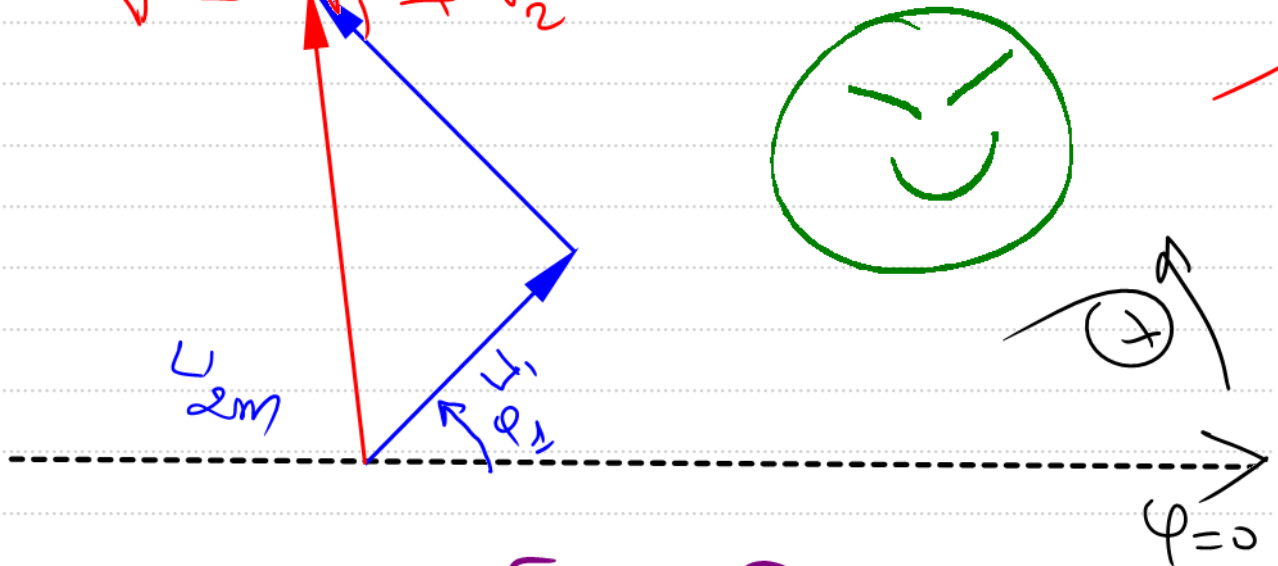
C.U. $\dot{\theta} = \omega$

$$\theta(t) = \dot{\theta} t + \theta_0$$

$$\theta(t) = \omega t + \varphi$$

$$\begin{aligned}
 \mu_1(H) &\longrightarrow \vec{V}_1 & \left(\begin{aligned} L_{1m} &= 4 \text{ V} \\ \varphi_1 &= \frac{\pi}{4} \end{aligned} \right) \\
 \mu_2(H) &\longrightarrow \vec{V}_2 & \left(\begin{aligned} L_{2m} &= 1 \text{ V} \\ \varphi_2 &= \frac{3\pi}{4} \end{aligned} \right) \\
 \mu(H) &\longrightarrow \vec{V} & \left(\begin{aligned} L_m &? \\ \varphi &? \end{aligned} \right)
 \end{aligned}$$

$$\vec{V} = \vec{V}_1 + \vec{V}_2$$



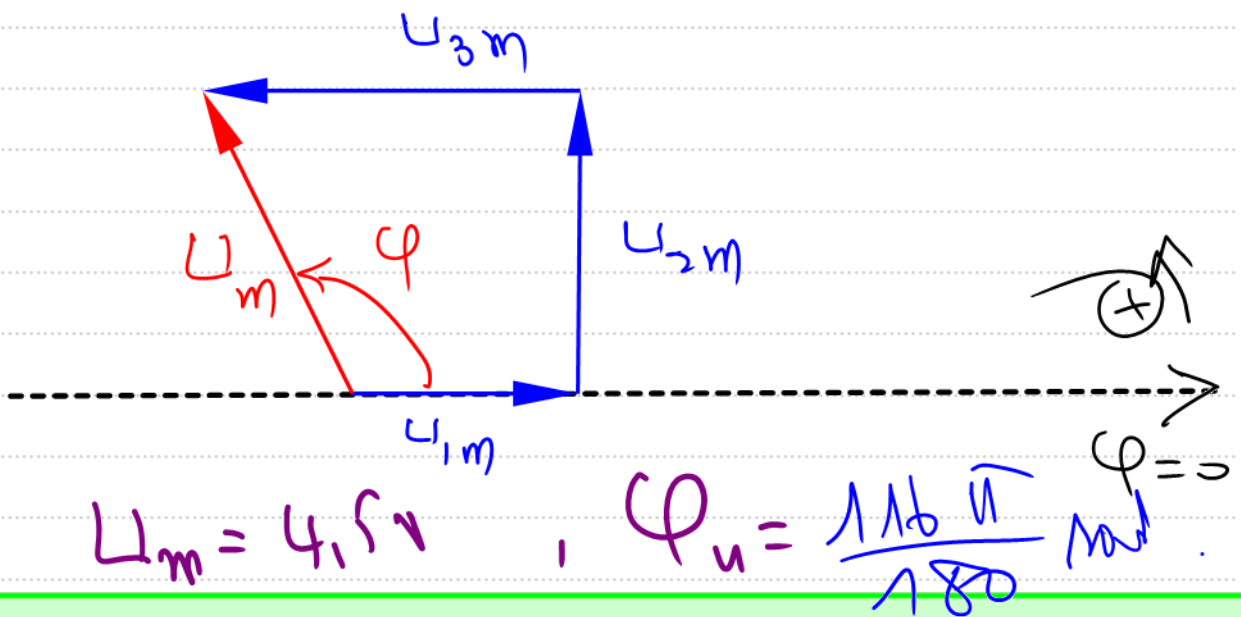
$$\mu(H) = 6.4 \text{ J/T} (1.05\pi + 1.69)$$

$$\begin{aligned}
 180^\circ &\longrightarrow \pi \\
 97 &\longrightarrow ? \quad \frac{97 \cdot \pi}{180}
 \end{aligned}$$

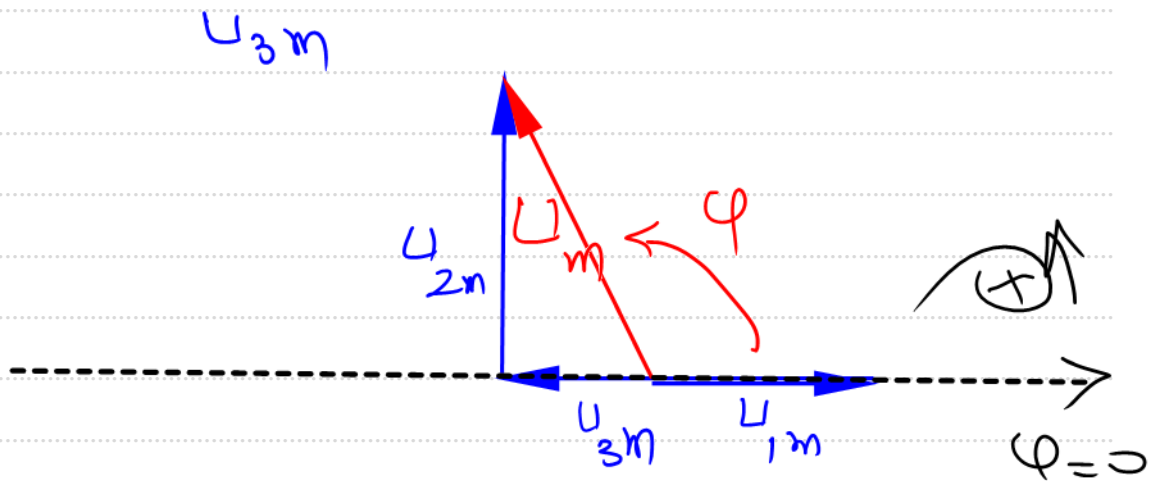
Application $u_1(t) = 3 \sin(\omega t) \rightarrow U_{1m} = 3V$
 $u_2(t) = 4 \sin(\omega t + \frac{\pi}{2}) \rightarrow U_{2m} = 4V$
 $u_3(t) = 5 \sin(\omega t + \pi) \rightarrow U_{3m} = 5V$

? $u(t) = u_1(t) + u_2(t) + u_3(t) = U_m \sin(\omega t + \varphi)$

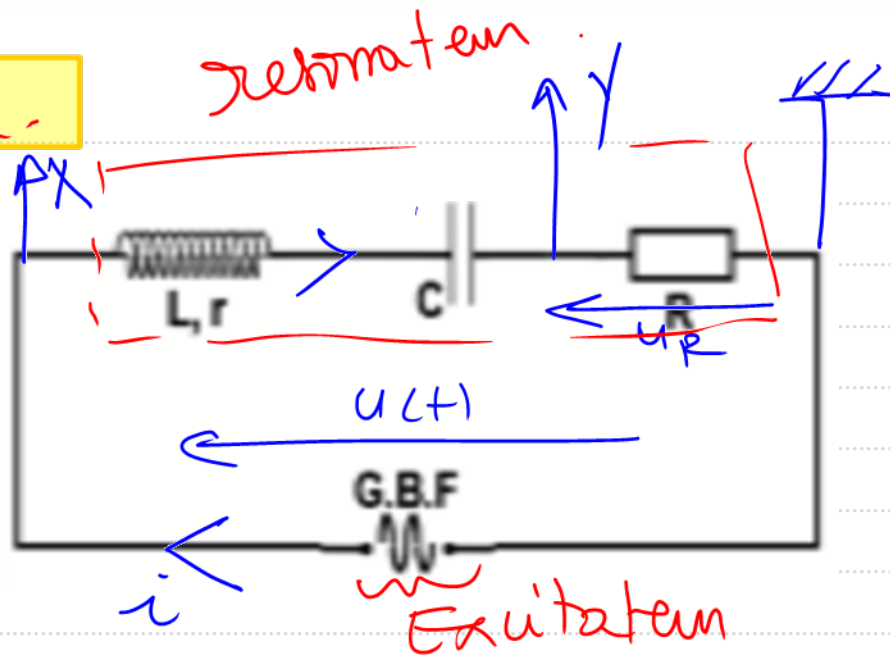
Handwritten notes on the right:
 $U_{1m} = 3V$
 $U_{2m} = 4V$
 $\varphi_2 = \frac{\pi}{2}$
 $U_{3m} = 5V$
 $\frac{3\pi}{11}$



$$u(t) = 4,5 \sin(\omega t + 2,02)$$



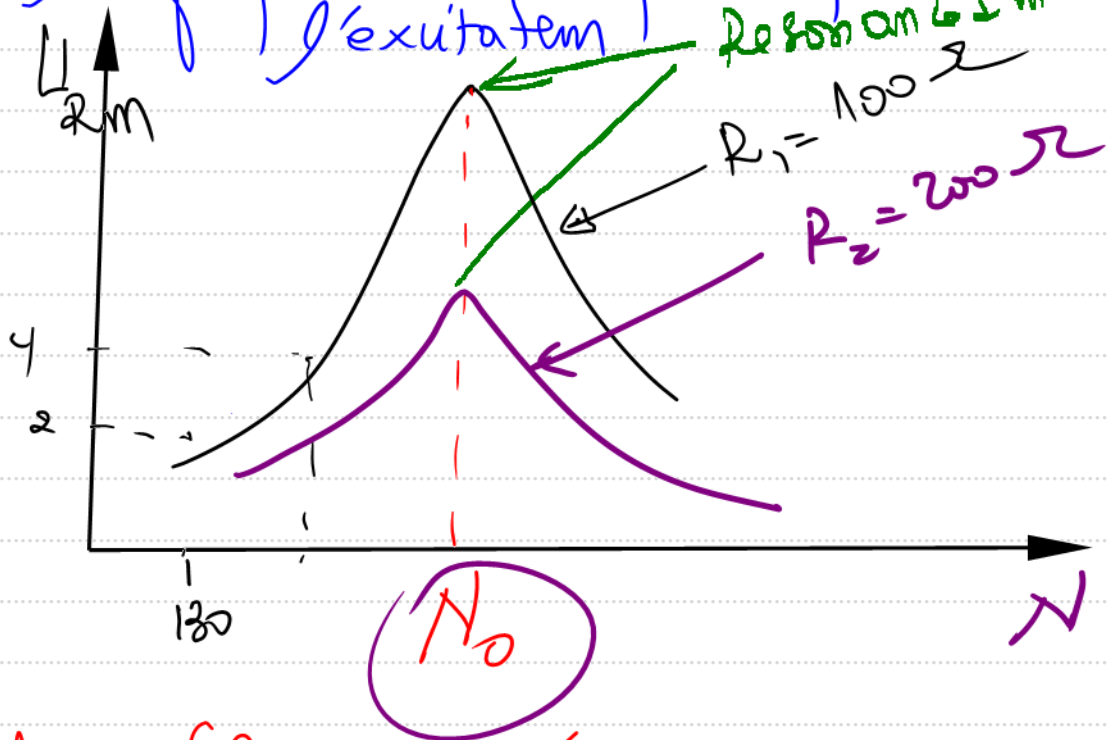
Exercice.

1^o

2) Excitateur \longrightarrow G.B.F
 Résonateur \longrightarrow dipôle R, L, C

3^o car la fréquence est imposée par l'intensité d'excitation

Courbe

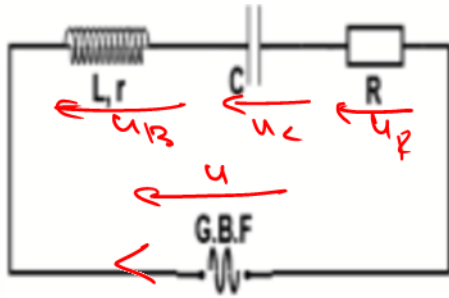


$$\text{si } N < N_0 \quad \varphi_u - \varphi_i < 0$$

$$\text{si } N = N_0 \quad \varphi_u - \varphi_i = 0$$

$$\text{si } N > N_0 \quad \varphi_u - \varphi_i > 0$$

4.2/



Loi des mailles

$$u_R(t) + u_C(t) + u_L(t) = 0$$

$$(R+r)i(t) + L \frac{di}{dt} + \frac{1}{C} q(t) = u(t)$$

$$i = \frac{dq}{dt} \Rightarrow q = \int i dt$$

$$(R+r)i(t) + L \frac{di(t)}{dt} + \frac{1}{C} \int i(t) dt = u(t)$$

$$i(t) = I_m \sin(\omega t + \varphi_i)$$

$$(\sin(at+b))' = a \cos(at+b) = a \sin(at+b + \frac{\pi}{2})$$

$$\int \sin(at+b) = -\frac{1}{a} \cos(at+b) = \frac{1}{a} \sin(at+b - \frac{\pi}{2})$$

$$5.2/ a) (R+r)i(t) = (R+r)I_m \sin(\omega t + \varphi_i) \rightarrow \vec{V}_1 \begin{pmatrix} (R+r)I_m \\ \varphi_i \end{pmatrix}$$

$$L \frac{di}{dt} = L\omega I_m \sin(\omega t + \varphi_i + \frac{\pi}{2}) \rightarrow \vec{V}_2 \begin{pmatrix} L\omega I_m \\ \varphi_i + \frac{\pi}{2} \end{pmatrix}$$

$$\frac{1}{C} \int i(t) = \frac{1}{C} \left(-\frac{I_m}{\omega} \cos(\omega t + \varphi_i) \right) = \frac{I_m}{\omega C} \sin(\omega t + \varphi_i - \frac{\pi}{2}) \rightarrow \vec{V}_3 \begin{pmatrix} \frac{I_m}{\omega C} \\ \varphi_i - \frac{\pi}{2} \end{pmatrix}$$

$$u(t) = U_m \sin(\omega t) \rightarrow \begin{pmatrix} U_m \\ 0 \end{pmatrix}$$

$$\begin{aligned} \downarrow \\ \varphi_u - \varphi_i > 0 \\ \varphi_u \nearrow \varphi_i \rightarrow \varphi. \end{aligned}$$

$$Lw > \frac{1}{cw}$$



$\delta: N < N_b \rightarrow \psi_u - \psi_i < 0 \rightarrow$ Circuit Capacitance

8: $N = n_b \rightarrow \phi_n - \phi_i = 0 \rightarrow$ Circuit resist \rightarrow ^{Capacitor} circuit resist

(b) Pythagoras $(R+Z)^2 I_m^2 + (L\omega I_m - \frac{E_m}{\omega})^2 = U_m^2$
 $I_m^2 \left[(R+Z)^2 + (L\omega - \frac{1}{\omega})^2 \right] = U_m^2$

$$T_m = \frac{L_m}{\sqrt{(R + r)^2 + (L\omega - \frac{1}{c\omega})^2}}$$

⑥ L'impédance Z :

$$Z = \frac{U^{(V)}}{I^{(A)}} = \frac{U_m}{I_m}$$

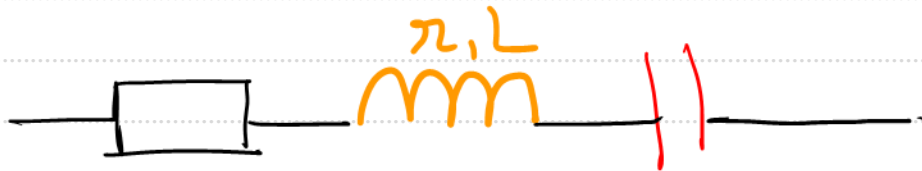
$$\begin{aligned} U &= \frac{U_m}{\sqrt{2}} \quad \text{(eff)} \\ I &= \frac{I_m}{\sqrt{2}} \quad \text{(eff)} \end{aligned}$$

Ampermètre

$$Z = \sqrt{(R+r)^2 + (L\omega - \frac{1}{C\omega})^2}$$

Impédance d'un dipôle R, L, C

NB



$$Z = \sqrt{(R + r)^2 + (L\omega - \frac{1}{C\omega})^2}$$

$$Z_R = R$$

$$Z_C = \frac{1}{C\omega} = \frac{U_{cm}}{I_m}$$

$$Z_B = \sqrt{r^2 + (L\omega)^2} = \frac{U_{Bm}}{I_m}$$

$$Z_{B-C} = \sqrt{r^2 + (L\omega - \frac{1}{C\omega})^2} = \frac{U_{Bcm}}{I_m}$$

$$\lg(\varphi_u - \varphi_i) = \frac{L_w - \frac{\lambda}{c w}}{R + r}$$

