

MA323(Lab-01)

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Problem 1

Case 1: $a=6$, $b=0$, $m=11$

For all x_0 (from 1 to 10), no. of distinct values before repetition are 10.

For $x_0=0$, all corresponding x are 0.

Case 2: $a=3$, $b=0$, $m=11$

For all x_0 (from 1 to 10), no. of distinct values before repetition are 5.

For $x_0=0$, all corresponding x are 0.

So considering both cases, Case 1($a=6$) is a better choice for random function generator because generators with longer period are preferred.

Below figures give output for code (python 180123060_Jatin_q1.py):

Part A) For $a=6$, $b=0$, $m=11$										
x_0	x_1	x_2	x_3	x_4	x_5	x_6	x_7	x_8	x_9	x_{10}
0	0	0	0	0	0	0	0	0	0	0
1	6	3	7	9	10	5	8	4	2	1
2	1	6	3	7	9	10	5	8	4	2
3	7	9	10	5	8	4	2	1	6	3
4	2	1	6	3	7	9	10	5	8	4
5	8	4	2	1	6	3	7	9	10	5
6	3	7	9	10	5	8	4	2	1	6
7	9	10	5	8	4	2	1	6	3	7
8	4	2	1	6	3	7	9	10	5	8
9	10	5	8	4	2	1	6	3	7	9
10	5	8	4	2	1	6	3	7	9	10

Part B) For $a=3$, $b=0$, $m=11$										
x_0	x_1	x_2	x_3	x_4	x_5	x_6	x_7	x_8	x_9	x_{10}
0	0	0	0	0	0	0	0	0	0	0
1	3	9	5	4	1	3	9	5	4	1
2	6	7	10	8	2	6	7	10	8	2
3	9	5	4	1	3	9	5	4	1	3
4	1	3	9	5	4	1	3	9	5	4
5	4	1	3	9	5	4	1	3	9	5
6	7	10	8	2	6	7	10	8	2	6
7	10	8	2	6	7	10	8	2	6	7
8	2	6	7	10	8	2	6	7	10	8
9	5	4	1	3	9	5	4	1	3	9
10	8	2	6	7	10	8	2	6	7	10

Problem 2

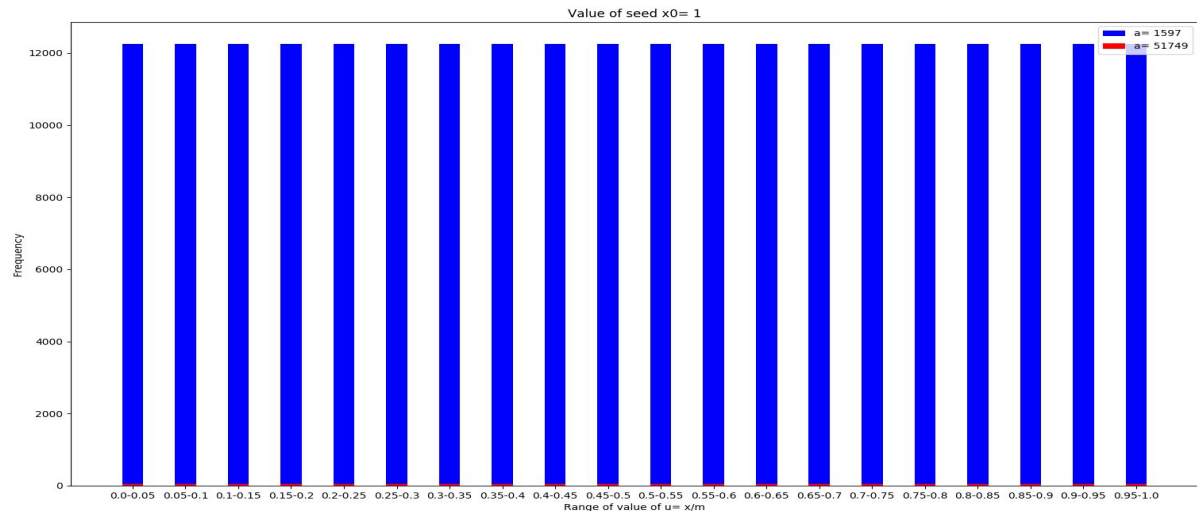
Case 1) $a = 1597$, $m = 244944$

For any x_0 (except 0), period of random generator is 244943. (For code purpose taken x_0 are 1, 2, 3, 4, 5). Frequency in every range was nearly equal (almost 12,247 no. fall in every range).

Case 2) $a = 51749$, $m = 244944$

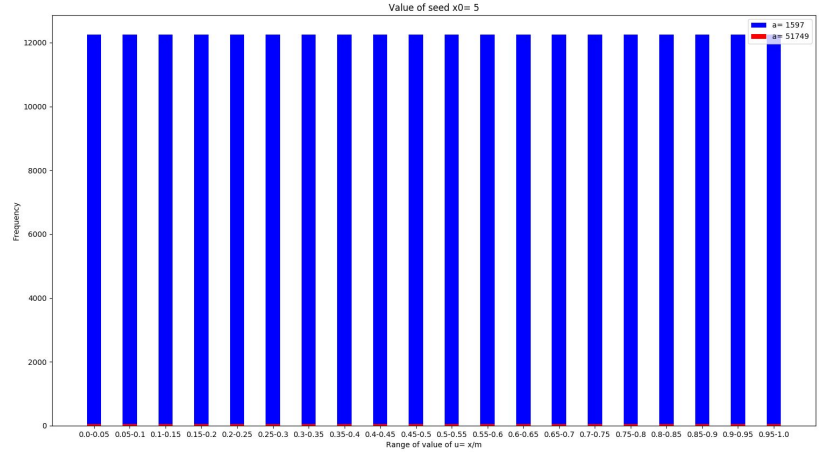
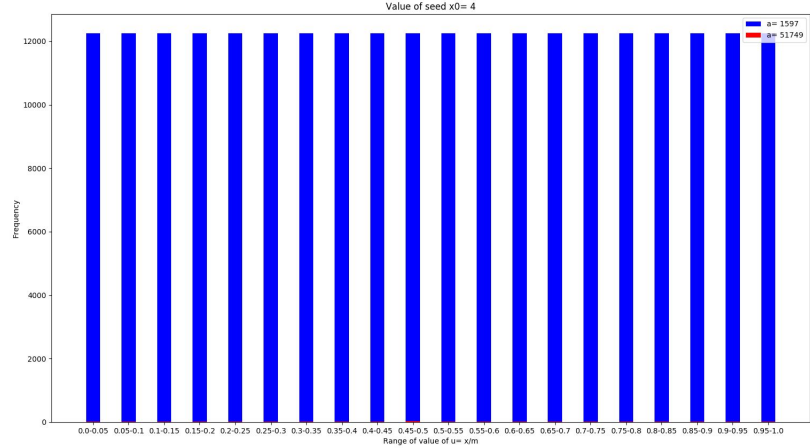
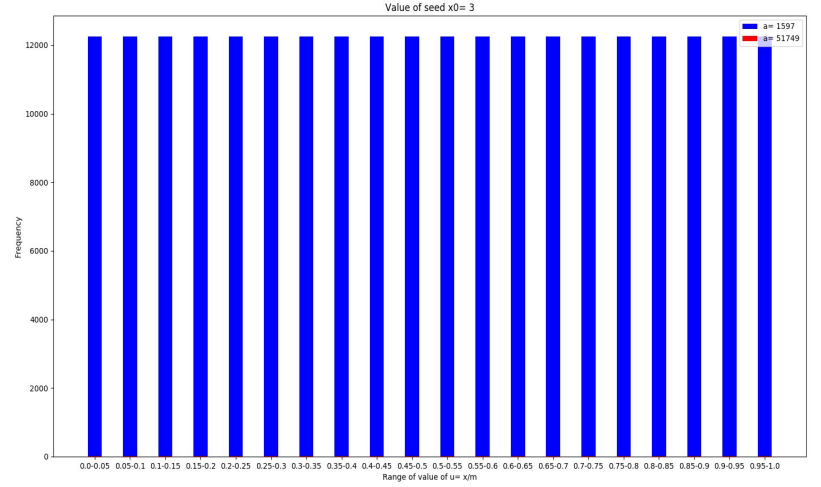
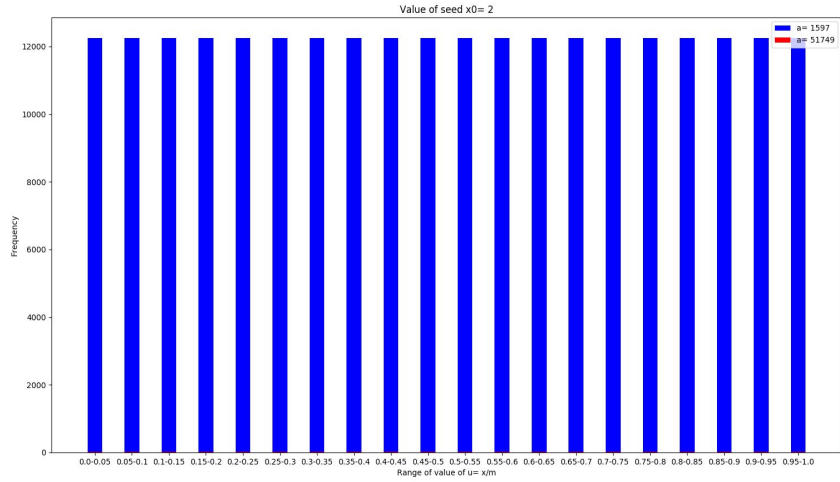
For all x_0 (from 1 to 5), period was different. Frequency in every range was nearly equal but Frequency corresponding to Case 1 was very less. Due to which for all x_0 (from 1 to 5), bars for this case are very small.

Below are 5 bar graph corresponding to $x_0 = 1, 2, 3, 4, 5$. (python 180123060_Jatin_q2.py)



For $x_0 = 1$, \Rightarrow

Red bars are very small because of frequency of every range in Case 2 is very small as compared to Case 1.



Frequency table for a= 1597

For a=1597																				
x\0	0.0-0.05	0.05-0.1	0.1-0.15	0.15-0.2	0.2-0.25	0.25-0.3	0.3-0.35	0.35-0.4	0.4-0.45	0.45-0.5	0.5-0.55	0.55-0.6	0.6-0.65	0.65-0.7	0.7-0.75	0.75-0.8	0.8-0.85	0.85-0.9	0.9-0.95	0.95-1.0
1	12247	12247	12247	12247	12247	12248	12247	12247	12247	12247	12248	12247	12247	12247	12247	12248	12247	12247	12247	12247
2	12247	12247	12247	12247	12247	12248	12247	12247	12247	12247	12248	12247	12247	12247	12247	12248	12247	12247	12247	12247
3	12247	12247	12247	12247	12247	12248	12247	12247	12247	12247	12248	12247	12247	12247	12247	12248	12247	12247	12247	12247
4	12247	12247	12247	12247	12247	12248	12247	12247	12247	12247	12248	12247	12247	12247	12247	12248	12247	12247	12247	12247
5	12247	12247	12247	12247	12247	12248	12247	12247	12247	12247	12248	12247	12247	12247	12247	12248	12247	12247	12247	12247

Frequency table for a= 51749

For a=51749																				
x\0	0.0-0.05	0.05-0.1	0.1-0.15	0.15-0.2	0.2-0.25	0.25-0.3	0.3-0.35	0.35-0.4	0.4-0.45	0.45-0.5	0.5-0.55	0.55-0.6	0.6-0.65	0.65-0.7	0.7-0.75	0.75-0.8	0.8-0.85	0.85-0.9	0.9-0.95	0.95-1.0
1	48	48	49	48	48	49	48	49	49	49	49	48	49	48	48	49	48	49	49	49
2	24	24	24	24	25	24	24	24	24	24	25	24	24	24	25	24	25	24	25	24
3	14	17	17	15	16	17	16	16	17	16	15	17	17	15	16	17	16	16	17	16
4	25	24	24	24	24	24	24	24	24	26	24	24	24	25	24	24	25	24	24	24
5	48	49	49	48	48	49	49	49	48	48	49	49	49	48	48	49	49	49	48	48

Problem 3

Graph b/w $u(i-1)$ and $u(i)$ after running code (python 180123060_Jatin_q3.py)

