

* Longest Subarray with Sum K. {ONLY POSITIVE & 0}

⇒ We have an array arr, of size N with a constant K
all elements in arr are "0 or +ve"

⇒ Find the longest subarray with sum K

$$\left\{ \begin{array}{l} N=7, K=3 \\ [1 \ 2 \ 3 \ \underline{1 \ 1 \ 1}] \end{array} \right\}$$

⇒ Brute Force :- $T(m^3)$, $S(1)$
Sum of all possible subarrays.

⇒ Better Approach :- $T(m)$, $S(m)$
Using unordered map to store the prefix sum till current element, while traversing the array.

On each iteration we have ~~curr~~ sum till current element and the prefix sums till each previous element in a unordered map.

- If the current Sum is found equal to K then compare the maxlenght till now with $i+1$.
- Else if current Sum is greater then K then we need to remove some elements from start w/h we will find in Prefix sum, if found then calculate length and compare with maxlen.
- And finally put current sum with current index in map.

• Example :-

0	1	2	3	4	5
10	5	2	7	1	9
\times	\times	\times	\times	\times	\times

arr = $K=15$

Sum = 10, 15, 17, 24, 25, 34

maxlen = 0, 2, 4

↑ (Ans)

34	→	5
25	→	4
24	→	3
17	→	2
15	→	1
10	→	0

MAP

• NOTE: If there are Negative elements too in array then then the scenerio changes

: because now as we move right in array the prefix sum is not guaranteed to increase

⇒ Suppose prefix sum is S keeps increasing and suddenly a messive \ominus ve number minues the prefix sum back to S, so the longest sum will be array till now.

⇒ But if we apply the same logic of \oplus ve and \ominus s here then the "S" prefix sum appears

⇒ multiple times in array so, the index associated to it will update with the latest index where this prefix sum is found. Which is wrong for max len.
 ⇒ So we will not update ~~the~~ the index with prefix sum even if found again in array. This way we get max len.

• Example

arr =

7	2	13	5	-9	4
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 0 1 2 3 4 5 6

Sum = 7, 9, 10, 13, 18, 9, 13

maxL = 0, 2, 5

18 - 4	
13 → 3	
10 → 2	
9 → 1	Map
7 → 0	

∴ Here we have not updated 9's indices and 13's indices to keep as many as possible elements in subarray

⇒ OPTIMIZED APPROACH :- $T(n)$, $S(1)$

:- Using 2 pointers, we will take in instance the sum of subarray ~~from~~ b/w both pointers.

:- if its equal to k then compare its length with previous max length and update, finally increase right pointer.

:- if its smaller than k then only increase the right pointer to increase subarray size for more sum.

:- else its greater than k so increase the left pointer to remove elements from subarray and decrease the sum.

There is edge case if left exceeds the right then increase right to with it.

:- This whole iteration will run till right pointer is less than "n".