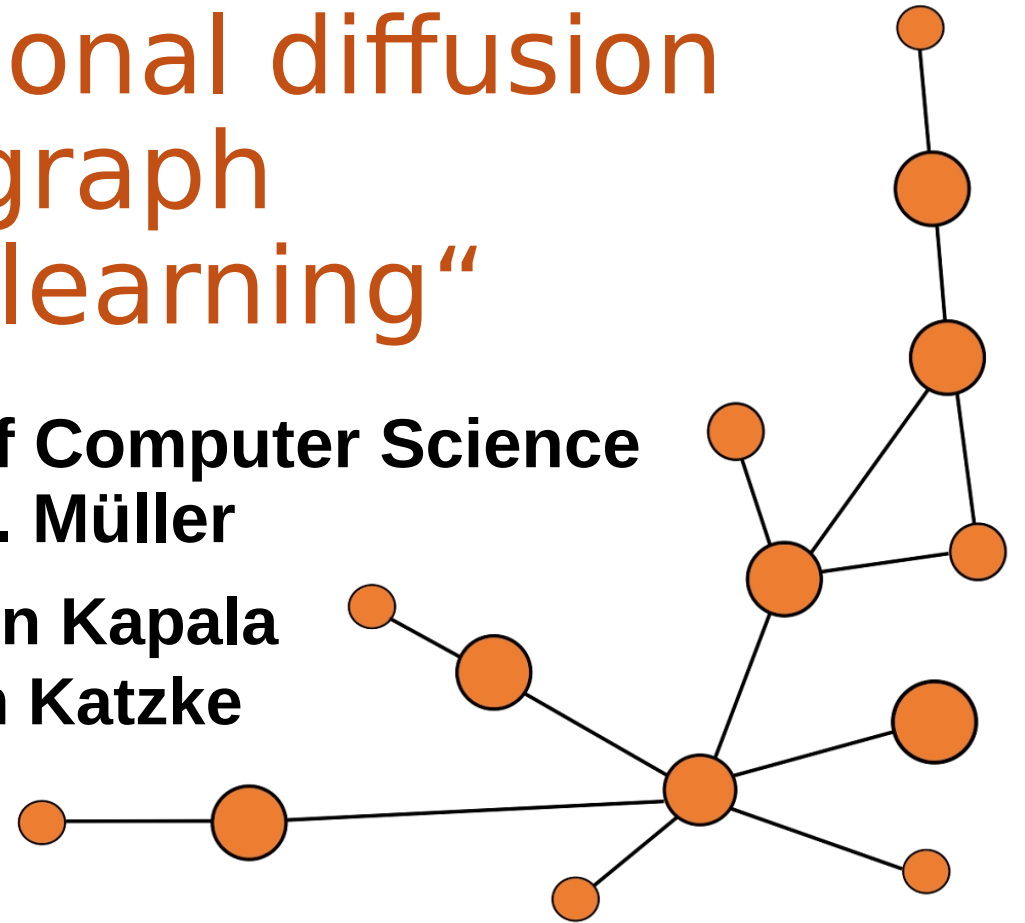


# Hot Topics Of Generative AI: LLMs and Diffusion Models

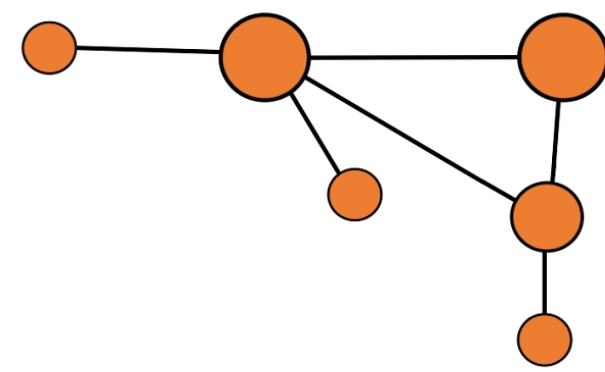
## Yang et al. - “Directional diffusion models for graph representation learning”

**TU Dortmund – Department of Computer Science  
Chair 9 – Prof. Dr. Müller**

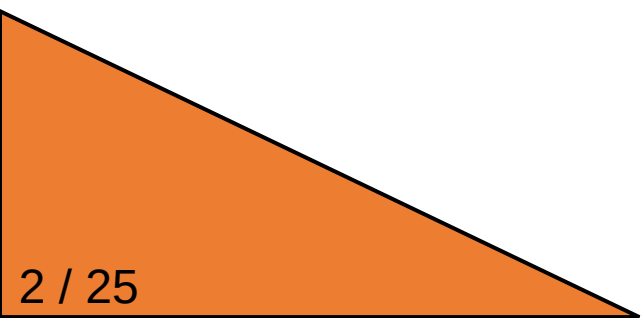
**presented by Marlon Kapala  
supervised by Tim Katzke**

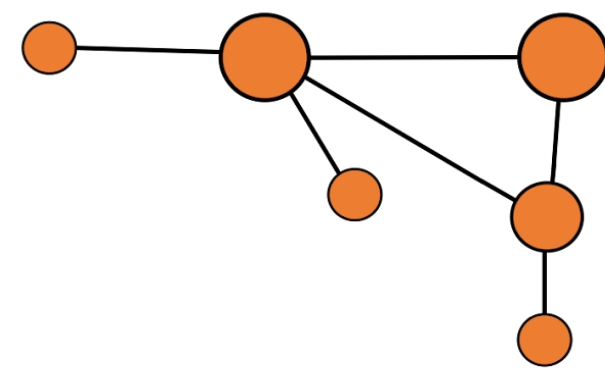


# Agenda

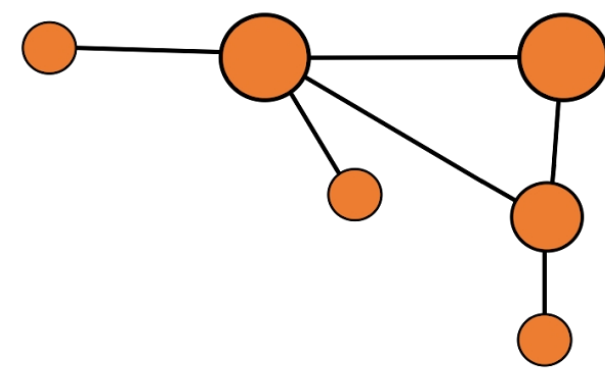


- 1 What is Graph Representation Learning?
- 2 The Emergence of Diffusion Models
- 3 Graphs vs. Images
- 4 The Architecture of Directed Diffusion Models
- 5 Benchmarks
- 6 Conclusion



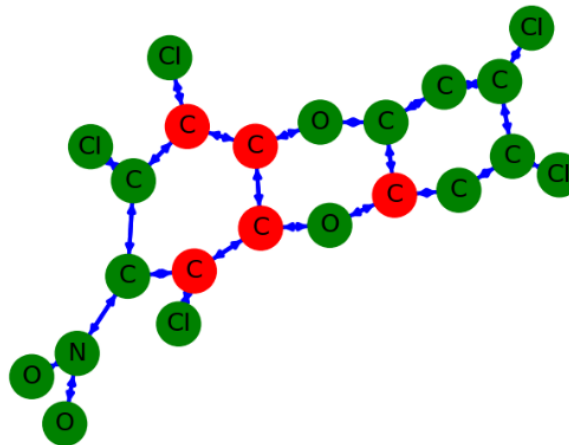


# 1 What is Graph Representation Learning?



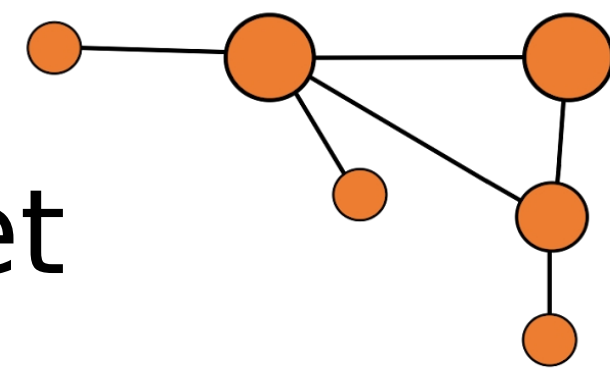
# What is a graph?

- ▶  $G = (V, E)$ , vertices  $V$  and edges  $E$
- ▶ Graphs can represent anything from molecules to road networks or social networks
- ▶ Nodes can also have node features  $X$

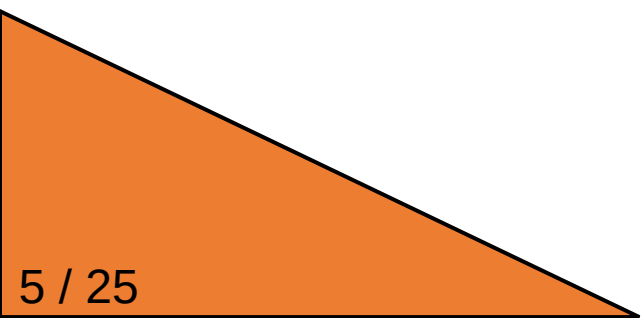
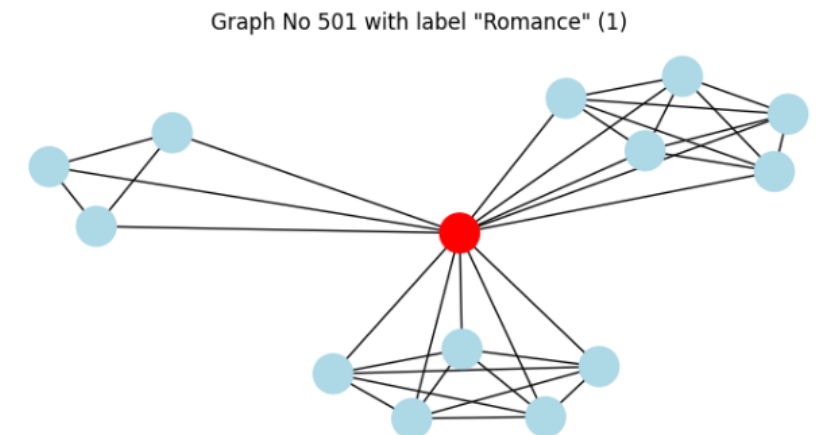
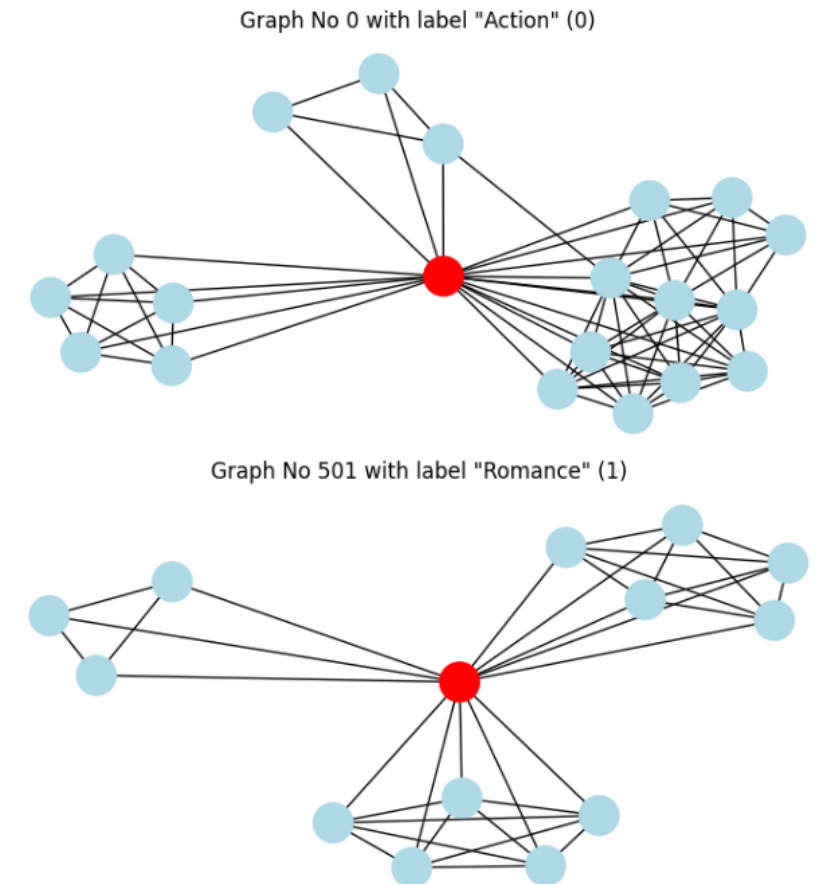


Zhu et al., 2020

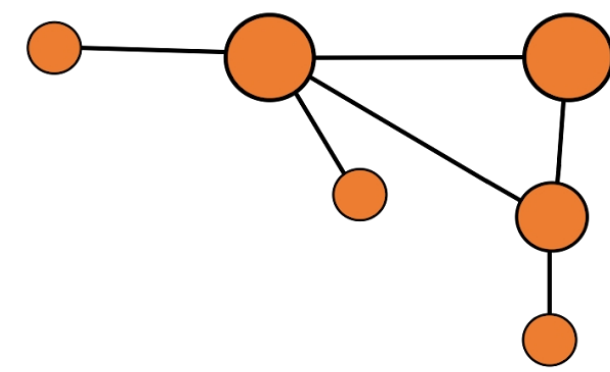
# IMDB-Binary – A Graph Dataset



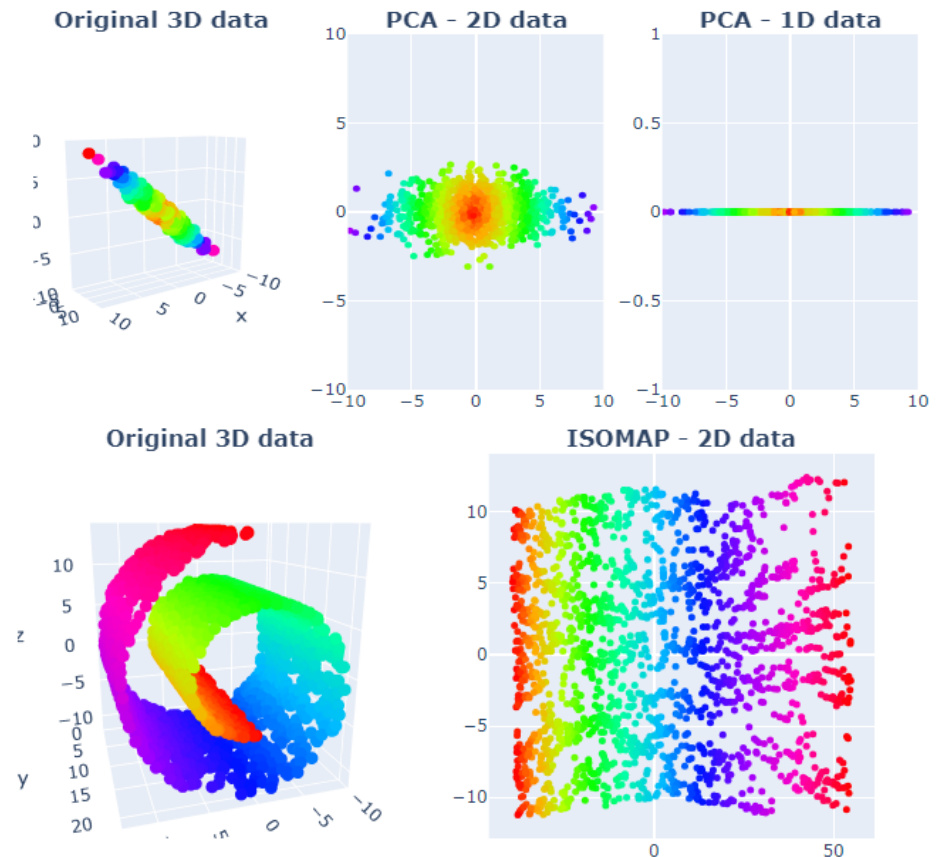
- ▶ Graph Learning works with Graph Datasets
- ▶ IMDB-B contains ego-networks of actors from Action or Romance movies (Yanardag et al., 2015)
- ▶ From only the knowledge how actors have co-starred, models can determine the genre with an accuracy of up to 95% (Nguyen et al., 2019)



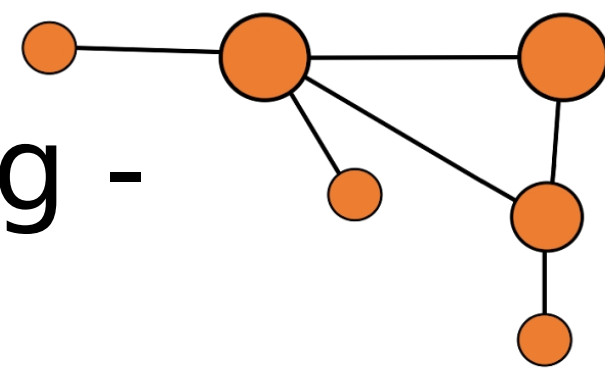
# Representation Learning



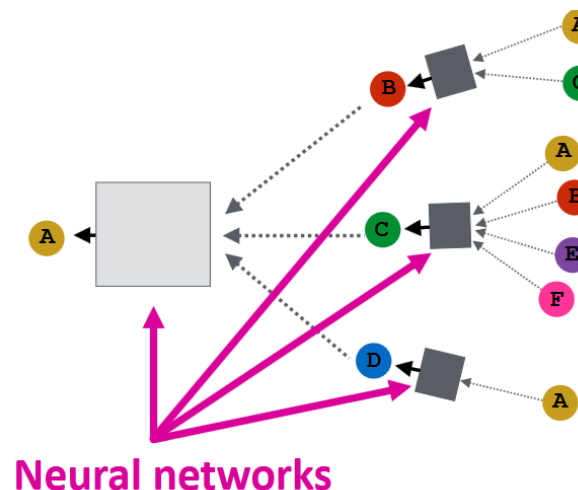
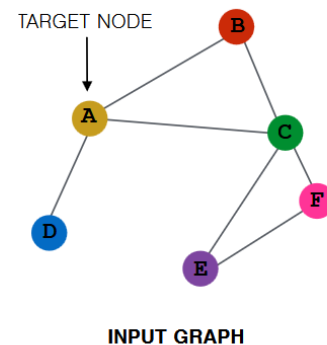
- ▶ RL is an important part of Machine Learning that converts data to a form that can be worked with more easily
- ▶ Here, there is also a difference between unsupervised (without labels) and supervised learning (with labels)
- ▶ Dimensionality Reduction is a prominent subfield

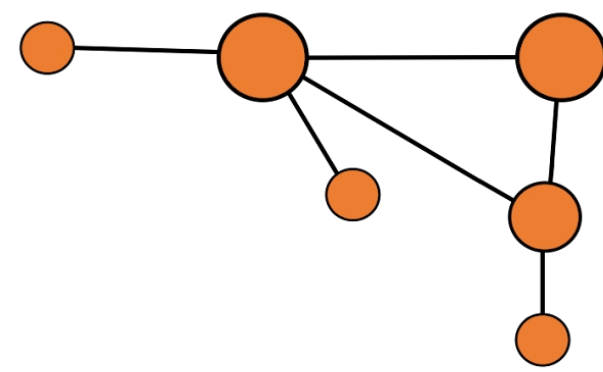


# Graph Representation Learning - GNNs

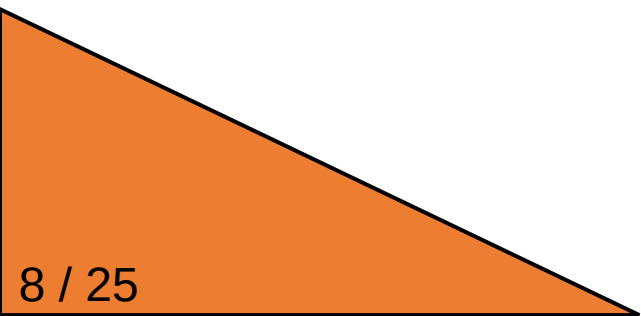


- ▶ For RL on Graphs, Graph Neural Networks are often used
- ▶ They work similar to Convolutional Neural Networks (CNNs)
- ▶ Instead of using neighboring pixels, the adjacency matrix, which encodes the edges, is used

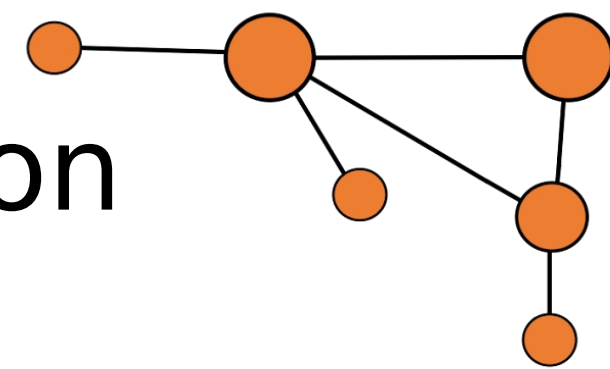




## 2 The Successful Diffusion Model

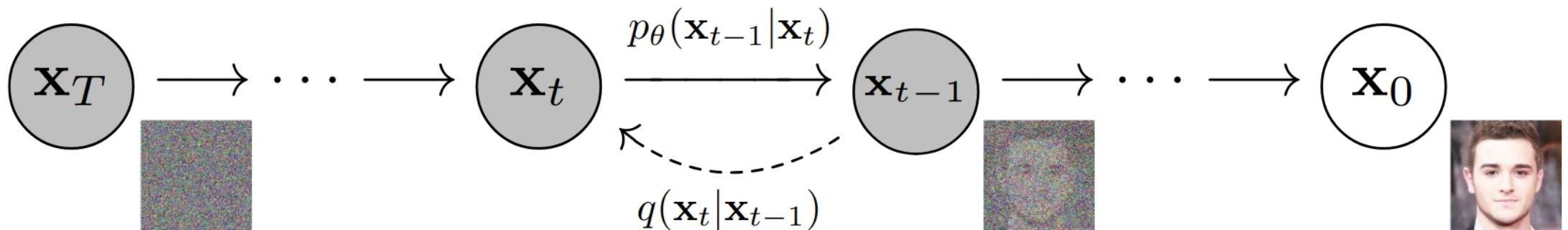




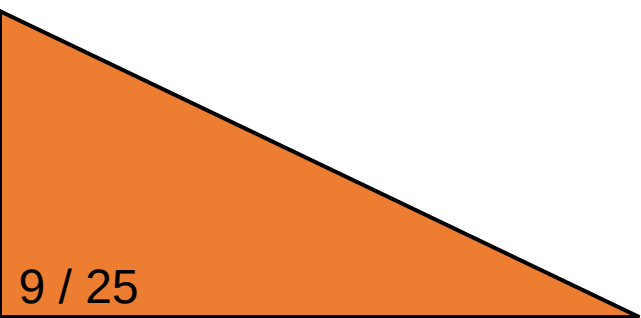


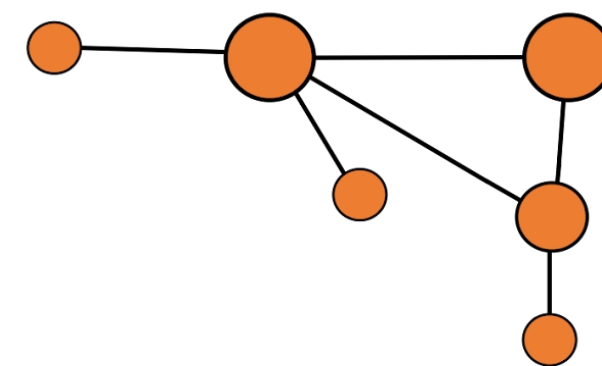
# Denoising Probabilistic Diffusion Models

- Introduced to Machine Learning only recently (Ho et al., 2020), but has become the standard for image generation beating former SOTA technologies (Dhariwal et al., 2021)



Ho et al., 2020





# The DM's Algorithm

- To add noise to the images, Diffusion Models add Gaussian noise in each training step

---

## Algorithm 1 Training

---

```

1: repeat
2:    $\mathbf{x}_0 \sim q(\mathbf{x}_0)$ 
3:    $t \sim \text{Uniform}(\{1, \dots, T\})$ 
4:    $\epsilon \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$ 
5:   Take gradient descent step on
        $\nabla_{\theta} \|\epsilon - \epsilon_{\theta}(\sqrt{\bar{\alpha}_t} \mathbf{x}_0 + \sqrt{1 - \bar{\alpha}_t} \epsilon, t)\|^2$ 
6: until converged
    
```

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## Algorithm 2 Sampling

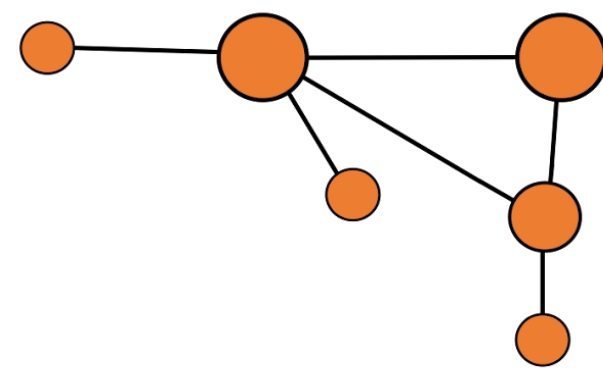
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```

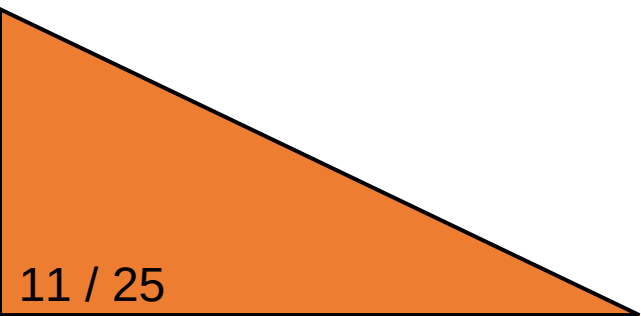
1:  $\mathbf{x}_T \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$ 
2: for  $t = T, \dots, 1$  do
3:    $\mathbf{z} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$  if  $t > 1$ , else  $\mathbf{z} = \mathbf{0}$ 
4:    $\mathbf{x}_{t-1} = \frac{1}{\sqrt{\alpha_t}} \left( \mathbf{x}_t - \frac{1 - \alpha_t}{\sqrt{1 - \bar{\alpha}_t}} \epsilon_{\theta}(\mathbf{x}_t, t) \right) + \sigma_t \mathbf{z}$ 
5: end for
6: return  $\mathbf{x}_0$ 
    
```

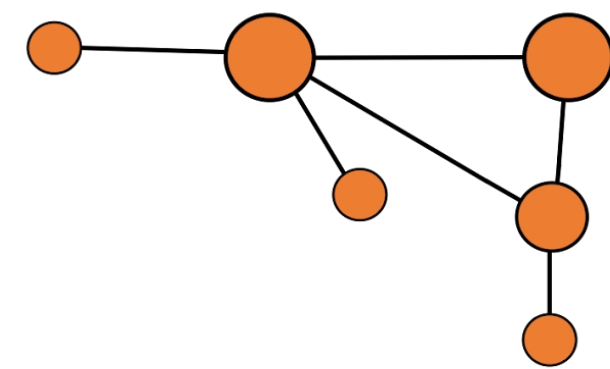
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Ho et al., 2020



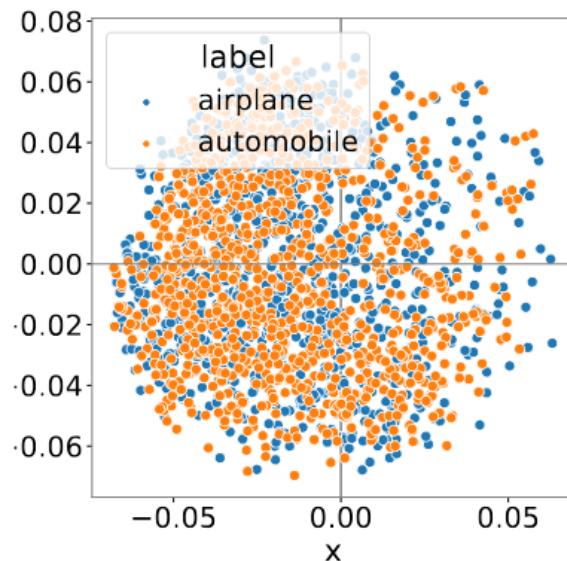
# 3 Graphs vs. Images



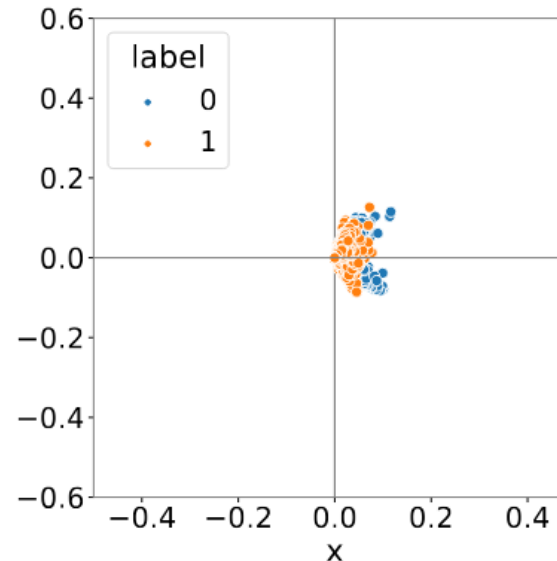


# The Anisotropy of Graphs

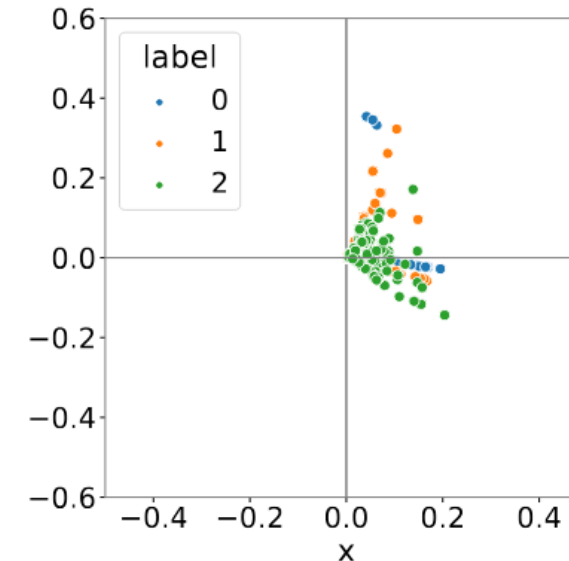
- ▶ While images are naturally isotropic and euclidean, Graphs are anisotropic (i. e., properties vary with direction)



(a) CIFAR-10

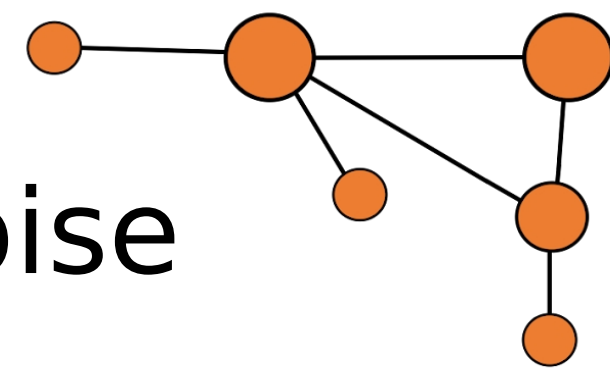


(b) Amazon-Photo



(c) IMDB-M

Yang et al., 2023



# White Noise vs. Directional Noise

- ▶ Hence, Yang et al. introduce “Directional Noise”:

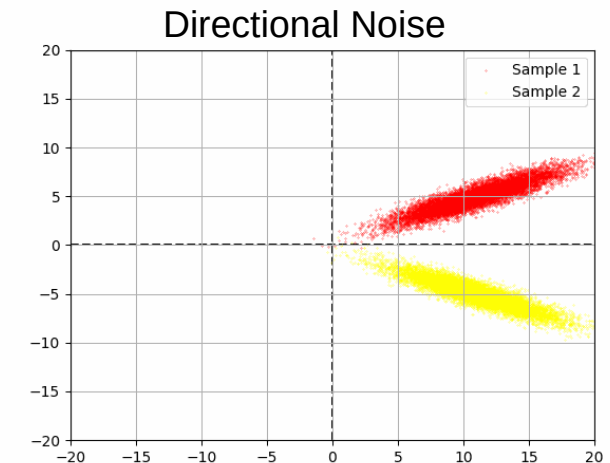
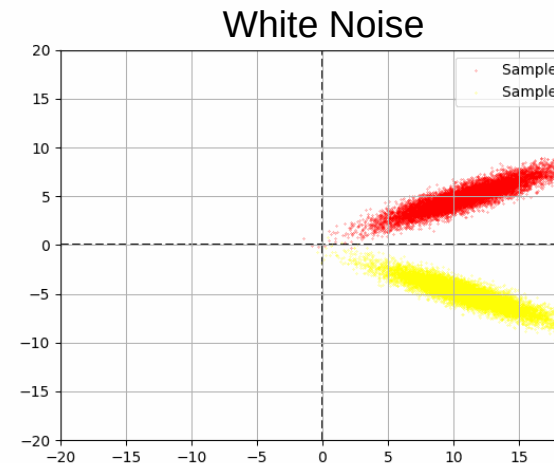
$$x_{t,i} = \sqrt{\bar{\alpha}_t} x_{0,i} + \sqrt{1 - \bar{\alpha}_t} \epsilon',$$

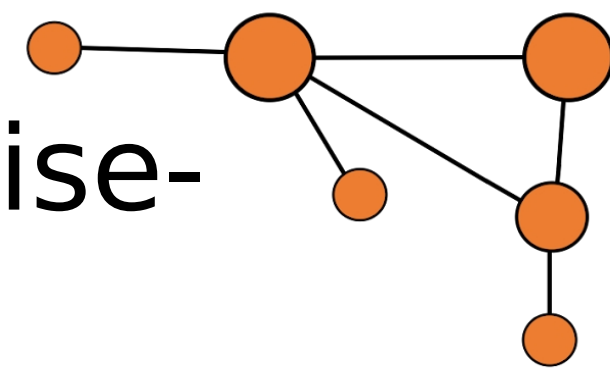
$$\epsilon' = \text{sgn}(x_{0,i}) \odot |\bar{\epsilon}|,$$

$$\bar{\epsilon} = \mu + \sigma \odot \epsilon \quad \text{where } \epsilon \sim \mathcal{N}(0, \mathbf{I})$$

- ▶  $\alpha$  and  $\beta$  are the noise schedule analogous to Ho’s paper

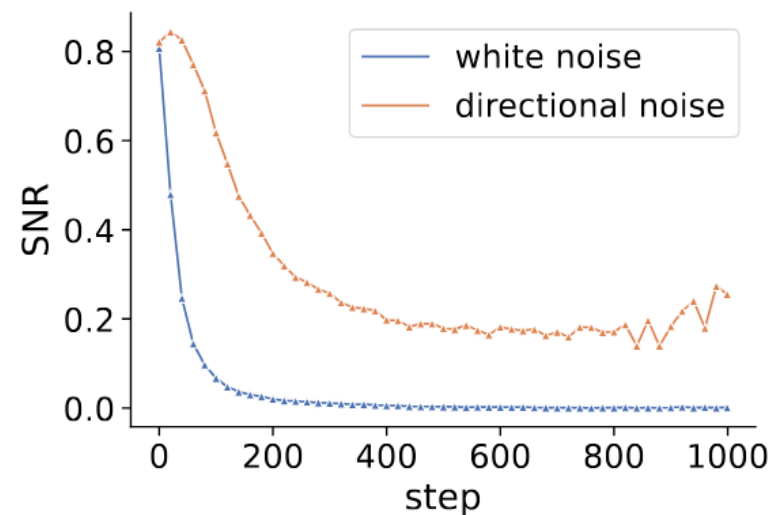
$$\bar{\alpha}_t := \prod_{i=0}^t (1 - \beta_i) \in (0, 1)$$





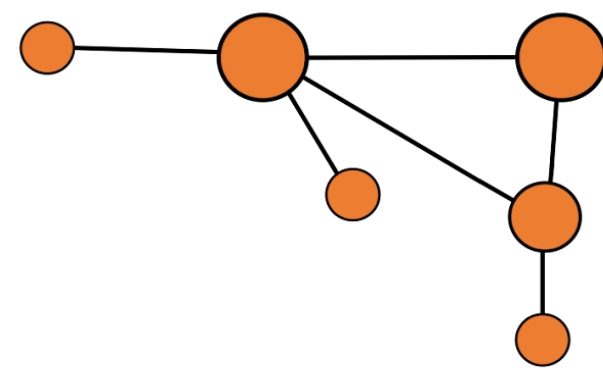
# The effect on the Signal-To-Noise-Ratio

- ▶ The Signal-To-Noise-Ratio is fundamental for the learning process of Diffusion Models
- ▶ The application of directional noise has a vital effect on the SNR

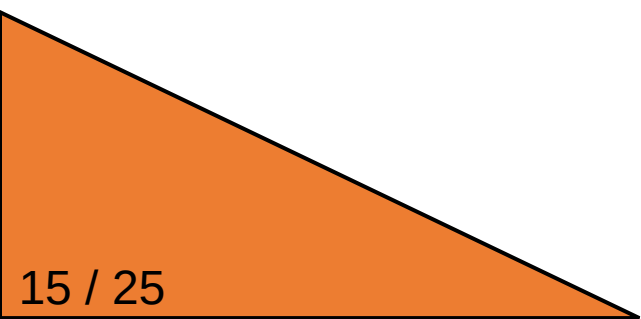


(a) Amazon-Photo

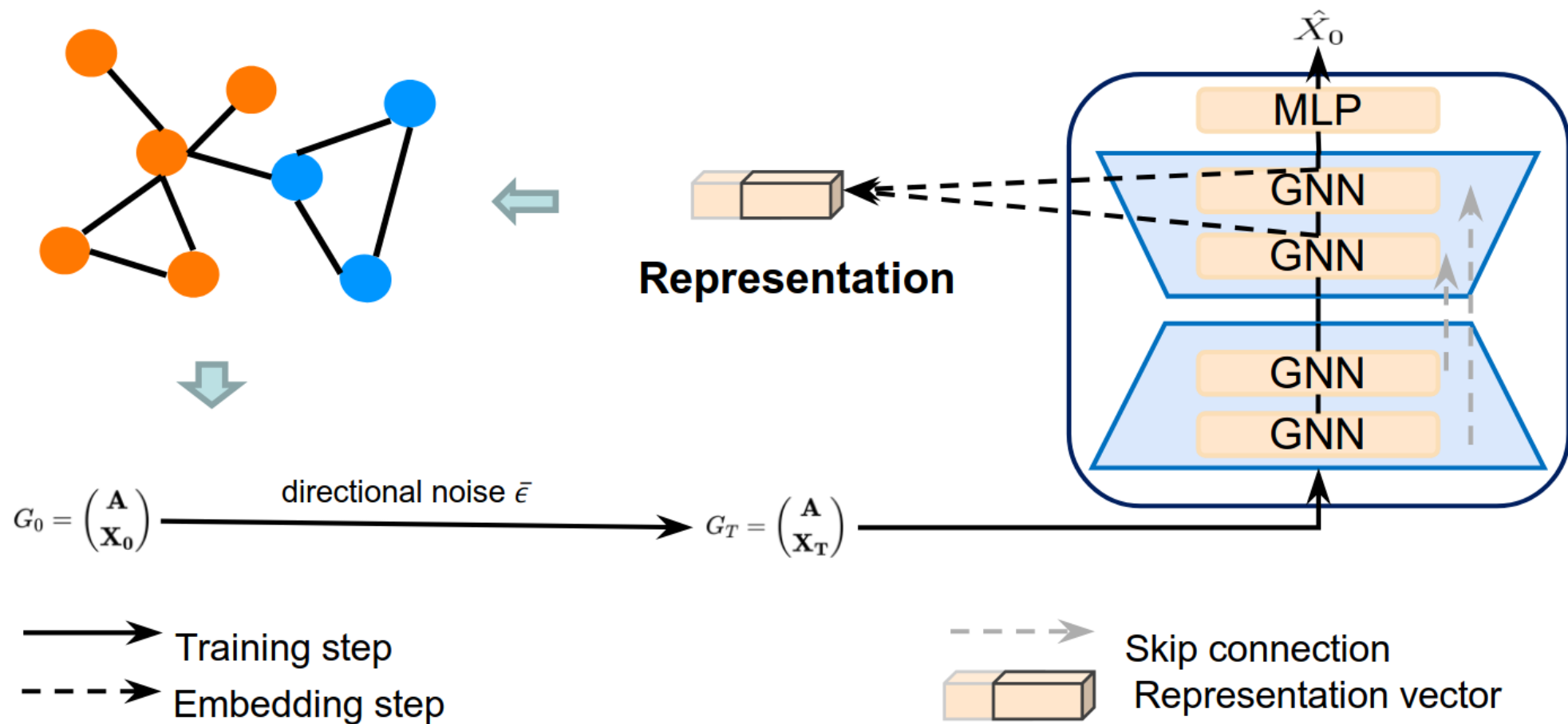
Yang et al., 2023



# 4 Directional Diffusion Models - Architecture

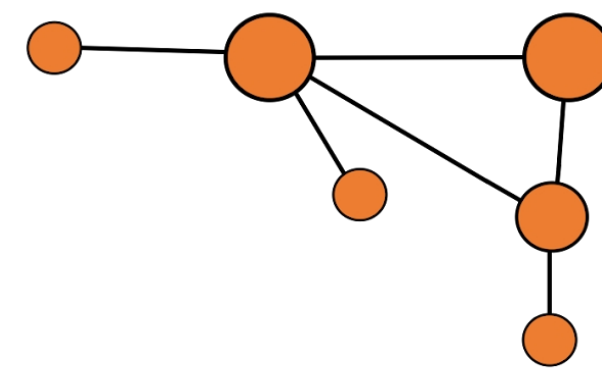


# Components of the Model



Yang et al., 2023





# The Training Algorithm

- Similar to the DPDM algorithm

---

**Algorithm 1** The training algorithm.

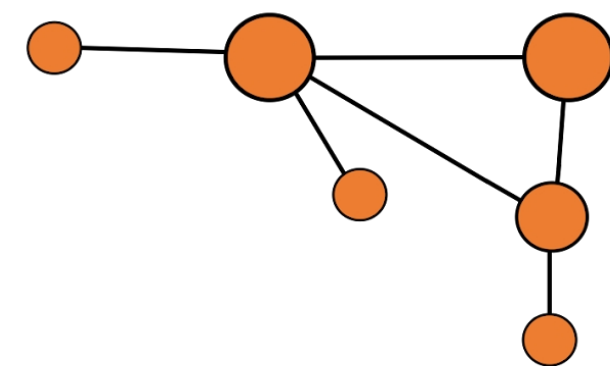
---

**Input:** A batch of graphs  $\mathcal{G} = \{G_1, \dots, G_B\}$

**Output:** The denoising network  $f_\theta$

---

- 1: **Initialize:** the denoising network  $f_\theta$
  - 2: **Compute**  $\mu$ , the mean of node features across batch  $\mathcal{G}$
  - 3: **Compute**  $\sigma$ , the standard deviation of node features across batch  $\mathcal{G}$
  - 4: **while** not convergence **do**
  - 5:     **for**  $G_i$  in  $\mathcal{G}$  **do**
  - 6:         **for**  $t = 1, \dots, T$  **do**
  - 7:             **Sample** directional noise  $\epsilon'$  using equation (2)
  - 8:             **Take** gradient descent step on  
 $\nabla_\theta \|\mathbf{X}_0 - f_\theta(\sqrt{\bar{\alpha}_t}\mathbf{X}_i + \sqrt{1 - \bar{\alpha}_t}\epsilon', \mathbf{A}, t)\|$
  - 9:         **end for**
  - 10:     **end for**
  - 11: **end while**
-



# The Extraction Algorithm

- Instead of generating an image, a representation is generated

---

**Algorithm 2** Extracting representations.

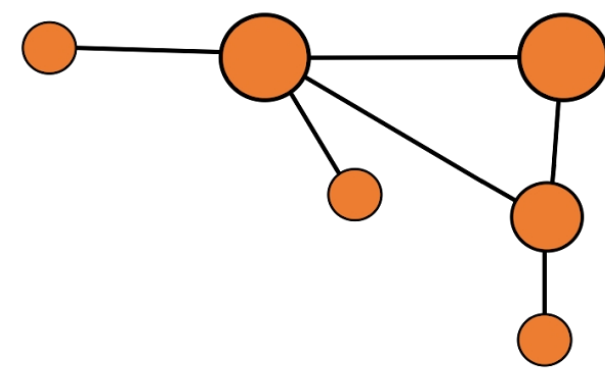
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**Input:**  $G = (\mathbf{A}, \mathbf{X})$ , forward step set  $\{T_0, T_1, \dots, T_K\}$ , pre-trained denoising network  $f_\theta$

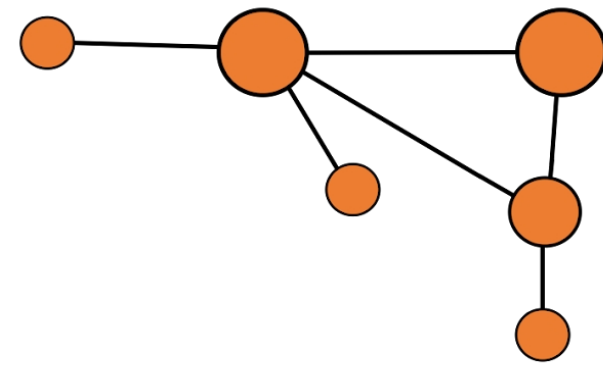
**Output:**  $\mathbf{H}$ , the representation of  $G$

---

- 1: **Compute**  $\mu$  the mean of node features
  - 2: **Compute**  $\sigma$  the standard deviation of node features
  - 3: **for**  $k$  in  $\{T_0, T_1, \dots, T_K\}$  **do**
  - 4:     **Sample** directional noise  $\epsilon'$  using equation (2)
  - 5:      $\mathbf{X}_k \leftarrow \sqrt{\bar{\alpha}_k} \mathbf{X}_0 + \sqrt{1 - \bar{\alpha}_k} \epsilon'$
  - 6:      $\mathbf{H}_k \leftarrow f_\theta(\mathbf{X}_k, \mathbf{A}, k)$
  - 7: **end for**
  - 8: **Concatenate**  $\mathbf{H} = [\mathbf{H}_{T_0}, \mathbf{H}_{T_1}, \dots, \mathbf{H}_{T_K}]$
  - 9: **return**  $\mathbf{H}$
-

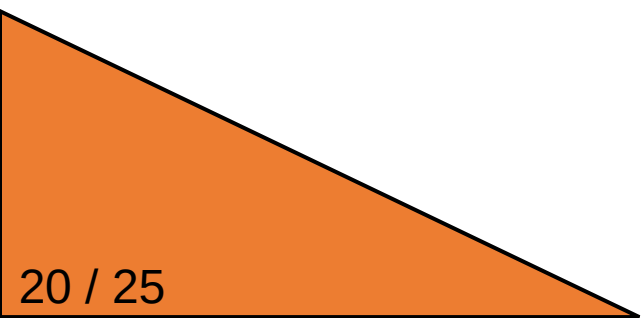


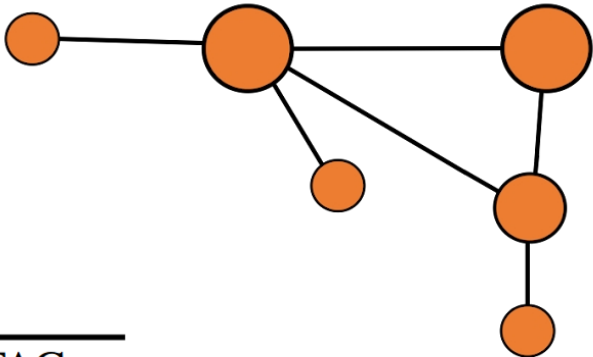
# 5 Resulting Benchmarks



# Graph Classification

- ▶ The paper compares multiple State-Of-The-Art models with DDMs
- ▶ SVMs are used on the learned representations
- ▶ While here only graph classification results are presented, the results from node classification are similarly promising

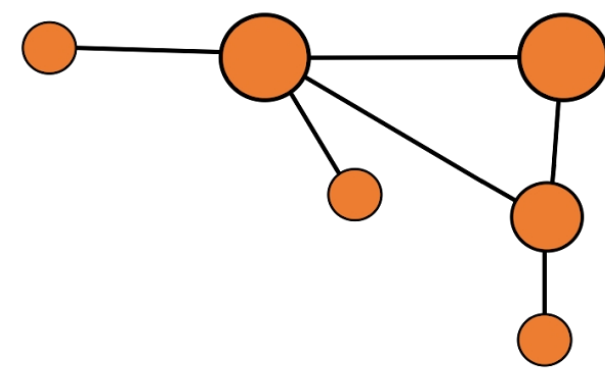




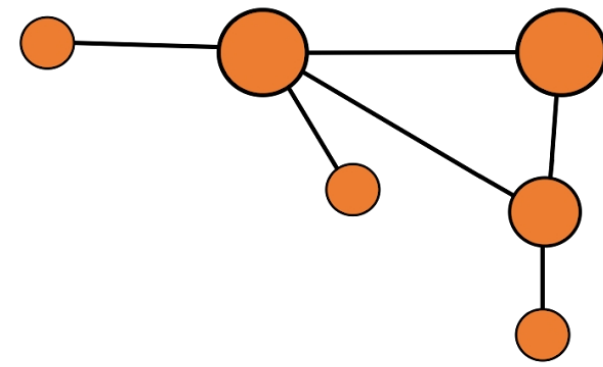
# Results

Dataset	IMDB-B	IMDB-M	COLLAB	REDDIT-B	PROTEINS	MUTAG	
GIN	75.1±5.1	52.3±2.8	80.2±1.9	92.4±2.5	76.2±2.8	89.4±5.6	} supervised
DiffPool	72.6±3.9	-	78.9±2.3	92.1±2.6	75.1±2.3	85.0±10.3	
Infograph	73.03±0.87	49.69±0.53	70.65±1.13	82.50±1.42	74.44±0.31	89.01±1.13	} unsupervised
GraphCL	71.14±0.44	48.58±0.67	71.36±1.15	89.53±0.84	74.39±0.45	86.80±1.34	
JOAO	70.21±3.08	49.20±0.77	69.50±0.36	85.29±1.35	74.55±0.41	87.35±1.02	
GCC	72	49.4	78.9	89.8	-	-	
MVGRL	74.20±0.70	51.20±0.50	-	84.50±0.60	-	89.70±1.10	
GraphMAE	75.52±0.66	51.63±0.52	80.32±0.46	88.01±0.19	75.30±0.39	88.19±1.26	
DDM	<b>76.40±0.22</b>	<b>52.53±0.31</b>	<b>81.72±0.31</b>	89.15 ±1.3	<b>75.47 ±0.50</b>	<b>91.51 ±1.45</b>	

Yang et al., 2023

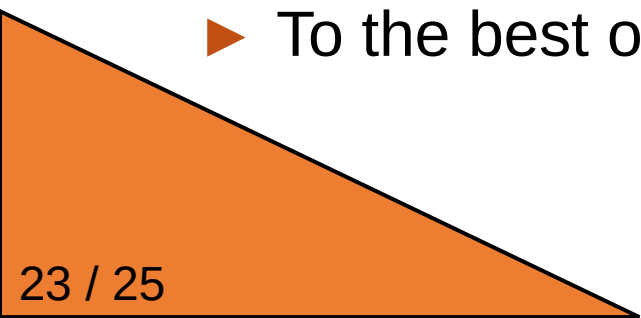


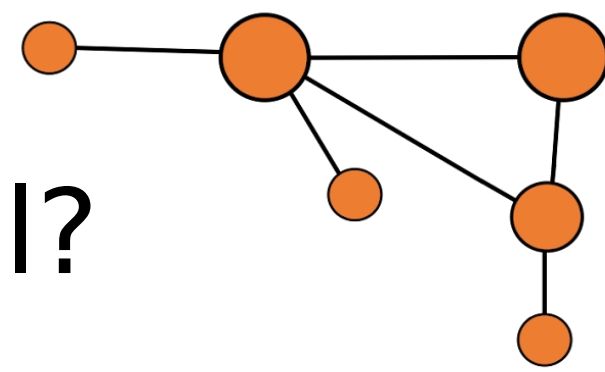
# 6 Conclusion



# Research Outlook

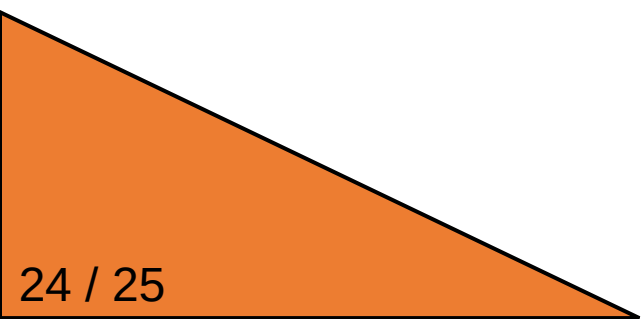
- ▶ Yang et al. only introduce the idea, they admit that their hyperparameters are not optimal yet
- ▶ One open question is how the optimal set of diffusion steps can be determined
- ▶ Variants of DDMMs could bring value to areas such as computer vision and natural language processing
- ▶ To the best of my knowledge, nobody has yet continued their work



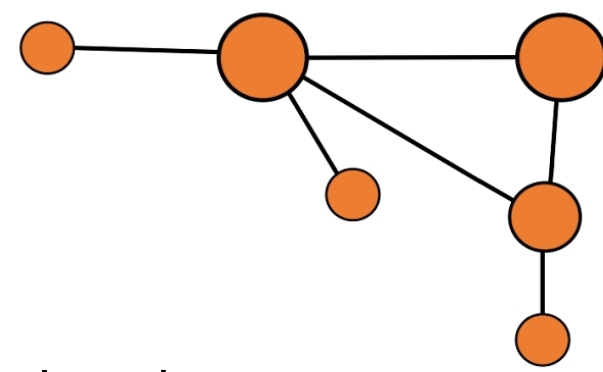


# What makes this paper special?

- ▶ As mentioned, the technology introduced holds great potential for future research
- ▶ The benchmarks are remarkable, particularly compared to the supervised models
- ▶ The researchers consider themselves „among the pioneers in the literature“ regarding the „exploration of anisotropic structure in graph data“







# References & Weblinks

- ▶ Yang et al. (2023). Directional diffusion models for graph representation learning
- ▶ Zhu et al. (2020). GSSNN: Graph Smoothing Splines Neural Networks
- ▶ Yanardag et al. (2015). Deep Graph Kernels
- ▶ Nguyen et al. (2019). Universal Graph Transformer Self-Attention Networks
- ▶ Ho et al. (2020). Denoising Diffusion Probabilistic Model
- ▶ Dhariwal et al. (2021). Diffusion Models Beat GANs on Image Synthesis
  
- ▶ Presentation Code: <https://github.com/JavaLangMarlon/ddm-proseminar-tu-dortmund>
- ▶ CC BY-SA 3.0: <https://creativecommons.org/licenses/by-sa/3.0>
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