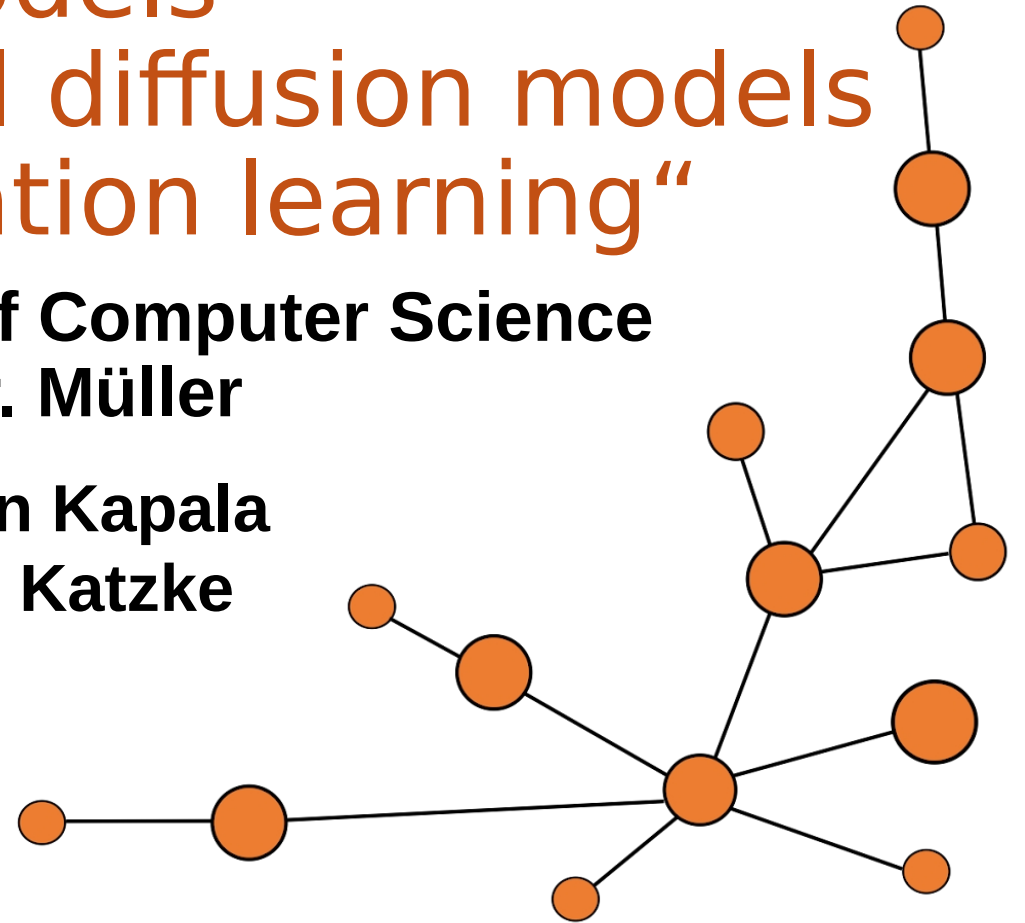


# Hot Topics Of Generative AI: LLMs and Diffusion Models

"Yang et al. - Directional diffusion models for graph representation learning"

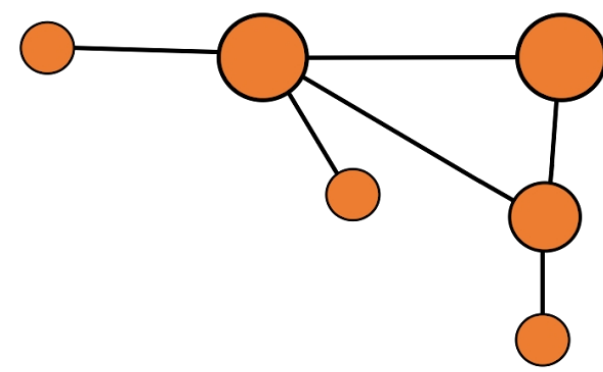
**TU Dortmund – Department of Computer Science  
Chair 9 – Prof. Dr. Müller**

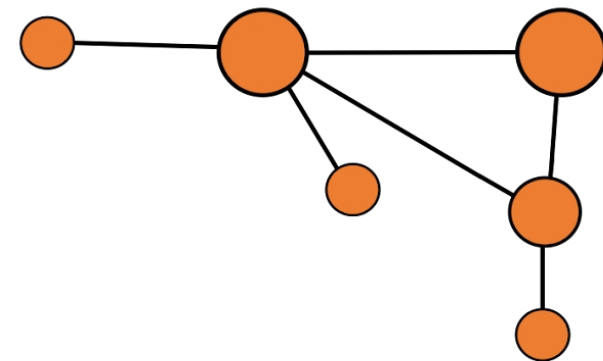
**presented by Marlon Kapala  
supervised by Tim Katzke**



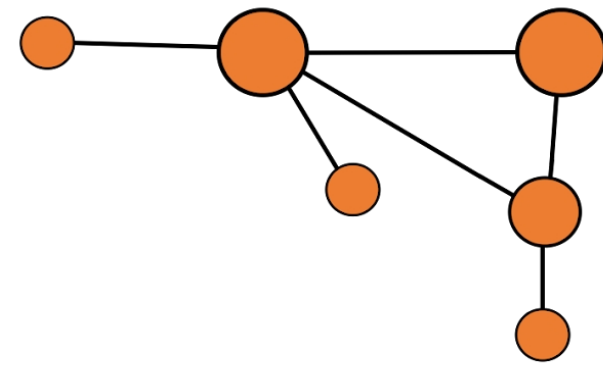
# Agenda

- 1 What is Graph Representation Learning?
- 2 The Emergence of Diffusion Models
- 3 Graphs vs. Images
- 4 The Architecture of Directed Diffusion Models
- 5 Benchmarks
- 6 Conclusion



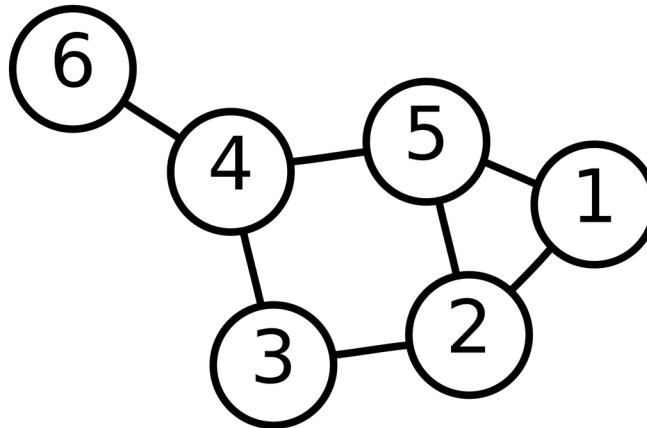


# 1 What is Graph Representation Learning?

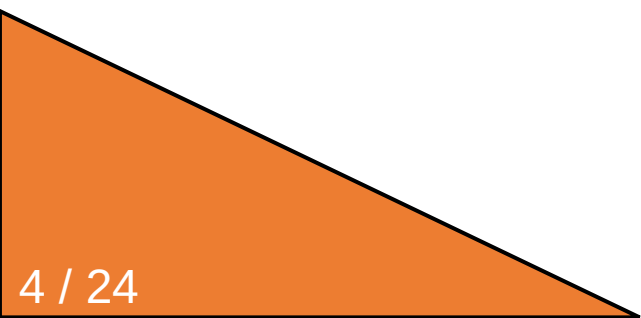


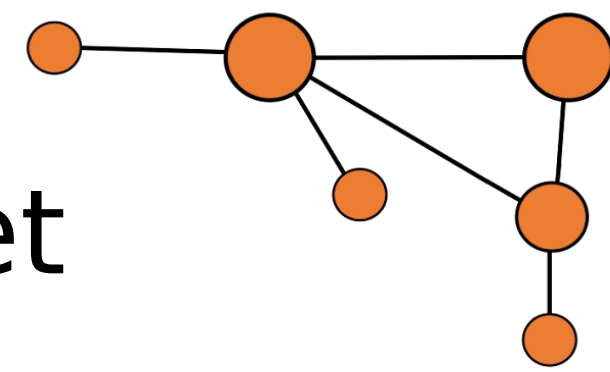
# What is a graph?

- ▶  $G = (V, E)$ , vertices  $V$  and edges  $E$
- ▶ Graphs can represent anything from molecules to road networks or social networks



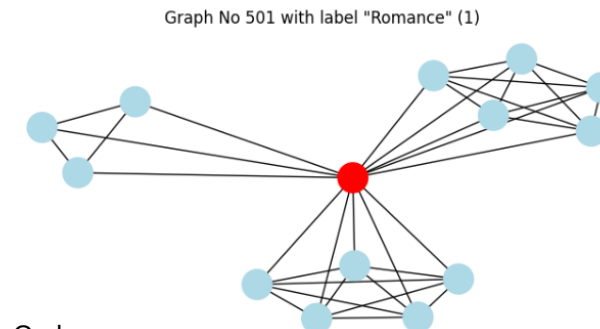
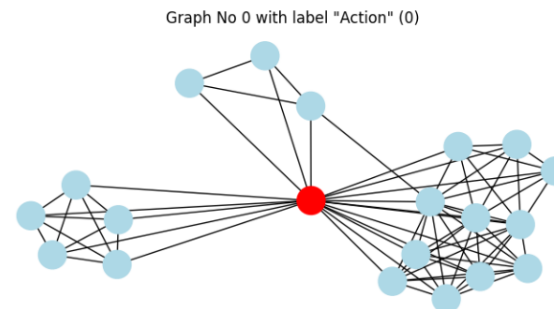
User:AzaToth, Public domain, via Wikimedia Commons



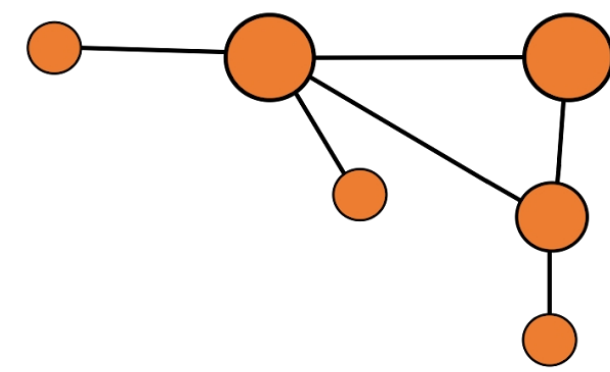


# IMDB-Binary – A Graph Dataset

- ▶ Graph Learning on Graph Datasets enables the use of AI on those data structures
- ▶ IMDB-B contains ego-networks of actors from Action or Romance movies (Yanardag et al., 2015)
- ▶ From only the knowledge of which actors have co-starred, models can determine the genre with an accuracy of up to 95% (Nguyen et al., 2019)

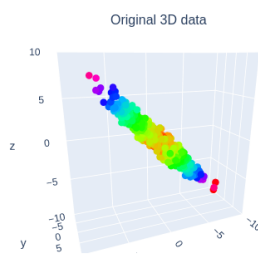


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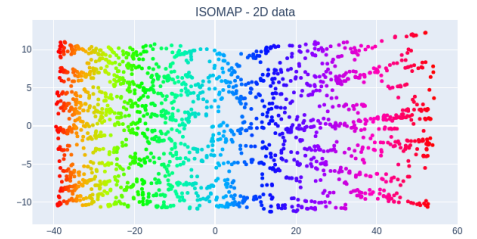
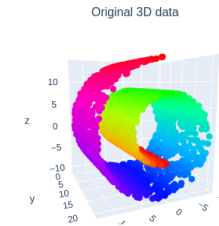
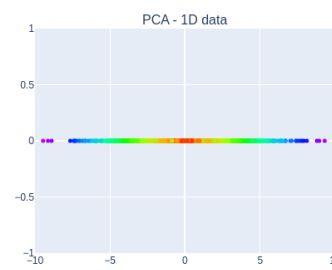


# Representation Learning

- ▶ RL is an important part of Machine Learning that converts data to a form that can be worked with more easily
- ▶ Here, there is also a difference between unsupervised and supervised learning
- ▶ Dimensionality Reduction is a prominent subfield

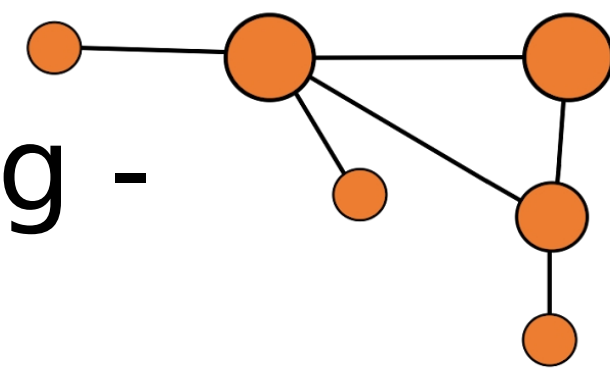


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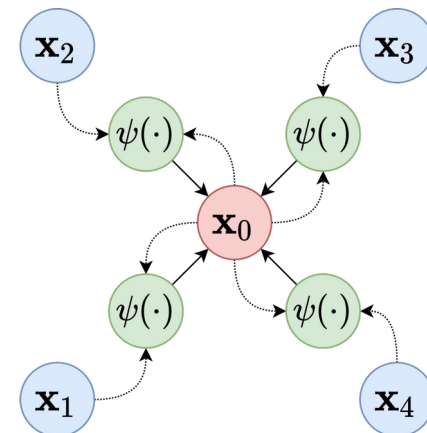


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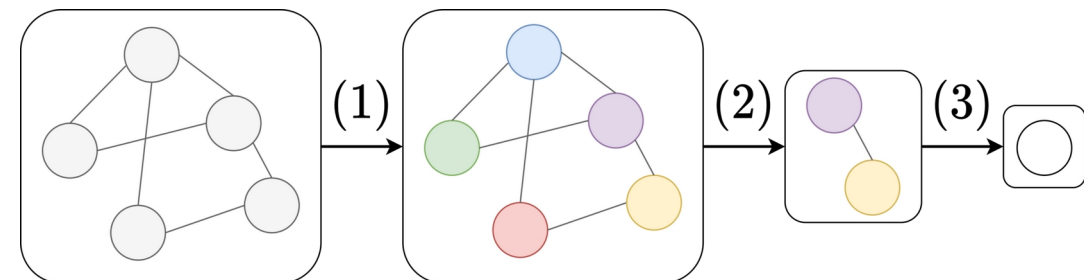
# Graph Representation Learning - GNNs



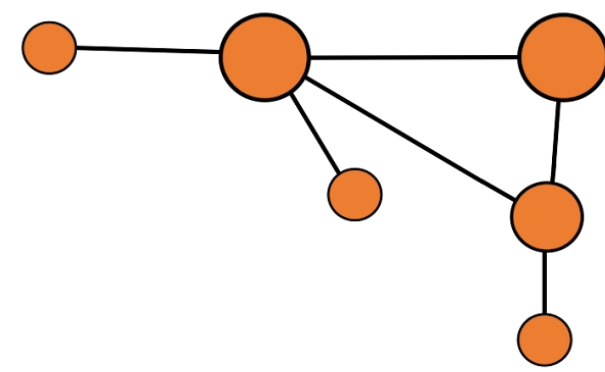
- ▶ For RL on Graphs, Graph Neural Networks are often used
- ▶ They work similar to Convolutional Neural Networks (CNNs)
- ▶ Instead of using neighboring pixels, the adjacency matrix, which contains the edges, is used



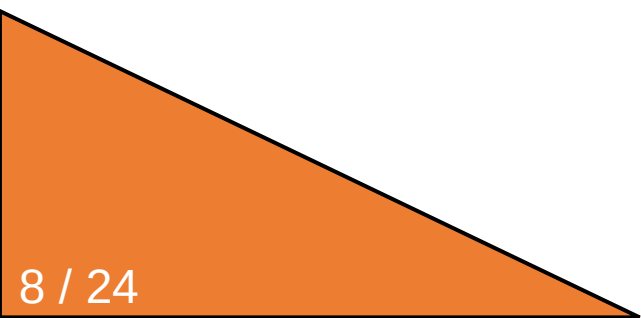
By NickDiCicco - Own work, CC BY-SA 4.0



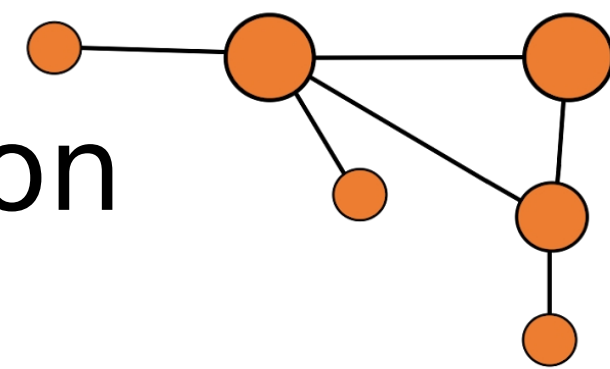
By NickDiCicco - Own work, CC BY-SA 4.0



## 2 The Successful Diffusion Model







# Denoising Probabilistic Diffusion Models

- Introduced to Machine Learning only recently (Ho et al., 2020), but has become the standard for image generation beating former SOTA technology (Dhariwal et al., 2021)

## Algorithm 1 Training

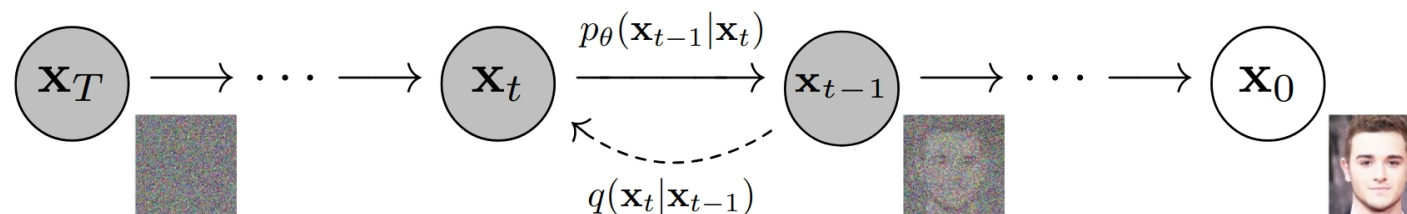
- 1: **repeat**
- 2:  $\mathbf{x}_0 \sim q(\mathbf{x}_0)$
- 3:  $t \sim \text{Uniform}(\{1, \dots, T\})$
- 4:  $\epsilon \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$
- 5: Take gradient descent step on  

$$\nabla_{\theta} \left\| \epsilon - \epsilon_{\theta}(\sqrt{\bar{\alpha}_t} \mathbf{x}_0 + \sqrt{1 - \bar{\alpha}_t} \epsilon, t) \right\|^2$$
- 6: **until** converged

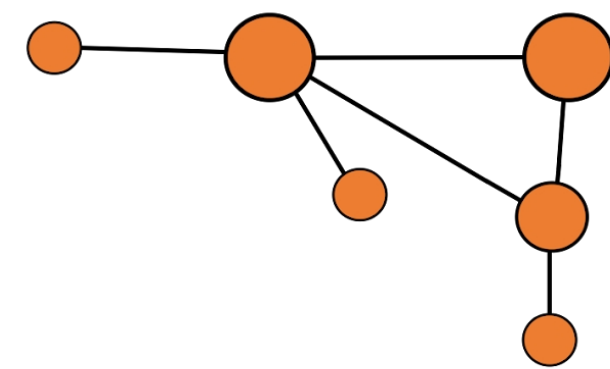
## Algorithm 2 Sampling

- 1:  $\mathbf{x}_T \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$
- 2: **for**  $t = T, \dots, 1$  **do**
- 3:  $\mathbf{z} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$  if  $t > 1$ , else  $\mathbf{z} = \mathbf{0}$
- 4:  $\mathbf{x}_{t-1} = \frac{1}{\sqrt{\alpha_t}} \left( \mathbf{x}_t - \frac{1 - \alpha_t}{\sqrt{1 - \bar{\alpha}_t}} \epsilon_{\theta}(\mathbf{x}_t, t) \right) + \sigma_t \mathbf{z}$
- 5: **end for**
- 6: **return**  $\mathbf{x}_0$

Ho et al., 2020



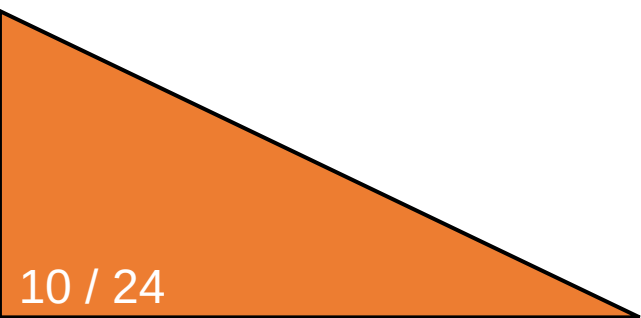
Ho et al., 2020

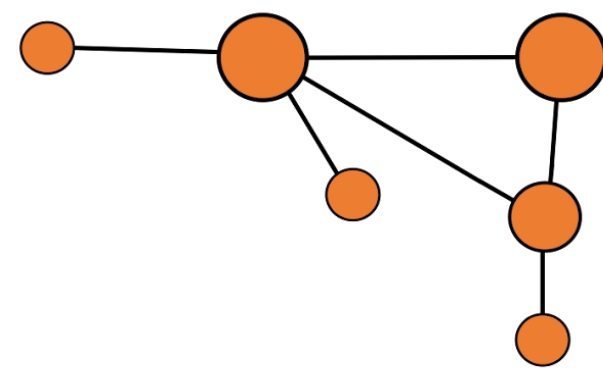


# The DM's forward step

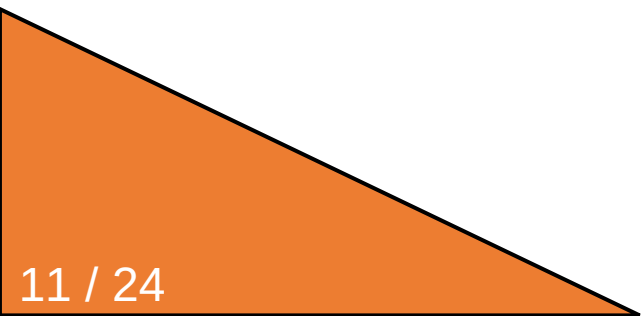
- ▶ To gradually add noise to the images, Diffusion Models add Gaussian noise in each step
- ▶ Thus, all data is asymptotically converted to a standard Gaussian distribution (Ho et al., 2020)

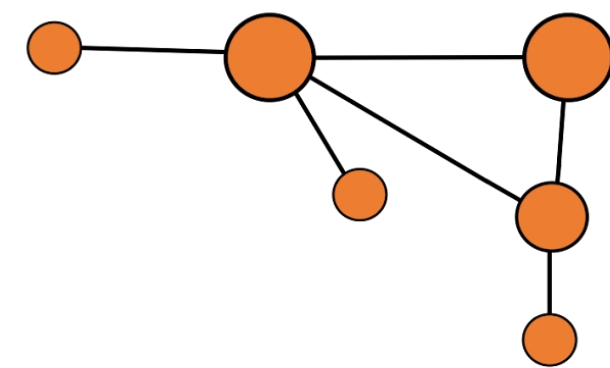
$$q(\mathbf{x}_{1:T}|\mathbf{x}_0) := \prod_{t=1}^T q(\mathbf{x}_t|\mathbf{x}_{t-1}) \quad q(\mathbf{x}_t|\mathbf{x}_{t-1}) := \mathcal{N}(\mathbf{x}_t; \sqrt{1 - \beta_t}\mathbf{x}_{t-1}, \beta_t\mathbf{I})$$





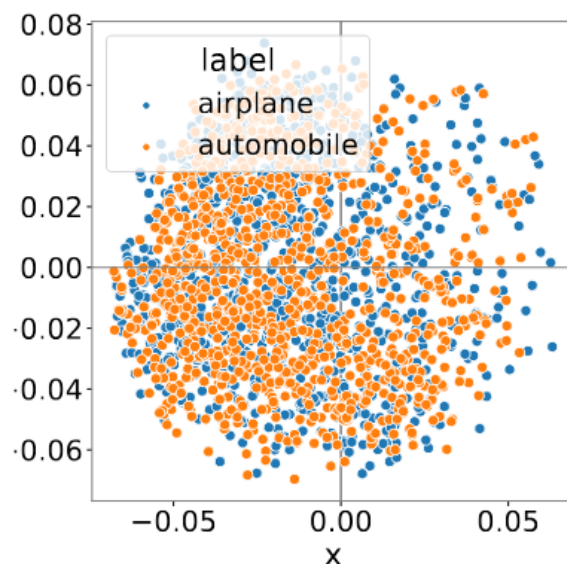
# 3 Graphs vs. Images



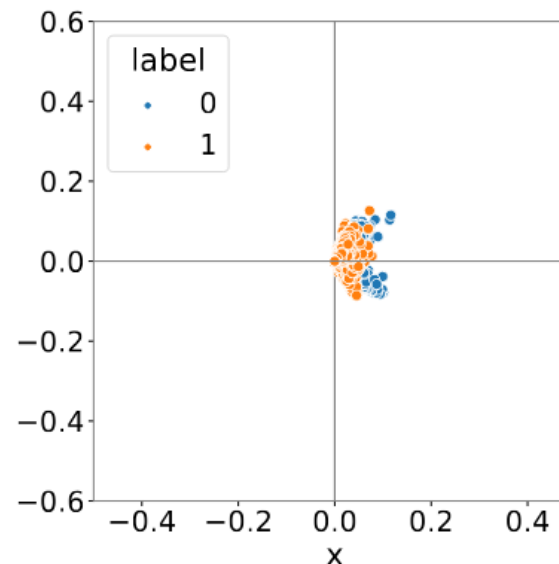


# The Anisotropy of Graphs

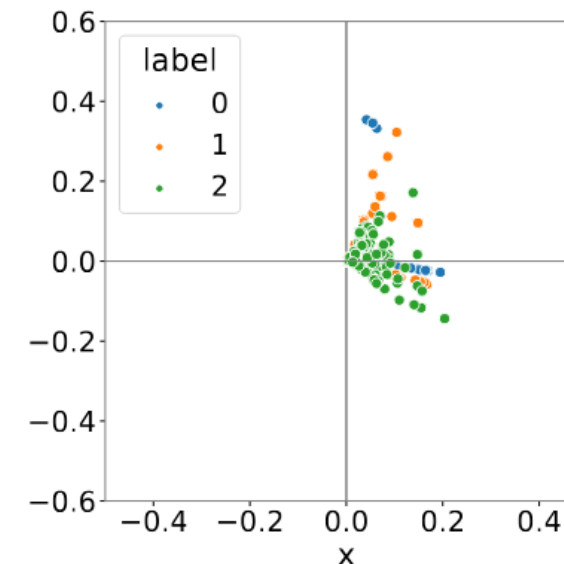
- While images are naturally isotropic and euclidean, Graphs are anisotropic



(a) CIFAR-10

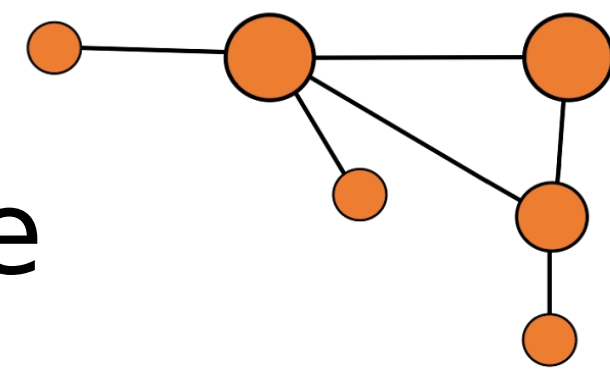


(b) Amazon-Photo



(c) IMDB-M

(Yang et al., 2023)



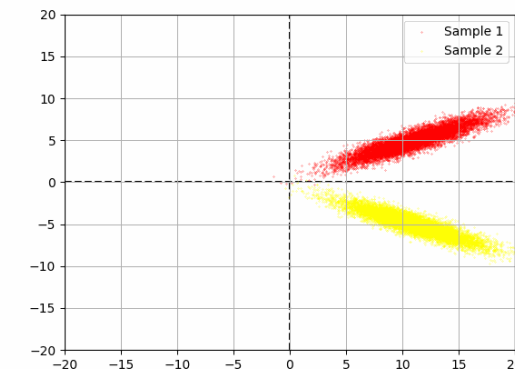
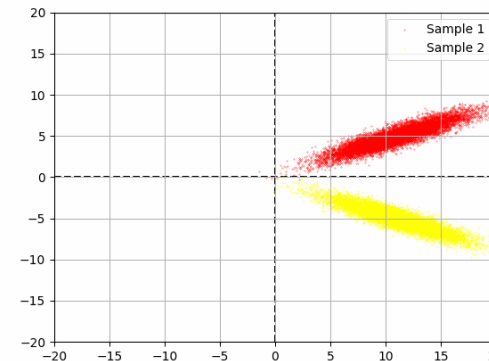
# White Noise vs. Directed Noise

- ▶ The information density of a directed Gaussian declines quickly if White Noise is applied
- ▶ Hence, Yang et al. introduce “Directional Noise”:

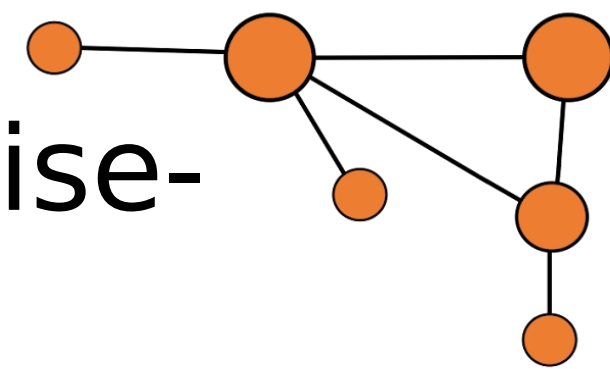
$$x_{t,i} = \sqrt{\bar{\alpha}_t} x_{0,i} + \sqrt{1 - \bar{\alpha}_t} \epsilon',$$

$$\epsilon' = \text{sgn}(x_{0,i}) \odot |\bar{\epsilon}|,$$

$$\bar{\epsilon} = \mu + \sigma \odot \epsilon \quad \text{where } \epsilon \sim \mathcal{N}(0, \mathbf{I})$$

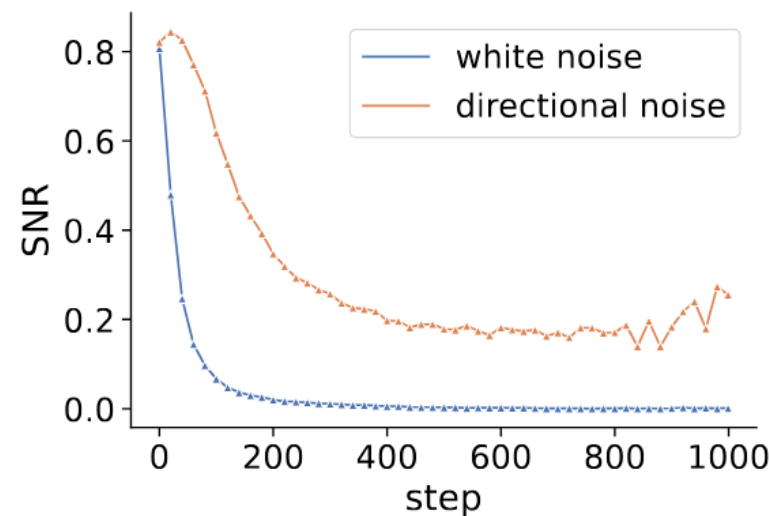


Presentation Code



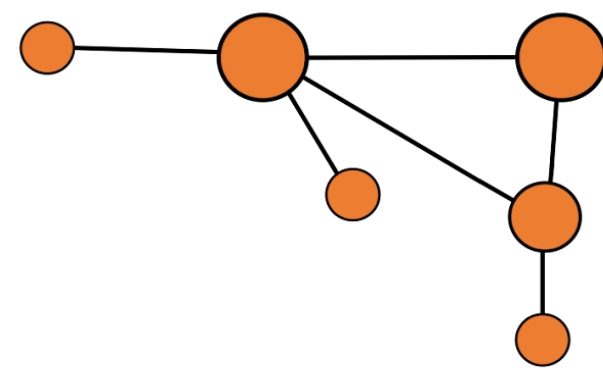
# The effect on the Signal-To-Noise-Ratio

- ▶ The Signal-To-Noise-Ratio is fundamental for the learning process of Diffusion Models
- ▶ The application of directional noise has a vital effect on the SNR

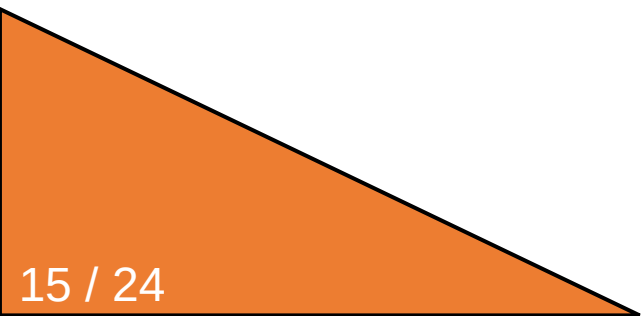


(a) Amazon-Photo

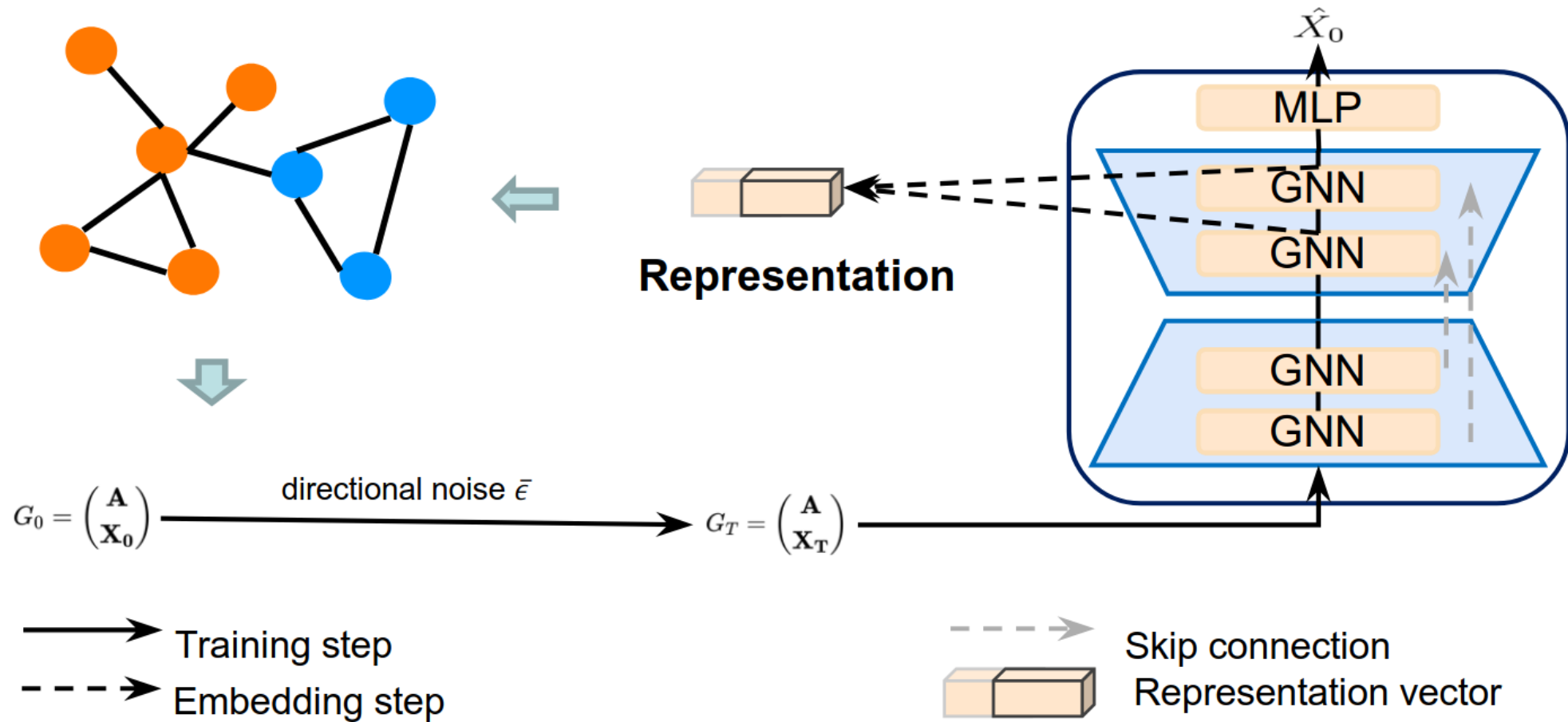
Yang et al., 2023



# 4 Directed Diffusion Models - Architecture



# Components of the Model

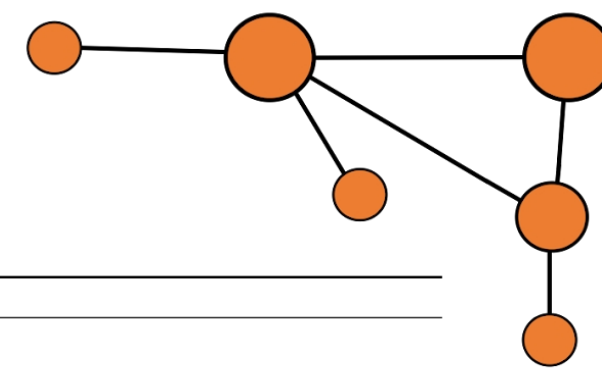


Yang et al., 2023



# The Algorithm

- ▶ The two algorithms work similar to Ho's algorithm
- ▶ Instead of generating an image, a representation is generated




---

**Algorithm 1** The training algorithm.

---

**Input:** A batch of graphs  $\mathcal{G} = \{G_1, \dots, G_B\}$

**Output:** The denoising network  $f_\theta$

---

```

1: Initialize: the denoising network  $f_\theta$ 
2: Compute  $\mu$ , the mean of node features across batch  $\mathcal{G}$ 
3: Compute  $\sigma$ , the standard deviation of node features across batch  $\mathcal{G}$ 
4: while not convergence do
5:   for  $G_i$  in  $\mathcal{G}$  do
6:     for  $t = 1, \dots, T$  do
7:       Sample directional noise  $\epsilon'$  using equation (2)
8:       Take gradient descent step on
           $\nabla_\theta \|\mathbf{X}_0 - f_\theta(\sqrt{\bar{\alpha}_t}\mathbf{X}_0 + \sqrt{1 - \bar{\alpha}_t}\epsilon', \mathbf{A}, t)\|$ 
9:     end for
10:   end for
11: end while

```

---

**Algorithm 2** Extracting representations.

---

**Input:**  $G = (\mathbf{A}, \mathbf{X})$ , forward step set  $\{T_0, T_1, \dots, T_K\}$ , pre-trained denoising network  $f_\theta$

**Output:**  $\mathbf{H}$ , the representation of  $G$

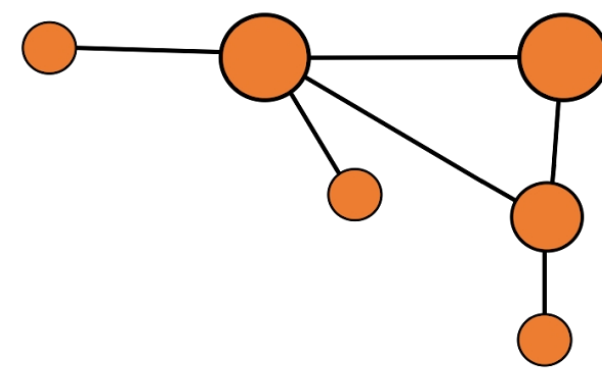
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```

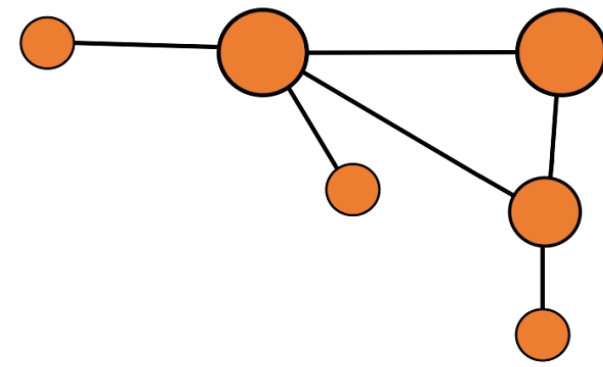
1: Compute  $\mu$  the mean of node features
2: Compute  $\sigma$  the standard deviation of node features
3: for  $k$  in  $\{T_0, T_1, \dots, T_K\}$  do
4:   Sample directional noise  $\epsilon'$  using equation (2)
5:    $\mathbf{X}_k \leftarrow \sqrt{\bar{\alpha}_k}\mathbf{X}_0 + \sqrt{1 - \bar{\alpha}_k}\epsilon'$ 
6:    $\mathbf{H}_k \leftarrow f_\theta(\mathbf{X}_k, \mathbf{A}, k)$ 
7: end for
8: Concatenate  $\mathbf{H} = [\mathbf{H}_{T_0}, \mathbf{H}_{T_1}, \dots, \mathbf{H}_{T_K}]$ 
9: return  $\mathbf{H}$ 

```

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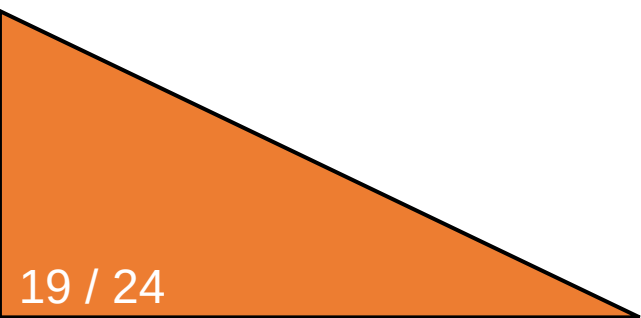


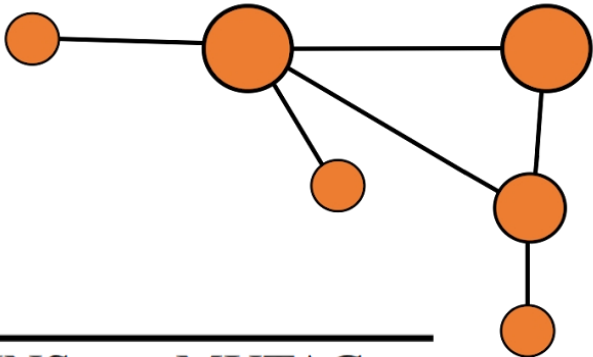
# 5 Resulting Benchmarks



# Graph Classification

- ▶ The paper compares multiple State-Of-The-Art models with DDMs
- ▶ The hyperparameters of the DDM were obtained by 10-fold cross validation
- ▶ SVMs are used on the learned representations
- ▶ While here only graph classification results are presented, the results from node classification are similarly promising

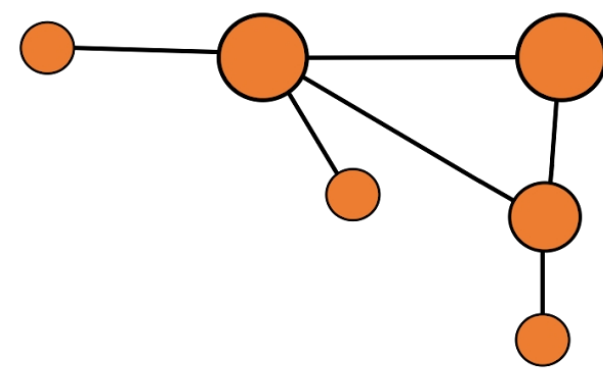




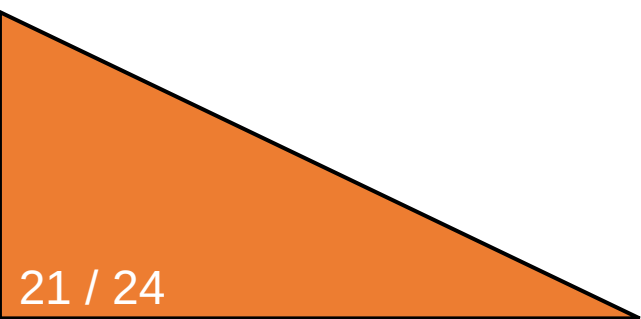
# Results

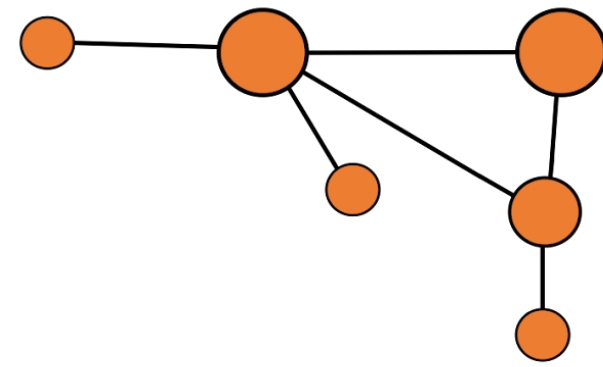
Dataset	IMDB-B	IMDB-M	COLLAB	REDDIT-B	PROTEINS	MUTAG
GIN	75.1±5.1	52.3±2.8	80.2±1.9	92.4±2.5	76.2±2.8	89.4±5.6
DiffPool	72.6±3.9	-	78.9±2.3	92.1±2.6	75.1±2.3	85.0±10.3
Infograph	73.03±0.87	49.69±0.53	70.65±1.13	82.50±1.42	74.44±0.31	89.01±1.13
GraphCL	71.14±0.44	48.58±0.67	71.36±1.15	89.53±0.84	74.39±0.45	86.80±1.34
JOAO	70.21±3.08	49.20±0.77	69.50±0.36	85.29±1.35	74.55±0.41	87.35±1.02
GCC	72	49.4	78.9	89.8	-	-
MVGRL	74.20±0.70	51.20±0.50	-	84.50±0.60	-	89.70±1.10
GraphMAE	75.52±0.66	51.63±0.52	80.32±0.46	88.01±0.19	75.30±0.39	88.19±1.26
DDM	<b>76.40±0.22</b>	<b>52.53±0.31</b>	<b>81.72±0.31</b>	89.15 ±1.3	<b>75.47 ±0.50</b>	<b>91.51 ±1.45</b>

Yang et al., 2023



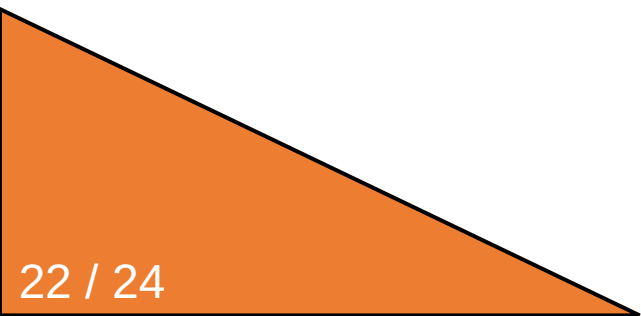
# 6 Conclusion

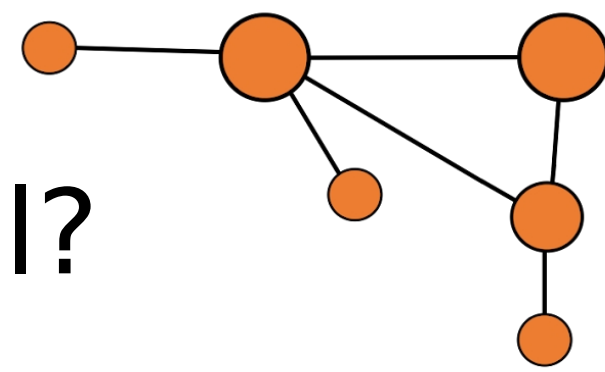




# Research Outlook

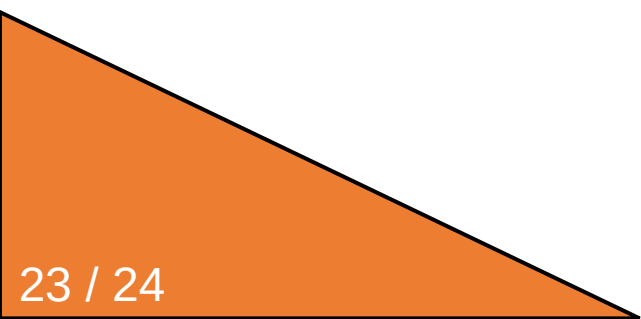
- ▶ Yang et al. only introduce the idea, they admit that their hyperparameters are not optimal yet
- ▶ One open question is how the optimal set of diffusion steps can be determined
- ▶ Variants of DDMMs could bring value to areas such as computer vision and natural language processing

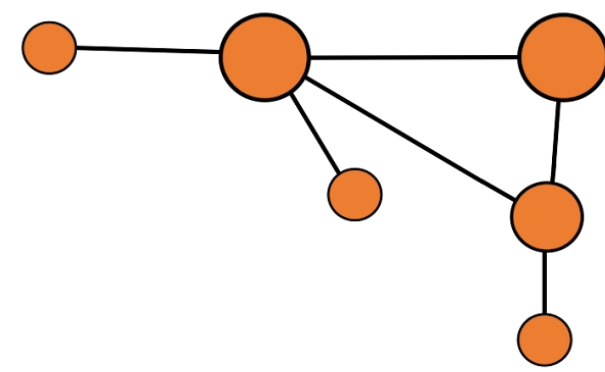




# What makes this paper special?

- ▶ The benchmarks are remarkable
- ▶ As mentioned, the technology introduced holds great potential for the future
- ▶ The researchers consider themselves „among the pioneers in the literature“ regarding the „exploration of anisotropic structure in graph data“





# References & Weblinks

- ▶ Yang et al. (2023). Directional diffusion models for graph representation learning
- ▶ Yanardag et al. (2015). Deep Graph Kernels
- ▶ Nguyen et al. (2019). Universal Graph Transformer Self-Attention Networks
- ▶ Ho et al. (2020). Denoising Diffusion Probabilistic Model
- ▶ Dhariwal et al. (2021). Diffusion Models Beat GANs on Image Synthesis
  
- ▶ Presentation Code: <https://github.com/JavaLangMarlon/ddm-proseminar-tu-dortmund>
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