6. Language Modeling for Retrieval

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- Know what a language model is
- Understand differences between different language models (unigram, bigram)
- Understand how to use language modeling for information retrieval
- Learn about different smoothing schemes for LM for IR
- Be able to compare LM for IR with vector space model and classic probabilistic models

- Recap of Lecture #5
- Language Models
 - Unigram LM
 - Bigram LM
- Query likelihood model for ranking
- Smoothing schemes
- Projects
 - Topics explained
 - Organization

- Probabilistic retrieval
 - Q: Why probability theory in IR, and why probabilistic ranking?
 - Q: What are the uncertainties of the IR process that we model probabilistically?
- Probability ranking principle
 - Q: What does Robertson's probabilistic ranking principle say?
 - Q: How do we formalize the probability ranking principle?
- Probabilistic ranking
 - Q: What is the ranking task formulation in the probabilistic setting?
 - Q: Starting from (log-)odds of relevance, how do we derive the general probabilistic ranking score?
- Binary independence model and extensions
 - Q: What assumptions does binary independence model introduce?
 - Q: What does the ranking function look like under these assumptions?
 - Q: Derive the BIM ranking function with and without relevance judgements
 - Q: How do Two Poisson, BM11, and BM25 extend BIM? What assumptions do they introduce?

The ranking score at the core of all probabilistic models:

$$log\left(\frac{P(D|Q,r)}{P(D|Q,\bar{r})}\right)$$

- Ranking function of Binary Independence Model
 - Without (left) and with (right) relevance judgements

$$rel(D,Q) = \sum_{t \in Q} log \left(\frac{P(D_t|Q,r)}{P(D_t|Q,\bar{r})} \right) \qquad rel(D,Q) = \sum_{t \in Q} log \left(\frac{P(D_t|Q,r)}{P(D_t|Q,\bar{r})} \right)$$

$$= \sum_{t \in Q} log \left(\frac{0.5}{\frac{N_t}{N}} \right) \qquad = \sum_{t \in Q} log \left(\frac{\frac{r_t + 0.5}{R+1}}{\frac{N_t - r_t + 0.5}{N-R+1}} \right)$$

$$= \sum_{t \in Q} log \left(0.5 \cdot \frac{N}{N_t} \right) \qquad = \sum_{t \in Q} log \left(\frac{(r_t + 0.5) \cdot (N - R + 1)}{(R+1) \cdot (N_t - r_t + 0.5)} \right)$$

- Example for BIM (without relevance judgements)
- Document collection consists of the following documents:
 - d₁: "Frodo and Sam stabbed orcs"
 - d₂: "Sam chased the orc with the sword"
 - d₃: "Sam took the sword"
- The query is: "Sam stabbed orc"

	d_1			d	d_3	
t	Sam	stabbed	orcs	Sam	orc	Sam
$P(D_t q,r)$	0.5	0.5	0.5	0.5	0.5	0.5
$P(D_t q,\bar{r})$	3/3	1/3	2/3	3/3	2/3	3/3
w_t	0.5	1.5	0.75	0.5	0.75	0.5
$\sum w_t$	2.75			1.	0.5	

Note: computations in this example are done without taking the logarithm

- Example for BIM (with available relevance judgements)
- Document collection contains N = 30 documents, including:
 - d₁: "Frodo and Sam stabbed orcs"
 - d₂: "Sam chased the orc with the sword"
 - d₃: "Sam took the sword"
- The query is: "Sam stabbed orc"
- User has indicated R = 6 relevant documents for this query
- Query terms: t₁ = "Sam", t₂ = "stab", t₃ = "orc"
- Document frequencies of query terms in relevant documents and overall collection are given as follows:
 - $r_{t1} = 3$, $N_{t1} = 15$
 - $r_{t2} = 4$, $N_{t2} = 16$
 - $r_{t3} = 2$, $N_{t3} = 14$

Example for BIM (with available relevance judgements)

	d_1			d_2		d_3
t	Sam	stabbed	orcs	Sam	orc	Sam
$P(D Q,r) = \frac{r_t + 0.5}{R+1}$	0.5	0.64	0.36	0.5	0.36	0.5
$P(D Q,r) = \frac{r_t + 0.5}{R+1}$ $P(D Q,\bar{r}) = \frac{N_t - r_t + 0.5}{N - R + 1}$	0.5	0.5	0.5	0.5	0.5	0.5
w_t	1	1.28	0.72	1	0.72	1
$\sum_t w_t$		3		1.	72	1

Note: computations in this example are done without taking the logarithm

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Language Modeling (for Information Retrieval)

- Language models are probabilistic models that capture the probabilities of sequences of words in a language
 - Unigram model: how likely is the word "frodo" to appear (in a language)?
 - P("frodo") = ?
 - **Bigram model**: given that current word is "frodo", what is the probability of next word being "baggins"?
 - P("baggins" | "frodo") = ?
 - **Trigram model**: given the current sequence "frodo baggins", what is the probability of next word being "shire"?
 - P("shire" | "frodo baggins") = ?
- Q: How do we estimate probabilities of words and sequences in a language?
 - I.e., What do we use as a representation of the language?

Language Modeling (for Information Retrieval)

- We use the instantiations of the language to estimate the probabilities of words and sequences
 - I.e., large corpora the larger the corpora, it is the better approximation of the true word distributions in language
- In other applications we build language models largest corpora we can compile
- In information retrieval, we build language models
 - 1. From individual documents
 - 2. From the whole document collections

Language Modeling (for Information Retrieval)

- Language models for IR are also probabilistic models
- Language models for IR model the query generation process
- Given a documet d and a query q, what is the probability of <u>query being sampled</u> from the <u>language model of the document</u>
- In other words, we want to estimate $P(Q = q \mid D = d)$
 - Q: Compare this with the probability we estimated in classic probabilistic retrieval
 - P(R = 1 | Q = q, D = d)
- The probability of a document generating a query is directly the function according to which we rank the documents
 - I.e., We rank the documents in decreasing order of $P(Q = q \mid D = d)$
- **Key question:** how do we estimate P(Q = q | D = d)?

Language Bowl Metaphor

- Assume we have a document in with following occurrences of terms:
 - "frodo" (5x), "baggins" (3x), "sam" (3x), "shire" (2x), "gandalf" (2x), "orc" (1x)
- Let's represent each term with balls of one color:
 - "frodo" -> 5 blue balls, "baggins" -> 3 red balls, "sam" -> 3 yellow balls
 - "shire" -> 2 green balls, "gandalf" -> 2 orange balls, "orc" -> 1 purple ball
- We put all balls into one bowl and randomly take them out one by one
- Q: What is the probability of drawing a yellow ball?
 - $P(\bigcirc) = P(\text{"sam"}) = 3 / (5 + 3 + 3 + 2 + 2 + 1) = 3 / 16$
- Q: What is the probability of drawing first orange then blue ball?
 - Replacement: P(●, ●) = P(",gandalf", ",frodo") = P(",gandalf") * P(",frodo") = 2/16 * 5/16
 - No replacement: P(●, ●) = P(",gandalf", ",frodo") = P(",gandalf") * P(",frodo" | ",gandalf")
 - **=** = 2/16 * 5/15

Language Model – Generative Story

- Language model can be observed as a statistical model for generating data
- Example (toy language, consisting of four words):
 - P("frodo") = 0.3, P("sam") = 0.25, P("gandalf") = 0.35, P("shire") = 0.1
 - P("sam" | "frodo") = 0.4, P("gandalf" | "frodo") = 0.4, P("shire" | "frodo") = 0.2
- Generative process:
 - 1. Randomly draw the first word (e.g., from a uniform distribution)



2. Draw the second word from conditional distribution of the first word (e.g., "frodo")



• Q: What is the probability of the sequence "frodo shire"?

We want to estimate the probability of the sequence:

$$P(\bigcirc \bigcirc \bigcirc \bigcirc) = P(\bigcirc) * P(\bigcirc \bigcirc) * P(\bigcirc \bigcirc) * P(\bigcirc \bigcirc) * P(\bigcirc \bigcirc)$$

- Unigram language model
 - Word independence = probability of the word does not depend on previous words
 - We ignore conditioning

$$P(\bigcirc \bigcirc \bigcirc \bigcirc) = P(\bigcirc) * P(\bigcirc) * P(\bigcirc) * P(\bigcirc)$$

- Bigram language model
 - The probability of word appearing depends only on the immediately preceding word
 - Conditioning only one one word before

$$P(\bigcirc \bigcirc \bigcirc \bigcirc) = P(\bigcirc) * P(\bigcirc|\bigcirc) * P(\bigcirc|\bigcirc) * P(\bigcirc|\bigcirc)$$

■ Q: N-gram models for $N \ge 3$ are rarely used in practice. Why?

Sparseness issue of language models

- Language models have a major issue
 - The longer the phrase, the harder it is to estimate its true probability in language
 - E.g., P("bilbo" | "frodo ran around house found ring") = ?
- Long phrases have very few appearances even in very large corpora
 - Impossible to compute reliable estimates of their conditional probabilities
 - This is why language models for N ≥ 3 are almost never used
- In practice, we use unigram and bigram language models
 - In IR setting, we build language models from invidual documents
 - Even bigram probability hard to estimate
 - In IR, we most often employ the unigram language model

Estimating probabilities

- For the unigram language model we need to estimate
 - P(term) for every term in the text
- For the bigram language model we additionally need to estimate
 - P(term | previous term) for every pair of terms that appear one after another
- Q: How do we estimate these?
 - Unigram language model
 - $P(t_i) = n_i / n_T$
 - n_i is the number of occurences of term t_i in the collection
 - n_T is the total number of word occurences (i.e., tokens) in the collection
 - Bigram language model
 - $P(t_i | t_{i-1}) = n(t_{i-1}, t_i) / n(t_{i-1})$
 - $n(t_{i-1}, t_i)$ is the number of occurrences of bigram $t_{i-1}t_i$ in the collection
 - $n(t_{i-1})$ is the number of occurrences of term t_{i-1} in the collection

Estimating probabilities – example

- We are given a toy collection consisting of three documents
 - d₁: "Frodo and Sam stabbed orcs"
 - d₂: "Sam chased the orc with the sword"
 - d₃: "Sam took the sword"
- Estimating word probabilities for the unigram model:

				chased		
$P(t_i)$	1/16	3/16	2/16	1/16	2/16	

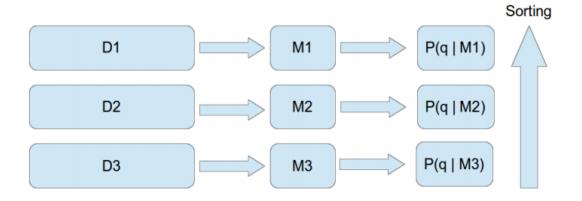
Estimating the conditional probabilities for the bigram model:

t_{i-1}, t_i	Frodo, chased	the, sword	the, orc	
$P(t_i t_{i-1})$	0	2/3	1/3	

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Query likelihood model for ranking

- Given a document collection D and a query q we need to estimate the probability
 P(q | d) for every document d in D
- In the query likelihood model, we estimate the probability P(q | d) as the probability that the language model built from d generates the query q
- Algorithm
 - Compute the language model M_i for every document d_i in D
 - 2. Compute the probability P(q | Mi) for every language model M_i



 Intuition: Language models of relevant documents should assign higher probability for the query

Query likelihood model for ranking – example

- We are given a toy collection consisting of three documents
 - d₁: "Sam chased the orc with the sword"
 - d₂: "Frodo and Sam stabbed orcs"
 - d₃: "Sam took the sword"
- We are given the query "Sam and orc and sword"
- Let's rank the documents according to unigram LM for IR (ignore stopwords)
- Step 1: Compute language models of individual documents
 - M_1 : P("sam") = 0.25, P("chase") = 0.25, P("orc") = 0.25, P("sword") = 0.25
 - M₂: P("frodo") = 0.25, P("sam") = 0.25, P("stab") = 0.25, P("orc") = 0.25
 - M_3 : P("sam") = 0.33, P("took") = 0.33, P("sword") = 0.33

Query likelihood model for ranking – example

- We are given a toy collection consisting of three documents
 - d₁: "Sam chased the orc with the sword"
 - d₂: "Frodo and Sam stabbed orcs"
 - d₃: "Sam took the sword"
- We are given the query "Sam and orc and sword"
- Let's rank the documents according to unigram LM for IR (ignore stopwords)
- **Step 2:** Let's compute the probabilities P(q | M_i)
 - $P(q \mid M_1) = P(\text{"sam"} \mid M_1) * P(\text{"orc"} \mid M_1) * P(\text{"sword"} \mid M_1) = 0.25 * 0.25 * 0.25$
 - $P(q \mid M_2) = P(\text{"sam"} \mid M_2) * P(\text{"orc"} \mid M_2) * P(\text{"sword"} \mid M_2) = 0.25 * 0.25 * 0$
 - $P(q \mid M_3) = P(\text{"sam"} \mid M_3) * P(\text{"orc"} \mid M_3) * P(\text{"sword"} \mid M_3) = 0.33 *$ **0*** 0.33
- Q: Is there any problem with query likelihoods given LMs of d_2 and d_3 ?

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24

Smoothing language models

- Zero frequency problem: Models we've considered so far give probability of 0 to queries containing any term that does not occur in the document
- We can prevent this by using smoothing techniques
- Smoothing techniques
 - Change the probability distribution of terms in the language model
 - Assign some small probability to unseen words
- Three prominent smoothing schemes
 - Laplace smoothing
 - Jelinek-Mercer smoothing
 - Dirichlet smoothing

Laplace smoothing

Laplace smoothing

- 1. Adds a fixed small count (often it's 1) to all word counts
- 2. Renormalizes to get a probability distribution

$$P(t_i|M_d) = \frac{n_{i,d} + \alpha}{n_d + |V| \cdot \alpha}$$

The probability of any unseen word equals

$$P(t_{uns}|M_d) = \frac{\alpha}{n_d + |V| \cdot \alpha}$$

• Q: What might be a potential shortcoming of the Laplace smoothing?

Jelinek-Mercer smoothing

- Laplace smoothing assumes that all unseen words are equally likely
- Jelinek-Mercer smoothing (also known as interpolated smoothing)
 - 1. Additionally builds a language model M_D from the whole document collection D
 - 2. Interpolates between probabilities of the query according to the
 - Local LM language model M_d built from the particular document d
 - Global LM language model M_D built from the whole collection

$$P(t_i|M_d) = \lambda \cdot P(t_i|M_d) + (1-\lambda) \cdot P(t_i|M_D)$$

- The probability of a word unseen in the document d still gets some probability from the global language model
 - Probability of an unseen word depends on its frequency in whole collection
- **Q:** What if $P(t_i | M_D) = 0$?

Dirichlet smoothing

- Dirichlet smoothing can be seen as a generalization of the Laplace smoothing
 - Each word unseen in the document gets an artificial extra count
 - But the extra count is not fixed, depends on the global probability of the term
 - In this respect, Dirichlet smoothing is similar to Jelinek-Mercer smoothing

$$P(t_i|M_d) = \frac{n_{i,d} + \mu \cdot P(t_i|M_D)}{n_d + \mu}$$

- Less frequent words in the document get more probability from the global component
 - The value of the constant μ determines the scale of the global probability's contribution

Language models for IR vs. VSM

- Let's compare the query likelihood model with the VSM model
- 1. Do we have a term frequency component in LM?
 - Q: do query terms that are more frequent in the document contribute more to the relevance score?
 - **A:** Yes! $P(t_i) = n_i / n_T$
- 2. Do we have a document frequency component in LM?
 - Q: does the global document frequency of the query term affect the relevance scores?
 - A: No! If we use Jelinek-Mercer or Dirichlet smoothing, we take into consideration collection frequency, but not document frequency
 - However, mixing term frequency (within document) and collection frequency has an effect similar to using IDF

Language models for IR vs. VSM

- Let's compare the query likelihood model with the VSM model
- 3. Does LM for IR account for different lengths of documents?
 - Q: Does it somehow normalize the frequencies of query terms in documents with the document length?
 - A: Yes! $P(t_i) = n_i / n_T$
- LM for IR vs. VSM: commonalities
 - 1. Term frequency directly in the model
 - 2. Contributions of terms are normalized to account for document length
- LM for IR vs. VSM: differences
 - 1. LM for IR is based in probability theory, VSM in vector algebra
 - 2. Collection frequency (LM) vs. Document frequency (VSM)

- Know what a language model is
- Understand differences between different language models (unigram, bigram)
- Understand how to use language modeling for information retrieval
- Are familiar with different smoothing schemes for LM for IR
- Are able to compare LM for IR with vector space model and classic probabilistic models