# Artificial Intelligence

Exercise Sheet 4

November 16, 2021

$$(B \vee \overline{D}) \wedge (\overline{A} \vee \overline{C}) \wedge (C \vee B \vee A) \wedge \overline{A} \wedge (\overline{B} \vee D) \wedge (A \vee B \vee D) \wedge (\overline{B} \vee \overline{D})$$

$$\big(B\vee\overline{D}\big)\wedge\big(\overline{A}\vee\overline{C}\big)\wedge\big(C\vee B\vee A\big)\wedge\overline{A}\wedge\big(\overline{B}\vee D\big)\wedge\big(A\vee B\vee D\big)\wedge\big(\overline{B}\vee\overline{D}\big)$$

Unit-Clause  $\overline{A}$ 

$$\big(B\vee\overline{D}\big)\wedge\big(\overline{A}\vee\overline{C}\big)\wedge\big(C\vee B\vee A)\wedge\overline{A}\wedge\big(\overline{B}\vee D\big)\wedge\big(A\vee B\vee D)\wedge\big(\overline{B}\vee\overline{D}\big)$$

Unit-Clause  $\overline{A}$   $(B \vee \overline{D}) \wedge (C \vee B) \wedge (\overline{B} \vee D) \wedge (B \vee D) \wedge (\overline{B} \vee \overline{D})$ 

$$\big(B\vee\overline{D}\big)\wedge\big(\overline{A}\vee\overline{C}\big)\wedge\big(C\vee B\vee A\big)\wedge\overline{A}\wedge\big(\overline{B}\vee D\big)\wedge\big(A\vee B\vee D\big)\wedge\big(\overline{B}\vee\overline{D}\big)$$

Unit-Clause  $\overline{A}$   $(B \vee \overline{D}) \wedge (C \vee B) \wedge (\overline{B} \vee D) \wedge (B \vee D) \wedge (\overline{B} \vee \overline{D})$ Pure-Symbol C

$$\big(B\vee\overline{D}\big)\wedge\big(\overline{A}\vee\overline{C}\big)\wedge\big(C\vee B\vee A\big)\wedge\overline{A}\wedge\big(\overline{B}\vee D\big)\wedge\big(A\vee B\vee D\big)\wedge\big(\overline{B}\vee\overline{D}\big)$$

Unit-Clause  $\overline{A}$   $(B \vee \overline{D}) \wedge (C \vee B) \wedge (\overline{B} \vee D) \wedge (B \vee D) \wedge (\overline{B} \vee \overline{D})$ Pure-Symbol C  $(B \vee \overline{D}) \wedge (\overline{B} \vee D) \wedge (B \vee D) \wedge (\overline{B} \vee \overline{D})$ 

 $D \wedge \overline{D}$ 

$$(B \vee \overline{D}) \wedge (\overline{A} \vee \overline{C}) \wedge (C \vee B \vee A) \wedge \overline{A} \wedge (\overline{B} \vee D) \wedge (A \vee B \vee D) \wedge (\overline{B} \vee \overline{D})$$
Unit-Clause  $\overline{A} (B \vee \overline{D}) \wedge (C \vee B) \wedge (\overline{B} \vee D) \wedge (B \vee D) \wedge (\overline{B} \vee \overline{D})$ 
Pure-Symbol  $C (B \vee \overline{D}) \wedge (\overline{B} \vee D) \wedge (B \vee D) \wedge (\overline{B} \vee \overline{D})$ 
Guess:  $B1 = B$ ,  $B2 = \overline{B}$ 
 $B1$ :

Unit-Clause D

$$(B \vee \overline{D}) \wedge (\overline{A} \vee \overline{C}) \wedge (C \vee B \vee A) \wedge \overline{A} \wedge (\overline{B} \vee D) \wedge (A \vee B \vee D) \wedge (\overline{B} \vee \overline{D})$$
Unit-Clause  $\overline{A}$   $(B \vee \overline{D}) \wedge (C \vee B) \wedge (\overline{B} \vee D) \wedge (B \vee D) \wedge (\overline{B} \vee \overline{D})$ 
Pure-Symbol  $C$   $(B \vee \overline{D}) \wedge (\overline{B} \vee D) \wedge (B \vee D) \wedge (\overline{B} \vee \overline{D})$ 
Guess:  $B1 = B$ ,  $B2 = \overline{B}$ 
 $B1$ :  $D \wedge \overline{D}$ 

$$(B \vee \overline{D}) \wedge (\overline{A} \vee \overline{C}) \wedge (C \vee B \vee A) \wedge \overline{A} \wedge (\overline{B} \vee D) \wedge (A \vee B \vee D) \wedge (\overline{B} \vee \overline{D})$$

Unit-Clause 
$$\overline{A}$$
  $(B \lor \overline{D}) \land (C \lor B) \land (\overline{B} \lor D) \land (B \lor D) \land (\overline{B} \lor \overline{D})$   
Pure-Symbol  $C$   $(B \lor \overline{D}) \land (\overline{B} \lor D) \land (B \lor D) \land (\overline{B} \lor \overline{D})$   
Guess:  $B1 = B$ ,  $B2 = \overline{B}$ 

B1:

$$D \wedge \overline{D}$$

Unit-Clause D

Unsolvable, backtracking

$$(B \vee \overline{D}) \wedge (\overline{A} \vee \overline{C}) \wedge (C \vee B \vee A) \wedge \overline{A} \wedge (\overline{B} \vee D) \wedge (A \vee B \vee D) \wedge (\overline{B} \vee \overline{D})$$

Unit-Clause 
$$\overline{A}$$
  $(B \lor \overline{D}) \land (C \lor B) \land (\overline{B} \lor D) \land (B \lor D) \land (\overline{B} \lor \overline{D})$   
Pure-Symbol  $C$   $(B \lor \overline{D}) \land (\overline{B} \lor D) \land (B \lor D) \land (\overline{B} \lor \overline{D})$ 

Guess: B1 = B,  $B2 = \overline{B}$ 

Unsolvable, backtracking

B2:  $\overline{D} \wedge D$ 

$$(B \vee \overline{D}) \wedge (\overline{A} \vee \overline{C}) \wedge (C \vee B \vee A) \wedge \overline{A} \wedge (\overline{B} \vee D) \wedge (A \vee B \vee D) \wedge (\overline{B} \vee \overline{D})$$

Unit-Clause 
$$\overline{A}$$
  $(B \lor \overline{D}) \land (C \lor B) \land (\overline{B} \lor D) \land (B \lor D) \land (\overline{B} \lor \overline{D})$   
Pure-Symbol  $C$   $(B \lor \overline{D}) \land (\overline{B} \lor D) \land (B \lor D) \land (\overline{B} \lor \overline{D})$   
Guess:  $B1 = B$ ,  $B2 = \overline{B}$ 

Guess: B1 = B. B2 =  $\overline{B}$ 

B1: Unit-Clause D

Unsolvable, backtracking

B2:  $\overline{D} \wedge D$ Unit-Clause  $\overline{D}$ 

$$(B \vee \overline{D}) \wedge (\overline{A} \vee \overline{C}) \wedge (C \vee B \vee A) \wedge \overline{A} \wedge (\overline{B} \vee D) \wedge (A \vee B \vee D) \wedge (\overline{B} \vee \overline{D})$$

Unit-Clause 
$$\overline{A}$$
  $(B \vee \overline{D}) \wedge (C \vee B) \wedge (\overline{B} \vee D) \wedge (B \vee D) \wedge (\overline{B} \vee \overline{D})$   
Pure-Symbol  $C$   $(B \vee \overline{D}) \wedge (\overline{B} \vee D) \wedge (B \vee D) \wedge (\overline{B} \vee \overline{D})$ 

Guess: B1 = B, B2 =  $\overline{B}$ 

B1:

 $\wedge \overline{D}$ 

Unit-Clause D

Unsolvable, backtracking

B2

 $\overline{D} \wedge D$ 

Unit-Clause  $\overline{D}$ 

Unsolvable, backtracking

$$(B \vee \overline{D}) \wedge (\overline{A} \vee \overline{C}) \wedge (C \vee B \vee A) \wedge \overline{A} \wedge (\overline{B} \vee D) \wedge (A \vee B \vee D) \wedge (\overline{B} \vee \overline{D})$$

Unit-Clause 
$$\overline{A}$$
  $(B \vee \overline{D}) \wedge (C \vee B) \wedge (\overline{B} \vee D) \wedge (B \vee D) \wedge (\overline{B} \vee \overline{D})$   
Pure-Symbol  $C$   $(B \vee \overline{D}) \wedge (\overline{B} \vee D) \wedge (B \vee D) \wedge (\overline{B} \vee \overline{D})$ 

Guess: B1 = B, B2 =  $\overline{B}$ 

B1:

 $\wedge \overline{D}$ 

Unit-Clause D

Unsolvable, backtracking

B2

 $\overline{D} \wedge D$ 

Unit-Clause  $\overline{D}$ 

Unsolvable, backtracking

#### Unsolvable

- 1. {Vater(a, Tim), Vater(Jakob, b)}
- 2.  $\{Kennt(Vater(y), y), Kennt(x, x)\}$
- 3.  $\{f(g(a,x),g(y,b)); f(z,g(v,w)); f(g(x,a),g(v,b))\}$

- 1. {Vater(a, Tim), Vater(Jakob, b)}
- 2.  $\{Kennt(Vater(y), y), Kennt(x, x)\}$
- 3.  $\{f(g(a,x),g(y,b)); f(z,g(v,w)); f(g(x,a),g(v,b))\}$

► {a/Jakob, b/Tim}

- 1. {Vater(a, Tim), Vater(Jakob, b)}
- 2.  $\{Kennt(Vater(y), y), Kennt(x, x)\}$
- 3.  $\{f(g(a,x),g(y,b)); f(z,g(v,w)); f(g(x,a),g(v,b))\}$

- $ightharpoonup \{a/Jakob, b/Tim\}$
- **▶** {/}

- 1. {Vater(a, Tim), Vater(Jakob, b)}
- 2.  $\{Kennt(Vater(y), y), Kennt(x, x)\}$
- 3.  $\{f(g(a,x),g(y,b)); f(z,g(v,w)); f(g(x,a),g(v,b))\}$

- ► {a/Jakob, b/Tim}
- **▶** {/}

## Task 3

#### Formulas and CNF:

- 1.  $\forall x \ Child(x) \rightarrow hasDragon(x)$  $\equiv \neg Child(x) \lor hasDragon(x)$
- 2.  $\forall x \ (Child(x) \land hasDragon(x) \land outside(x)) \rightarrow hasfun(x)$  $\equiv \neg Child(x) \lor \neg hasDragon(x) \lor \neg outside(x) \lor hasFun(x)$
- 3.  $\forall x \ (Child(x) \land \neg isIII(x) \rightarrow outisde(x))$  $\equiv \neg Child(x) \lor isIII(x) \lor outside(x)$
- 4. ¬isIII(Alfons)
- 5. Child(Alfons)
- 6. **Negated Aim:** ¬hasFun(Alfons)

## Task 3

#### Resolution:

- 7. hasDragon(Alfons) (from (1) and (5))
- 8.  $\neg hasDragon(Alfons) \lor \neg outside(Alfons) \lor hasFun(Alfons)$  (from (2) and (5))
- 9.  $isIII(x) \lor outside(x)$  (from (3) and (5))
- 10. outside(Alfons) (from (9) and (4))
- 11.  $\neg hasDragon(Alfons) \lor hasFun(Alfons)$  from (8) and (10)
- 12. hasFun(Alfons) from (7) and (11)
- 13. {} from (12) and (6)
- (Unifier is always  $o = \{x/Alfons\}$ )