Exercises 3; Probability Distributions

- 1) Suppose that X takes on one of the values 1, 2, 3, 4, or 5. If P(X < 3) = 0.4 and $P(X \ge 4) = 0.5$, find:
 - a. P(X = 3) = 0.5 0.4 = 0.1
 - b. P(X < 4) = 1 0.5 = 0.5
- 2) When two balanced dice are rolled, 36 equally likely outcomes are possible. Let Z denote the sum of the dice.
 - a. What are the possible values of the random variable *Z*?
 - b. Find P(Z = 7)
 - c. Find the probability distribution of *Z*. Leave your probabilities in fraction form.

d. Construct a graph of the probability distribution.

Exercises 3; Probability Distributions

3) The following table lists the number of employees of a food chain restaurant in eight cities:

City	Employees
Minneapolis, MN Newark, NJ Omaha, NE Portland, OR San Antonio, TX San Jose, CA	105 155 149 195 290 357
Tucson, AZ Tulsa, OK	246 178

One of the cities is to be randomly chosen and all the employees of this city are to be interviewed. All the cities have the same probability of being chosen. Find the expected number of people who will be interviewed.

4) The random variable W is the crew size of a randomly selected shuttle mission between April 1981 and July 2000. Its probability distribution is as follows:

w	2	3	4	5	6	7	8
P(W=w)	0.042	0.010	0.021	0.375	0.188	0.344	0.021

- a. Find the mean of the random variable W
- b. Obtain the standard deviation of W

c. Draw the distribution of the random variable

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Exercises 3; Probability Distributions

- **5)** A designer makes a profit of \$30 on each item that is produced in perfect condition, and suffers a loss of \$6 on each item that is produced in less-than-perfect condition. If each item produced is in perfect condition with probability 0.4, what is the designer's expected profit per item?
- **6)** Two people are randomly chosen from a group of 10 men and 20 women. Let X denote the number of men chosen, and let Y denote the number of women chosen.
 - a. Find E(X) =
 - b. Find E(Y) =
 - c. Find E(X + Y) =
- 7) A husband's year-end bonus will be:

\$0 with probability 0.3 \$1000 with probability 0.6 \$2000 with probability 0.1

His wife's bonus will be:

\$1000 with probability 0.7 \$2000 with probability 0.3

Let S be the sum of their bonuses, and assume that the bonus of the husband is independent from the bonus of the wife. Find E(S) and Var(S).

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Exercises 3; Probability Distributions

8) A small taxi company has 4 taxis. In a month's time, each taxi will get 0 traffic tickets with
probability 0.3, 1 traffic ticket with probability 0.5, or 2 traffic tickets with probability 0.2. What is
the expected number of tickets per month amassed by the fleet of 4 taxis?

9a) An engineering firm is deciding whether to prepare a bid for a construction project. If the probability of getting the contract is 0.4, and the probability that the weather will be bad is 0.6, find the following probabilities:

Outcome	Probability
Not getting the contract	
Getting the contract and weather is bad	
Getting the contract and weather is good	

- **9b)** Consider the following three possible outcomes for the gross profit:
- 1) If it does not get the contract, then the firm will make a gross profit of \$0.
- 2) If it gets the contract and the weather is bad, the firm will make a gross profit of \$3,000.
- 3) If it gets the contract and the weather is good, the firm will make a gross profit of \$6,000.

What is the company's expected gross profit?

What is the standard deviation of the company's gross profit?

9c) Knowing that the cost for preparing the bid is \$800, What is the company's **expected net profit**? *Hint: The net profit is the gross profit minus the preparation cost.*

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Exercises 3; Probability Distributions

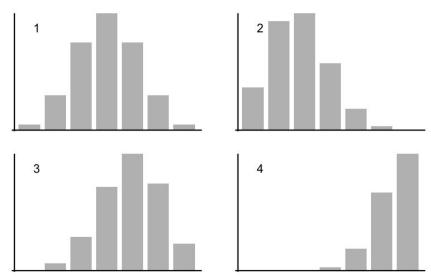
Use Binomial Probability Formula for problems 10, 11, 12

10)		air coin is tossed independently five times. P(heads) = P(tails) = 0.5. Compute: probability of all heads
	b.	probability of no heads
	C.	probability of at least one heads
	d.	probability of more heads than tails
	e.	probability of less than three heads
-	Y b	certain couple is equally likely to have either a boy or a girl. If the family has four children, e the number of boys.
	b.	Determine the probability distribution of Y
	C.	Find the probability that the couple has exactly two boys
	d.	Find the probability that the couple has at least two boys
	e.	Find the probability that the couple has at most two boys
	f.	Find the probability that the couple has between one and three two boys, inclusive
	g.	Find the probability that the couple has children all of the same gender

Exercises 3; **Probability Distributions**

- **12)** A large shipment of headphones ordered by a retail store contains 5% of defective devices. The retail store performs an inspection of the shipment by randomly selecting 20 headphones.
 - a. Find the probabilities that the inspection finds 0, 1, 2, 3 defective headphones. (*Hint: treat the random variable as a binomial random variable*):
 - b. The retail store has decided to accept the shipment if the inspection yields **no more than two** defective headphones. What is the probability of finding no more than two defective headphones?

13) The following figure shows four binomial distributions with n = 6 trials. Match the given probability of success with the corresponding graph.



- a) p = 0.30 goes with graph
- c) p = 0.65 goes with graph
- b) p = 0.50 goes with graph
- d) p = 0.90 goes with graph