

Pan & Tilt

Regulering og kontrol af robotsystemer- Gruppe 5

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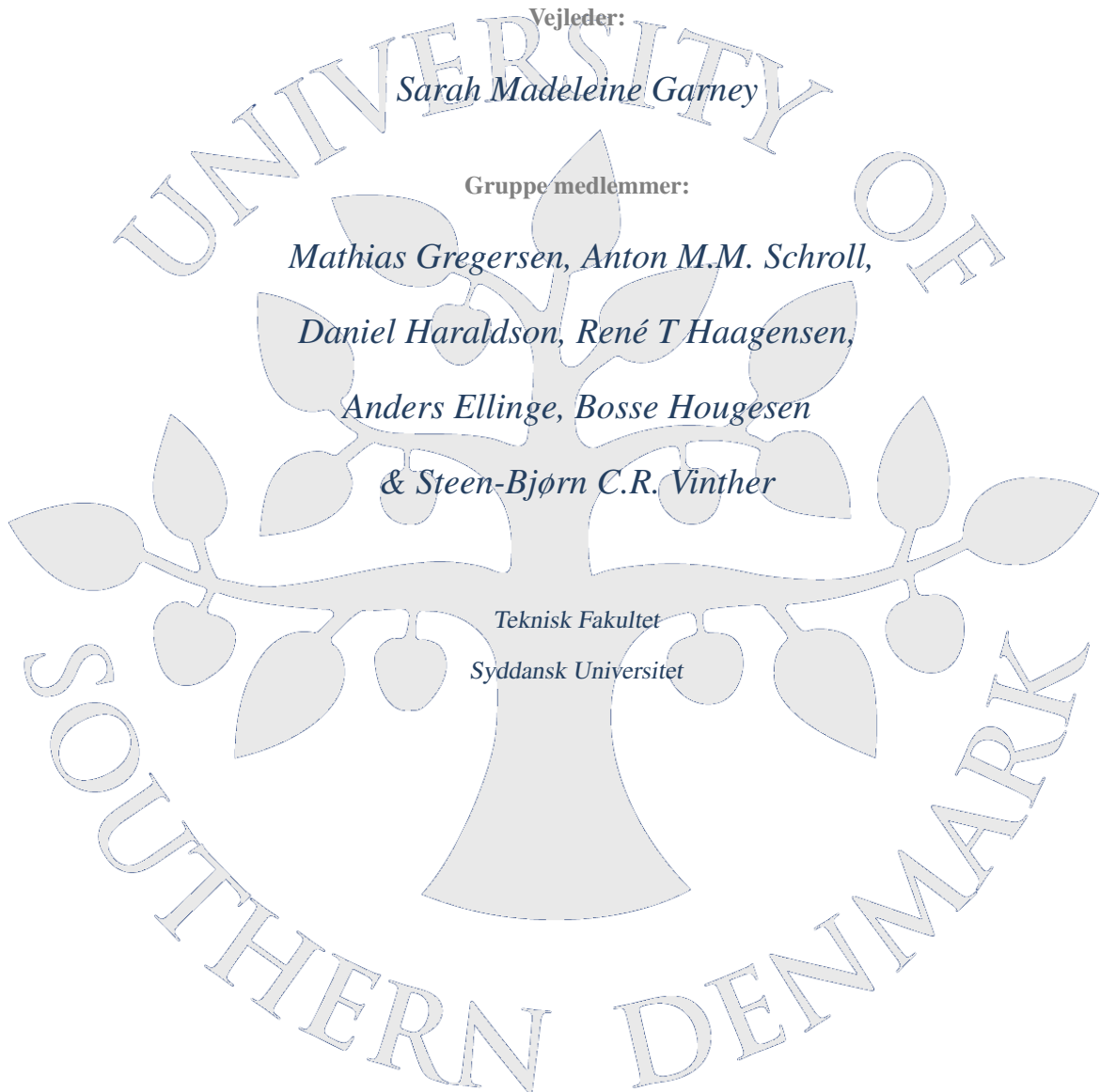
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Preface

This report is written by 7 4th semester Robotteknologi students from University of Southern Denmark in spring 2016. The report is based on the 4th semester project. It is aimed at people with basic knowledge in the disciplines: Digital programmable electronics, Embedded programming, Control Engineering and Computer systems. It describes the theory and analysis involved in designing the controller used to control the Pan & Tilt system.

The report is written as a conclusion to the project and contains documentation of the process and the experiences gained. It should therefore be possible to recreate the project using this report.

1 Abstract

The purpose of this paper is to show how to make a controller and how to use it to control a spotlight consisting of two connected frames, two motors and one light. Precise motor control is an essential requirement in most applications involving any kind of actuators that needs to behave in a predictable and controlled way. A spotlight capable of relative precise movement is important when performing on a stage. In order to make a controller, several measurements of the system's response to different voltages have been analysed. Using Matlab and control theory the values of the controller have been estimated. The results show; with the right controller, the system is easily controllable and will behave in a predictable way.

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2 Indledning

Indledning

3 Problem formulation

When performing on a stage, light in the right places is important. An easy way to get that, is via controllable spotlights. They have to be able to rotate horizontally and vertically, thereby targeting specific points on the stage and do so autonomously.

The Pan & Tilt System (P & T System) can be made to meet those requirements.

3.1 Definition of goals

The main goals of the product is, to be able to point the cone of light from the spotlight, at a specific point on a predefined surface or follow a human walking around on a surface. The user should have the option, to specify the limits of the spotlight's working space. The positions or paths should be set by the user and the movement of the cone should be pleasant to watch.

3.2 Requirements specification

The requirements will be divide into primary and secondary requirements, so as to identify the most important objectives.

3.2.1 Primary requirements

Hardware requirements

- The controller has to be implemented on the FPGA(Field-programmable gate array).
- The communication between the microprocessor and the FPGA has to be done with SPI(Serial Peripheral Interface Bus).
- The FPGA has to control the PWM(Pulse-width modulation) signal for the motors.

Driver requirements

- The system cannot have an overshoot of more than 10%.
- The system has to have a settling time of at least 1.5 sec for one revolution of either pan or tilt.
- At a scene of dimension 5 m x 5 m, from a hight of 5 meters, the system must achieve a velocity of at least $2.5m/s^1$ relative to the scene, which is the maximum velocity the average person would walk. ¹

Application requirements

- The application must support for the spotlight to be placed at different hight
- The application must support different stage dimensions up to 14 m x 14 m.

¹Wikipedia, Preferred walking speed, https://en.wikipedia.org/wiki/Preferred_walking_speed, 23/05/16

- The application must needs to be able to point its light towards a specific position on a 14 m x 14 m stage at a hight of 5 meter, with a error margin of +/- 10cm.

3.2.2 Secondary requirements

These are the requirements that would be nice to have, but is not necessary for the completion of the project.

- The movement between two points shall be in a smooth motion.
- The P&T system is to recalibrate the position of the Pan and the tilt under startup.
- The spotlight has to be able to be controlled by an application.
- The spotlight can be controlled by a joystick.
- The spotlight can have a steady state close to zero

4 Indledende idé fase

Applikation

Hvordan kan arbejdsområdet afgrænses efter brugerens behov?

Hvilke input / parametre skal kontrolsystemet manipulere?

Controller

Hvordan kan controlleren modelleres?

Hvordan kan de forskellige opgaver opdeles i tasks?

Hvordan udarbejdes en styring til motoren?

Hvilke parametre ønskes kontrolleret?

Hardware

Hvordan anvendes de indbyggede sensorer?

Hvordan kan platformen modelleres?

Hvordan kan systemet styres pålideligt?

Hvilke fysiske begrænsninger medfører hardwaren?

Dette bygger på antagelsen at pan and tilt projektet altid virker

Bevæge systemet i forhold til koordinater (Systemet skal kunne bevæge sig, i forhold til givne koordinater)

5 The System

Here goes the tekst.

6 The Microcontroller

Given the design requirements in section 3.2, and the block diagram in section 5. This includes all the functionality that is to be placed in the microcontroller. From here the next stage is to define the content of these blocks, and how they interact with each other.

The microcontroller is to establish an application programmer interface (API) to the P&T driver placed in the FPGA. The microcontroller will also run the application that uses this interface in order to help the user achieve his/her goal, which is to control the spotlight.

The program will be written in the C language, and it will be documented using task diagrams and states machines.

6.1 Choice of Operating System

Since it is safe to assume that this program will be using multipliable task, an operating system (OS) is required. This OS must support the ARM Cortex M-4 processor, which is used in this project. It must be supported by Code Composer Studio, which is the software used for programming the processor.

Using a Real Time Operating System freeRTOS would give the advantages of preemptive scheduling. Being able to preempt a low priority task to pave the way for a task of higher priority will ensure better performance if the project have a serden sive to it.

6.2 Program Structure

Given the above mentioned requirements, a task diagram for the system was created, here the program were to handle two different sources of user input, in a manner that would not effect the application.

Insert task diagram here

walk through the system, separating the program into tasks starting from the block diagram. (see the criteria in Morten's ppt.)

one task one input queue

what drivers where required to achieve the goal of the program,

now add the used semaphores at critical sections

Now when the task diagram has been made, it is time to considerer possible structural weakness such as deadlocks and handling og queues.

6.3 The Application Programmer Interface

what is this sorcery - and what will i achieve by using it it is there to represent all the functionality available for each driver in the program.

where in the program will this be used

how will it be implemented

6.4 Event Queues and Shared State Memory

it will ensure that only events can be found in the queue, data will be saved and an event stating that data can be read will be send instead

this is so that the data never will look like an event.

How is this implemented

6.5 Deadlock Protection

A deadlock is when one or more process cannot proceed because some of the resources it need is held by another process. The two processes will "compete" with each other and neither of them will finish.

1. **Mutual exclusion** is the concept of making sure that two or more concurrent processes are not in their critical section at the same time. The critical section is a part of the program that cant be used by more than one process at the time.
If more than one process is in the same critical section at the same time errors are bound to happen.
2. **Hold and wait** is when a process holds on to a resources and wait for the rest of the resources it needs.
3. **no preemption** means that only the process that holds the resource can release it. If preemption is allowed, the program is able to take resources from a process and allocate it to another process.
4. **Circular wait** is when one process is waiting for at resource that another process is has and the other process is waiting for a resource held by the first one. It could also be a chain of processes where every process needs a resource held by the next and the last one needs a resource held by the first.
(add source XXXX)

All four conditions needs to hold true in order for a deadlock to occur. You can therefore provide a deadlock-free environment by avoiding one of the conditions.

To avoid deadlocks in the system, the circular wait condition is removed via semaphores. This insures that deadlock cannot happen. In figure 1 a code example of how it is used.

First the process takes one semaphore. Then it takes another, do **SKRIV HVAD DEN GØR**. After that it releases the first semaphore and then the last. This insures that it has all the resources it needs to do its work and no deadlock is possible.

6.6 SPI-Master

using the build in free-scale spi-module in the TM4C123GH6PM Microcontroller, or creating the protocol from scratch.

The making of the state machine that is the SPI-master

A state is only a state if you have to wait till you move on

```

if (xSemaphoreTake(pt_semaphore, portMAX_DELAY) == pdTRUE)
{
    data_holder = get_msg_state(ssm_address);

    // convert the relative number to tacks
    if (address == ADR_TARGET_POS)
        //message = pt_api_convert_to_tach(PT, 5000);
        pt_api_convert_to_tach(PT, 5000);

    // 2 adress bit 1 p/t bit and 11 message bits
    // 0 0 a a p t d d d d d d d d d d
    placeholder = data_holder & 0x07FF;
    placeholder |= ((PT & 0x0001) << 11);
    placeholder |= ( address << 12 );

    // send the message via spi_master
    return_val = xQueueSend(spi_tx_queue, &( placeholder ), portMAX_DELAY);

    xSemaphoreGive(pt_semaphore);
}

```

Figur 1: Semaphore code example

6.7 The Application

6.7.1 The Kernel task

making the state mashine for the kernel-task

separating commands in groups depending on the number of parameters to use.

the list of commands that will be supported (se the list on google drive XXXX)

6.7.2 The light-show task

making the state machine for the light-show-task

6.8 Overview

The above mentioned functionality was ment as a fully dressed system containing all the features that would be needed while working with a real spotlight. However, not all features was primary requirements, which makes it okay that it never got implemented.

The joystick: Even though a driver was made for the joystick, it the the corresponding API was not. Therefore this

Point at a specific location.

This is the functions that did not made it to the implementation

1. ps2 controller and its corresponding api
2. calculating the tack-position from the relative coordinates given by the application
3. follow a waking person

7 The FPGA

Here goes the tekst.

8 Driver

This section describes how the driver is implemented in the FPGA. The section starts with an overall analysis of the system and afterwards goes into details with some blocks defined in the analysis and ends with an discussion on how the PID controller could have been implemented better as a filter.

8.1 Overall analysis

The easiest way to describe how the overall system works is by looking at the general components and how they are connected. The general components used in the implementation are: a comparator, a controller, a sensor, a motor driver with a PWM module and a SPI slave with a data bank. A generic multiplexer display was also added to simplify the debugging process, however this should not be seen as a part of the final product. Since the goal is to control two motors a separate controller setup was made for each motor. This means that each motor is connected to its own setup of a comparator, a sensor, a controller and a motor driver. The SPI slave component is common for the motors. On figure # Overall driver # an illustration of how the components are internally connected. This figure also shows information on the signals between the individual components.

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The components can be divided into the following blocks, each with a specific purpose.

The first block is the SPI slave block which contains only the SPI slave component. The purpose of this block is to receive and store information used by the rest of the components. It then shares the information with the components that are in need of them. An example of this could be the maximum and minimum speed of a motor which is send to the controller (this connection can also be seen on figure # Overall driver #).

The second block is the controller block which contains the comparator and the controller components. The purpose of this block is to regulate the motors according to a target input and the feedback. The block generates a duty cycle and a direction that is passed onto the motor driver.

The third block is the sensor block which consists only of the sensor component. The purpose of this block is to keep track of the current position of the motor. This is done by looking at the hall sensors from the motors and relating their output to the current position.

The last block is the motor driver which contain the motor driver component and its internal PWM module. The purpose of this block is to control and power the motor. This means that the block generates a PWM signal and outputs it on the correct pin according to the desired direction.

9 Motor driver block

This section will describe in detail how the motor driver block receives a duty cycle and a direction, then uses these to generate and output a **PWM** signal according to the direction and speed set by the controller block.

9.1 Description

An easy way to visualize the inner workings is to divide the Motor Driver into two separate blocks. The first block's task is to create a **PWM** signal which is equivalent to the duty cycle given by the controller. The second block's task is to set the output of the **PWM** signal to the right pin on the H-Bridge in order to control the direction of the motor.

9.2 Theory

This section will describe the theories used for the implementation.

9.2.1 PWM generation

The **PWM** signal is created based on a looping counter and a threshold. Imagine a counter resetting whenever it reaches a certain value, creating a loop. If the value is set to the period of the wanted **PWM** signal and the **PWM** signal output is dependent on the counter value relative to a threshold, then you will be able to create a looping output that is dependant on the threshold. Figure # PWM implementaion principle # show an illustration of the behavior of **PWM** signal based on the looping counter and threshold.

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9.3 Implementation

The implementation was done with the separation of the block described before. A **PWM** component was created which has the sole purpose of creating a **PWM** signal based on a duty cycle. The other part has the purpose of directing the **PWM** signal to the right output pins based on the direction wanted.

9.3.1 PWM part

The **PWM** block was implemented so that whenever the counter value is below the threshold the **PWM** signal output is high and when the counter value is above the threshold the **PWM** signal output is low. The section of the **PWM** code that makes the counter can be seen on picture # Counting example #.

9.3.2 Direction part

This block is simply implemented as a switch that toggles on the wanted direction. As an example if the wanted direction is set to 0 then the **PWM** is driven to the relevant motor control output and the other is kept at zero.

9.4 Tests

To verify that this motor controller is working as intended, a test bench was created and various inputs were tested. The enable was set and a duty cycle of 8 bits was input, which corresponds to a certain duty cycle. A clear spike in PWM output could be seen, of the same length every time PWM is outputting. To further verify the test, the edges of the PWM signal were measured and used to find the exact duty cycle. Table # Table from other motor driver # showcases the tests of PWM.

9.5 Discussion

The tests show a deviation from the desired duty cycle of a small percentage. However these deviations have been deemed insignificant. The error is created by the method that is used to calculate the PWM from the duty cycle, when converting the bit string, it is multiplied by the PWM period and divided by 256. This yields an integer, that when combined with the counter, yields a PWM very close to the desired duty cycle. Beyond that margin of error, a single clock cycle is lost due to resetting the counter, which corresponds to 1 ns.

9.6 Conclusion

The motor driver has been sufficiently explained and tested, and has become a solid module to create a PWM signal for the P & T system. The PWM calculation can be optimized very slightly by improving the conversion from duty cycle to PWM, and optimizing the counter, as to never lose any clock cycles.

10 Sensor block

This section describes in detail how the sensor block handles the output of the Hall effect sensors and sends it to the comparator block.

10.1 Description

The responsibility of the sensor block is to handle the output from the Hall effect sensors and determine the position of both the pan part and the tilt part of the system. The controller block relies on this information and thus this block forms the basis of the control method chosen.

10.2 Theory

Hall effect sensors are sensors that change their voltage output based on proximity of a magnetic field. If combined with the right circuitry it can be used as a switch, giving a digital output. When placed around the rotating axis of a motor with the right relative distance, the Hall effect sensors can be used to determine the position, direction, rotational velocity and the position of the axis. There is a disc on the axis of the motor. It is divided into 6 sections, alternating between two levels of magnetization. Around the magnet, two Hall effect sensors are placed at an angle of slightly less than 90 degrees (See figure 2). As the motor axis rotates, the magnetized parts move past the sensors and the magnetic field, they are subjected to, changes. Because the Hall effect sensor is a

little “off” the output will have an overlap see figure 3. This is what is used to determine the direction.

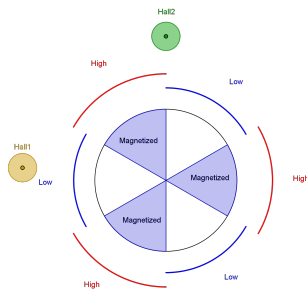


Figure 2: This is an example of how the Hall effect sensors is placed around the disk.

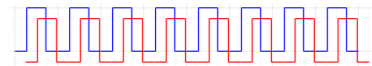


Figure 3: As the axis rotates, the output changes

10.3 Implementation

The Hall counter is the sensor block. Every time the Hall effect sensors gives an output the Hall counter is updated. There are 1080 “tachs” or changes in the output of the Hall effect sensor, for one revolution. To be able to move both clockwise and counterclockwise, the starting position is set to half of the total: 540. This is done to avoid working with negative values, as that can contribute to unnecessary difficulty in the implementation.

It starts out with sampling the value of the sensors. The value of the sensor is read and shifted into a vector of two bits as seen in figure 4

```
if rising_edge(CLK) then -- Sample and shift
    debounce_hall1 <= debounce_hall1(0) & HALL1;
    debounce_hall2 <= debounce_hall2(0) & HALL2;
end if;
```

Figure 4: An example of how the the value is sampled and shifted

If no change have been registered, the position doesn't change and a new sample is taken. As seen in figure 5. If a change is detected then a series of “if statements” determines whether the change in position is positive or negative.

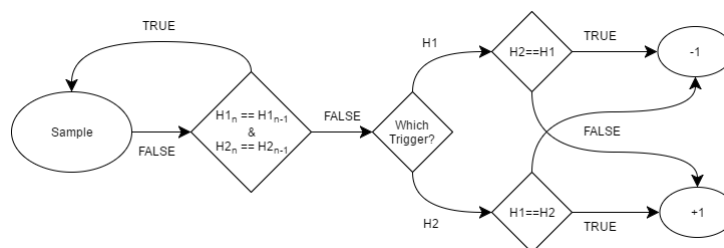


Figure 5: Flowchart of how the position changes in relation to different Hall effect sensor outputs

A small example of the of the code involved can be seen in figure 6

```

if falling_edge(CLK) then -- Calculate pos
  if debounce_hall1 = "01" then
    if HALL2 = '1' then
      pos := pos + 1;
    else
      pos := pos - 1;
    end if;
  end if;
end if;

```

Figur 6: Small bit of code that shows how the position is calculated based on the Hall effect sensor output

10.4 Test

To make sure the code behaves in the intended way a test bench have been made. It simulate the codes response to changing output from the Hall effect sensors. The first two bars show the Hall effect sensors and their changing values. The next bar is the clock and under that one the position.

As can be seen in figure 7, the position is steadily decreasing in value. If the position reaches the max value (108010 or 00000100001110002) the position is set to 0. If the position reaches -1 it is set to the max value minus one.

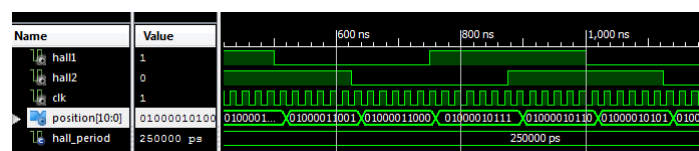


Figure 7: Testbench of how the position changes based on Hall effect sensor outputs

10.5 Discussion

As there is only two Hall effect sensors and the max rate of change in their output is a lot less than the possible sampling rate, it is fairly easy to calculate the change in position of the motor. However having only two sensors and only 6 different magnetization levels limits the accuracy of the measurements. If the axis of the motor moves in the area between a rising or falling edge but never reaching one on either sensors the change in position cannot be measured. More sensors would give a higher precision but also require more calculations in order to determine whether the change is positiv og negativ. One more error that can be experienced is if the axis end up in a position where one of the sensors is “stuck” on a rising or falling edge. If that happens the position will constantly flip between the two values. Lastly as magnets are used they sometimes “stick” to a certain position. All this combined with the slack in the belt transferring the rotation from the motor to either the pan or tilt and the small distance before the teeth of the belt and gear meshes, this limits the overall precision of the system

10.6 Conclusion

The component works as expected and sends the current position of the system to the comparator block.

11 SPI slave block

This section will describe in detail how the SPI slave in the FPGA receives and transmit data according to the description of the SPI communication protocol mentioned before.

11.1 Description

The SPI slave has two different tasks. The first task is to exchange data with the SPI master in the microcontroller. The second task is to store the information that is received and present it to the components that need the data.

The SPI slave could be called also some sort of information bank for the driver.

The data exchange part follow the SPI communication protocol mentioned before. The information bank part is made by having the block hold the information in the actual output of the block. This is done so that the data is constantly supplied to the block in need of the data. However this requires a lot of data paths, but this is not much of a problem since this is going on internally in the FPGA. The reason the data is stored in the SPI slave component was also to make it more manageable since all of the data is stored at the same place.

11.2 Implementation

The SPI slave could have been implemented as a state machine. However because of the rather simplistic nature of the SPI communication protocol it was chosen not to implement it as a state machine. Instead it was implemented as a series of different events that trigger different responses in the SPI block. The first event is the S_CLK pin is having an rising edge. This event makes the the SPI slave read the input from the MOSI pin and prepare the next output for the MISO pin. The code that handles this event can be seen in figure 8.

```

if S_CLK_event = "01" then -- S_CLK rising edge
    if S_CLK_counter = 10 then -- Received all of address
        case input_shift_register(13 downto 11) is
            when "000" =>
                output_buffer <= "000" & CURRENT_POS_TILT; -- Swap output buffer with current position tilt
            when "001" =>
                output_buffer <= "000" & CURRENT_POS_PAN; -- Swap output buffer with current position tilt
            when others =>
                output_buffer <= (others => '0'); -- Set output buffer to default
        end case;
    end if;

    if S_CLK_counter /= -1 then -- If last entry, move to input buffer
        input_shift_register(S_CLK_counter) <= MOSI; -- Put data in shift register
        S_CLK_counter <= S_CLK_counter - 1; -- Decrement counter
    end if;
end if;

```

Figur 8: An S_CLK code example

The second event is when the SS pin has a rising edge. This signifies that the transmission is over and that all of the packet should be sent. This event triggers the SPI slave to update the data received on the correct output according to the received address for the data. An example of the code doing this can be seen in figure 9.

```

--
if SS_event = "01" then -- SS rising edge
  S_CLK_counter <= 13; -- Counter is reset

  case input_shift_register(13 downto 11) is -- Send data to address
    when "000" =>
      TARGET_POS_TILT_temp <= input_shift_register(10 downto 0);

    when "001" =>
      TARGET_POS_FAN_temp <= input_shift_register(10 downto 0);

    when "010" =>
      MAX_SPEED_TILT_temp <= input_shift_register(7 downto 0);

    when "011" =>

```

Figure 9: An SS code example

Under the data transaction two temporary registers are used, one for the input and one for the output. This is done to stabilize the data send so that it does not change mid transmission which would cause the data to become corrupt. There are 4 different kinds of settings that can be controlled via the SPI slave. The first setting is the target position used in the controller block, the second setting is the maximum speed for the motor, the third setting is the minimum speed of the motor and the last setting is the enabling of the motor. All of these 4 settings can be set for the pan and tilt part separately. This results in 8 different values needing an address resulting in an address length of 3 bits. Since the data length has to be constant, the data length was chosen according to the largest value needed to be sent. This was the target position, needing 11 data bits hence the data length was chosen to be 11 bits.

The output from the SPI slave to the SPI master was chosen to mimic the address and then send some data according to the address received under the transmission. This means that the output buffer has to be changed under the transmission. This would be a problem in most cases, however since the FPGA works much faster than the microcontroller this is not a problem. Since the only information the SPI master is interested in is the current position, the output buffer is only changed when this information is polled. It was made so that this information was always polled when a target position was sent, meaning that if only a poll on the current position is wanted the target position is resend with the same value. In all other scenarios then the master sending the target position, the value returned to the master is the address the master sent and a data containing zeroes. The code handling this can also be seen in 8.

11.3 Tests

The SPI slave component has been tested in a Xilinx ISE testbench. This was done by simulating a transaction to the SPI slave. In figure 7 the test bench can be seen. SS can be seen going low signifying the start of the data transfer.

The S_CLK then starts to toggle and the data is shifted into the input register and as SS goes high the data from the input register is set to the placement the address is pointing to. In this case, a value to the target of the pan is being send. This has the address of 001 which can also be seen on the three first bits on in the input register.

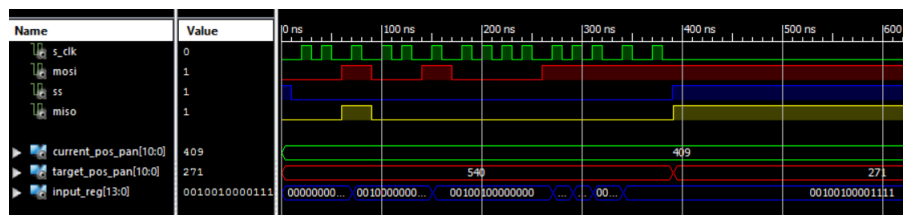


Figure 10: An Xilinx testbench simulation of the SPI

11.4 Discussion

One of the features you would get from creating the SPI slave component as a state machine is more robustness against errors. When an error happens in a state machine it would be unable to make the same amount of mess because it is locked to the state. However since no error should be happening and the fact that at no time while testing the connection was an error made, it is not really of any concern.

11.5 Conclusion

Both the testbench and physical test with the FPGA and microcontroller showed that this component functioned as it should.

12 The Controller

Here goes the tekst.

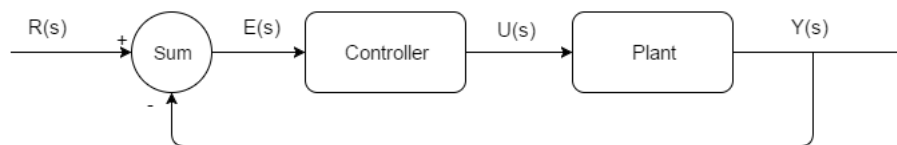
13 PID

13.1 Introduction

A controller is an essential part of most autonomous systems. This project is no exception - having control over where the pan and tilt system is pointing at is crucial to meeting the specified requirements. The following questions might then transpire.

- What controllers are available?
- Is a complex or simple controller desired?
 - Pros and cons?
- How do you determine which one to use?
- How do you implement them?

When discussing what controller to use, figure 11 is the point of reference, where the plant is the previously estimated transfer function, **SKRIV FORMLEN EQUATION REF**, of the motor of the system.



Figur 11: A generic way of representing a close-looped control system

13.2 The Controller

For simplicity's sake Proportional (P), Proportional-Integral (PI), Proportional-Derivative (PD) and Proportional-Integral-Derivative (PID) be the only controllers taken into considerations for this project. Though Lead-Lag compensators could be considered as well, since in essence they can do the same as before mentioned controllers.

A PID controller is made up by three parts: the proportional gain looks at the current error, the integral looks at the past errors and the derivative looks at current rate of change. Each term has a tuneable gain called the k constants. In general these constants are what defines a PID controller's behavior. See figure 12 for illustration.

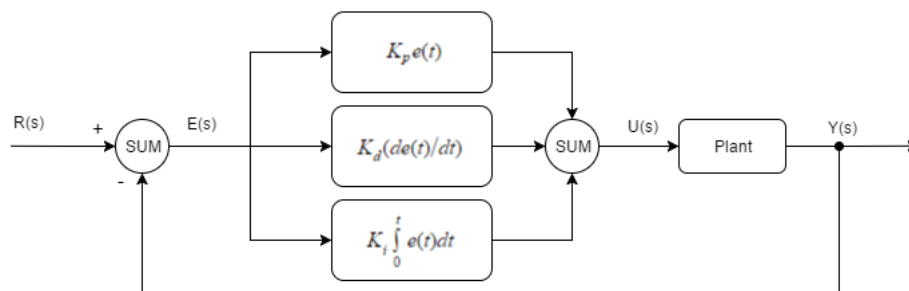


Figure 12: A representation of the PID controller principle

This is the equation of the standard PID controller in the time domain:

$$K_p e(t) + K_i \int_0^t e(t) dt + K_d \frac{de(t)}{dt}$$

If transformed to the s domain the equations looks like this:

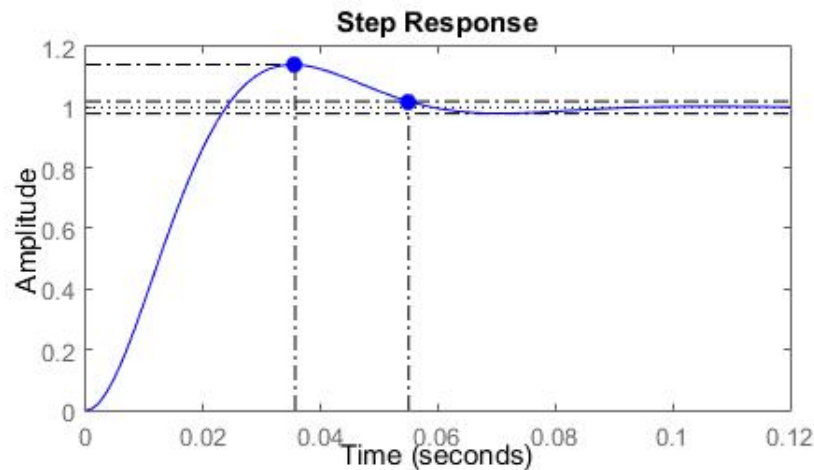
$$G(s) = K_p + \frac{K_i}{s} + K_d s$$

13.3 Proportional Controller

The P controller is by far the most straightforward controller, being that it is simply adding a gain to the open-loop transfer function. A P controller is a desired controller, since it is very simple to implement and tune, though this project have to meet the stated requirements.

To help analyse and give some intuition about how the motor's transfer function behaves, a root locus of the open-loop transfer function is plotted see figure 17. As one would expect it seems like this kind of controller will not suffice for the project.

As seen in figure 13, the step response of the closed-loop transfer function, has an overshoot of 14.1 percent, and a settling time of 0.055 seconds. Meeting the specified requirements for the project with this controller is not going to happen. The overshoot can be decreased by reducing the gain below 1, but this induces a longer settling time and vice versa.



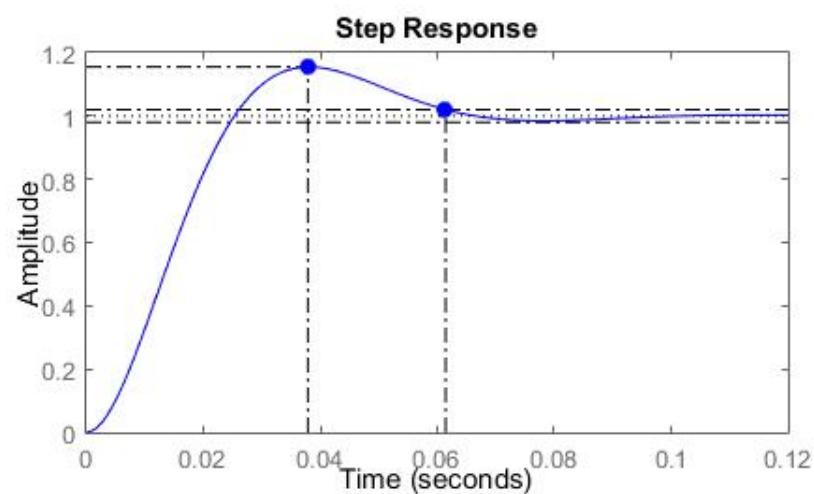
Figur 13: Peak amplitude: 1.14 - Overshot(%): 14.1 - At time(seconds): 0.0356 Settling time (seconds): 0.055

13.4 Proportional-Integral Controller

The PI controller accumulates past error terms over time to eliminate steady-state errors in the system. This can cause an increase in overshoot called the integrator wind up, and an increase in settling time. Though if a requirement is complying a steady-state error of 0, then it is up to the designer to decide, if reaching state-state is more vital to the system, than having more overshoot and a longer settling time.

Using a PI controller is the same as adding a pole and a zero to the open-loop transfer function. As seen in figure 17, this controller does not seem to live up to the requirements either. Placing the zero and pole differently could make a better controller, but it would never be able to adjust to both design criterias.

The step response of the PI controller is seen on figure 14, the only difference from the P controller is a slightly longer peak time and settling time and a larger overshoot, as expected. This controller would not meet the requirements.



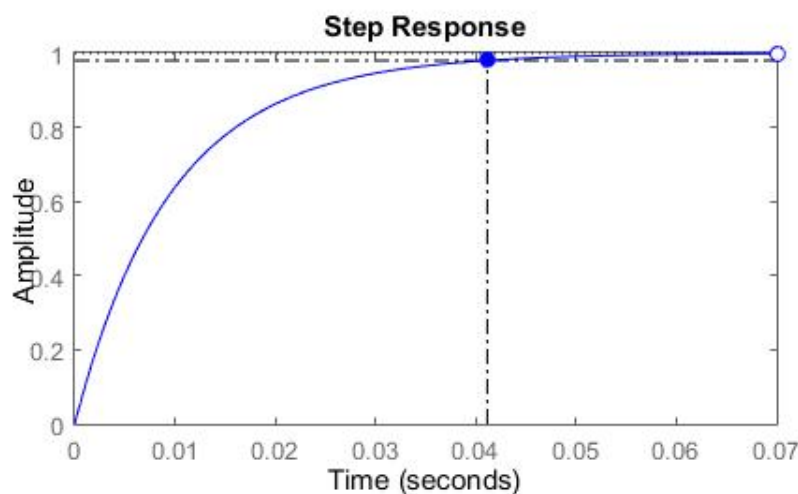
Figur 14: Peak amplitude: 1.15 - Overshot(%): 15.5 - At time(seconds): 0.0379 Settling time (seconds): 0.0614

13.5 Proportional-Derivative Controller

A PD controller is equivalent to the addition of a simple zero, **INSERT EQUATION HERE**, which improves the transient response. From a different point of view, the PD controller may also be used to improve the settling time or stability, because it anticipates large errors and attempts corrective action before they occur.

FIGURE5 shows a promising root locus of the PD controller, it seems like that with the right amount of gain the system would fulfill the requirements.

The step response on figure 15 shows, that in fact this controller would be ideal for this project. There is no overshoot, and the settling time is well below 0.05 seconds.



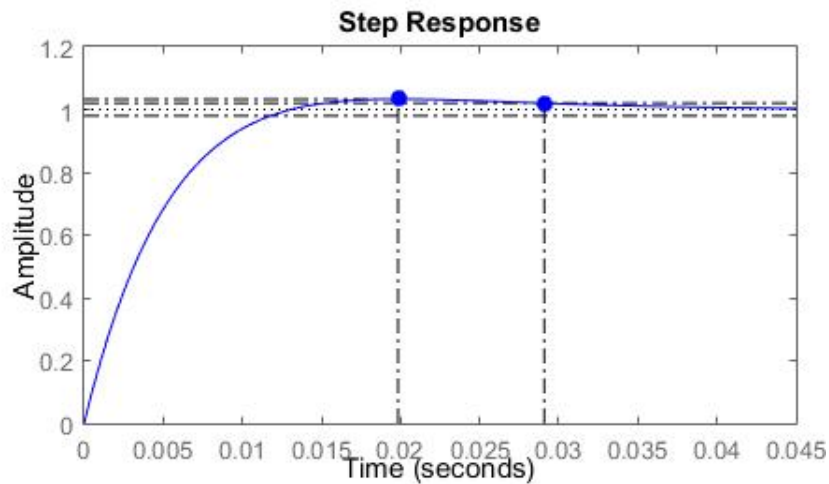
Figur 15: Peak amplitude: ≥ 0.998 - Overshoot(%): 0 - At time(seconds): > 0.07 Settling time (seconds): 0.0411

13.6 Proportional-Integral-Derivative Controller

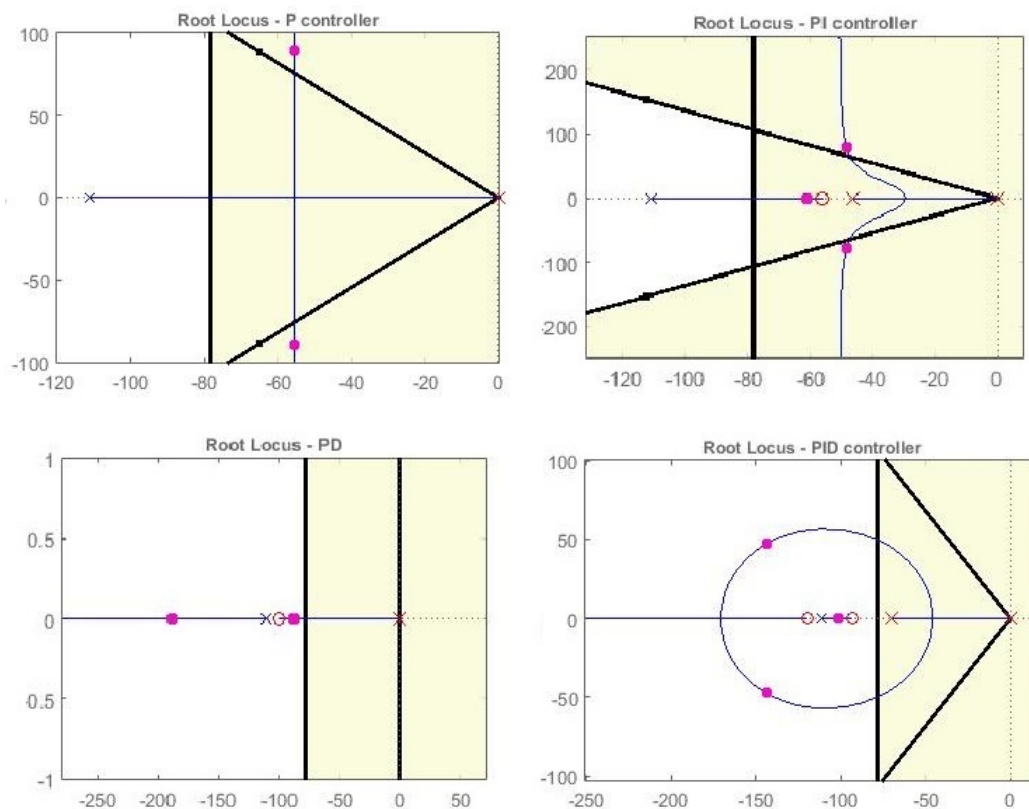
The PID controller is the most complex controller which is going to be discussed. As noted earlier an PD controller was sufficient for a controller. So why discuss the PID? The reason is that, in reality systems might have limitations which analysis have not taken into account yet. Reaching a steady-state error of 0 is actually a problem with a PD controller for this project, since the pan and tilt system does not function below a certain range of voltage, which means that an integral is needed.

Notice on figure 17, that an PID controller is the addition of 2 zeros and 1 pole to the open-loop transfer function. The root locus shows that this system with a relative gain still meets the requirements of the design.

The step response of the PID controller, figure 16, shows that indeed a PID controller would be a good choice of controller for this project. There is well below 10% overshoot and the settling time is a great deal below 0.05 seconds.



Figur 16: Peak amplitude: 1.03 - Overshot(%): 2.92 - At time(seconds): 0.0201 Settling time (seconds): 0.0277



Figur 17: Open-loop transfer function Root Locus plots of the estimated motor transfer function, EQUATION REF, with different controllers. The shaded areas indicates designs not met if poles of the closed-loop transfer function is placed there. The designs are: Overshoot $> 10\%$, settling time ≥ 0.05 seconds. 7

14 Perspectivation

Here goes the tekst.

15 Conclusion

16 References

- Ref1
- Ref2
- Ref3
- Ref4

A Appendix

1. Code
2. Report
3. Documents