CSE 803 Computer Vision: Homework 3

Instructions

- This homework is **due at 11:59:59 p.m. on** Thu October 17th, 2024.
- Please submit to D2L. The submission includes two parts:
 - 1. A pdf file as your write-up, including your plots and answers to all the questions and key choices you made.
 - The write-up must be an electronic version. **No handwriting, including plotting questions.** LATEX is recommended but not mandatory.
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 - 2. A ip Ale Ancluding All your Aode, And Ales specified An questions Aith **Submit**, All Ander the Aame Airectory. You Aan submit Aython Aode An either .py Ar .ipynb format.

1 RANSAC [30 pts]

1.1 Fitting a Line [10 pts]

In this section, each question depends on the previous one. By *putative model*, we mean the model that is fit in the inner loop of RANSAC.

- 1. (3 pts) Suppose we are fitting a line (e.g., y = mx + b). How many points do we need to sample in an iteration to compute a putative model?
- 2. (3 pts) In the previous setting, suppose the outlier ratio of the data set is 0.1. What is the probability that a putative model fails to get a desired model?
- 3. (4 pts) In the previous settings, to exceed a probability level of 95% for success, how many trials should we attempt to fit putative models?

1.2 Fitting Transformations [20 pts]

We'll begin by reviewing fitting transformations from 2D points to 2D points. You will need to use these results to solve the subsequent sections.

1. (1 pt) Recall that a matrix $\mathbf{M} \in \mathbb{R}^{2 \times 2}$ is a linear transformation: $\mathbb{R}^2 \to \mathbb{R}^2$. How many degrees of freedom does \mathbf{M} have? How many samples are required to find \mathbf{M} ?

2. (2 pts) Suppose we have a dataset $\{(\mathbf{x}_i, \mathbf{y}_i)\}_{i=1}^N$ and want to fit $\mathbf{y} = \mathbf{M}\mathbf{x}$. Formulate the fitting problem into the form of a least squares problem:

$$\mathrm{argmin}_{\mathbf{m}} \|\mathbf{Am} - \mathbf{b}\|^2$$

where m is some vector that has all the parameters of M. Write out the form of A.

3. (3 pts) Use numpy.load() to load p1/transform.npy. Each row contains two points x and y, represented in the form $[\mathbf{x}_i^T, \mathbf{y}_i^T]_{1 \times 4}$. Then fit a transformation

$$y = Sx + t$$

where $\mathbf{S} \in \mathbb{R}^{2 \times 2}, \mathbf{t} \in \mathbb{R}^{2 \times 1}$. Solve the problem by setting up an optimization of the form of $\underset{\mathbf{v}}{\operatorname{argmin}}_{\mathbf{v}} \|\mathbf{A}\mathbf{v} - \mathbf{b}\|^2$. Report \mathbf{S} and \mathbf{t} .

- 4. (2 pts) Plot the points x, y and $\hat{y} = Sx + t$ in one figure with different colors. **Display** the figure.
- 5. (2 pts) Explain how you transform the points in words based on S and t. Is the fitting result good?
- 6. (4 pts) We have 8 cases of homography transformation of letter M. In each case, there are two sets of 2D points X and Y, which are represented in the same format as 1.2.3 (a N×4 array with each row in the form $[\mathbf{x}_i^T, \mathbf{y}_i^T]_{1\times 4}$, we have loaded the data for you). For each case, fit a homography

$$\begin{bmatrix} \mathbf{y} \\ 1 \end{bmatrix} \equiv \mathbf{H} \begin{bmatrix} \mathbf{x} \\ 1 \end{bmatrix}$$

where $\mathbf{H} \in \mathbb{R}^{3\times 3}$. Solve the problem by dealing with the optimization of the form of $\operatorname{argmin}_{\mathbf{h}} ||A\mathbf{h}||^2$ with $||\mathbf{h}|| = 1$ where \mathbf{h} has all the parameters of \mathbf{H} . Report matrix \mathbf{H} of each case.

- 7. (4 pts) Visualize the original points, the target points and the points after homography transformation in one figure (three separate images in one figure). **Display** the figure of each case.
- 8. (2 pts) Discuss the transformations your observed in visualization with the homography matrix **H**. Do they make sense to you?

2 Image Stitching [55 pts]

Image stitching or photo stitching combines multiple photographic images that have overlapping fields of view to produce a segmented panorama or high-resolution image. You'll be able to do this by the end of this problem (which is derived from an assignment developed by Svetlana Lazebnik at UIUC). For this part, you will be working with the following images.





Figure 1: Input of Image Stitching.

Here are the instructions:

- 1. (3 pts) Load both images: p2/uttower_left.jpg and p2/uttower_right.jpg. Convert them to double and to grayscale. **Display** the grayscale images.
- 2. (4 pts) Use SIFT/SURF descriptors in OpenCV to detect feature points in both images. **Display** both the images along with the feature points.
- 3. (6 pts) Compute distances between every descriptor in one image and every descriptor in the other image. Alternatively, experiment with computing normalized correlation, or Euclidean distance after normalizing all descriptors to have zero mean and unit standard deviation. Report your choices.
 Note: You are not allowed to use built-in functions to match features for you, including but not limit to cv2.BFMatcher. However, you can use them to debug your code and compare to your implementation.
- 4. (10 pts) Select putative matches based on the matrix of pairwise descriptor distances obtained above. You can (i) select all pairs whose descriptor distances are below a specified threshold; (ii) select the top few hundred descriptor pairs with the smallest pairwise distances; or (iii) as described in lecture, compute the ratio test described in lecture (nearest-neighbor to second-nearest-neighbor ratio test). **Report** your choices.
- 5. (12 pts) Run RANSAC to estimate a homography mapping one image onto the other. For the best fit, **Report** the number of inliers and the average residual for the inliers (squared distance between the point coordinates in one image and the transformed coordinates of the matching point in the other image). Also, **display** the locations of inlier matches in both images. (i.e. for the inliers matches, show lines between matching locations in the two images). You can use cv2.drawMatches to draw matches.
 - **Note:** You need to implement RANSAC and calculate the transform matrix. You are not allowed to use functions that do RANSAC in one line, including but not limit to cv2.findHomography or cv2.getPerspectiveTransform. However, it's a good idea to use them to debug your implementation.
- 6. (8 pts) Warp one image onto the other using the estimated transformation. To do this, you will need to learn about cv2.warpPerspective. Please read the documentation.

7. (8 pts) Create a new image big enough to hold the panorama and composite the two images into it. You can composite by simply averaging the pixel values where the two images overlap. **Display** a colored image, which might look like this:



Figure 2: Sample output of Image Stitching.

8. (4 pts) Try to run your code on p2/bbb_left.jpg and p2/bbb_right.jpg. Display the detected feature points, the matching result, the inliers after RANSAC, and the stitched image.

Python Environment

We are using Python 3.7 for this course. You can find references for the Python standard library here: https://docs.python.org/3.7/library/index.html. To make your life easier, we **recommend** you to install the latest Anaconda for Python 3.7 (https://www.anaconda.com/download/). This is a Python package manager that includes most of the modules you need for this course.

We will make use of the following packages extensively in this course:

- Numpy (https://docs.scipy.org/doc/numpy-dev/user/quickstart.html).
- Matplotlib (http://matplotlib.org/users/pyplot_tutorial.html).
- OpenCV (https://opencv.org/). Especially, we'll use **OpenCV 3.4** in this homework.
 - 1. To install it on your computer, run conda install -c menpo opency.
 - 2. To use OpenCV 3.4 on Colab, run the following codes before import cv2:

```
- !pip uninstall opency-python
```

- !pip install --force-reinstall opency-python==3.4.2.16
- !pip install --force-reinstall opency-contrib-python==3.4.2.16

References

Recognising Panoramas: http://matthewalunbrown.com/papers/iccv2003.pdf.

Acknowledgement

The homework is prepared by Dr. David Fouhey and Dr. Svetlana Lazebnik. We are grateful for their generosity.