CSE 849 Deep Learning
Spring 2025

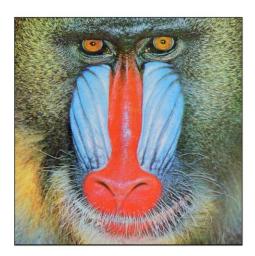
Zijun Cui

#### **Notation**

• "Channel": the number of filters

• "Depth": for each filter, the depth equals to the number of feature maps from the previous layer

# **Convolutional Filters**



Original: Mandrill



Smoothed with Gaussian kernel



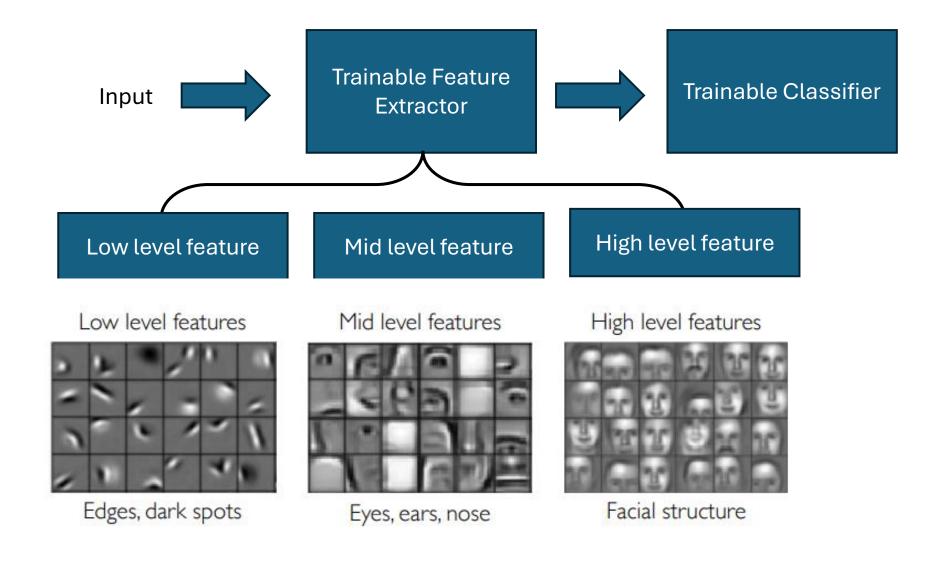
Original Image



Edges

More can be found in computer vision

# Recall: Deep Learning = Learning Representations



#### **Outline**

An CNN model for image classification

- More recent CNN architecture designs
  - Group Convolution and ResNeXt
  - Neural Architecture Search and EfficientNets
  - RegNets and NFNets

# Setting everything together

- Typical image classification task
  - Assuming maxpooling..



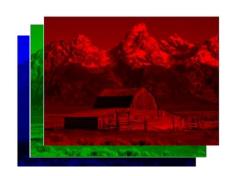








- Input: 1 or 3 images
  - Grey scale or color
  - Will assume color to be generic



• Input: 3 pictures

# Preprocessing

- Large images are a problem
  - Too large
  - Compute and memory intensive to process
- Sometimes scaled to smaller sizes, e.g. 128x128 or even 32x32
  - Based on how much will fit on your GPU
  - Typically cropped to square images
  - Filters are also typically square



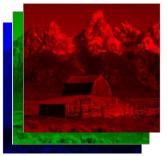


K<sub>1</sub> total filters Filter size:  $L \times L \times 3$ 









 $I \times I$  image

- Input is convolved with a set of K₁ filters
  - Typically  $K_1$  is a power of 2, e.g. 2, 4, 8, 16, 32,...
  - Filters are typically 5x5, 3x3, or even 1x1



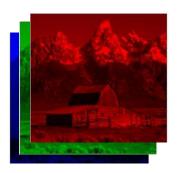


K<sub>1</sub> total filters

Filter size:  $L \times L \times 3$ 







 $I \times I$  image

Small enough to capture fine features (particularly important for scaled-down images)

- Input is convolved with a set of K<sub>1</sub> filters
  - Typically  $K_1$  is a power 4, e.g. 2, 4, 8, 16, 32,...
  - Filters are typically 5x5, 3x3, or even 1x1





K₁ total filters

Filter size:  $L \times L \times 3$ 







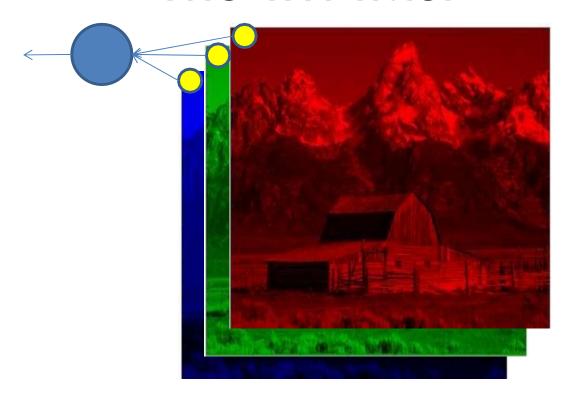
 $I \times I$  image

Small enough to capture fine features (particularly important for scaled-down images)



- Input is convolved with a set of K<sub>1</sub> filters
  - Typically  $K_1$  is a power 4, e.g. 2, 4, 8, 4, 32,...
  - Filters are typically 5x5, 3x3, or even 1x1

# The 1x1 filter



- A 1x1 filter is simply a perceptron that operates over the *depth* of the stack of maps, but has no spatial extent
  - Takes one pixel from each of the maps (at a given location) as input



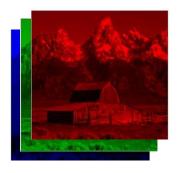


K<sub>1</sub> total filters





Filter size:  $L \times L \times 3$ 

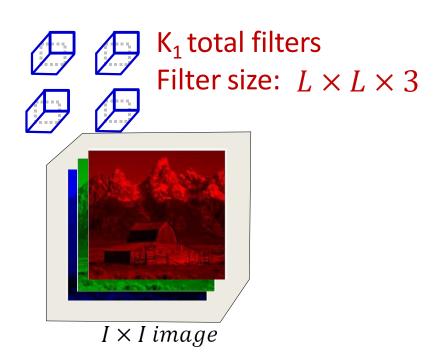


 $I \times I$  image

#### Parameters to choose: $K_1$ , L and S

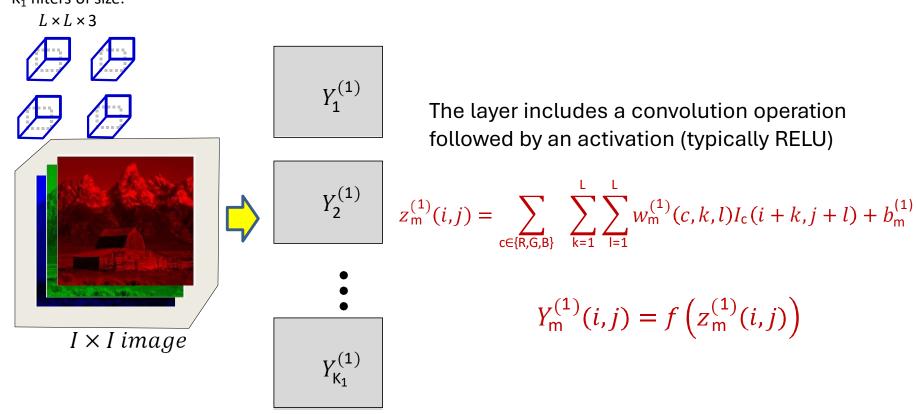
- 1. Number of filters  $K_1$
- 2. Size of filters  $L \times L \times 3 + bias$
- 3. Stride of convolution S

- Input is convolved with a set of K<sub>1</sub> filters
  - Typically  $K_1$  is a power of 2, e.g. 2, 4, 8, 16, 32,...
  - Filters are typically 5x5(x3), 3x3(x3), or even 1x1(x3)
  - Typical stride: 1 or 2



 The input may be zero-padded according to the size of the chosen filters

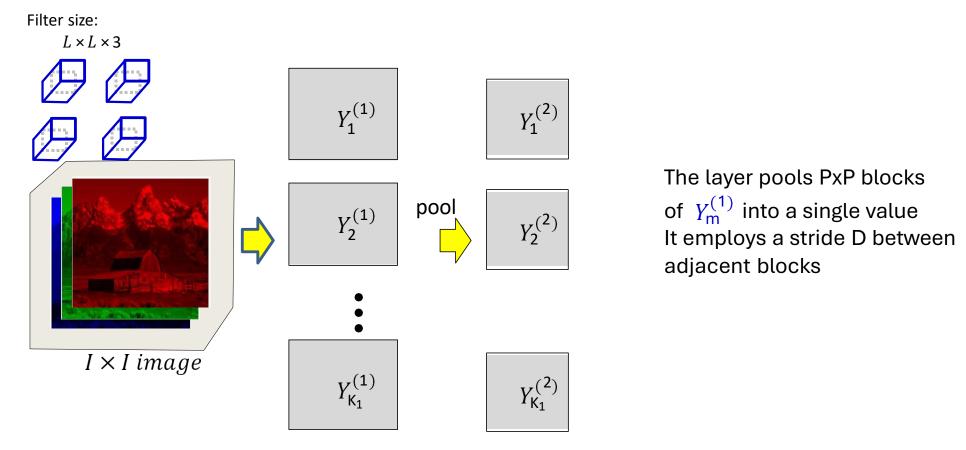
K<sub>1</sub> filters of size:



- First convolutional layer: Several convolutional filters
  - Filters are "3-D" (third dimension is color)
  - Convolution followed typically by a RELU activation
- Each filter creates a single 2-D output map

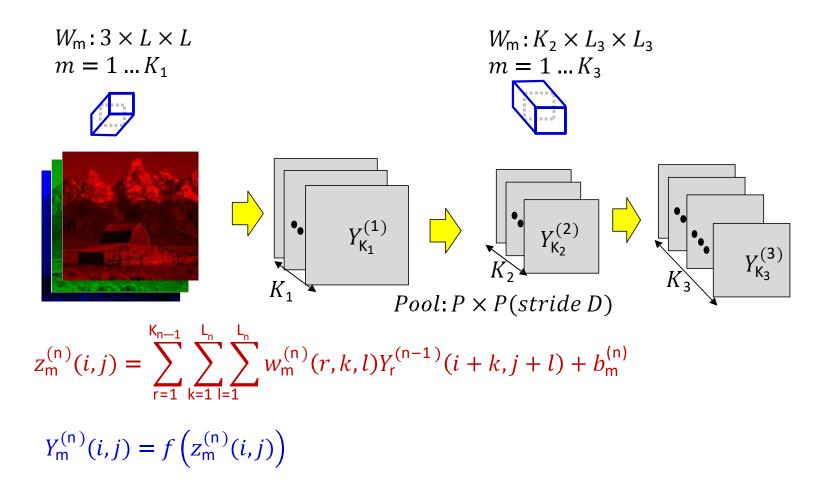
# Learnable parameters in the first convolutional layer

- The first convolutional layer comprises  $K_1$  filters, each of size  $L \times L \times 3$ 
  - Spatial span:  $L \times L$
  - Depth : 3 (3 colors)
- This represents a total of  $K_1(3L^2+1)$  parameters
  - "+ 1" because each filter also has a bias
- All of these parameters must be learned

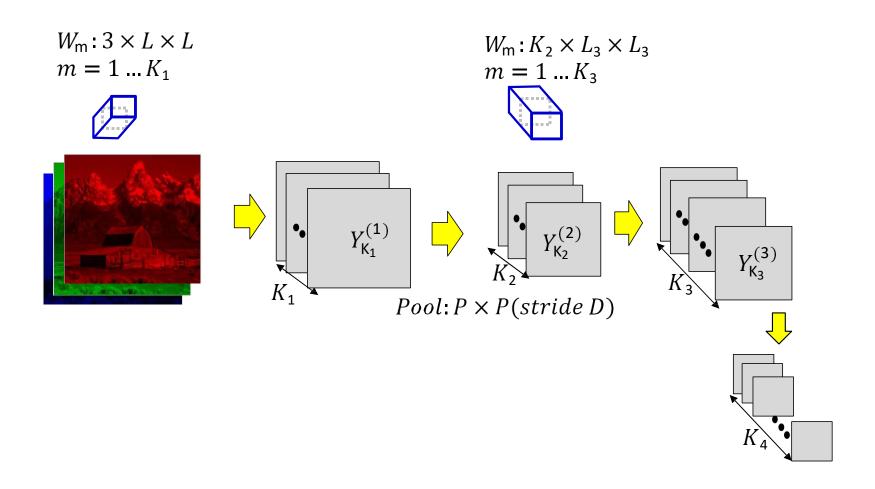


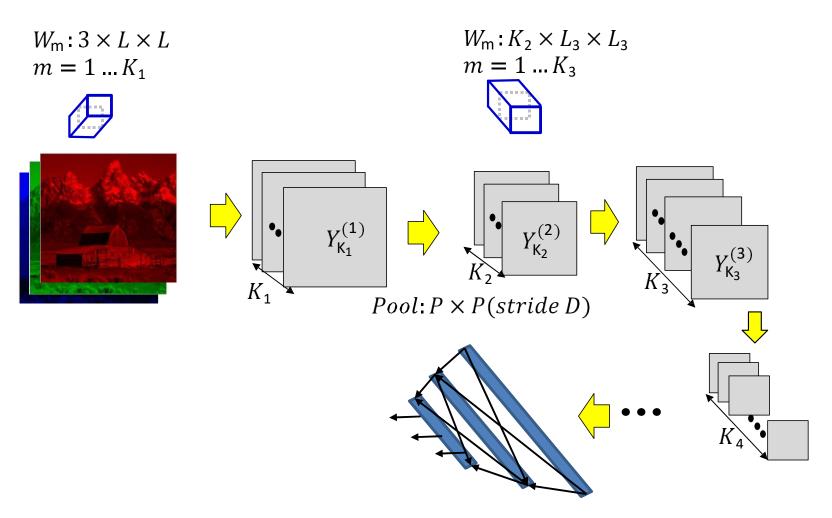
First pooling/downsampling layer: From each  $P \times P$  block of each map, pool down to a single value

 For max pooling, during training keep track of which position had the highest value



• Second convolutional layer:  $K_3$  3-D filters resulting in  $K_3$  2-D maps





- This continues for several layers until the final convolved output is fed to a softmax
  - Or a full MLP

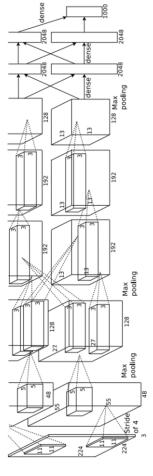
# The Size of the Layers

- Each convolution layer with stride 1 typically maintains the size of the image
  - With appropriate zero padding
  - If performed without zero padding it will decrease the size of the input
- Each convolution layer will generally increase the number of maps from the previous layer
  - In general, the number of convolutional filters increases with layers
- Each pooling layer with stride D decreases the size of the maps by a factor of D
- Filters within a layer must all be the same size, but sizes may vary with layer
  - Similarly for pooling

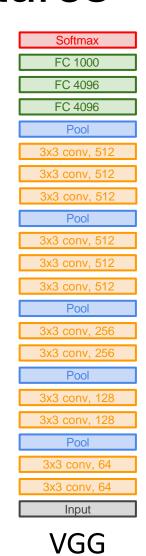
# Parameters to choose (design choices)

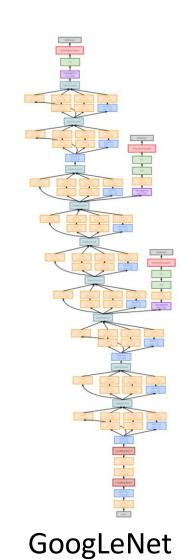
- Number of convolutional and downsampling layers
  - And arrangement (order in which they follow one another)
- For each convolution layer:
  - Number of filters  $K_i$
  - Spatial extent of filter  $L_i \times L_i$ 
    - The "depth" of the filter is fixed by the number of filters in the previous layer  $K_{i-1}$
  - The stride  $S_i$
- For each downsampling/pooling layer:
  - Spatial extent of filter  $P_i \times P_i$
  - The stride  $D_i$
- For the final MLP:
  - Number of layers, and number of neurons in each layer

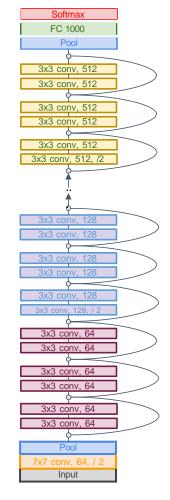
# **CNN** Architectures



AlexNet

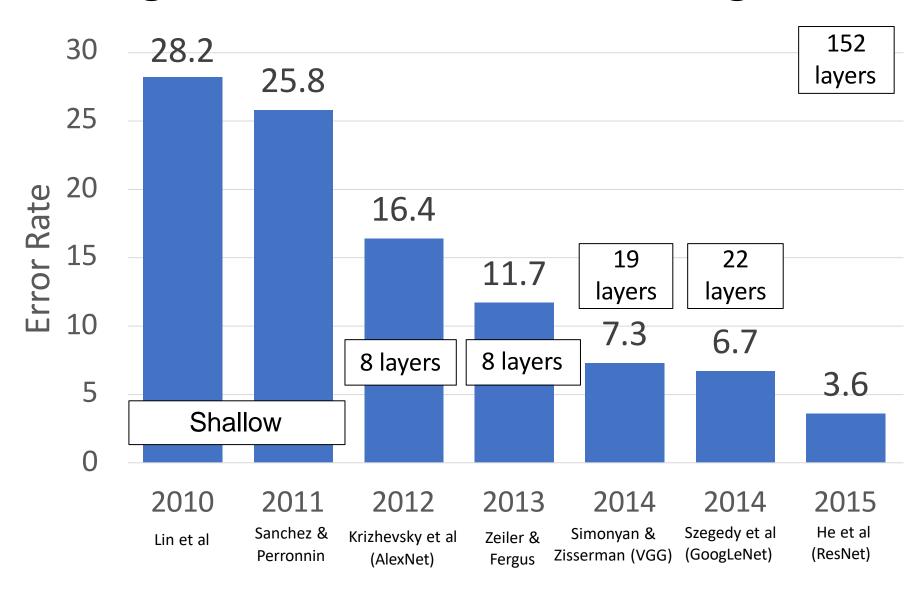




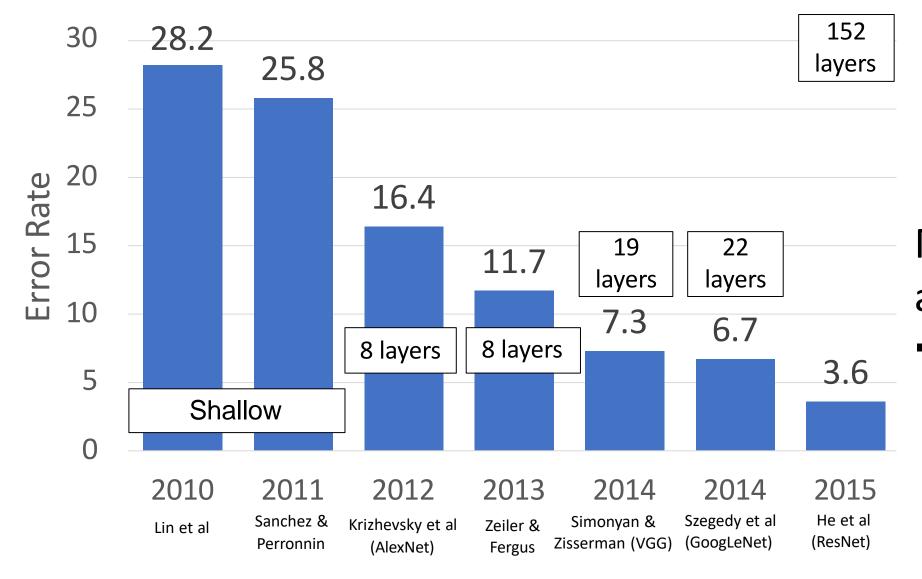


ResNet

# ImageNet Classification Challenge



# ImageNet Classification Challenge

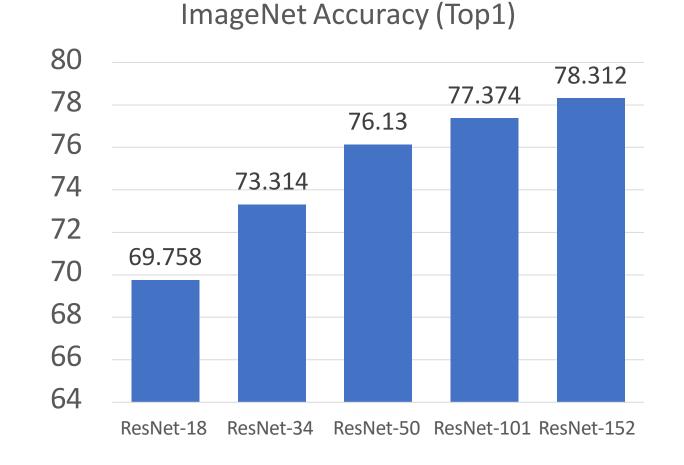


More recent CNN architectures

#### Post-ResNet Architectures

ResNet made it possible to increase accuracy with larger, deeper models

Many followup architectures emphasize efficiency: can we improve accuracy while controlling for model "complexity"?



FC 1000 Pool

3x3 conv, 512

3x3 conv. 64

# Measures of Model Complexity

**Parameters**: How many learnable parameters does the model have?

**Floating Point Operations (FLOPs)**: How many arithmetic operations does it take to compute the forward pass of the model?

Watch out, lots of subtlety here:

- Many papers only count operations in conv layers (ignore ReLU, pooling, BatchNorm)
- Most papers use "1 FLOP" = "1 multiply and 1 addition" so dot product of two N-dim vectors takes N FLOPs
- Other sources (e.g. NVIDIA marketing material) count "1 multiply and one addition" = 2
   FLOPs, so dot product of two N-dim vectors takes 2N FLOPs

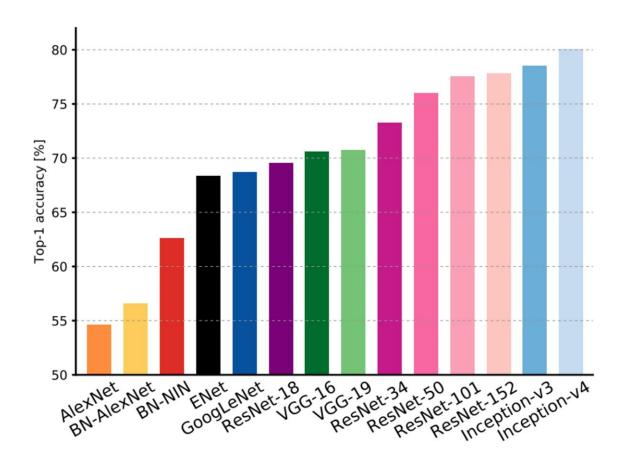
**Network Runtime**: How long does a forward pass of the model take on real hardware?

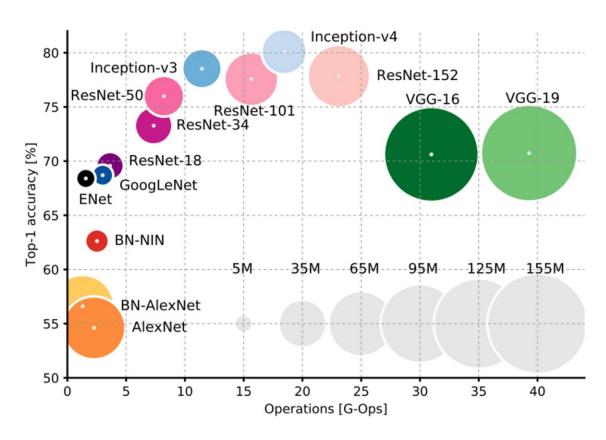
#### **Standard Convolution**

- Standard Convolution (groups=1)
- All convolutional kernels touch all C<sub>in</sub> channels of the input
- Input: C<sub>in</sub> x H x W
- Weight: C<sub>out</sub> x C<sub>in</sub> x K x K
- Output: C<sub>out</sub> x H' x W'

- Define: 1 FLOP" = "1 multiply and 1 addition
- For each output element,
   FLOP = C<sub>in</sub> x K x K
- In total, the number of output elements is C<sub>out</sub> x H' x W'
- Hence, the total FLOPS is CoutCinK<sup>2</sup>H'W'

# **Comparing Complexity**

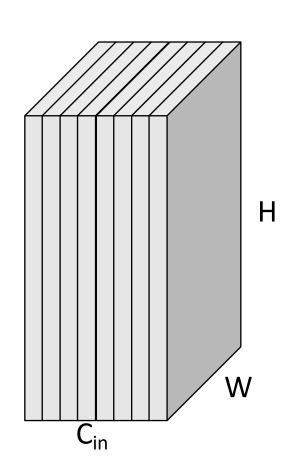


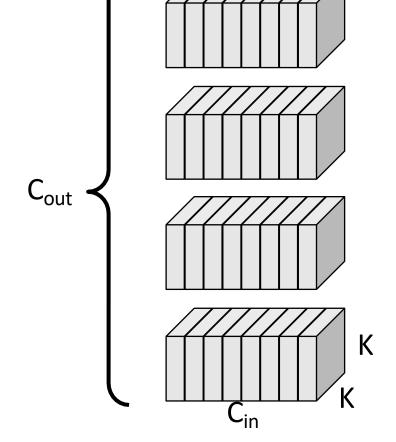


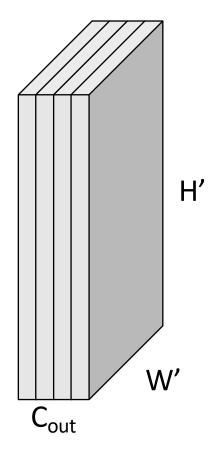
Key ingredient: Grouped / Separable convolution

# **Convolution Layer**

Each filter has the same number of channels as the input







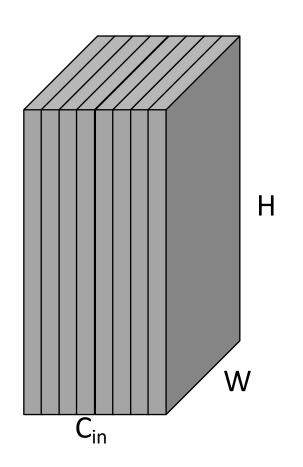
Input: C<sub>in</sub> x H x W

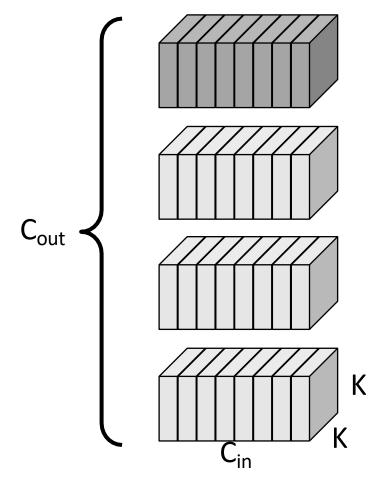
Weights: C<sub>out</sub> x C<sub>in</sub> x K x K

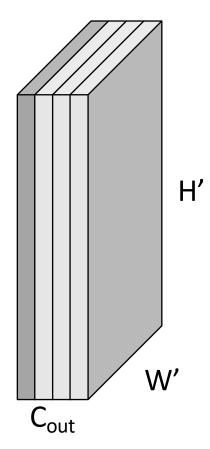
Output: C<sub>out</sub> x H' x W'

Each filter has the same number of channels as the input

Each plane of the output depends on the full input and one filter







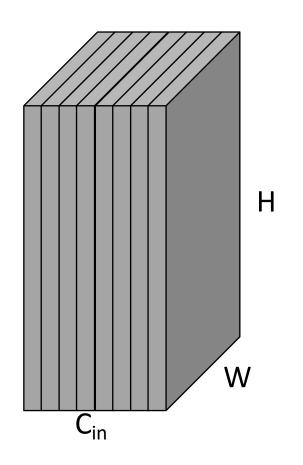
Input: C<sub>in</sub> x H x W

Weights: C<sub>out</sub> x C<sub>in</sub> x K x K

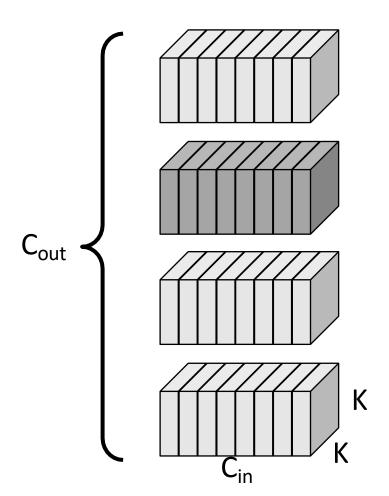
Output: Cout x H' x W'

Each filter has the same number of channels as the input

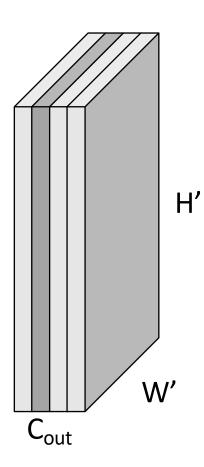
Each plane of the output depends on the full input and one filter







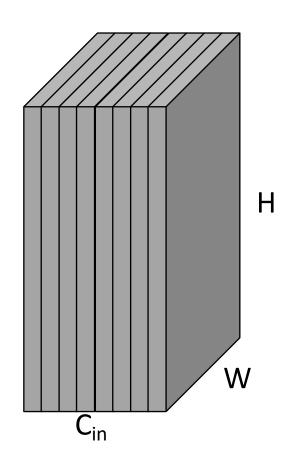
Weights: C<sub>out</sub> x C<sub>in</sub> x K x K



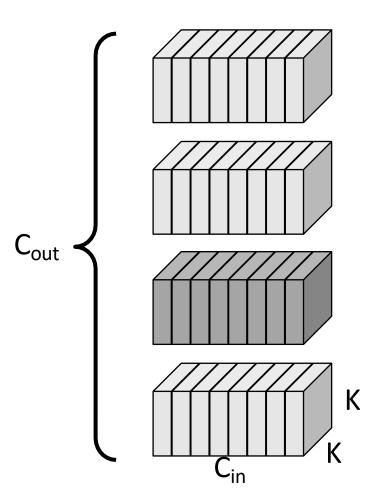
Output: Cout x H' x W'

Each filter has the same number of channels as the input

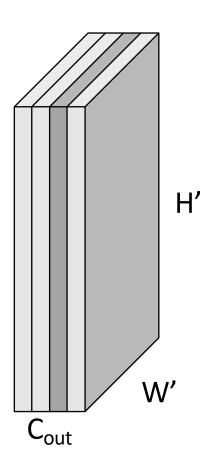
Each plane of the output depends on the full input and one filter







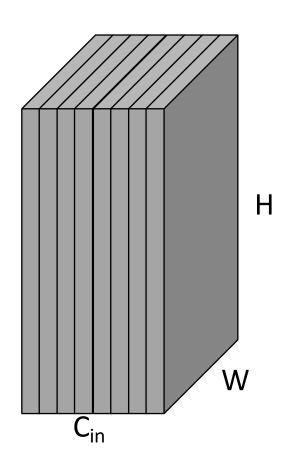
Weights: C<sub>out</sub> x C<sub>in</sub> x K x K



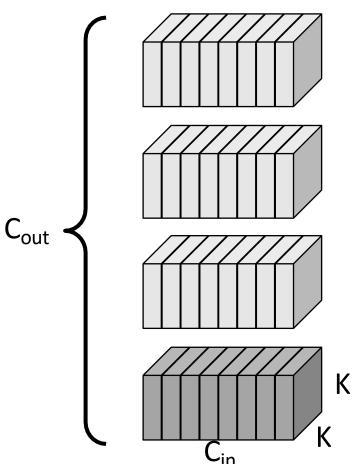
Output: Cout x H' x W'

Each filter has the same number of channels as the input

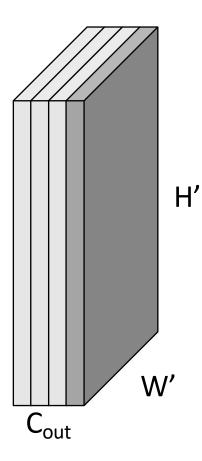
Each plane of the output depends on the full input and one filter



Input: C<sub>in</sub> x H x W

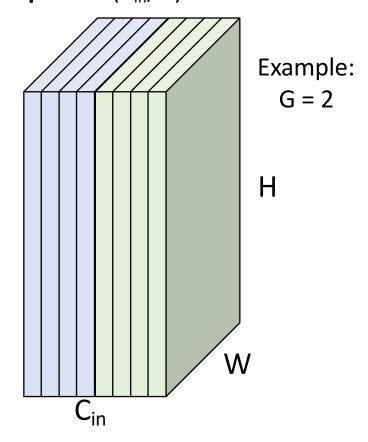


Weights: C<sub>out</sub> x C<sub>in</sub> x K x K



Output: C<sub>out</sub> x H' x W'

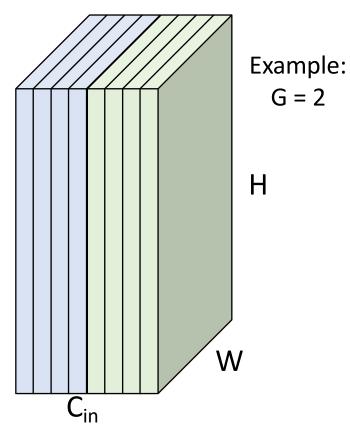
Divide channels of input into G groups with (C<sub>in</sub>/G) channels each



Input: C<sub>in</sub> x H x W

Divide filters into G groups; each group looks at a **subset** of input channels

Divide channels of input into G groups with (C<sub>in</sub>/G) channels each



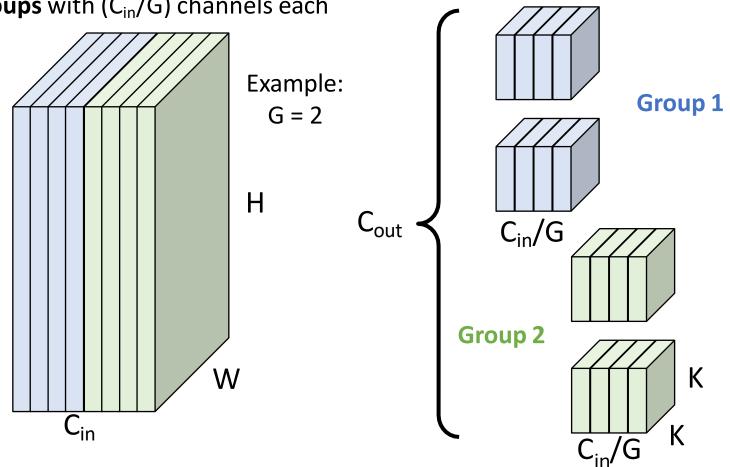
**Group 1** Cout C<sub>in</sub>/G **Group 2** K

Input: C<sub>in</sub> x H x W

Weights:  $C_{out} \times (C_{in}/G) \times K \times K$ 

Divide filters into G groups; each group looks at a **subset** of input channels Each plane of the output depends on one filter and a **subset** of the input channels

Divide channels of input into G groups with (C<sub>in</sub>/G) channels each



H' W'

Input: C<sub>in</sub> x H x W

Weights:  $C_{out} \times (C_{in}/G) \times K \times K$ 

Output: C<sub>out</sub> x H' x W'

Divide filters into G groups; each group looks at a **subset** of input channels Each plane of the output depends on one filter and a **subset** of the input channels

Divide channels of input into G groups with (C<sub>in</sub>/G) channels each

Example: **Group 1** G = 2H  $C_{out}$ C<sub>in</sub>/G **Group 2** K W

H' W'

Input: C<sub>in</sub> x H x W

Weights:  $C_{out} \times (C_{in}/G) \times K \times K$ 

Output: C<sub>out</sub> x H' x W'

Divide filters into G groups; each group looks at a **subset** of input channels Each plane of the output depends on one filter and a **subset** of the input channels

Divide channels of input into G groups with (C<sub>in</sub>/G) channels each

Example: **Group 1** G = 2H  $C_{out}$ C<sub>in</sub>/G **Group 2** K W

H' W'

Input: C<sub>in</sub> x H x W

Weights:  $C_{out} \times (C_{in}/G) \times K \times K$ 

Output: Cout x H' x W'

Divide filters into G groups; each group looks at a **subset** of input channels Each plane of the output depends on one filter and a **subset** of the input channels

Divide channels of input into G groups with (C<sub>in</sub>/G) channels each

Example: **Group 1** G = 2H  $C_{out}$ C<sub>in</sub>/G **Group 2** K W

H' W'  $C_{out}$ 

Input: C<sub>in</sub> x H x W

Weights:  $C_{out} \times (C_{in}/G) \times K \times K$ 

Output: C<sub>out</sub> x H' x W'

Divide filters into G groups; each group looks at a **subset** of input channels

Each plane of the output depends on one filter and a **subset** of the input channels

Divide channels of input into G groups with (C<sub>in</sub>/G) channels each

Example: G = 2H

Input: C<sub>in</sub> x H x W

**Group 1**  $C_{out}$ C<sub>in</sub>/G **Group 2** K

Weights:  $C_{out} \times (C_{in}/G) \times K \times K$ 

H' W' Cout

Output: Cout x H' x W'

Divide filters into G groups; each group looks at a **subset** of input channels

**Group 1** 

**Group 2** 

Each plane of the output depends on one filter and a **subset** of the input channels

Divide channels of input into G groups with (C<sub>in</sub>/G) channels each

H

Input: C<sub>in</sub> x H x W

Example:
G = 4

H C<sub>out</sub>

Group 3

Group 4

k

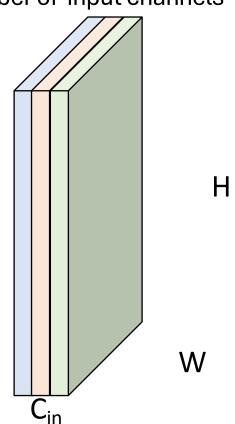
Weights:  $C_{out} \times (C_{in}/G) \times K \times K$ 

H' W'

Output: Cout x H' x W'

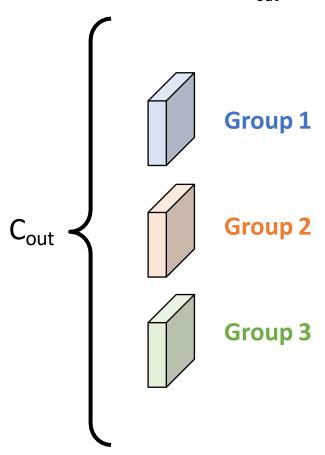
# Special Case: Depthwise Convolution

Number of groups equals number of input channels



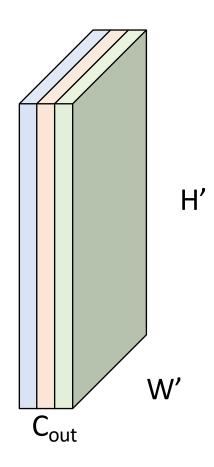
Input: C<sub>in</sub> x H x W

Common to also set  $C_{out} = G$ 



Weights: C<sub>out</sub> x 1 x K x K

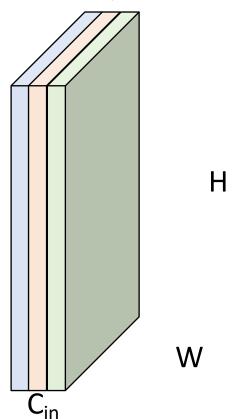
Output only mixes *spatial* information from input; *channel* information not mixed



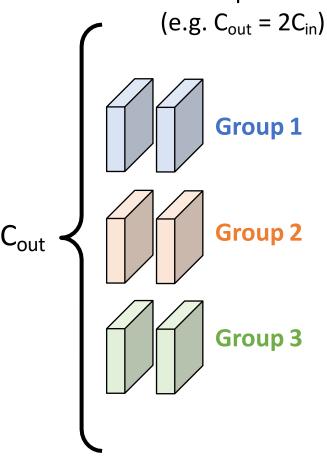
Output: C<sub>out</sub> x H' x W'

### Special Case: Depthwise Convolution

Number of groups equals number of input channels

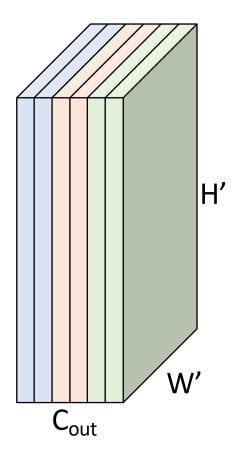


Can still have multiple filters per group



Input: C<sub>in</sub> x H x W Weights: C<sub>out</sub> x 1 x K x K

Output only mixes *spatial* information from input; *channel* information not mixed



Output: Cout x H' x W'

#### **Grouped Convolution vs Standard Convolution**

#### **Grouped Convolution (G groups):**

G parallel conv layers; each "sees"  $C_{in}/G$  input channels and produces  $C_{out}/G$  output channels

Input: C<sub>in</sub> x H x W

Split to  $G \times [(C_{in}/G) \times H \times W]$ 

Weight:  $G \times (C_{out} / G) \times (C_{in} \times G) \times K \times K$ 

G parallel convolutions

Output:  $G \times [(C_{out}/G) \times H' \times W']$ 

Concat to Cout x H' x W'

FLOPs: CoutCinK2H'W'/G

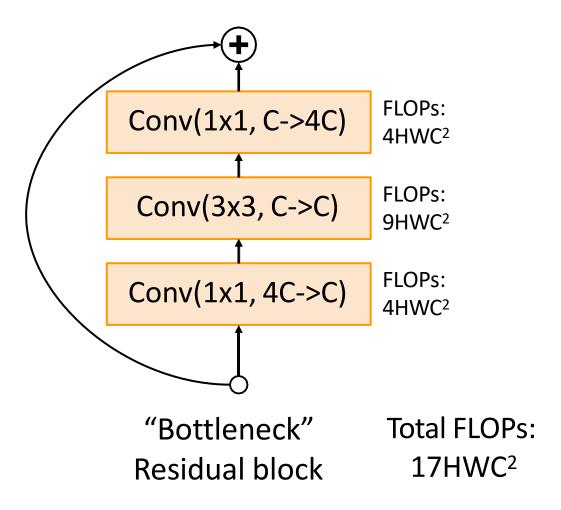
- Standard Convolution (groups=1)
- All convolutional kernels touch all C<sub>in</sub> channels of the input
- Input: C<sub>in</sub> x H x W
- Weight: C<sub>out</sub> x C<sub>in</sub> x K x K
- Output: C<sub>out</sub> x H' x W'
- FLOPs: C<sub>out</sub>C<sub>in</sub>K<sup>2</sup>H'W'

#### **Grouped Convolution in PyTorch**

PyTorch convolution gives an option for groups!

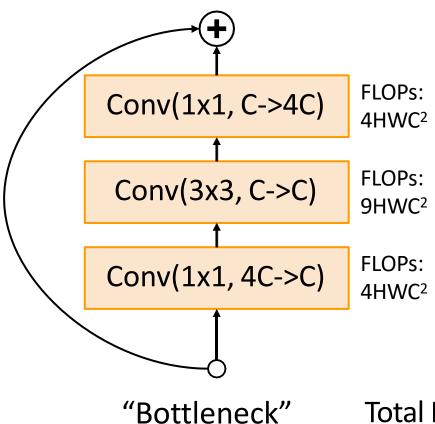
#### Conv2d

#### Improving ResNets

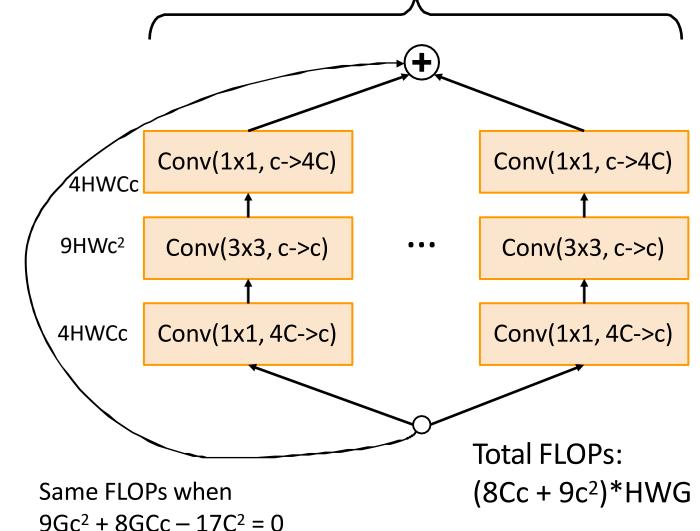


Improving ResNets: ResNeXt

G parallel pathways



Total FLOPs: 17HWC<sup>2</sup>

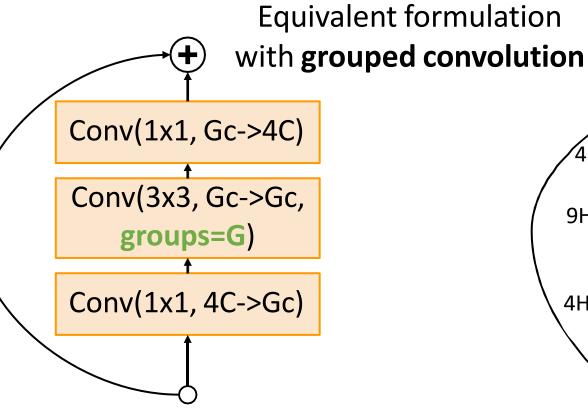


Example: C=64, G=4, c=24; C=64, G=32, c=4

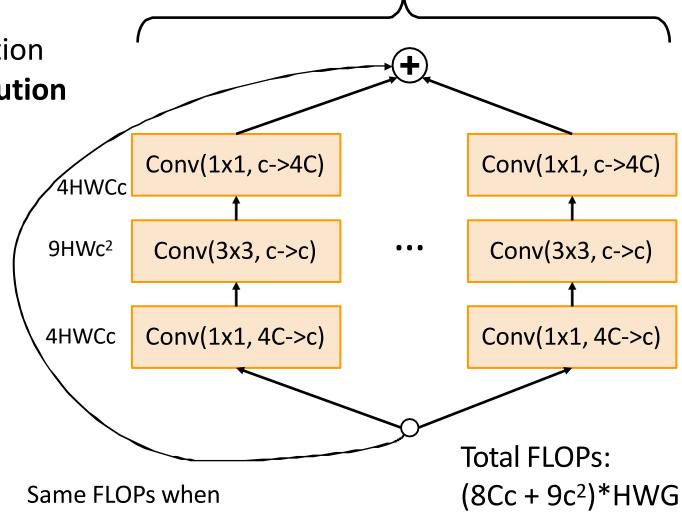
Residual block

## Improving ResNets: ResNeXt

G parallel pathways



ResNeXt block: Grouped convolution



Example: C=64, G=4, c=24; C=64, G=32, c=4

 $9Gc^2 + 8GCc - 17C^2 = 0$ 

# ResNeXt: Maintain computation by adding groups!

Model	Groups	Group width	Top-1 Error
ResNet-50	1	64	23.9
ResNeXt-50	2	40	23
ResNeXt-50	4	24	22.6
ResNeXt-50	8	14	22.3
ResNeXt-50	32	4	22.2

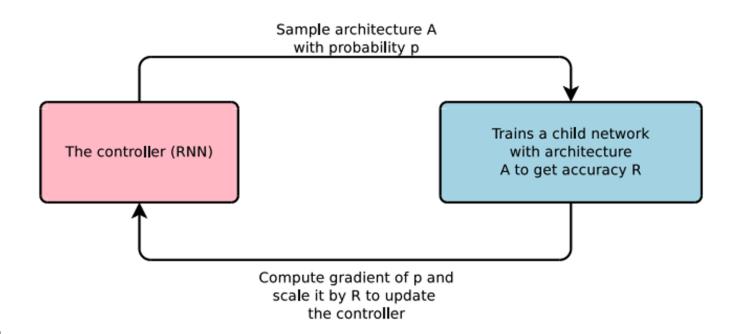
Model	Groups	<b>Group width</b>	Top-1 Error
ResNet-101	1	64	22.0
ResNeXt-101	2	40	21.7
ResNeXt-101	4	24	21.4
ResNeXt-101	8	14	21.3
ResNeXt-101	32	4	21.2

Adding groups improves performance with same FLOPs!

Often denoted e.g. ResNeXt-50-32x4d: 32 groups, Blocks in first stage have 4 channels per group (#channels still doubles at each stage)

Designing neural network architectures is hard – let's automate it!

- One network (controller) outputs network architectures
- Sample child networks from controller and train them
- After training a batch of child networks, make a gradient step on controller network (Using policy gradient)
- Over time, controller learns to output good architectures!

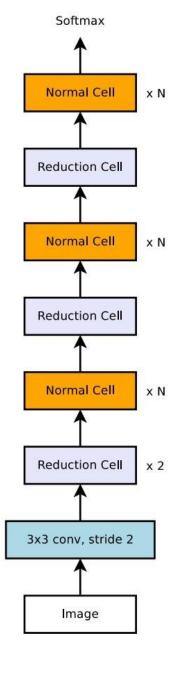


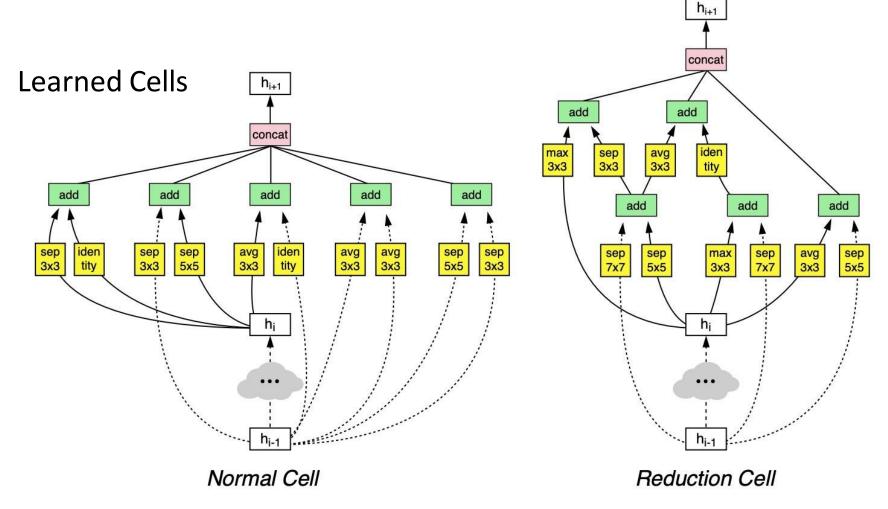
- Search for reusable "block" designs which can use the following operators:
- Identity
- 1x1 conv
- 3x3 conv
- 3x3 dilated conv
- 1x7 then 7x1 conv
- 1x3 then 3x1 conv
- 3x3, 5x5, or 7x7 depthwiseseparable conv
- 3x3 avg pool
- 3x3, 5x5, or 7x7 max pool

The "Normal cell" maintains the same image resolution

The "Reduction cell" reduces image resolution by 2x

Combine two learned cells in a regular pattern to create overall architecture

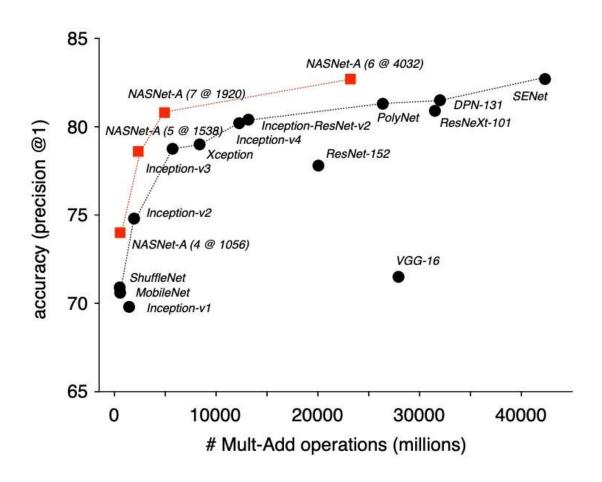


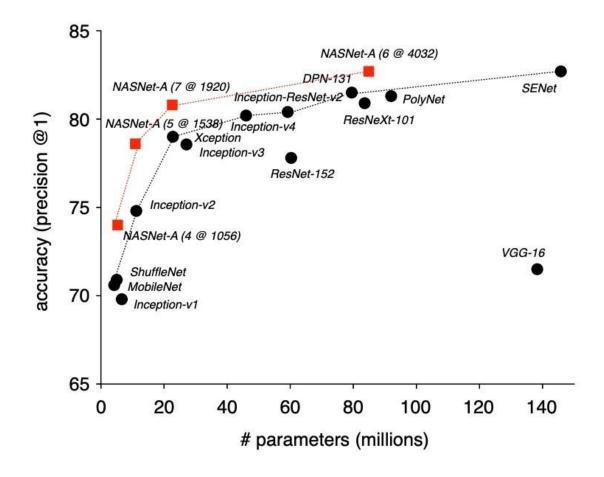


Normal Cell x N Reduction Cell Normal Cell x N Reduction Cell Normal Cell x N **Reduction Cell** 3x3 conv, stride 2 Image

Softmax

Zoph and Le, "Neural Architecture Search with Reinforcement Learning", ICLR 2017 Zoph et al, "Learning transferable architectures for scalable image recognition", CVPR 2018



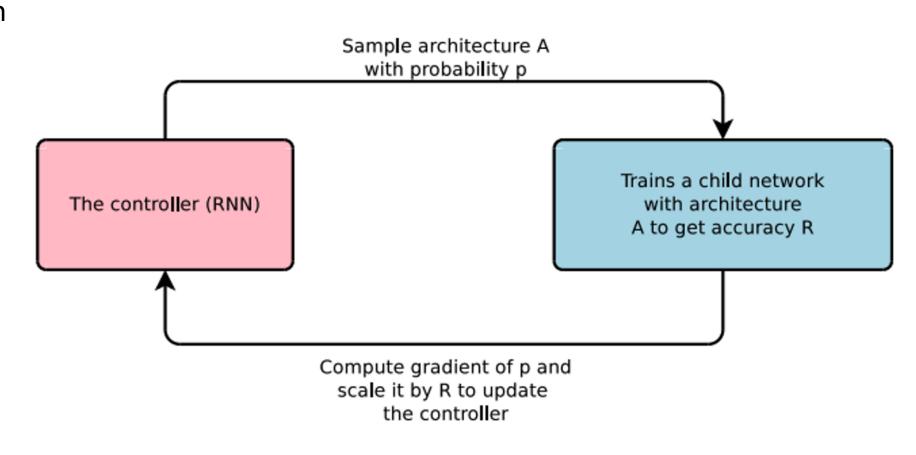


Zoph and Le, "Neural Architecture Search with Reinforcement Learning", ICLR 2017 Zoph et al, "Learning transferable architectures for scalable image recognition", CVPR 2018

# Big Problem: NAS is Very Expensive!

Original NAS paper: Each update to the controller requires training **800 child models** for 50 epochs on CIFAR10; Total of **12,800** child models are trained

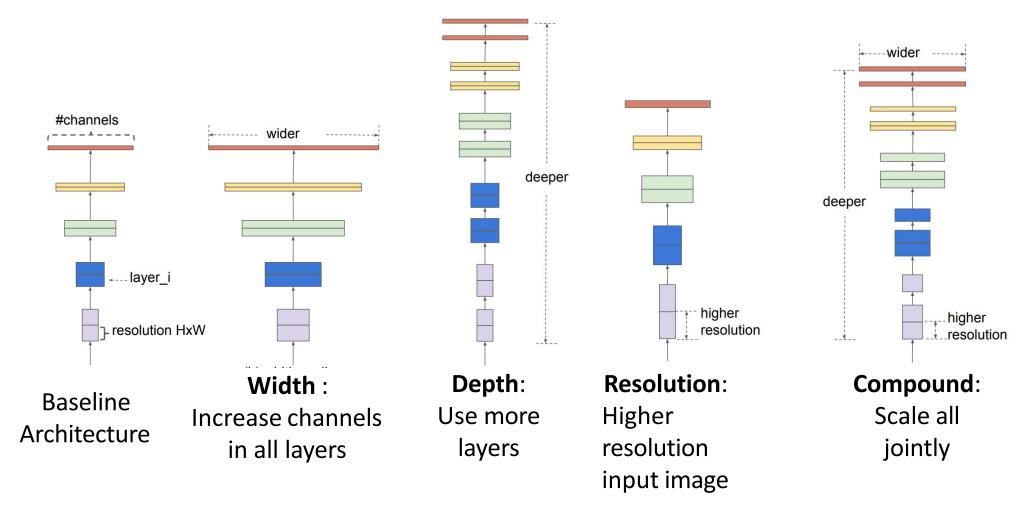
Later work improved efficiency, but still expensive



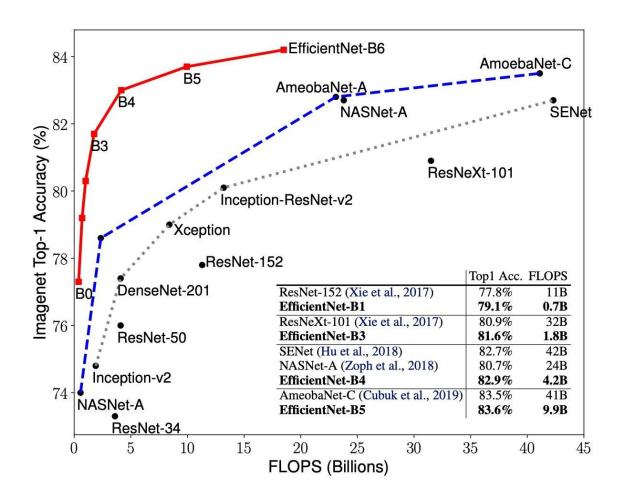
Zoph and Le, "Neural Architecture Search with Reinforcement Learning", ICLR 2017

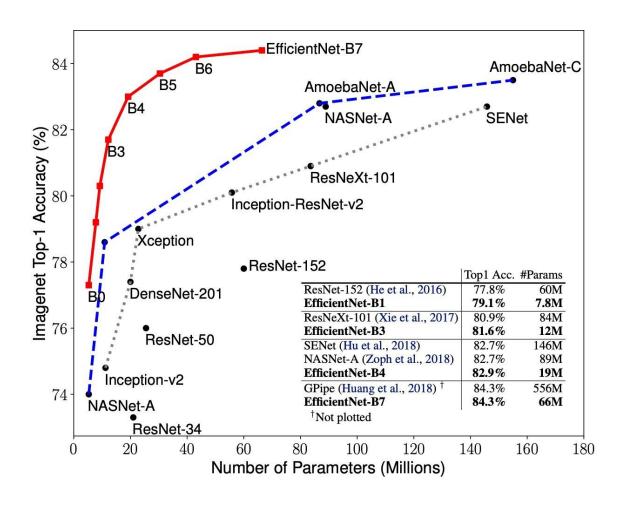
# Model Scaling

Starting from a given architecture, how should you scale it up to improve performance?

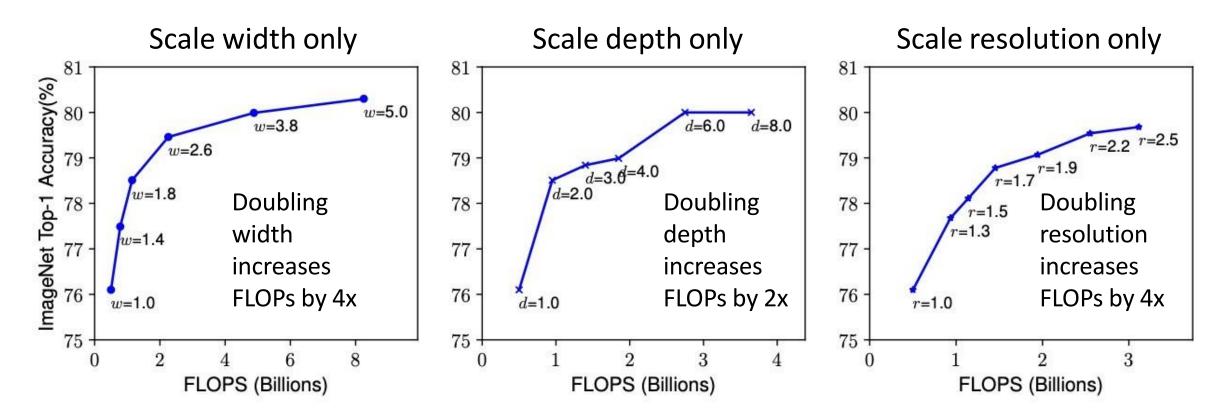


# Model Scaling: EfficientNets



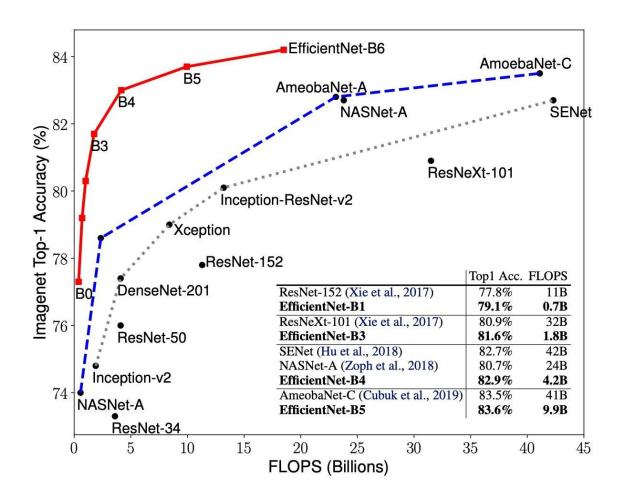


# Model Scaling: EfficientNets



Scaling any of width, depth, or resolution has diminishing returns. For optimal results, need to scale them all jointly!

# Model Scaling: EfficientNets



# **Big problem**: Real-world runtime does not correlate well with FLOPs!

- Runtime depends on the device (mobile CPU, server CPU, GPU, TPU); A model which is fast on one device may be slow on another
- Depthwise convolutions are efficient on mobile, but not on GPU / TPU – they become memory-bound
- The "naïve" FLOP counting we have done for convolutions can be incorrect alternate conv algorithms can reduce FLOPs in some settings (FFT for large kernels, Winograd for 3x3 conv)
- EfficientNet was designed to minimize FLOPs,
   not actual runtime so it is surprisingly slow!

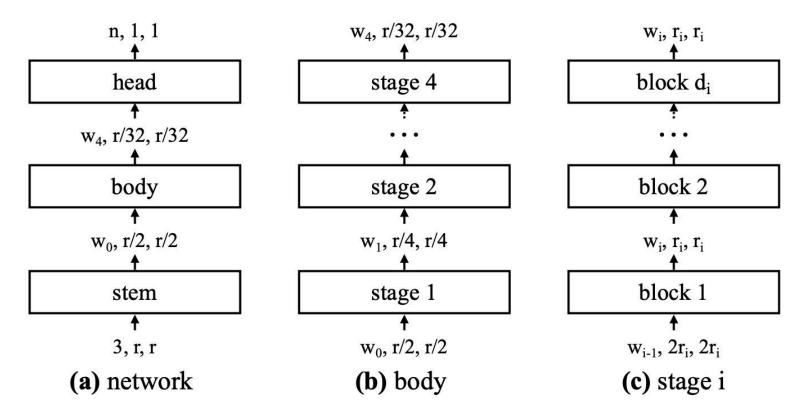
# Beyond NAS – back to hand-designed models!

Instead of using NAD smartly tweak ResNet-style models to improve performance, scaling, runtime on GPU / TPU

RegNets: Simple block design, optimize macro architecture and scaling

**NFNets:** Remove Batch Normalization

Network design is simple: **Stem** of 3x3 convs, a **body** of 4 *stages*, and a **head**; Each stage has multiple **blocks**: First block downsamples by 2x, others keep resolution the same

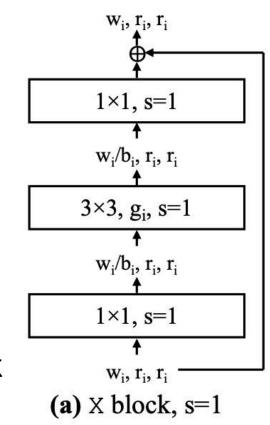


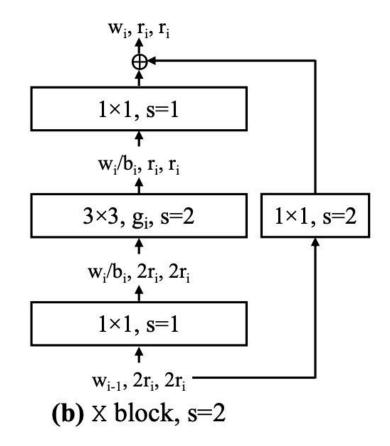
Radosavovic et al, "Designing Network Design Spaces", CVPR 2020 Dollar et al, "Fast and Accurate Model Scaling", CVPR 2021

Block design is simple, generalizes ResNext Each stage has 4 parameters:

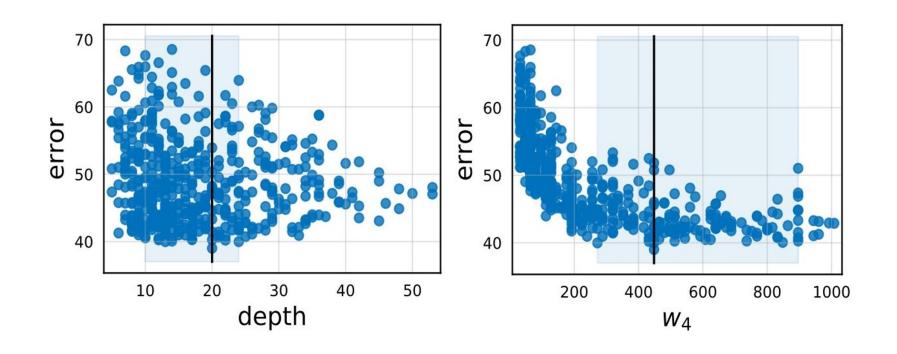
- Number of blocks
- Number of input channels w
- Bottleneck ratio b
- Group width g

The *design space* for the network has just 16 parameters





Randomly sample architectures from the design space, examine trends:

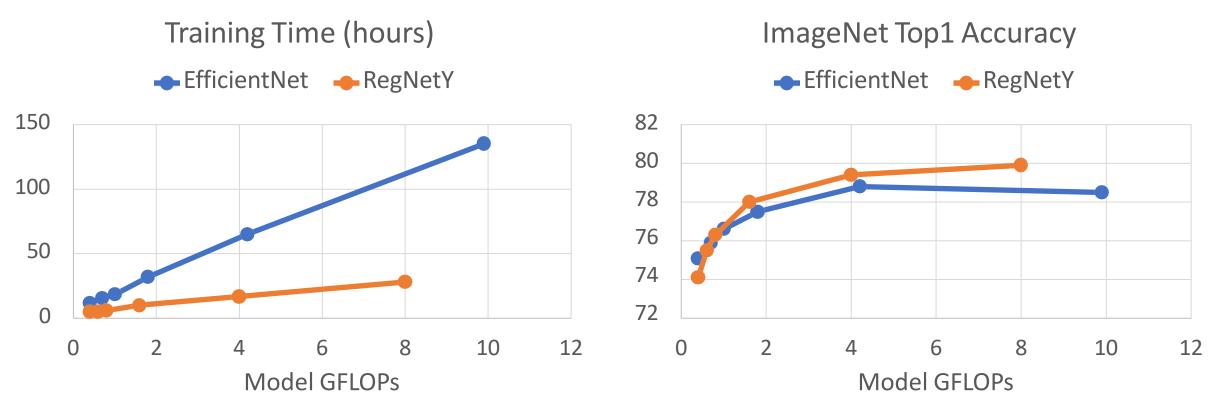


Use results to *refine* the design space: Reduce degrees of freedom from 16 to bias toward better-performing architectures:

- Share bottleneck ratio across all stages (16 -> 13 params)
- Share group width across all stages (13 -> 10 params)
- Force width, blocks per stage to increase linearly across stages

#### Final design space has 6 parameters:

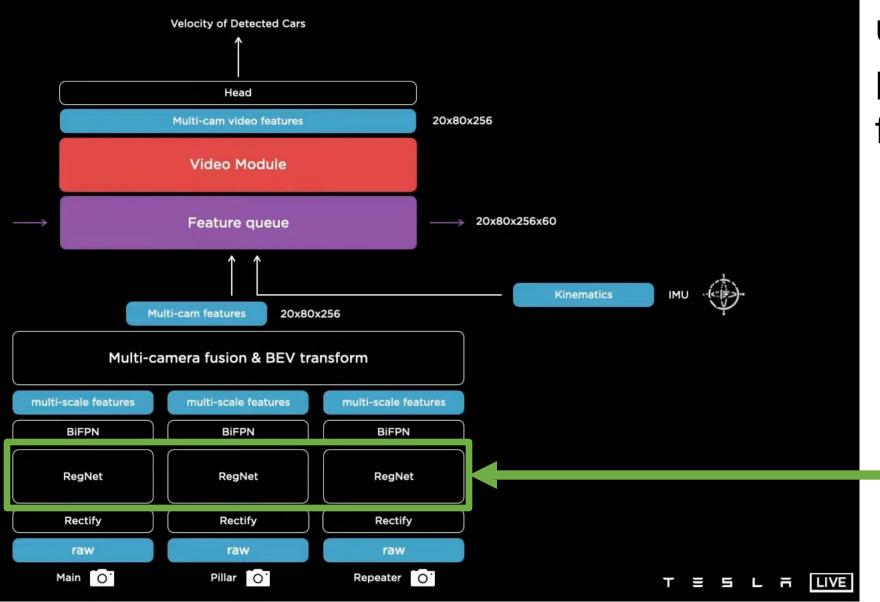
- Overall depth d, bottleneck ratio b, group width g
- Initial width  $w_0$ , width growth rate  $w_a$ , blocks per stage  $w_m$



At same FLOPs, RegNet models get similar accuracy as EfficientNets but are up to 5x faster in training (each iteration is faster)

Radosavovic et al, "Designing Network Design Spaces", CVPR 2020 Dollar et al, "Fast and Accurate Model Scaling", CVPR 2021

#### Video Neural Net Architecture



Tesla Vision system uses RegNets to process inputs from each camera

Tesla AI Day 2021, https://www.youtube.com/watch?v=j0z4FweCy4M

## Training ResNets without Batch Normalization

- Batch Normalization has good properties:
  - Makes it easy to train deep networks >= 10 layers
  - Makes learning rates, initialization less critical
  - Adds regularization
  - "Free" at inference: can be merged into linear layers
- But also has bad properties:
  - Doesn't work with small minibatches
  - Different behavior at train and test
  - Slow at training time

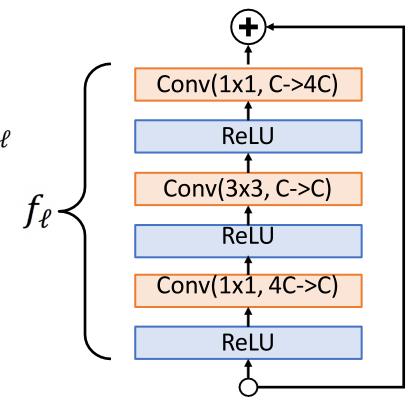
#### NFNets are ResNets without Batch Normalization!

#### **NFNets**

Consider a pre-activation ResNet block  $x_{\ell+1} = f_{\ell}(x_{\ell}) + x_{\ell}$ 

Problem: Variance grows with each block:

$$Var(x_{\ell+1}) = Var(x_{\ell}) + Var(f_{\ell}(x_{\ell}))$$



Brock et al, "Characterizing Signal Propagation to Close the Performance Gap in Unnormalized ResNets", ICLR 2021 Brock et al, "High-Performance Large-Scale Image Recognition without Normalization", ICML 2021 He et al, "Identity Mappings in Deep Residual Networks", ECCV 2016

#### NFNets: Scaled Residual Blocks

Consider a pre-activation ResNet block  $x_{\ell+1} = f_{\ell}(x_{\ell}) + x_{\ell}$ 

Problem: Variance grows with each block:

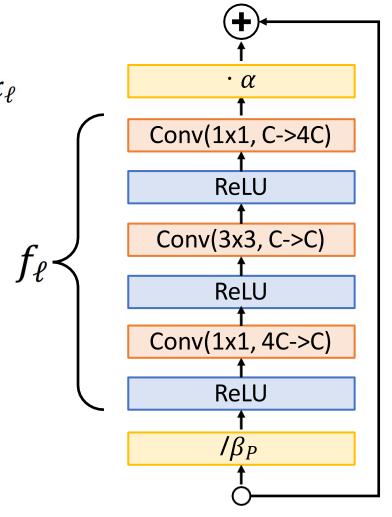
$$Var(x_{\ell+1}) = Var(x_{\ell}) + Var(f_{\ell}(x_{\ell}))$$

Solution: Re-parameterize block:

$$x_{\ell+1} = x_{\ell} + \alpha f_{\ell}(x_{\ell}/\beta_{\ell})$$

 $\alpha$  is a hyperparameter,  $\beta_{\ell} = \sqrt{Var(x_{\ell})}$  at initialization;

both are constants during training



#### NFNets: Scaled Residual Blocks

Consider a pre-activation ResNet block  $x_{\ell+1} = f_{\ell}(x_{\ell}) + x_{\ell}$ 

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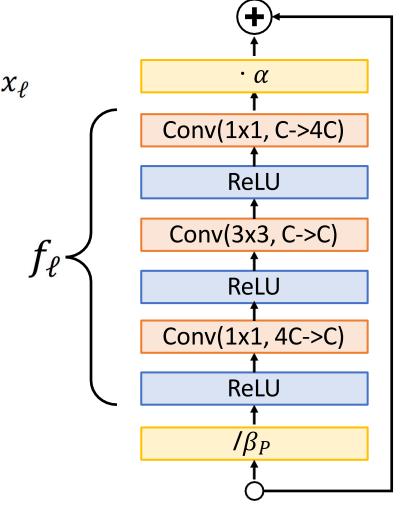
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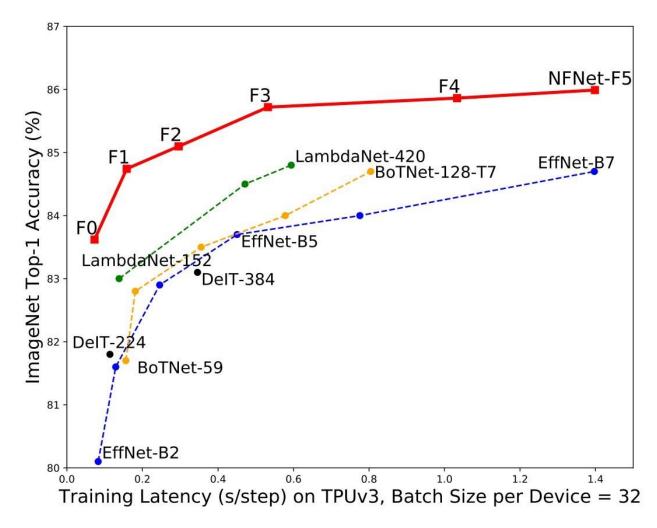
$$x_{\ell+1} = x_{\ell} + \alpha f_{\ell}(x_{\ell}/\beta_{\ell})$$

 $\alpha$  is a hyperparameter,  $\beta_\ell = \sqrt{Var(x_\ell)}$  at initialization; both are constants during training

Now  $Var(x_{\ell+1}) = Var(x_{\ell}) + \alpha^2$ ; resets to  $1 + \alpha^2$  after each downsampling block



#### **NFNets**



Brock et al, "Characterizing Signal Propagation to Close the Performance Gap in Unnormalized ResNets", ICLR 2021 Brock et al, "High-Performance Large-Scale Image Recognition without Normalization", ICML 2021

Always be careful with plots like this – different papers use different metric for x-axis:

- FLOPs
- Params
- Test-time runtime
- Training-time runtime
- Runtime on CPU / GPU / TPU /...