

{Learn, Create, Innovate};

Closed Loop Control

Mobile Robot Control

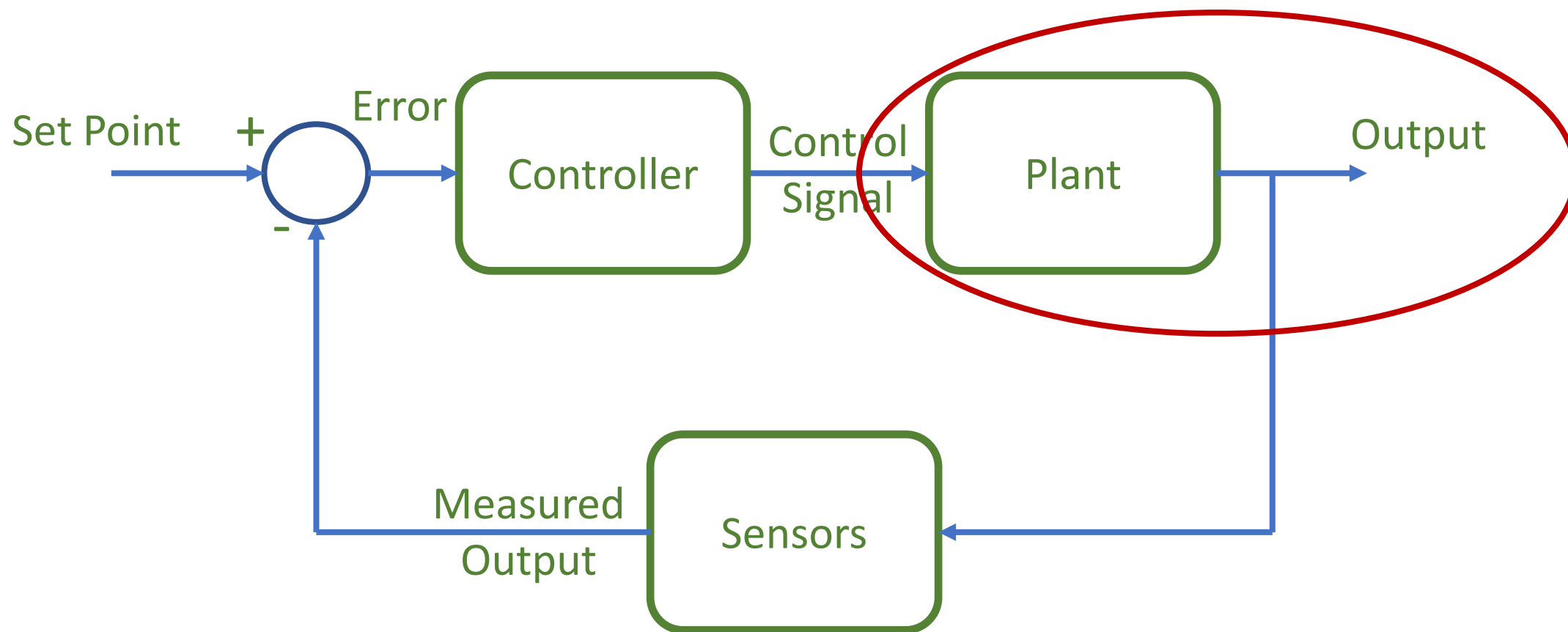




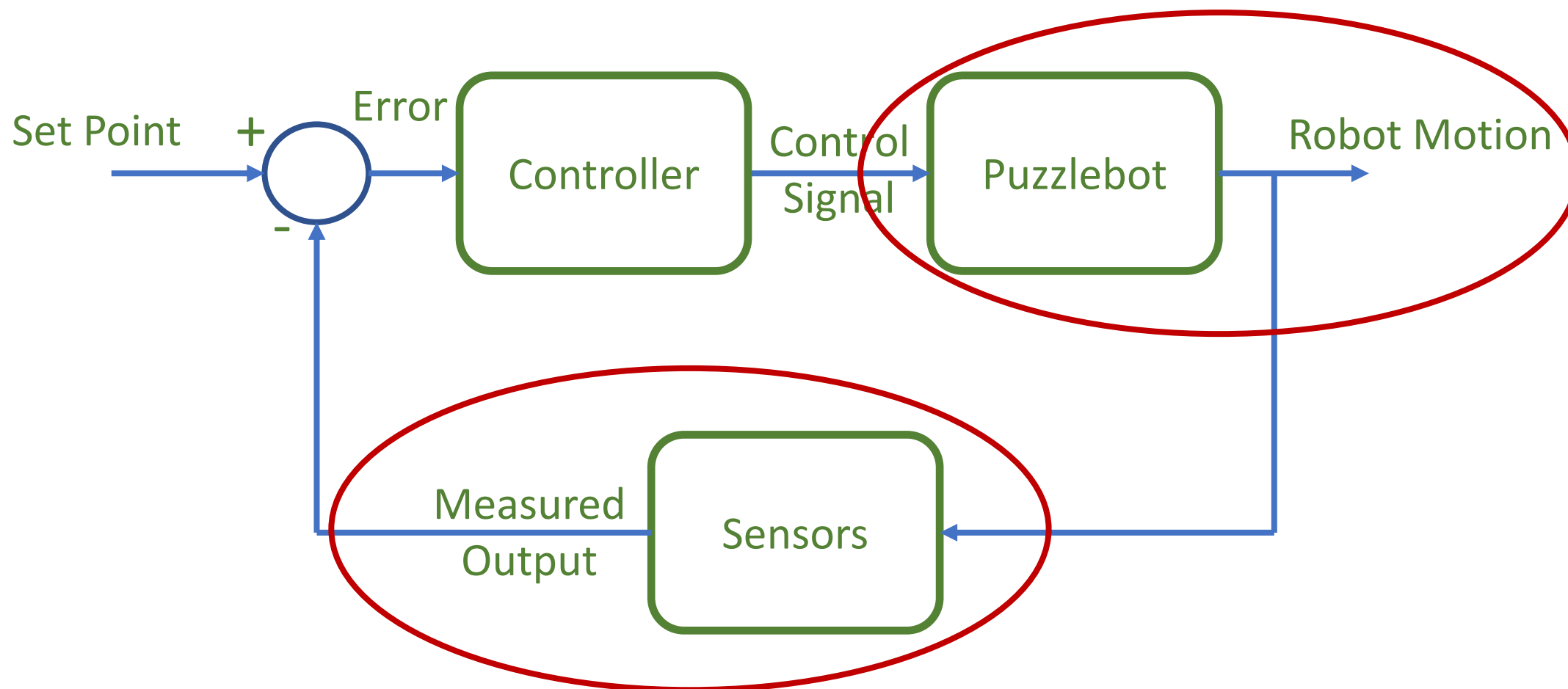
The Task



The Control System

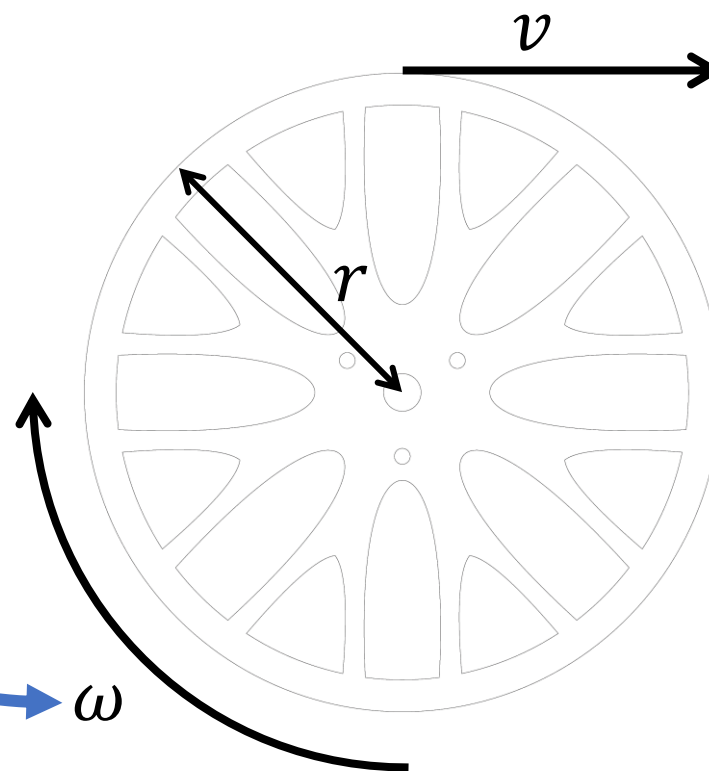


The Control System



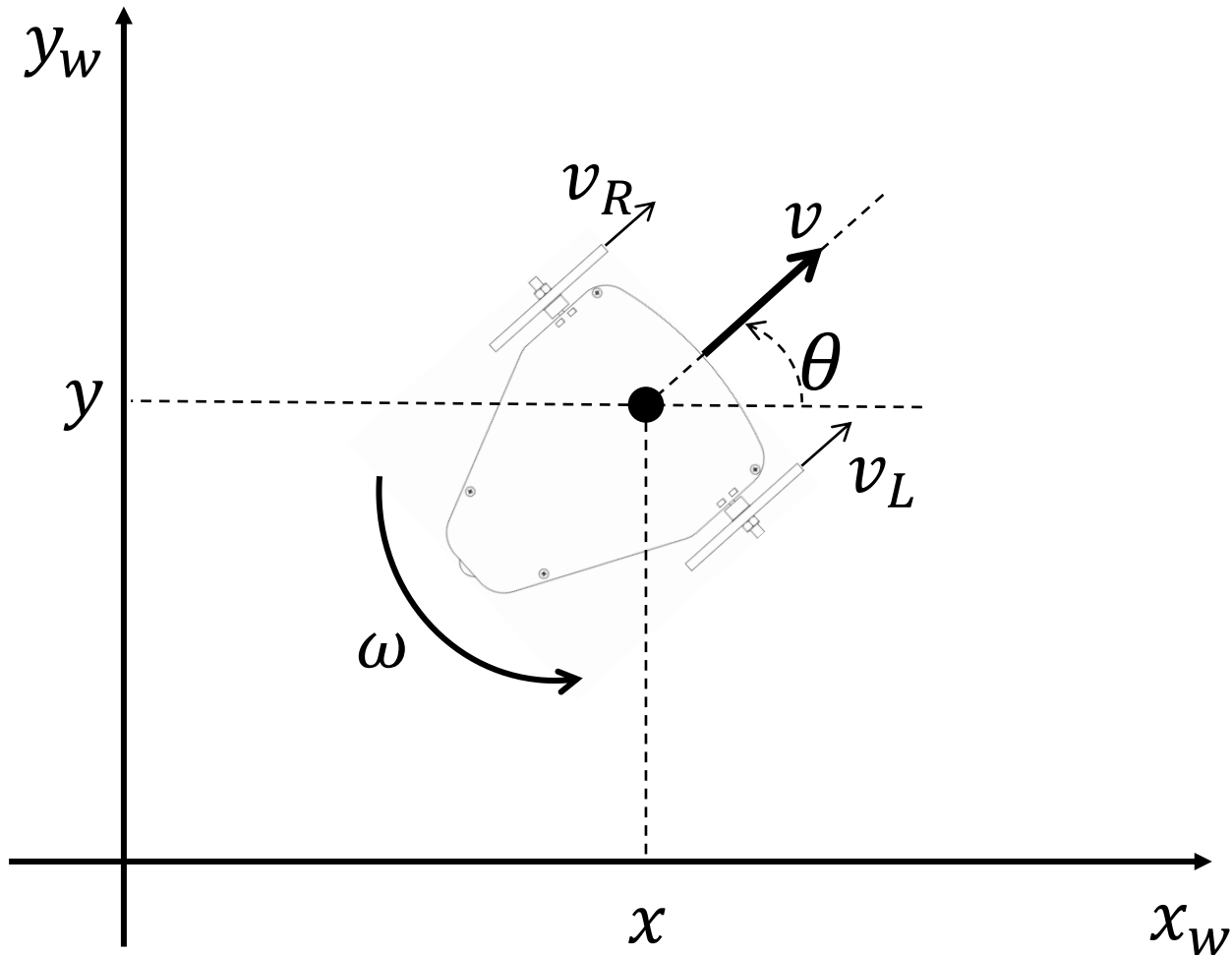
Determining the Robot Position

```
/cmd_vel  
/diagnostics  
/rosout  
/rosout_agg  
/wl  
/wr
```



$$v_{Wheel} = r\omega_{Wheel}$$

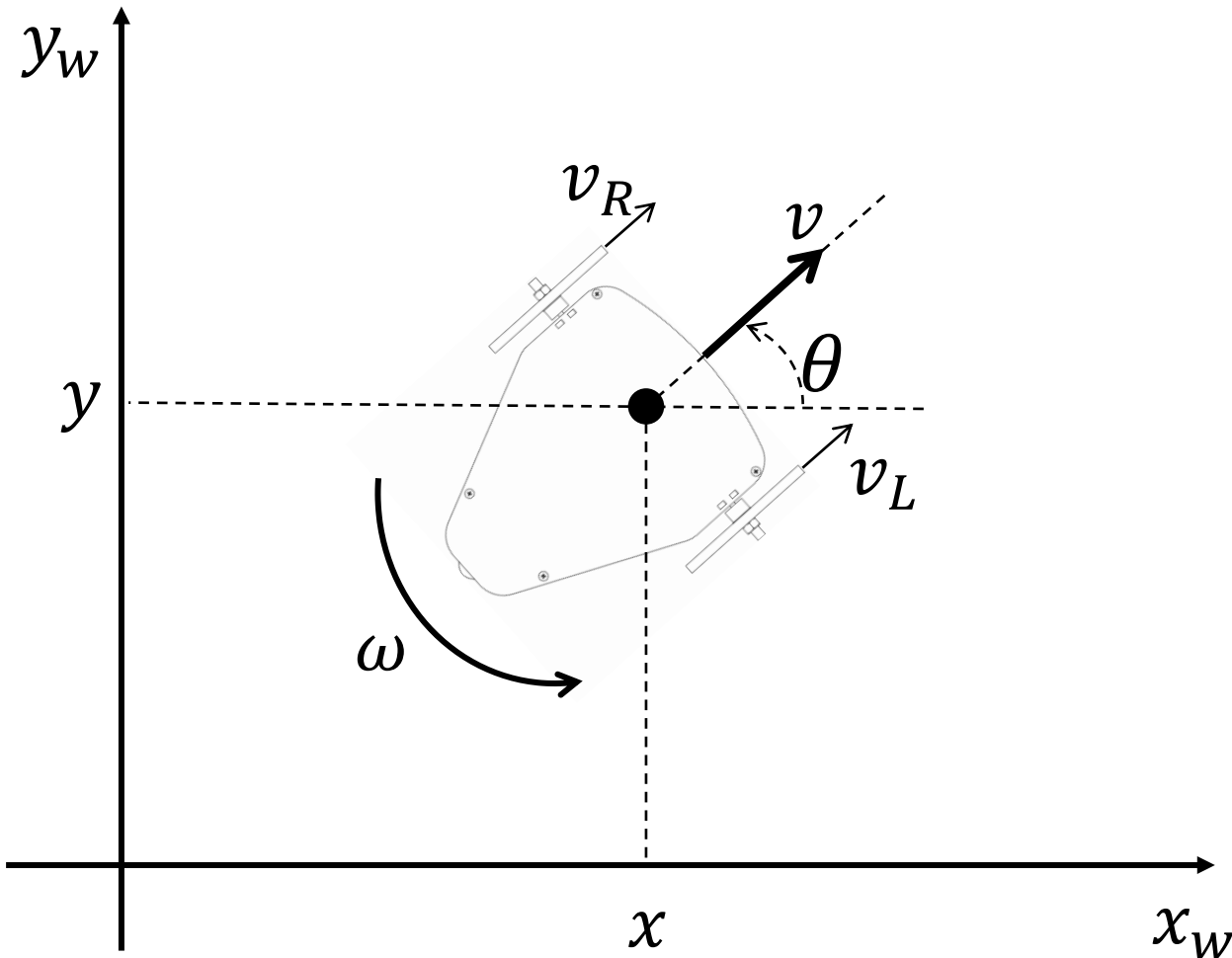
Determining the Robot Position



$$v_{Robot} = \frac{v_R + v_L}{2} = r \frac{\omega_R + \omega_L}{2}$$

$$\omega_{Robot} = \frac{v_R - v_L}{l} = r \frac{\omega_R - \omega_L}{l}$$

Determining the Robot Position



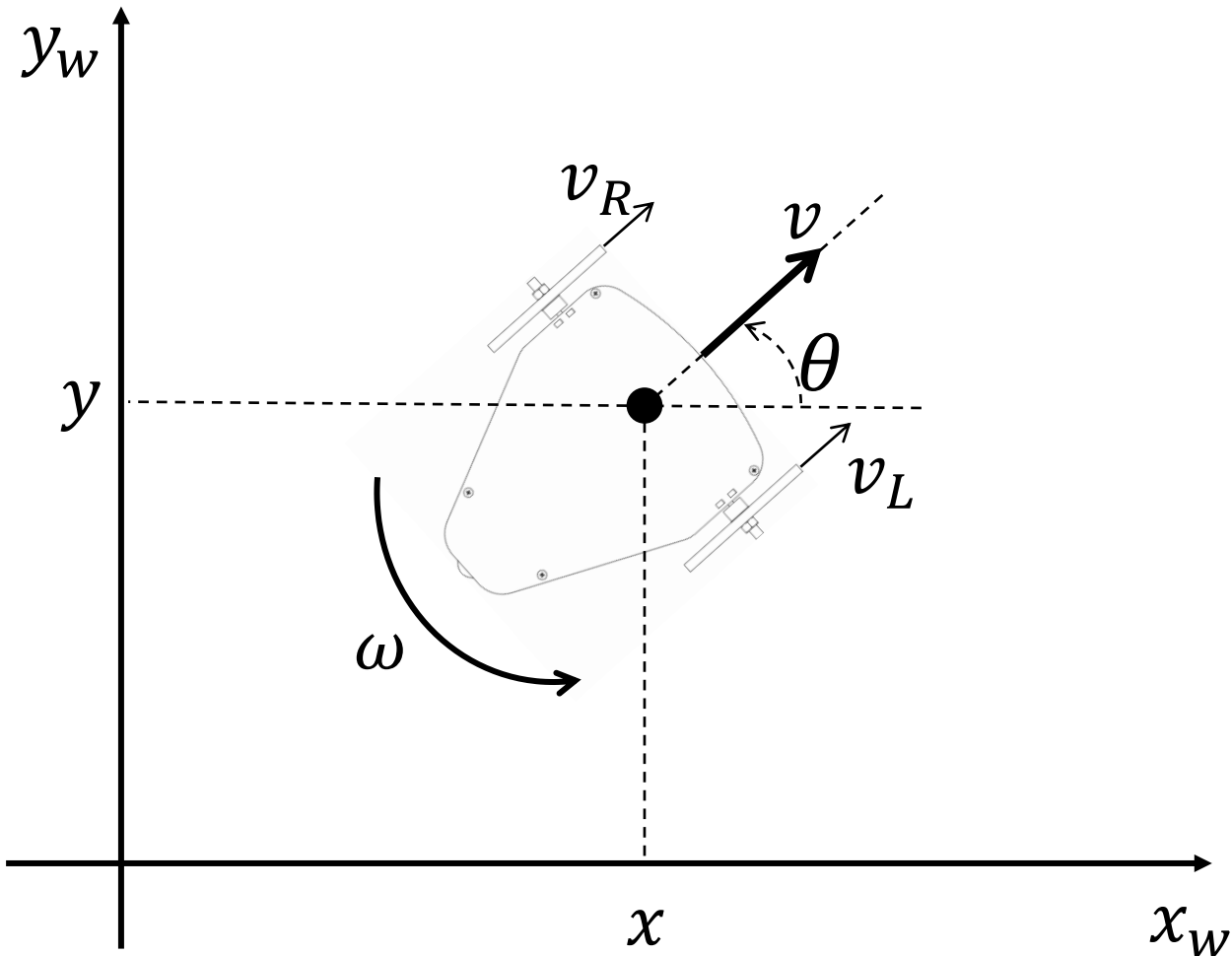
$$v_{Robot} = \frac{v_R + v_L}{2} = r \frac{\omega_R + \omega_L}{2}$$

$$\omega_{Robot} = \frac{v_R - v_L}{l} = r \frac{\omega_R - \omega_L}{l}$$

$$\dot{x} = v \cos \theta = r \frac{\omega_R + \omega_L}{2} \cos \theta$$

$$\dot{y} = v \sin \theta = r \frac{\omega_R + \omega_L}{2} \sin \theta$$

Determining the Robot Position



$$x_{k+1} = x_k + r \frac{\omega_R + \omega_L}{2} dt \cos \theta$$

$$y_{k+1} = y_k + r \frac{\omega_R + \omega_L}{2} dt \sin \theta$$

$$\theta_{k+1} = \theta_k + r \frac{\omega_R - \omega_L}{l} dt$$

Determining the Robot Position

$$\begin{aligned}
 \theta_{k+1} &= \theta_k + r \frac{\omega_R - \omega_L}{l} dt \\
 x_{k+1} &= x_k + r \frac{\omega_R + \omega_L}{2} dt \cos \theta_k \\
 y_{k+1} &= y_k + r \frac{\omega_R + \omega_L}{2} dt \sin \theta_k
 \end{aligned}$$

Robot Location:

(x_k, y_k, θ_k) : Pose of the robot at timestep k (m, m, rad). Stored in memory, initial value 0

Robot Constants:

r : Wheel radius = 0.05 m

l : Distance between robot wheels = 0.19 m

Measured variables

(ω_R, ω_L) : Wheel velocity (rad/s)

dt : Time between samples (s)

Values of θ must be contained within a single circle:
Either:

$$-\pi \leq \theta < \pi$$

Or:

$$0 \leq \theta < 2\pi$$

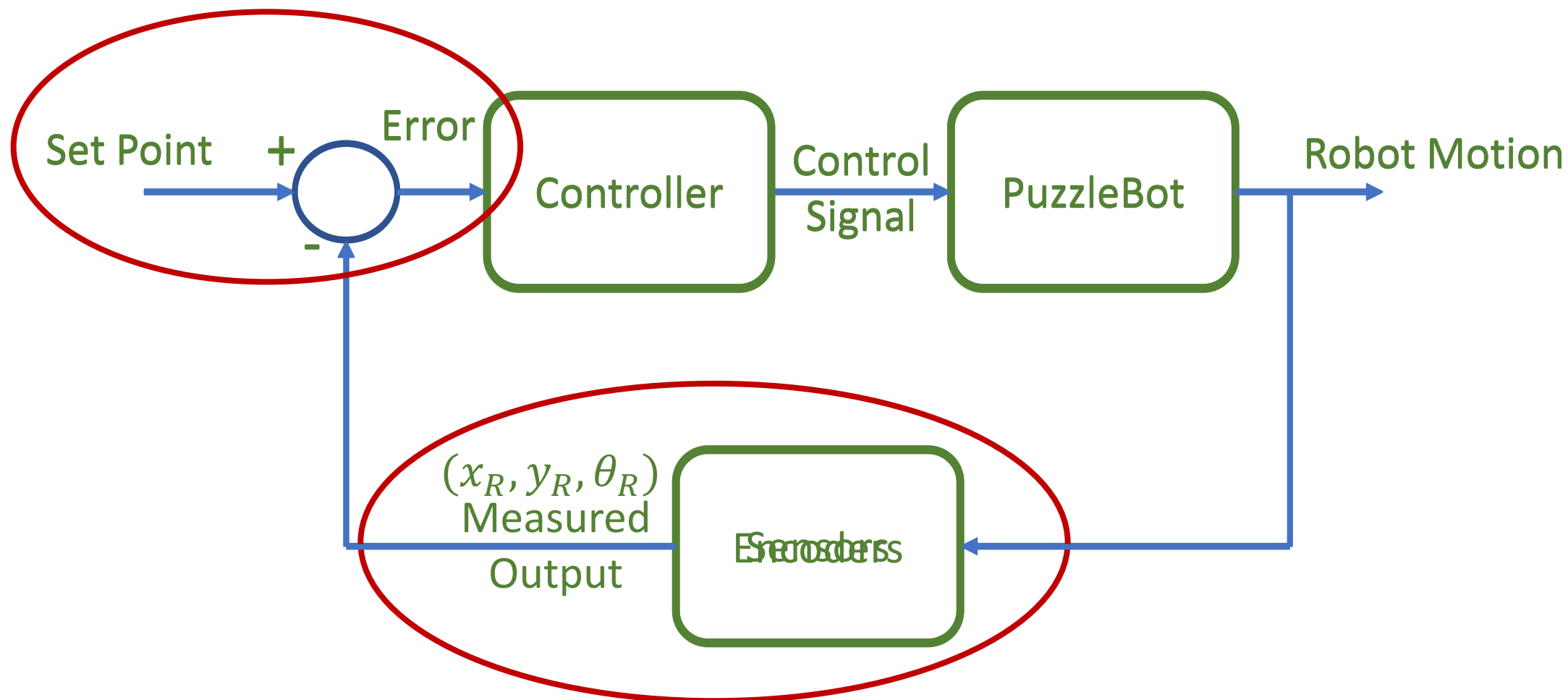


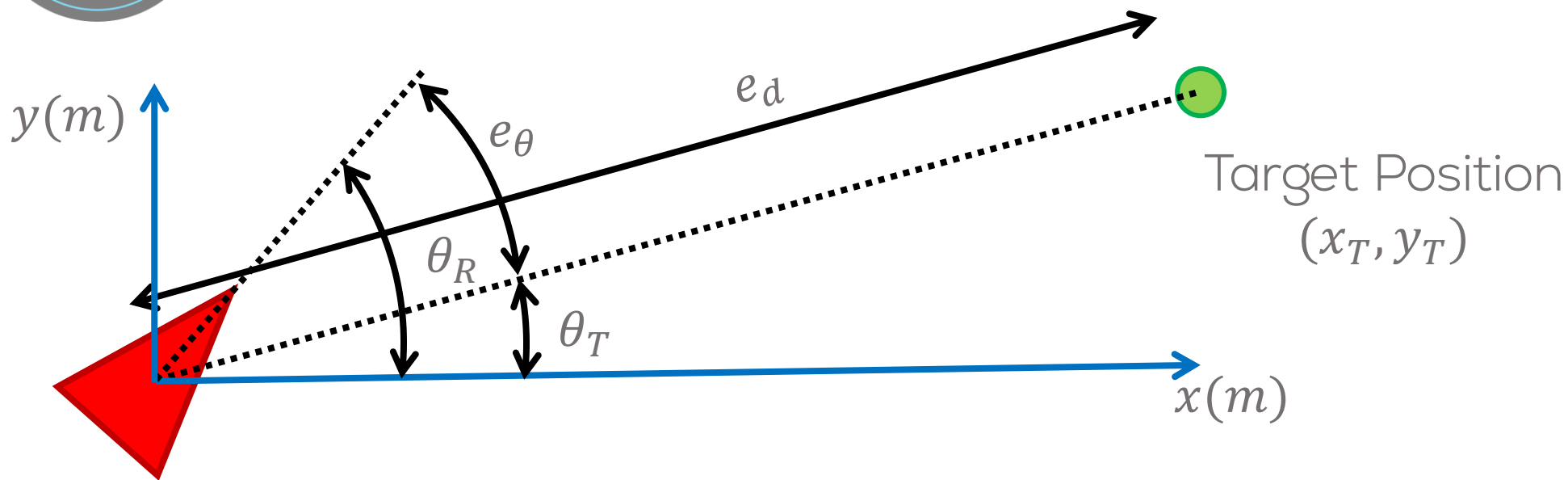
Activity



- Implement a ROS node that computes the robot location using the encoder data
 - It should subscribe to `/wl` and `/wr`, and publish the data to a suitable set of topics
 - The published messages could be a set floats, or you can combine them in any way you see fit

The Control System





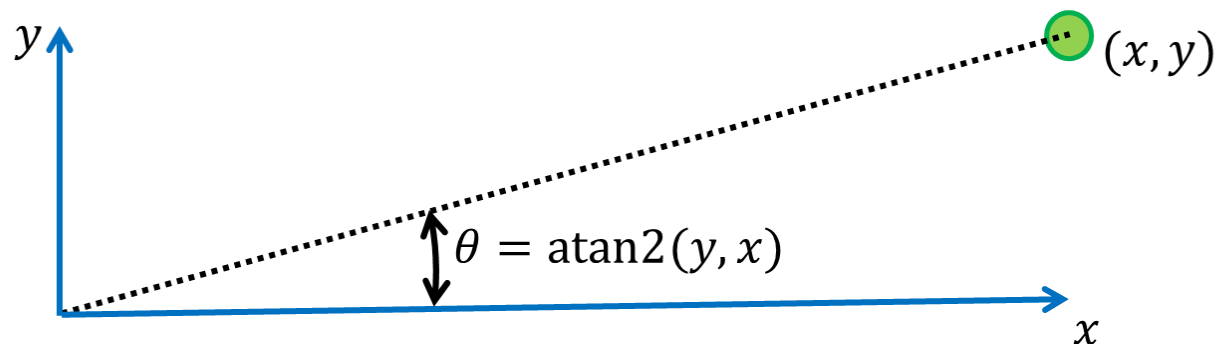
Robot Position
 (x_R, y_R, θ_R)

Target Position
 (x_T, y_T)

$$e_\theta = \theta_T - \theta_R = \text{atan2}(x_T, y_T) - \theta_R$$

$$e_d = \sqrt{(x_T - x_R)^2 + (y_T - y_R)^2}$$

- The atan2 function is a special form of arctan or \tan^{-1} .
- It takes two arguments, y and x , and returns the angle to the x axis:



- It is included in most maths libraries, but it is recommended to use numpy, as numpy will be necessary later on in the course

```
import numpy  
theta = numpy.arctan2(y, x)
```

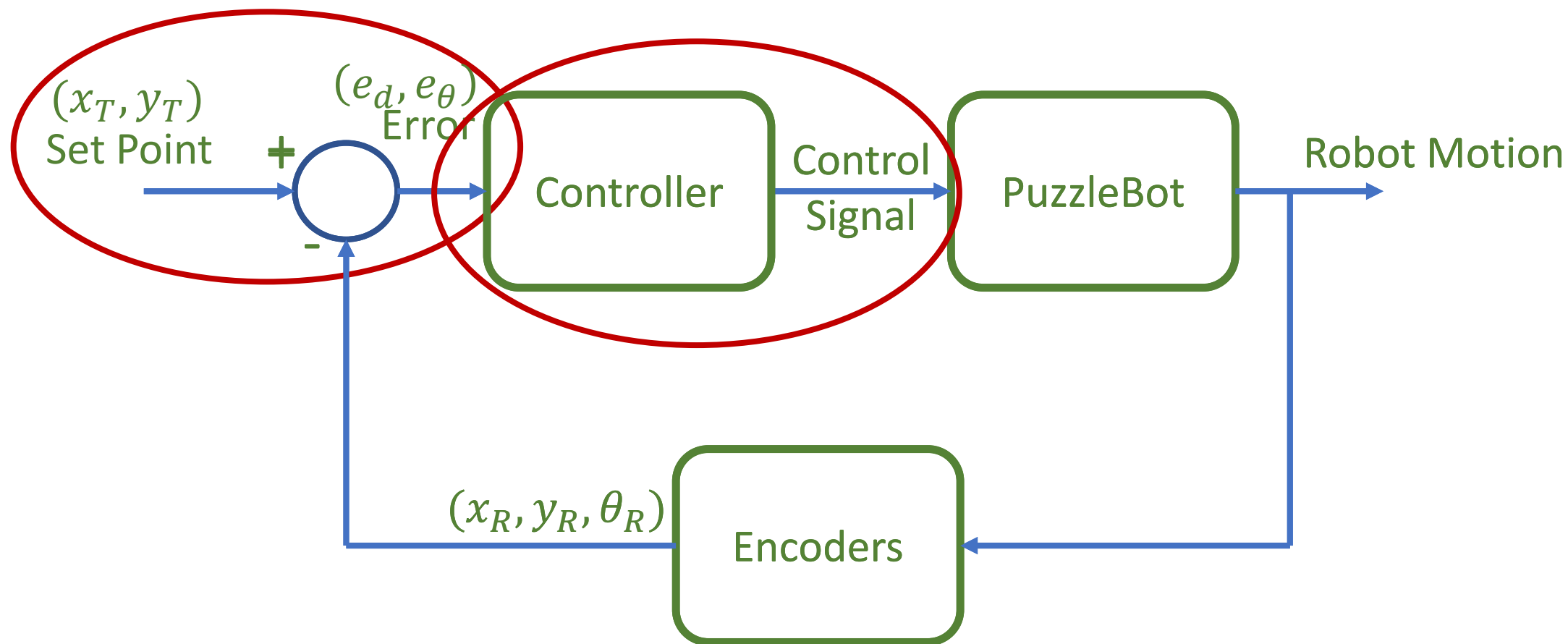


Activity



- Modify the previous node to publish θ and $\dot{\theta}$.
- Set a target, and drive the robot around, checking that the angle to the target and the distance from the target are updated correctly
- Remember to wrap all angles to within 1 circle

The Control System





The Controller

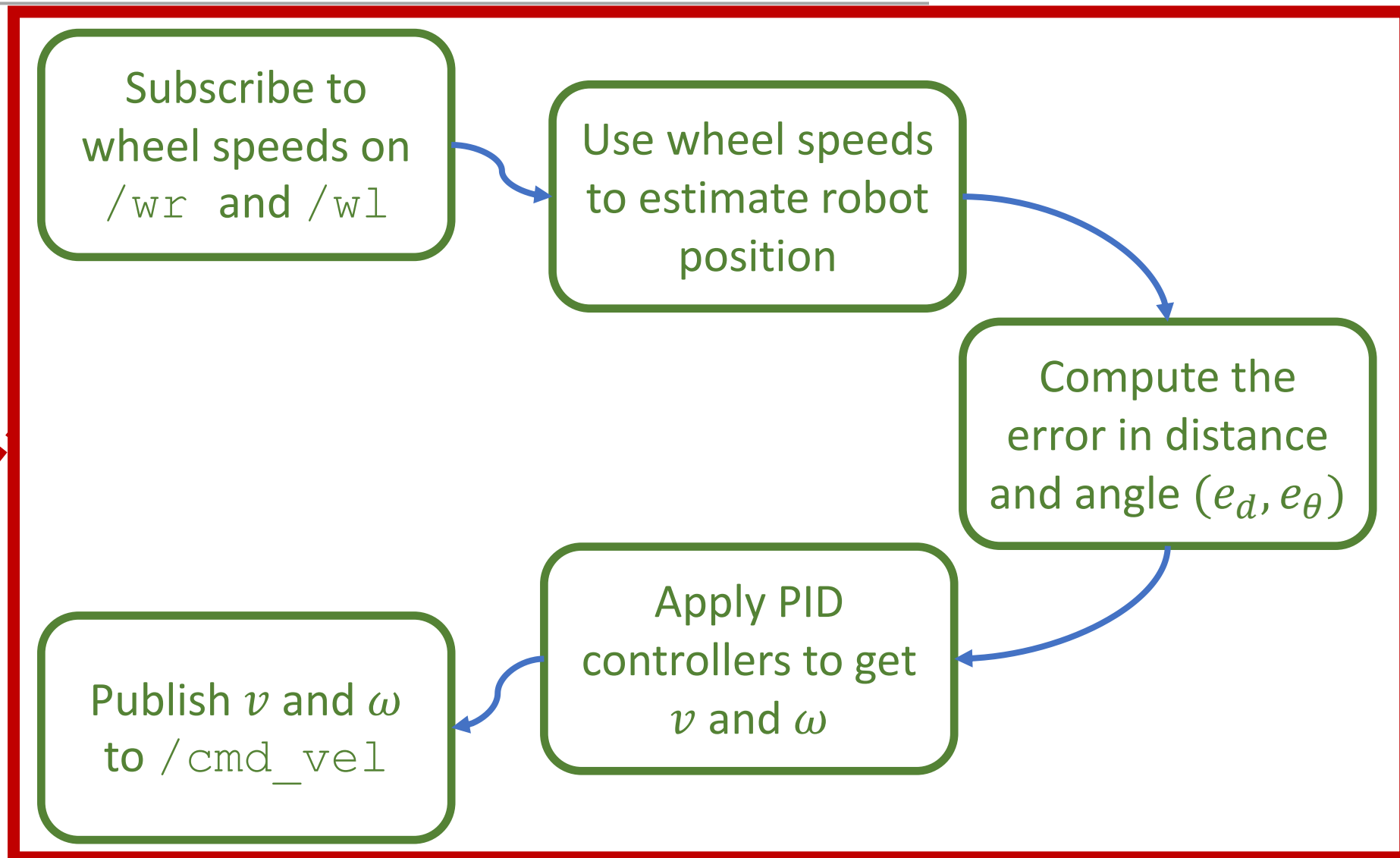
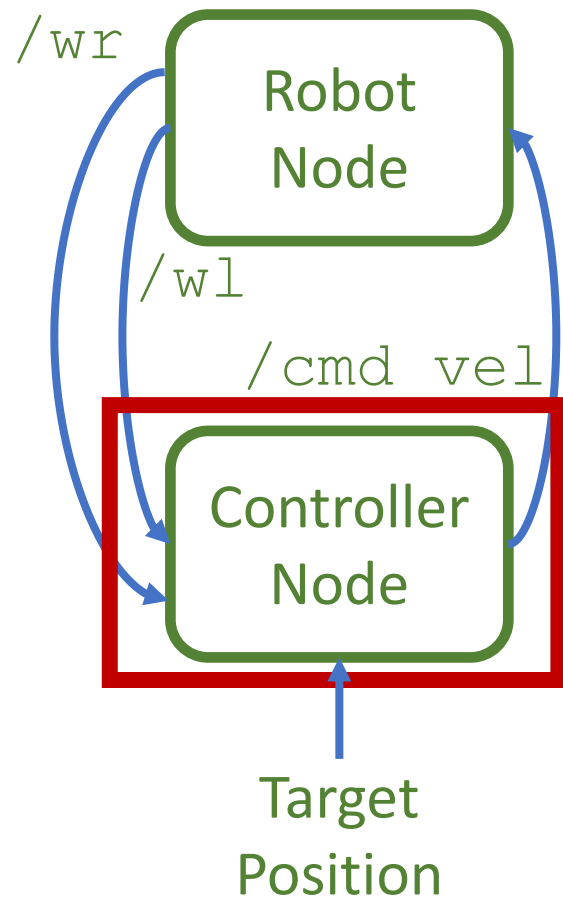


- Since the robot is inherently stable, a simple PID scheme should be sufficient.
- Start with a pair of proportional controllers:

$$v = K_v e_d$$

$$\omega = K_\omega e_\theta$$

... and add integral and derivative elements if necessary.





Tips and Tricks



- Write and test your node with the PuzzleBot off the ground:
 - Use this to check the basics of your code are working correctly, such as the sign (+/-) of your controller parameters K_v and K_ω
 - Does the robot turn towards the goal?
 - Does the robot move towards or away from the goal?
- Tune one of the controllers at a time. You may find it easier to tune K_ω first, while setting your robot to move with a fixed forward speed.
- If in doubt, *lower* the value of the control constants.
- You may find it helpful to use a launch file to load your controller constants in from a config.yaml file.



Accuracy



- It will not be possible to tune the controllers such that the robot moves perfectly into position.
 - You will need a threshold after which your algorithm decides it has successfully arrived.
 - Suggested initial threshold: 10 cm
- Additionally, if you measure the position of the robot, it will likely not match up with the measurement computed from the encoders.
 - This is inevitable due to additive noise in the encoder readings.
 - The solution to this is to use sensors that can measure the position of the robot relative to its environment.



ROS Tools

ROS Launch Syntax



- Launch files are sets of commands written in xml that allow executing various scripts at the same time.
- The general syntax is the following

```
<?xml version="1.0"?>
```

```
<launch>
```

```
[Body of the launchfile]
```

```
</launch>
```

- This syntax allows to run any object used within the ROS architecture and has a wide variety of tools that allow to parametrize the launch file so that it can be adapted to the requirements of you project.
- An extensive documentation can be found in <http://wiki.ros.org/roslaunch>



ROS Tools

ROS Launch code tools



- Running a node

```
<node name="listener" pkg="basic_comms" type="listener.py" output="screen"/>
```

- Running another file or launch file

```
<include file="$(dirname)/other.launch" />
```

- Set parameters

```
<param name="publish_frequency" type="double" value="10.0" />
```

- Pass args to the launch file

```
<arg name="camera_id" value="cam_3" />
```

- Load files into the system

```
<rosparam command="load" file="$(find package_name)/config/file_name.yaml" />
```



The Task

