



Pentathlon (Part III): Next Product to Buy Modeling

The e-mail frequency test changed the dynamics of the monthly Product Department Director meetings.¹ The test had put to rest the question of whether limiting the number of promotional e-mails to customers was in the best interest of the company. The test had also increased Anna Quintero's credibility in digital marketing. Most surprising to Anna, however, was that the department directors had started to seek her advice on problems that required some customer analytics to solve.

Such a problem had been at the center of the most recent meeting. In fact it was a problem of Anna's own making. The company-wide agreement to limit promotional e-mails to twice a week meant that the different departments now had to coordinate their promotional e-mail activities with each other. Having to coordinate was not in and of itself something that departments objected to. They were used to negotiating over scarce resources such as marketing budgets, retail space, and head counts. Instead, the problem was a lack of information. François Cabret, the department head of Endurance Sports put it this way:

"When we negotiate over budgets or space allocation in our stores, there are some important metrics we all agree on. For example, no one is going to argue that sales per square foot of store space does not matter. However, when we negotiate over how to allocate promotional e-mails across departments, we just can't see eye-to-eye. For example, I have argued that endurance-themed e-mails should have highest priority for women because running is just as popular among women as it is among men. But Patricia [the department head of Racquet Sports] says that, online, her category has particular sales appeal to women, even if this is not our experience in stores. Frankly, I don't know how to resolve these questions. We can get reports about which customer segments buy which products online. But that is not what we need. What we really want to know is how effective different promotional e-mail messages are for different customer segments. But there are so many different customer types with different purchase histories that I don't even know how to start thinking about finding out the answer."

¹ Each department director oversaw one of the seven major product categories sold at Pentathlon: Endurance (e.g., running, cycling), Strength and Fitness (e.g., gymnastics, yoga), Water Sports (e.g., sailing, kayaking), Team Sports (e.g., soccer, basketball, rugby), Backcountry (hiking, climbing), Winter Sports (e.g., skiing, snowboarding), and Racquet (e.g., tennis, badminton).

During the meeting, the department heads had discussed the idea of running another test in order to clarify the effectiveness of different promotional e-mail messages for different customer segments. But the idea had fizzled because no one felt that they could wait another six months, the length of the e-mail frequency test, to get an answer. Ten minutes after the idea of a test had been rejected Anna suddenly spoke up:

“I think we have been thinking about this the wrong way. I agree, we should not run a test--- but not because it is going to take too long. We don’t need to run a test because we already have all the data we need to figure out which promotional e-mail message works best for which customer segment. In fact, I think my analytics team will be able to do better than that. If I am not mistaken, we should be able to analyze the effectiveness of different promotional e-mail messages for individual customer, not just for broad segments. Give me a few days and I will get you some answers.”

The Idea

In the months since the decision to limit customer e-mails, the departments – unable to agree on an optimal allocation procedure – had used a simple random rule as an interim compromise. Anna’s sudden realization during the meeting was that the random allocation rule had created something close to experimental data that could be used to analyze the effect of different promotional messages.

The random allocation rule had been implemented as follows:

- Each week the digital marketing department split customers with valid e-mail addresses into seven randomly assigned e-mail groups.
- Each of the seven departments was allocated one of these e-mail groups for their exclusive use during one week, subject to the e-mail frequency limitation.
- The e-mails sent by each department would be designed by that department and would feature products from that department. Of course, once customers clicked on the promotional e-mail and were on the Pentathlon website they could buy products from any department they were interested in.

While this procedure had been chosen because it did not favor one department over another and because it was easy to administer, Anna noticed that it was ideally suited to analyze how different customers reacted to different messages. The key was that customers were being allocated to departments – and therefore to different-themed messages – randomly.

The Data

Anna asked her analytics team to pull the following data:

- The data pull should be based on the last e-mail sent to each customer. Hence, an observation would be a “customer–promotional e-mail” pair.
- The data should contain the basic demographic information available to Pentathlon:
 - “age”: Customer age (coded in 4 buckets: “1” < 30, “2” 30 to 44, “3” 45 to 59, “4” ≥ 60)
 - “female”: Gender, coded as a female dummy

- “income”: Income in Euro, rounded to the nearest 5,000 €
- “education”: Percent of college graduates at the neighborhood level of the customer, coded from 0-100
- “children:” Average number of children at the neighborhood level of the customer
- The data should contain some basic historical information about customer purchases, specifically, a department-specific frequency measure.
 - “freq_endurance – freq_racquet”: the number of purchases in each department over the last year, excluding the two test weeks.
- The key outcome variables should be:
 - “buyer” – Did the customer click on the e-mail and complete a purchase within two days of receiving the e-mail (if yes, buyer=1, 0 otherwise)?
 - “total_os”– Total order size (in Euro) conditional on the customer having purchased (buyer==1). This measured spending for all products, not just for the department that sent the message.
- *While of no importance for the prediction model*, Anna also wanted to see from which departments consumer had ordered when they purchased. This was capture in:
 - “endurance_os – racquet_os”: Department-specific order size (in Euro) – This was a breakdown of the total order size. Even if buyer==1 this was zero for many departments since customers would rarely buy products from all departments on a single purchase occasion.

Finally, Anna requested that her team pull a total of 600,000 observations and divide the data into a training sample and a validation sample using a 70-30 split.

The Analysis

After compiling the data, the digital marketing analytics team began to work through the instructions Anna had e-mailed them:

“Please perform all estimations using the training sample and for now let’s only use a logistic regression for the probability prediction. Use the test sample to assess logistic model performance for the binary decision of whether a consumer buys after receiving a particular message. Please do this:

1. **For each customer**, determine the message (endurance, strength, water, team, backcountry, winter, or racquet) that is predicted to lead to the highest **probability of purchase**. Describe what approach you took to predict probability of purchase.
2. Report for each message the percent of customers in the test sample for whom that message maximizes their **probability of purchase**.
3. For each customer, determine the message (endurance, strength, water, team, backcountry, winter, or racquet) that is predicted to lead to the highest **predicted profit** (the COGS is 60%). Heads-up: There are different ways to predict order size, pick one that you think predicts order size the best. Explain how you calculated expected profit.
4. Report for each message the percent of customers in the test sample for whom that message maximizes their **predicted profit**.
5. Using the **predicted profit** for all consumers in the test sample, what profit can we obtain on average per e-mailed customer when we customize the message to each customer?
6. Using the **predicted profit** for all consumers in the test sample, what profit can Pentathlon obtain on average per e-mailed customer if every customer receives the

same message? Answer the question for each of the seven possible message (endurance, strength, water, team, backcountry, winter, or racquet).

7. Using the **predicted profit** for all consumers in the test sample, what profit can Pentathlon obtain on average per e-mailed customer if every customer is assigned at random to one of the seven messages?
8. Based on the numbers calculated in question 5 and 7, for the typical promotional e-mail blast to 5,000,000 customers, what improvement (in percent and in total Euro) does Pentathlon expect to get from customizing the message to each customer rather than assigning customers a message at random?

A New Policy Proposal

In addition to presenting the results of the analysis during the next monthly department director meeting, Anna Quintero decided to propose a new process for allocating promotional e-mails across departments that was based on her team's analytical results. She wrote down a draft for a new e-mail policy proposal:

- A. Promotional e-mails will be allocated to departments on a monthly basis.
- B. For the first month after this policy goes into effect we assign customer e-mails to departments as follows:
 - a. For each customer the analytics team forecasts the messages that yield the highest and the second highest expected profit among the seven possible messages.
 - b. The two departments whose messages yield the highest and the second highest expected profit for a customer each control $\frac{1}{2}$ of the allowed e-mail messages to that customer during that month.
- C. During the last week of each subsequent month the analytics team uses the data from e-mails sent during the first three weeks in that month and repeats the analysis described in step 2.

Case Questions

1. Perform the analysis following the instruction e-mailed by Anna to the analytics team (Step 1 to 8 above). **(22 points)**
2. Comment on the draft for a new e-mail policy proposal. What are its weaknesses? Can you suggest at least one improvement? **(8 points)**

Hints

- It is important to understand that the company's profit depends on the total order size (total_os) that follows an e-mail offer, not on the order size in the department for which a message was sent (i.e. endurance_os – racquet_os). The reason is that each e-mail may lead to purchases in many departments, not just the one that was the focus of the e-mail. Hence, endurance_os – racquet_os are only included in the dataset to give you a sense of how consumers allocate their money across categories. However, these variables have *no value for the predictive model*.
- In each assignment I focus on some specific set of issues. Hence, for this assignment don't spend much time thinking about taking out insignificant variables or maximizing the predictive performance of the model.