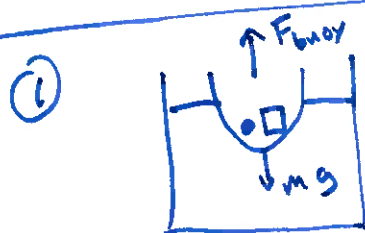


- ① Quick Buoyancy Prob Review
- ② Waves on strings
- ③ Change in v, λ, f upon change in media
- ④ Practice Problems



what is V_{disp} ? (neglecting mass of boat)

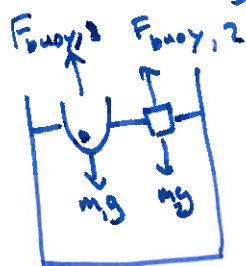
$$F_{buoy} - m_{\text{everything in boat}} g = 0$$

(scenario A)

$$\Rightarrow \rho_{\text{water}} V_{disp} g = (m_{\text{rock}} + m_{\text{ice cube}}) g$$

$$\Rightarrow V_{disp} = \frac{m_{\text{rock}} + m_{\text{ice cube}}}{\rho_{\text{water}}}$$

(scenario B)



$$F_{buoy,1} - m_{\text{rock}} g = 0$$

$$F_{buoy,2} - m_{\text{ice cube}} g = 0$$

$$\Rightarrow V_{\text{tot disp}} = V_{disp,1} + V_{disp,2} = \frac{m_{\text{rock}} + m_{\text{ice cube}}}{\rho_{\text{water}}}$$

Same water displaced \Rightarrow same water level

(scenario C)



rock sinks because buoyant force is not enough to balance weight

$$F_{buoy,1} - m_{\text{ice cube}} g = 0$$

$$F_{buoy,2} - m_{\text{rock}} g = m_{\text{rock}} a < 0$$

water ~~rise~~ falls

$$V_{\text{tot disp}} < \frac{m_{\text{rock}} + m_{\text{ice cube}}}{\rho_{\text{water}}}$$

② Waves on Strings: $v = f\lambda$

②

can't change v by changing f or λ

$$v = \sqrt{\frac{T}{\mu}}$$

..... tension
..... $\frac{\text{mass}}{\text{length}}$

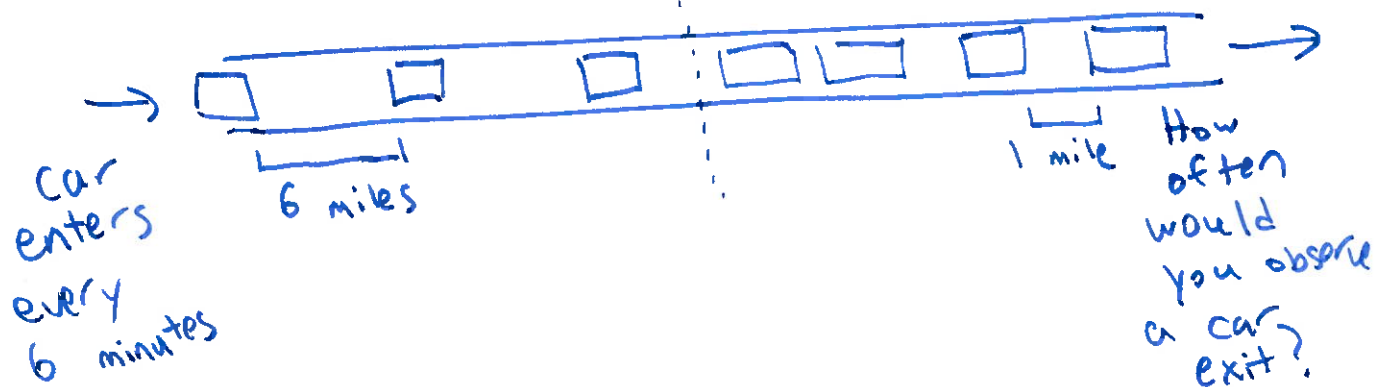
v is a property of medium
(or nature)

③

What about f ?

60 mph

10 mph



* key: frequency is a property of
the source
wavelength adjusts

$$v = f\lambda$$

(3 clickers)

Two strings with different unit mass are tied in the center and attached with a tension of 1000N to two walls, as shown. What is the ratio of the wave's speed in the two strings?

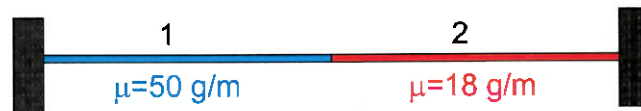
The wave speed in a wire is $v = \sqrt{\frac{T}{\mu}}$



1. $v_1/v_2 = 9/25$
2. $v_1/v_2 = 3/5$
3. $v_1/v_2 = 5/3$
4. $v_1/v_2 = 25/9$
5. $v_1/v_2 = 1$

$$\begin{aligned} \frac{v_1}{v_2} &= \frac{\sqrt{\frac{T}{\mu_1}}}{\sqrt{\frac{T}{\mu_2}}} \\ &= \sqrt{\frac{\mu_2}{\mu_1}} \\ &= \frac{3}{5} \end{aligned}$$

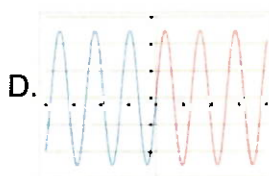
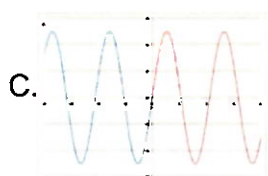
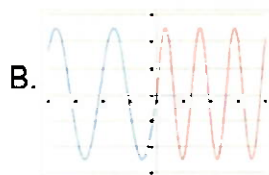
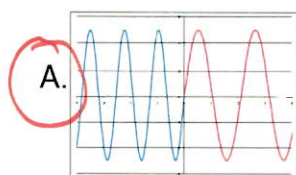
Two strings with different unit mass are tied in the center and attached with a tension of 1000N to two walls, as shown. What is the ratio of the wave's frequencies in the two strings?



1. $f_1/f_2 = 9/25$
2. $f_1/f_2 = 3/5$
3. $f_1/f_2 = 5/3$
4. $f_1/f_2 = 25/9$
5. $f_1/f_2 = 1$

frequency is
a property of
the source!

Two strings with different unit mass are tied together as shown.
What will the waves look like in the two strings?



$$\frac{v_1}{v_2} = \frac{3}{5}$$

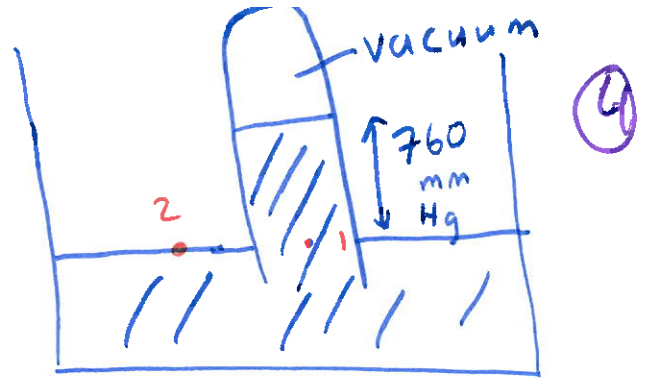
$$v_1 = \lambda_1 f$$

$$v_2 = \lambda_2 f$$

$$\frac{5}{3} v_1 = \lambda_2 f$$

$$\frac{5}{3} \lambda_1 f = \lambda_2 f$$

- ④ Practice Problems
 ① Given this picture, what is the density of mercury?



$$1 \text{ atm} = 1.01 \times 10^5 \text{ Pa}$$

$$P_2 = P_{\text{atmos}}$$

$$P_1 = \rho_{\text{Hg}} g h + \cancel{P_{\text{vacuum}}}$$

$$P_1 = P_2 \Rightarrow \rho_{\text{Hg}} g h = 1.01 \times 10^5 \text{ Pa}$$

$$\begin{aligned} \rho_{\text{Hg}} &= \frac{1.01 \times 10^5 \text{ Pa}}{(10 \text{ m/s}^2)(0.76 \text{ m})} \\ &= 13600 \text{ kg/m}^3 \end{aligned}$$

Phase:

$$D(x, t) = A \sin [kx \mp \omega t + \phi_0]$$

phase ϕ "where you are in the wave cycle"

If I look @ Δx (const t) or Δt (const x), I get

$$\Delta \phi = k \Delta x$$

$$= 2\pi \left(\frac{\Delta x}{\lambda} \right)$$

$$\Delta \phi = \omega \Delta t$$

$$= 2\pi \left(\frac{\Delta t}{T} \right)$$

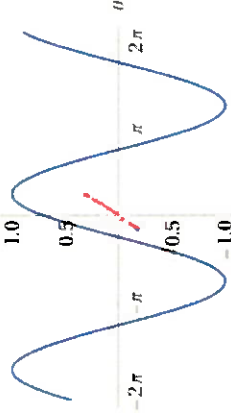
Hint: take
sin θ & shift

it left/right
by some angle

Which of the following
best describes $f(\theta)$?

$f(\theta)$

- (A) $\sin(\theta + \pi/4)$
- (B) $\sin(\theta - \pi/4)$
- (C) $\sin(\theta + 3\pi/4)$
- (D) $\sin(\theta - 3\pi/4)$
- (E) None of the above



This is a snapshot of a wave @ $t = T/2$,
where T is the period. Find an equation for

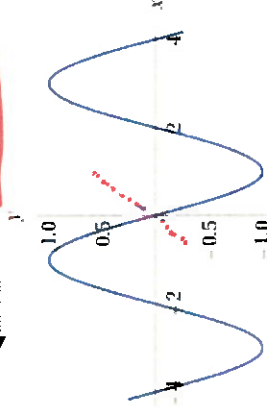
$$y(x, t) = A \sin[kx \pm \omega t + \phi_0] \quad (A > 0)$$

with $\phi_0 \in [0, 2\pi)$

$t = \frac{1}{2}T$

2 m/s

what's sign
and ϕ_0 ?



← left $y(x, t) = A \sin[kx + \omega t + \phi_0]$

$$y(x, \frac{1}{2}T) = A \sin[kx + \pi + \phi_0]$$

$$\Rightarrow \phi_0 = 0$$

$$y(x, t) = A \sin[kx + \omega t]$$