

### Question 1.



Sarah and Mike are communicating using Internet for communication. They want to make sure that their communication should not be intercepted by an attacker.

[Part-A]

They are using Asymmetric encryption, in which each user has two keys i.e. Private Key and Public Keys, which are issued by Certification Authority in the form of Digital Certificate.

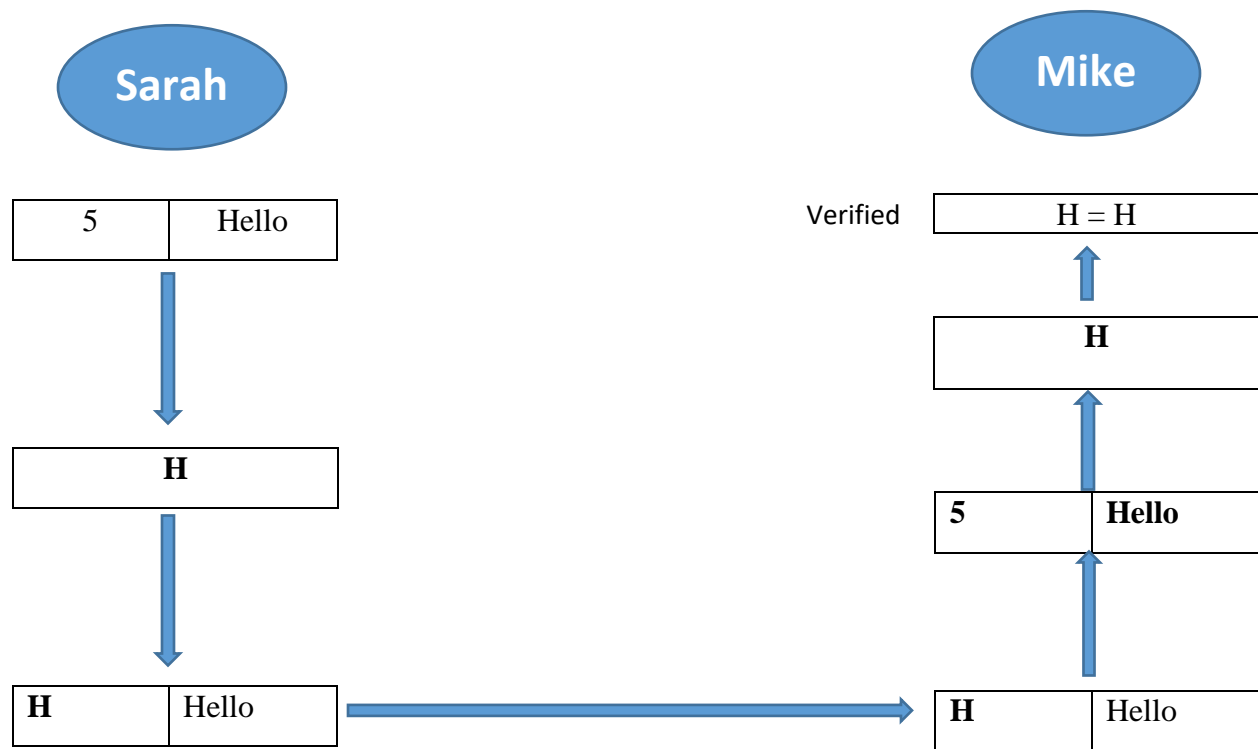
They want to achieve Confidentiality, Authentication, Integrity and Non-Repudiation using their Private and Public Keys. Suppose Sarah is sending a Message. Fill the blanks on the question paper using the format e.g. Pub-Name and Pri-Name, where Pub is Public Key, Pri is Private key and name is the party name e.g. Mike.

	Encryption	Decryption
Confidentiality	Pub-Mike	Pri-Mike
Integrity	Pri-Sarah	Pub-Sarah
Non-Repudiation	Pri-Sarah	Pub-Sarah
Digital Signature	Pri-Sarah	Pub-Sarah
Authentication	Pri-Sarah	Pri-Sarah
Digital Certificate	Pri-Certification Authority	Pub-CA

- Mike will get Public key of Sarah in a Digital Certificate issued by Certification Authority
- To Achieve Confidentiality and Authentication of a single message it should be encrypted using Pri-Sarah first and then encrypted using Pub-Mike
- Mike will decrypt the message received from step-ii using Pri-Mike first and then Pub-Sarah.

[Part-B]

The Integrity of message can also be achieved using Hashing. Suppose Sarah is sending a message “Hello” and the pre-shared key is 5. How Sarah and Mike will achieve Integrity and Non-Repudiation. You can use Variable “H” for Hashing output. Fill the blanks and make sure that you perform hashing in a correct sequence.



## Question 2.

**Question:** Alice and Bob wish to communicate securely over an insecure channel. After authentication, they decide to use the Diffie-Hellman key exchange to generate a shared secret key. Here are the details of their setup:

$q = 17$  Select a value between 13 and 19 (  $13 < q < 19$  )

[1 mark]

$\alpha = 3$  Select Smallest Possible Primitive Root

[2 marks]

$X_{\text{Alice}} = 4$

$X_{\text{Bob}} = 5$

Compute the following for Alice and Bob:

Alice	Bob
$q = 17$	$q = 17$
$\alpha = 3$	$\alpha = 3$
$X_{\text{Alice}} = 4$	$X_{\text{Bob}} = 5$
$Y_A = \alpha^{X_{\text{Alice}}} \bmod q$ [3 marks for correct answer] $= 3^4 \bmod 17$ 1 for only formula $= 81 \bmod 17$ $= 13$	$Y_B = \alpha^{X_{\text{Bob}}} \bmod q$ $= 3^5 \bmod 17$ $= 243 \bmod 17$ $= 5$
$K = Y_B^{X_{\text{Alice}}} \bmod q$ $5^4 \bmod 17$ $5^4 = 625, \quad 625 \bmod 17 = 13$	$K = Y_A^{X_{\text{Bob}}} \bmod q$ $13^5 \bmod 17$ $13^5 = 371293, \quad 371293 \bmod 17 = 13$

**Question 3.** Encrypt the plaintext "System is hacked" using a columnar transposition cipher. Use the key "SUN". Solve this question in Answer Sheet. [10 marks]

Follow and fill the Steps as mentioned below.

1. Fill the Grids and assign column order using the key: (4 marks assigned to the grid on the left side under SUN and 4 marks assigned to the grid on the right side under NSU)

Key is "SUN", so re-write as rows of 3-letter blocks:	
S U N	N S U
2 3 1	1 2 3
S Y S	S S Y
T E M	M T E
I S H	H I S
A C K	K A C
E D X	X E D

2. Highlight columns in the new order and provide the corresponding ciphertext: **(2 numbers for identifying proper ciphertext by writing column wise)**

Corresponding Ciphertext: SMHKXSTIAEYESCD

**Another solution if spaces are considered.**

Follow and fill the Steps as mentioned below.

1. Fill the Grids and assign column order using the key: **(4 marks assigned to the grid on the left side under SUN and 4 marks assigned to the grid on the right side under NSU)**

Key is "SUN", so re-write as rows of 3-letter blocks:

S U N

2 3 1

S Y S

T E M

I S

H A

C K E

D X X

N S U

1 2 3

S S Y

M T E

S I

A H

E C K

X D X

2. Highlight columns in the new order and provide the corresponding ciphertext: **(2 numbers for identifying proper ciphertext by writing column wise)**

Corresponding Ciphertext: SMSAEXT CDYEIHKX

Answer 4:

**Case 1**

$\{x^6 + x^5 + x^4 + x^3 + x^2 + x + 1\} + 1(x^6 + x^5 + x^4 + x^3 + x^2 + x + 1)$   
 $2x^6 + x^5 + x^4 + x^3 + x^2 + x + 1$   
 $x^7 + x^6 + x^5 + x^4 + x^3 + x^2 + x$

57	20	4D	20	b0
69	69	69	4E	b1
46	73	6E	6F	b2
69	20	65	77	b3

W0 W1 W2 W3

$1101$   $1110$   
 $0010$   $0000$   
 $0100$   $1110$   
 $1001$   $1001$   


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 $0010$   $1001$   
 $\rightarrow 29$

**Mix Column Transformation :**

02	03	01	01
01	02	03	01
01	01	02	03
03	01	01	02

57	20	4D	20
69	69	69	4E
46	73	6E	6F
69	20	65	77

**Equation :**

$\{01\} * \{20\} \oplus \{01\} * \{4E\} \oplus \{02\} * \{6F\} \oplus \{03\} * \{77\}$   
 $01 = 0000 \ 0001 = X^0 = 1$   
 $20 = 0010 \ 0000 = X^5$   
 $01 = 0000 \ 0001 = 1$   
 $4E = 0100 \ 1110 = X^6 + X^3 + X^2 + X$   
 $02 = 0000 \ 0010 = X$   
 $6F = 0110 \ 1111 = X^6 + X^5 + X^3 + X^2 + X + 1$   
 $03 = 0000 \ 0011 = X + 1$   
 $77 = 0111 \ 0111 = X^6 + X^5 + X^4 + X^2 + X + 1$

Case 2

57	20	4D	20	b1
69	69	69	4E	b2
46	73	6E	6F	b3
69	20	65	77	b4

$W_1 \ W_2 \ W_3 \ W_4$

Mix Column Transformation:

02	03	01	01
01	02	03	01
01	01	02	03
03	01	01	02

\*

57	20	4D	20
69	69	69	4E
46	73	6E	6F
69	20	65	77

0100	1101
0110	0101
1101	0010
1011	0010
<del>0110</del>	1000
0100	
48	

4D  
65

$02 \times 69$

0000 0010  
0110 1001

$x(x^6, x^5, x^3 + 1)$   
 $x^7 + x^6 + x^4 + x$

$03 \times 6E$

0000 0011  
0110 1110

$x(x^7 + x^6 + x^4 + x)$   
 $x^8 + x^7 + x^5 + x^2 + x$

Equation

$\{01\} \times \{4D\} \oplus \{02\} \times \{69\} \oplus \{03\} \times \{6E\} \oplus \{01\} \times \{65\}$

- $01 = 0000 \ 0001 = 1$
- 0  $4D = 0100 \ 1101 = x^6 + x^3 + x^2 + 1$   $\left. \begin{array}{l} x^6 + x^3 + x^2 + 1 \\ 0100 \ 1101 \end{array} \right\}$
- 2  $02 = 0000 \ 0010 = x$
- c  $69 = 0110 \ 1001 = x^6 + x^5 + x^3 + 1$   $\left. \begin{array}{l} x^7 + x^6 + x^4 + x \\ 11010010 \end{array} \right\}$
- l  $03 = 0000 \ 0011 = x + 1$
- c  $6E = 0110 \ 1110 = x^6 + x^5 + x^3 + x^2 + x$   $\left. \begin{array}{l} x^7 + x^5 + x^4 + x \\ 10110010 \end{array} \right\}$
- e  $01 = 1$
- c  $65 = 0110 \ 0101 = x^6 + x^5 + x^2 + 1$   $\left. \begin{array}{l} x^6 + x^5 + x^2 + 1 \\ 01100101 \end{array} \right\}$


c) 44 words

Given words 4

$$\text{No of rounds} \times \text{Words} = 10 \times 4 = 40$$

$$4 + 40 = 44$$

d) W11

49
17
A0
9F

+

56
17
1F
12