

$$= \frac{18}{43}$$

$$= 0.4186$$

① (DELL given that Red) = ?

$$= P(\text{DELL and Red})$$

$$P(\text{DELL})$$

$$= \frac{16}{188}$$

$$\frac{31}{188}$$

$$= \frac{16}{31}$$

$$= 0.5161$$

0.5161 is the Probability that randomly selected Laptop which is given in Red Color.

#### 4- ADDITIVE RULE or

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

(m) Red or HP ?

$$P(R \text{ or } HP) = P(\text{Red}) + P(\text{HP}) - P(\text{Red and HP})$$

$$P(R \text{ or } HP) = \frac{31}{188} + \frac{69}{188} - \frac{10}{188}$$

$$P(R \text{ or } HP) = 0.4787$$

(n)  $P(\text{HP or DELL})$  ?

$$P(\text{HP or DELL}) = P(\text{HP}) + P(\text{DELL}) - P(\text{HP and DELL})$$

$$P(\text{HP or DELL}) = \frac{69}{188} + \frac{76}{188} - \frac{0}{188}$$

$$P(\text{HP or DELL}) = 0.7712$$

#### 5- COMPLEMENT RULE

P(Ā)

$$P(Ā) = 1 - P(A)$$

Ā

$$P(Ā) = P(\text{Not A})$$

QUE

Deliver

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a. The

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## QUESTION #17:

Class	Yes	No	No Opinion
Freshmen	15	8	5
Sophomores	24	4	2

If a student is selected at random, find the probability that the student-

- a. Has no opinion
- b. Is a freshman or is against the issue
- c. Is a sophomore & favours the issue

Class	Yes	No	No Opinion	Total
Freshmen	15	8	5	28
Sophomores	24	4	2	30
Total	39	12	7	58

$$a. P(\text{no opinion}) = \frac{7}{58} = 0.1206.$$

$$b. P(\text{freshman or against issue}) = P(\text{freshmen}) + P(\text{against issue}) - P(\text{freshman and against issue})$$

$$P(\text{freshman or against issue}) = \frac{28}{58} + \frac{12}{58} - \frac{8}{58}$$

$$\therefore P(\text{freshman or against issue}) = 0.5517$$

$$c. P(\text{sophomore & favours}) = \frac{\text{Intersection frequency}}{\text{total # of outcomes}}$$

$$P(\text{sophomore & favours}) = \frac{24}{58}$$

$$P(\text{sophomore & favours}) = 0.4137$$

## QUESTION # 18:

	Delivered to Letters	Ads	Magazines	Total
Home	325	406	203	934
Business	732	1021	97	1850
Total	1057	1427	300	2784

If an item of mail is selected at random, find these probabilities

- The item went to a home
- The item was an ad, or it went to a business
- The item was a first class letter, or it went to a home.

a-  $P(\text{item went to a home}) = \frac{934}{2784}$

$P(\text{item went to a home}) = 0.335$

b-  $P(\text{ad or went to business}) = P(\text{ad}) + P(\text{business}) - P(\text{ad and business})$

$$P(\text{ad or business}) = \frac{1427}{2784} + \frac{1057}{2784} - \frac{1021}{2784}$$

$P(\text{ad or business}) = 0.5255$

c-  $P(\text{letter or home}) = P(\text{letter}) + P(\text{home}) - P(\text{letter and home})$

$$P(\text{letter or home}) = \frac{1057}{2784} + \frac{934}{2784} - \frac{325}{2784}$$

$P(\text{letter or home}) = 0.5984$

QUESTION # 30:

	Cookies	Mugs	Candy	Total
Coffee	20	13	10	43
Tea	12	10	12	34
Total	32	23	22	77

Choose 1 basket at random. Find the

Probability that it contains -

a- Coffee or Candy

b- Tea given that it contains Mugs

c- Tea and Cookies

$$\text{a- } P(\text{coffee or candy}) = P(\text{coffee}) + P(\text{candy}) - P(\text{coffee and candy})$$

$$P(\text{coffee or candy}) = \frac{43}{77} + \frac{22}{77} - \frac{10}{77}$$

$$P(\text{coffee or candy}) = 0.71428$$

$$\text{b- } P(\text{Tea given that mugs}) = \frac{P(\text{Tea and mugs})}{P(\text{mugs})}$$

$$P(\text{Tea given that mugs}) = \frac{10/77}{23/77}$$

$$P(\text{Tea given that mugs}) = \frac{10}{23}$$

$$\text{c- } P(\text{Tea & cookies}) = 0.4347$$

$$P(\text{Tea & cookies}) = \frac{\text{Interaction Frequency}}{\text{Total # of outcomes}}$$

$$P(\text{Tea & cookies}) = \frac{12}{77} = 0.1558$$

### QUESTION #33

	Gold	Silver	Bronze	Total
United States	36	38	36	110
Russia	23	21	28	72
China	51	21	28	100
Great Britain	19	13	15	47
Others	173	209	246	628
Total	302	302	353	957

- a - Find the Probability that the winner won the gold medal, given that the winner was from the United States
- b - Find the Probability that the winner was from the United States, given that she or he won a gold medal
- c - Are the events "medal" winner is from United States & "gold medal won" independant?  
 Explain : No  $P(G \cap US) \neq P(G)P(US)$

$$P(\text{gold medal given that United States}) = \frac{P(\text{gold and United States})}{P(\text{United States})}$$

$$P(\text{gold medal given that US}) = \frac{36/957}{110/957}$$

$$P(\text{gold M given that US}) = 0.3272$$

$$P(\text{United given that Goldm}) = \frac{P(\text{united and Gold})}{P(\text{Gold})}$$

$$P(\text{united given that G}) = \frac{36/957}{302/957}$$

$$P(\text{United given that GoldM}) = 0.1192$$

c: Not same dependant

SAME INDEPENDANT

$$P(A/B) = P(A)$$

NOT SAME DEPENDANT

$$P(A/B) \neq P(A)$$

QUESTION #24

## MULTIPLICATIVE RULE

$n \geq 2$

If we select  $\textcircled{2}$  events at random  
 $P(A_1 \text{ And } B_2) = P(A_1) P(B_2)$

If we select  $\textcircled{3}$  events at random

$$P(A_1 \text{ and } B_2 \text{ and } C_3) = P(A_1) P(B_2) P(C_3)$$

### Example NO 12

- \* 10 white cars
- \* 12 black cars ] Total 22 Cars

If we select 2 cars at random Find the Probability that

(a) Both cars are white

$$P(W_1 \text{ and } W_2) = P(W_1) P(W_2)$$

$$P(W_1 \text{ and } W_2) = \left(\frac{10}{22}\right) \left(\frac{10}{22}\right)$$

$$P(W_1 \text{ and } W_2) = 0.2066$$

(b) Both cars are Black

$$P(B_1 \text{ and } B_2) = P(B_1) P(B_2)$$

$$P(B_1 \text{ and } B_2) = \left(\frac{12}{22}\right) \left(\frac{12}{22}\right)$$

$$P(B_1 \text{ and } B_2) = 0.2975$$

(c) First is White & Second is Black

$$P(W_1 \text{ and } B_2) = P(W_1) \cdot P(B_2)$$

$$P(W_1 \text{ and } B_2) = \left(\frac{10}{22}\right) \left(\frac{12}{22}\right)$$

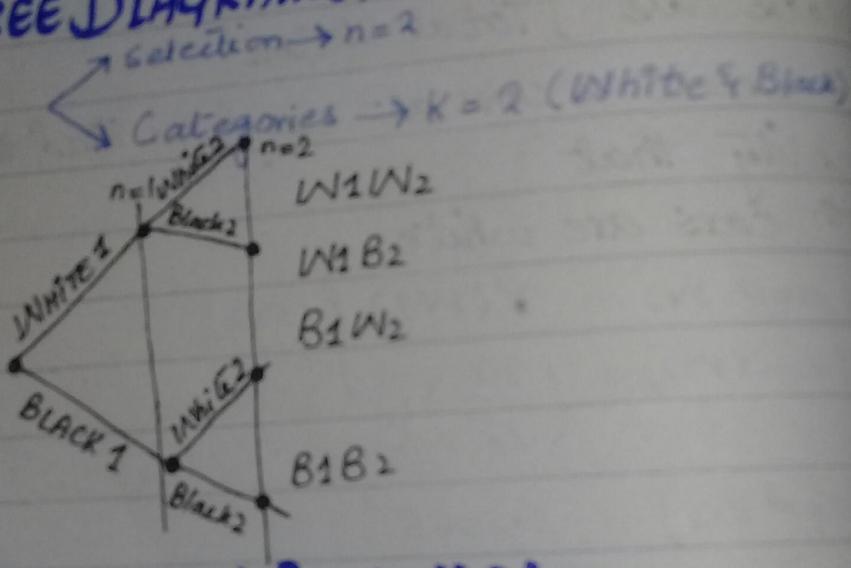
$$P(W_1 \text{ and } B_2) = 0.2479$$

④ First is Black & second is White  
 $P(B_1 \text{ and } W_2) = P(B_1) \cdot P(W_2)$   
 $P(B_1 \text{ and } W_2) = \left(\frac{12}{22}\right) \cdot \left(\frac{10}{22}\right)$

$$P(B_1 \text{ and } W_2) = 0.2479$$

\* NOTE: Sample Space = 1  
 $P(S) = 1$

### FOR TOTAL OUTCOMES: (TREE DIAGRAMS):



### ⑤ ATLEAST 1 is White

$X = \text{The Number of White}$

$P(\text{at least 1 is white})$

$$\begin{aligned} P(X \geq 1) &= P(W_1W_2) + P(W_1B_2) + P(B_1W_2) \\ &= 0.2066 + 0.2479 + 0.2479 \\ &= 0.7024 \end{aligned}$$

\* OR

$$P(\text{at least 1 is white}) = 1 - P(NW_1 - NW_2)$$

### QUESTION

- Computer Owners  
At A Local University  
year students  
selected at random  
a- None have  
b- At least one  
c- All have
- a-  $\frac{54}{100}$

$$P(\text{none})$$

$$P(\text{none})$$

$$P(\text{none})$$

$$P(\text{none})$$

$$P(\text{none})$$

$$P(\text{at least one})$$

$$P(\text{at least one})$$

$$P(\text{at least one})$$

$$P(\text{All have})$$

$$P(\text{All have})$$

$$\begin{aligned}
 P(\text{at least 1 is white}) &= 1 - P(B_1 \text{ and } B_2) \\
 &= 1 - 0.2975 \\
 &= 0.7025
 \end{aligned}$$

### QUESTION #34:

Computer Ownership

At a local university 54.3% of incoming first year students have computers. If 3 students are selected at random, find the following probabilities

- a- None have Computers
- b- Atleast one has a Computer
- c- All have Computers.

$$a- \frac{54.3}{100} = 0.543$$

$$P(\text{none have computers}) = 1 - P(\text{have computers})$$

$$P(\text{none have computers}) = 1 - 0.543$$

$$P(\text{none have computers}) = 0.457$$

$$P(\text{none have computers}) = (0.457)(0.457)(0.457)$$

$$P(\text{none have computers}) = 0.09544$$

$$b- P(\text{Atleast one has a Computer}) = 1 - 0.09544$$

$$P(\text{Atleast one has a Computer}) = 0.90456$$

$$c- P(\text{All have computers}) = P(C_1) P(C_2) P(C_3)$$

$$P(\text{All have computers}) = (0.543)(0.543)(0.543)$$

$$P(\text{All have computers}) = 0.1601$$

## QUESTION #35:

Leisure time exercise. Only 27% of US adults get enough leisure time exercise to achieve cardiovascular fitness. Choose 3 adults at random. Find the probability that:

- a - All 3 get enough daily exercise
- b - At least 1 of the three gets enough exercise

$$a - P(\text{All 3 gets enough exercise}) = 27\%$$

$$P(\text{All 3 gets enough exercise}) = \frac{27}{100}$$

$$P(\text{All 3 gets enough exercise}) = 0.27$$

$$P(A_1 \text{ and } A_2 \text{ and } A_3) = P(A_1) P(A_2) P(A_3)$$

$$P(A_1 \text{ and } A_2 \text{ and } A_3) = (0.27)(0.27)(0.27)$$

$$P(A_1 \text{ and } A_2 \text{ and } A_3) = 0.0196$$

$$b - P(\text{At least 1 get enough exercise}) = 1 - 0.27$$

$$P(\text{At least 1 get enough exercise}) = 0.73$$

$$P(\text{At least 1 of 3 get enough exercise}) = (0.73)(0.73)(0.73)$$

$$P(\text{At least 1 of 3 get enough}) = 0.3890$$

$$P(\text{At least 1 of 3 get enough}) = 1 - 0.3890$$

$$P(\text{At least 1 of 3 get enough}) = 0.611$$

## QUESTION

Customer Purcha

10 customers,

5 customers

Find the prob

120 .

90 of

(C<sub>1</sub> and C<sub>2</sub>)

(C<sub>1</sub> & C<sub>2</sub> & C<sub>3</sub>)

(C<sub>1</sub> & C<sub>2</sub> & C<sub>3</sub>)

Percent

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Percent

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P(A<sub>1</sub>)

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P(A<sub>1</sub>)

## QUESTION # 36:

Customer Purchases: In a department store, there are 120 customers, 90 of whom will buy at least 1 item. If 5 customers are selected at random, one by one, find the probability that all will buy at least 1 item.

120 customers

90 of whom will buy at least 1 item

$$P(C_1 \text{ and } C_2 \text{ and } C_3 \text{ and } C_4 \text{ and } C_5) = \left(\frac{90}{120}\right) \left(\frac{90}{120}\right) \left(\frac{90}{120}\right) \left(\frac{90}{120}\right) \left(\frac{90}{120}\right)$$

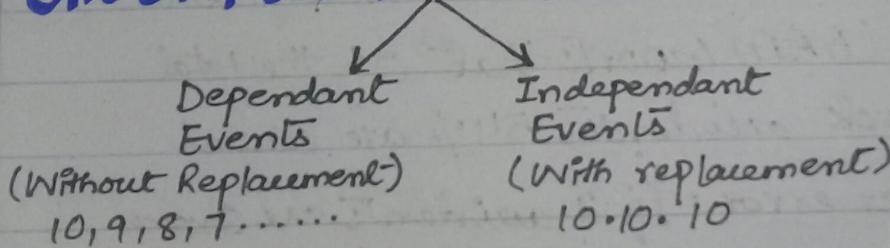
$$P(C_1 \in C_2 \in C_3 \in C_4 \in C_5) = \left(\frac{90}{120}\right) \left(\frac{89}{119}\right) \left(\frac{88}{118}\right) \left(\frac{87}{117}\right) \left(\frac{86}{116}\right)$$

$$P(C_1 \in C_2 \in C_3 \in C_4 \in C_5) = 0.2306$$

\* If Percentage is given then, it is called "Independent Events"

If Percentage is not given, then it is called "Dependant Events".

## MULTIPLICATIVE RULE:



$$P(A_1 \text{ and } B_2) = P(A_1) \cdot P(B_2)$$

If we select 3 events at random

$$P(A_1 \in B_2 \in C_3) = P(A_1) P(B_2) P(C_3)$$

## RANDOM VARIABLES:

which associated      interested  
It's Probability      things

## QUESTION #37

Marital Status of Women: According to the Statistical Abstract of the United States, 70.3% of female ages 20 to 24 have never been married. Choose 5 young women in this age category at random. Find the probability that,

- a- None has ever been married
- b- At least 1 has been married.

$$a- \quad P(\text{None}) = \frac{70.3\%}{100} = 0.703$$

$$\begin{aligned} P(W_1 \cap W_2 \cap W_3 \cap W_4 \cap W_5) &= P(W_1)P(W_2)P(W_3)P(W_4)P(W_5) \\ &= (0.703)(0.703)(0.703)(0.703)(0.703) \\ &= 0.17170 \end{aligned}$$

$$b- P(\text{At least 1 has been Married}) = 1 - 0.17170$$

$$P(\text{At least 1 has been Married}) = 0.8283$$

## QUESTION #38

Fatal Accidents: The American Automobile Association (AAA) reports that of the fatal car and truck accidents, 54% are caused by car driver error. If 3 accidents are chosen at random, find the Probability that:

- a: All are caused by car driver error
- b: None is caused by car driver error
- c: At least 1 is caused by car driver error

$$P(\text{All are caused by car driver error}) = \frac{54}{100} = 0.54$$

$$P(\text{All are caused by car driver error}) = (0.54)(0.54)(0.54) \\ = 0.15746$$

$$b - P(\text{None is caused by car driver error}) = 1 - 0.54 \\ = 0.46 \\ = (0.46)(0.46)(0.46)$$

$$P(\text{None is caused by car driver error}) = 0.0973$$

$$c - P(\text{At least 1 is caused by car driver error}) = 1 - 0.0973$$

$$P(\text{At least 1 is caused by car driver error}) = 0.9027$$

### QUESTION #39

On Time Airplane Arrivals The greater cincinnati airport led major US airports on-time arrivals in the last quarter of 2005 with an 84.3% on-time rate. Choose 5 arrivals at random & find the probability that at least one was not on time.

$$84.3\% = \frac{84.3}{100} = 0.843$$

$$P(A_1 \text{ & } A_2 \text{ & } A_3 \text{ & } A_4 \text{ & } A_5) = (0.843)(0.843)(0.843)(0.843)(0.843) \\ = 0.4257$$

$$P(\text{At least 1 was not on time}) = 1 - 0.4257$$

$$P(\text{At least 1 was not on time}) = 0.5743$$

$X = \text{No of white cars}$

$X$	$P(X)$	$x_i P(x_i)$	$x_i^2 P(x_i)$	
0	0.2975	0.0	0	
1	0.4958	0.4958	0.495	
2	<u>0.2065</u>	<u>0.8264</u>	<u>0.4132</u>	
	$P(S)=1$	1.3222	0.909	

Num  
Sold X  
19  
20  
21  
22  
23

$E[X] = \mu = \text{Expected Value of } X$

$$\mu = \sum x_i P(x_i)$$

$$\sigma^2 = \sum x_i^2 P(x_i) - \mu^2$$

$\sigma = \sqrt{\text{Variance}}$

$$\mu = \sum x_i P(x_i)$$

$$= 0(0.2975) + 1(0.4958) + 2(0.2066)$$

$$= 0.909$$

$$\sigma^2 = \sum x_i^2 P(x_i) - \mu^2$$

$$\sigma^2 = (0)^2(0.2975) + (1)^2(0.4958) + 2^2(0.2066)$$

$$\sigma^2 = 1.322 - 0.8262$$

$$\sigma^2 = 0.4959$$

$$\sigma = \sqrt{\text{Variance}}$$

$$\sigma = \sqrt{0.4959}$$

$$\sigma = 0.704$$

Discrete  
Probability

Sold X	Probability P(x)	$x_i P(x_i)$	$x_i^2 P(x_i)$
19	0.2	3.8	72.2
20	0.2	4	80
21	0.3	6.3	132.3
22	0.2	4.4	96.8
23	0.1	2.3	52.9
	$P(S)=1$	20.8	434.2

$$\begin{aligned}\sigma^2 &= \sum x_i^2 P(x_i) - \bar{x}^2 \\ &= 434.2 - (20.8)^2 \\ &= 434.2 - 432.64 \\ &= 1.56\end{aligned}$$

$\sigma = \sqrt{\text{variance}}$

$$\sigma = \sqrt{1.56}$$

$$\sigma = 1.2489$$

$\therefore$  AVERAGE \* MEAN

$$= 20.8 \times 5 = 104$$

## NUMBER OF CREDIT CARDS:

Cards X	Probability P(x)	$x_i P(x_i)$	$x_i^2 (P x_i)$
0	0.18	0	0
1	0.44	0.44	0.44
2	0.27	0.54	1.08
3	0.08	0.24	0.72
4	0.03	0.12	0.48
		1.34	2.72

$$\begin{aligned}\sigma^2 &= \sum x_i^2 P(x_i) - \mu^2 \\ &= 2.72 - (1.34)^2 \\ &= 2.72 - 1.7956\end{aligned}$$

$$\sigma^2 = 0.9244$$

$$\sigma = \sqrt{\text{variance}}$$

$$\sigma = \sqrt{0.9244}$$

$$\sigma = 0.9614$$

Question #04

$$\begin{array}{l} X \quad \text{Probability}(x) \quad x_i P(x_i) \quad x_i^2 P(x_i) \end{array}$$

$$5 \quad 0.05 \quad 0.25 \quad 1.25$$

$$6 \quad 0.2 \quad 1.2 \quad 7.2$$

$$7 \quad 0.4 \quad 2.8 \quad 19.6$$

$$8 \quad 0.1 \quad 0.8 \quad 6.4$$

$$9 \quad 0.15 \quad 1.35 \quad 12.15$$

$$10 \quad \underline{0.1} \quad \underline{1} \quad \underline{10}$$

$$P(s) = 1 \quad 7.4 \quad 56.6$$

$$\sigma^2 = \sum x_i^2 P(x_i) - \mu^2$$

$$= 56.6 - (7.4)^2$$

$$= 56.6 - 54.76$$

$$= 1.84$$

# BINOMIAL DISTRIBUTION

A binomial experiment is a probability experiment that satisfies the following four requirements:

- 1- There must be a fixed number of trials.
- 2- Each trial can have only two outcomes or outcomes that can be reduced to two outcomes. These outcomes can be considered as either success or failure.
3. The outcomes of each trial must be independent of one another
4. The probability of a success must remain the same for each trial

Remember

Binomial means 2 outcomes like success / failure like defective / not defective like working / non working

- We discuss  $(n)$  in binomial distribution
- We fix  $(n)$  means number of trials
- $(n)$  can be any number
- Any thing which can we present in 2 groups

→ First is in  
P(interest)  
P(not int)

→ summision

P-

Probab  
= 1

When a  
other's

→ First is in which we are interested

$$P(\text{interested}) = P$$

$$P(\text{not interested}) = q$$

→ summision of Relative Frequency is 1

$$P + q = 1$$

→ Probability of interested + probability of failure  
= 1

- When one probability is given we can find other's probability through the given one.

Pg # 274

Example 5-19:

→ Survey on Fear of Being Home Alone or  
at Night

- Public opinion reported that 5% of Americans are afraid of being alone in a house at night.
- If a random sample of 20 students is selected, find these probabilities by using table

$x$  = The number of People

$$P = 5\% = 0.05$$

$$q = 1 - P = 1 - 0.05 = 0.95$$

sum should be = 1

2       $n = 20$

3       $q = 0.95$

3      ①  $P(x=5) = ?$

Binomial Probability Formula

In a binomial experiment, the probability of exactly  $x$  successes in  $n$  trials is

$$P(X) = \frac{n!}{(n-x)!x!} \cdot p^x \cdot q^{n-x}$$

We will not use formula, we use table to find out Probability

see table on Pg # 775

When we use Table for Binomial distribution, so we required 2 values  $P \& n$  with respect to  $X$

$$X = 5 \& 5 = 0.002$$

$$P(X) = ?$$

$$X = 4 \& 4 = 0.013$$

$$\begin{aligned} \textcircled{a} \quad P(X < 2) &= P(0) + P(1) \\ &= 0.358 + 0.377 \\ &= 0.735 \end{aligned}$$

$$\begin{aligned} \textcircled{b} \quad P(X < 3) &= P(0) + P(1) + P(2) \\ &= 0.358 + 0.377 + 0.189 \\ &= 0.924 \end{aligned}$$

$$\begin{aligned} \textcircled{c} \quad P(\text{atmost } 3) &= P(X \leq 3) \\ &= P(0) + P(1) + P(2) + P(3) \\ &= 0.358 + 0.377 + 0.189 + 0.060 \\ &= 0.984 \end{aligned}$$

$$\begin{aligned} \textcircled{d} \quad P(X \geq 3) &= P(3) + P(4) + \dots + P(5) \\ &= 0.060 + 0.013 + 0.002 \\ &= 0.075 \end{aligned}$$

$$(X=2) \quad P = 0.4 \quad n = 5$$

a) Exactly 2 people will agree with that statement

$$P(\text{exactly } 2) = 0.346$$

b) At most 3 people will agree with that statement

$$\begin{aligned} P(\text{at most } 3) &= P(0) + P(1) + P(2) + P(3) \\ &= 0.078 + 0.259 + 0.346 + \\ &\quad 0.230 \\ &= 0.913 \end{aligned}$$

c- At least 2 people will agree with that statement

$$\begin{aligned} P(\text{atleast 2}) &= 0.346 + 0.230 + 0.077 + 0.010 \\ &= 0.663 \end{aligned}$$

d- Fewer than 3 people will agree with that statement.

$$\begin{aligned} P(x < 3) &= P(0) + P(1) + P(2) \\ &= 0.078 + 0.259 + 0.346 \\ &= 0.683 \end{aligned}$$

In a company 60% employees have cellphones. If we select 10 employees randomly

Find the prob that

(a) Exactly 4 have cellphone

$$60\% = \frac{60}{100} = 0.6$$

$$n = 10$$

$$X = 4$$

$$P(\text{exactly } 4) = 0.111$$

(b) less than 5 have cellphones

$$\begin{aligned} P(\text{less than } 5) &= P(0) + P(1) + P(2) + P(3) + P(4) \\ &= 0.02 + 0.011 + 0.042 + 0.111 \\ &= 0.166239 \end{aligned}$$

(c) more than 8 have cellphones

$$\begin{aligned} P(X \geq 8) &= P(9) + P(10) \\ &= 0.040 + 0.006 \\ &= 0.046 \end{aligned}$$

(d) at least 3 have cellphones

$$\begin{aligned} P(\text{at least } 3) &= 0.042 \\ &= 0.040 + 0.006 \\ &= 0.046 \end{aligned}$$

$$\begin{aligned} P(\text{at least } 3) &= P(3) + \dots + P(10) \\ &= 0.987 \end{aligned}$$

(e) almost 2 have

$$\begin{aligned} P(X \geq 2) &= P(2) \\ &= 0.046 \end{aligned}$$

from 3 to

$$\begin{aligned} P(X > 3) &= P(4) \\ &= 0.006 \end{aligned}$$

(e)

at most 2 have cellphones

$$P(X \geq 2) = P(0) + P(1) + P(2)$$

$$= 0 + 0.002 + 0.011$$

$$= 0.013$$

(f)

from 3 to 7 have cellphones

$$P(X > 3 \text{ to } X \geq 7) = P(3) + P(4) + P(5) + P(6) + P(7)$$

$$= 0.043 + 0.111 + 0.201 + 0.251$$

$$= 0.215$$

$$= 0.82$$

# POISSON PROBABILITY DISTRIBUTION

Introduction:

- 1- Discrete random variable.
- 2- Variable will be depend over either:
  - a. time
  - b. space (area)
  - c. volume

Example:

Time: The number of calls per hour

Space: The number of errors per page  
(Area)

Volume: The number of tablets in  
a water tank.

# POISSON PROBABILITY DISTRIBUTION

Formula

$$P(X=x) = \frac{e^{-\lambda} (\lambda)^x}{x!}$$

$x = 0, 1, 2, \dots$

## EXAMPLE 1:

The average number of calls per hour is 3. The number of calls follows Poisson probability dist. If we select an hour randomly, Find the probability that exactly 5 calls would be

Table

X	$\lambda = 3.0$
$x=5$	$\rightarrow$

$$\lambda = 3$$

(a)  $P(X=5)$

$$P(X=5) = ?$$

$$P(X=5) = 0.1008$$

Table

X	$\lambda = 3.0$
$x=5$	$\rightarrow$

(b)  $P(\text{less than } 4) =$

$$P(X < 4) = ?$$

$$P(X < 4) = 0.0498 + 0.1494 + 0.2240 + 0.2240.$$

$$P(X < 4) = 0.6472$$

(c)  $P(\text{more than } 6) =$

$$P(X \geq 6) = ?$$

$$P(X \geq 6) = 0.0216 + 0.0081 + 0.0027 + 0.0008 + \\ = 0.0002 + 0.0001$$

$$P(X \geq 6) = 0.0335$$

(d)  $P(\text{at least } 3) =$

$$P(X \geq 3) = P(3) + P(4) + \dots + P(10)$$

~~P(0) + P(1) + P(2)~~

$$= 0.5767$$

(e)  $P(\text{at most } 10) = ?$

$$P(X \leq 10) = P(0) + P(1) + P(2) + \dots + P(10) \\ = 0.9996$$

(f)  $P(\text{from 2 to 7}) =$

$$P(2 \leq X \leq 7) = 0.7888$$

# POISSON PROBABILITY DISTRIBUTION

Example 2:

The average number of errors per page is, aver  
4. If we select 2 pages randomly, find the probability that the number of errors would be exactly 7

$$P(X=7) = ?$$

Step #01: Per page  $\lambda = 4$

Two page  $\lambda = 2 \times 4 = 8$

$$\lambda = 8$$

$$P(X=7) = 0.3196$$

	$\lambda = 8$
$X=7$	0.3196

27. (Opt). Computer Help Hot Line receives, on average, 6 calls per hour asking for assistance. The distribution is Poisson. For any randomly selected hour, find the probability that the company will receive

a- At least 6 calls  $\lambda = 6$

$$P(X) = ?$$

$$P(X \geq 6) = P(6) + P(7) + P(8)$$

$$P(X \geq 6) = 0.5542$$

b- 4 or more calls

$$P(X \geq 4) = P(4) + P(5) + P(6) + \dots$$

$$P(X \geq 4) = 0.8488$$

c- At most 5 calls (5-4)

$$P(X \leq 5) = P(5) + P(4) + \dots + P(0)$$

$$P(X \leq 5) = 0.4457$$

Jaweria Asif (9442)

q- Study of robberies. A recent study of robberies for a certain geographic region showed an average of 1 robbery per 20,000 people. In a city of 80,000 people, find the probability of the following

a- 0 robberies

$$P(0) = 0.0183 \quad 4 \times 1 = 4, \lambda = 4$$

b- 1 robbery

$$P(1) = 0.0733$$

c- 2 robberies

$$P(2) = 0.1465$$

d- 3 or more robberies

$$P(x \geq 3) = P(3) + P(4) + P(5) + \dots + P(14)$$

$$= 0.1954 + 0.1954 + \dots + 0.00$$

$$= 0.7619$$

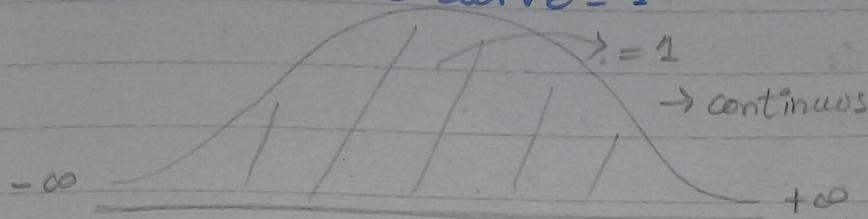
We can't use direct Table to Normal distribution  
→ Previous 2 are discrete We Transform it into Standard  
Continuous

Pg# 784 & 785

## NORMAL DISTRIBUTION:

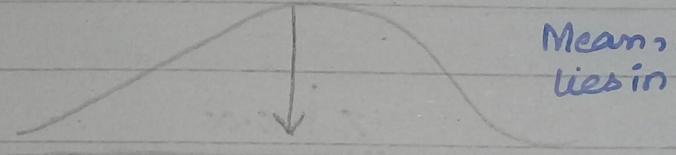
Properties:

- 1- Continuous random Variable such as time, price, weight etc
- 2- Area under the curve = 1



$$3- f(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}} -\infty < x < +\infty$$

4-



Mean, Median, Mode  
lies in between

mean, Median, Mode

→ How to solve Problem?

We Transform

Normal distribution

into standard normal distribution

$$z = \frac{x - \mu}{\sigma}$$

$$P(x < x) \approx P(z < z)$$

Why we Transform?

To use z table