

College of Engineering Pune
Department of Mathematics
MA 19003: Univariate Calculus
Tutorial on Unit III

(1) Which of the following sequences converge and which diverge? Find the limit of each convergent sequence and justify your answers.

(a) $a_n = (-1)^n(1 - \frac{1}{n})$ (e) $a_n = \frac{n}{n^{\frac{1}{n}}}$ (j) $a_n = (n + 4)^{\frac{1}{n+4}}$

(b) $a_n = \frac{n+(-1)^n}{n}$ (f) $a_n = \sin(\frac{\pi}{2} + \frac{1}{n})$ (k) $a_n = \sqrt[n]{4^n n}$

(c) $a_n = \frac{n^2}{e^n}$ (g) $a_n = n\pi \cos(n\pi)$ (l) $a_n = \ln n - \ln(n + 1)$

(d) $a_n = (\frac{3n+1}{3n-1})^n$ (h) $a_n = \tan^{-1} n$ (m) $a_n = \frac{n!}{10^{6n}}$

$$\begin{matrix} 1 & 2 & 3 \\ a & b & c \end{matrix} \begin{bmatrix} 1 & 2 & 3 \\ a & b & c \end{bmatrix} \left\{ \begin{matrix} 1 & 2 & 3 \\ a & b & c \end{matrix} \right\} \begin{vmatrix} 1 & 2 & 3 \\ a & b & c \end{vmatrix} \left\| \begin{matrix} 1 & 2 & 3 \\ a & b & c \end{matrix} \right\|$$