ELECTRIC POTEMCIAL AND CAPACITAMCE

Electric potential

Sum injusty to that point against the electrostatic forces.

Electric potential = work done charge

SI unit of electric potential is vott.

Potential difference

from one point to other inside the electric field of other change



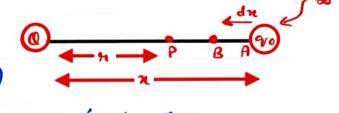
Potential ove to a point charge

Charge from injinity to point A

which is imide the electric field of

main charge a

Now furie experienced by 90:-



Now,

Small work done to move the charge towards the charge of

Then total work done on change go to bring it to point P.

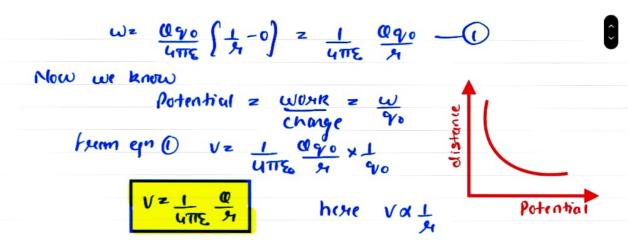
$$\int_{0}^{\infty} d\omega z \int_{0}^{\infty} \frac{1}{4\pi \epsilon} \frac{\alpha y_{0}}{4\pi \epsilon} dM = -\frac{1}{4\pi \epsilon} \frac{\alpha y_{0}}{4\pi \epsilon} \int_{0}^{\infty} \frac{1}{4\pi \epsilon} dM$$

$$\int_{0}^{\infty} \omega z - \int_{0}^{\infty} \frac{1}{4\pi \epsilon} \frac{\alpha y_{0}}{4\pi \epsilon} dM = -\frac{1}{4\pi \epsilon} \frac{\alpha y_{0}}{4\pi \epsilon} \int_{0}^{\infty} \frac{1}{4\pi \epsilon} dM$$

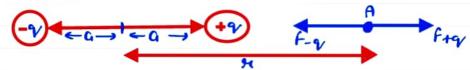
$$\int_{0}^{\infty} \omega z - \int_{0}^{\infty} \frac{1}{4\pi \epsilon} \frac{\alpha y_{0}}{4\pi \epsilon} dM = -\frac{1}{4\pi \epsilon} \frac{\alpha y_{0}}{4\pi \epsilon} \left[\frac{M^{-2+1}}{4\pi \epsilon} \right]_{0}^{\infty}$$

$$\omega = -\frac{\alpha y_{0}}{4\pi \epsilon} \left[\frac{M^{-1}}{4\pi \epsilon} \right]_{0}^{\infty} = \frac{\alpha y_{0}}{4\pi \epsilon} \left[\frac{M^{-1}}{4\pi \epsilon} \right]_{0}^{\infty}$$

$$\omega = \frac{Q q_0}{4\pi \epsilon} \left(\frac{1}{2} \right)_{\infty}^{R} = \frac{Q q_0}{4\pi \epsilon} \left(\frac{1}{2} - \frac{1}{2} \right)$$



Potential due to a dipute at axial Point

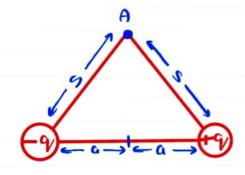


det V+q = Potential at A due to +q unange V-q = Potential at A due to -q charge

VNet =
$$V_{+q} + V_{-q} = \frac{1}{4\pi\epsilon} \frac{4q}{(n-q)} + \frac{1}{4\pi\epsilon} \frac{-q}{(n+q)}$$
 $V_{Net} = \frac{1}{4\pi\epsilon} q \int \frac{1}{n-q} - \frac{1}{n+q} = \frac{1}{4\pi\epsilon} q \int \frac{(n+q)-(n-q)}{(n+q)(n+q)}$
 $V_{Net} = \frac{1}{4\pi\epsilon} q \int \frac{n+q-n+q}{(n^2-q^2)} = \frac{1}{4\pi\epsilon} q \int \frac{2q}{n^2-q^2}$
 $V_{Net} = \frac{1}{4\pi\epsilon} \frac{(q_1 \times 2q)}{n^2-q^2}$

here $q_1 \times 2q = \text{dipple}$
 $V_{Net} = \frac{1}{4\pi\epsilon} \frac{(q_1 \times 2q)}{n^2-q^2}$

Potential at equationial Point



Potential at Point A is given by
$$V_{NC+} = V_{+q} + V_{-q} \\
= \left(\frac{1}{4} + \frac{4q}{5}\right) + \left(\frac{1}{4\pi\epsilon} - \frac{-q}{5}\right)$$

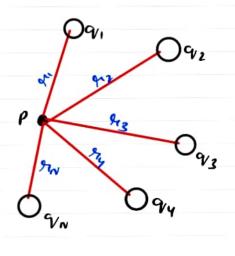
$$V_{NC+} = \frac{1}{4\pi\epsilon} \left(\frac{4q}{5} - \frac{q}{5}\right)$$

$$V_{NC+} = \frac{1}{4\pi\epsilon} \left[0\right] = 0$$

$$V_{NC+} = 0$$

So Potential at equationial point is 2010.

Electric potential due to a system of charges



We need to find Potential at Point P ave to N changes.

We know potential due to a point charge is $V = \frac{1}{4\pi\epsilon} \frac{Q}{2\pi}$ Similarly for Point P;- $V_1 = \frac{1}{4\pi\epsilon} \frac{QV_1}{2\pi}$ $V_2 = \frac{1}{4\pi\epsilon} \frac{QV_2}{2\pi\epsilon}$ $V_3 = \frac{1}{4\pi\epsilon} \frac{CV_3}{2\pi\epsilon}$ and so on for other charges

Total Rotential = $V_1 + V_2 + V_3 - - - V_N$ $V_{Net} = V_1 + V_2 + V_3 - - - V_N$ $V_{Net} = \frac{1}{4\pi\epsilon} \frac{9v_1}{4_1} + \frac{1}{4\pi\epsilon} \frac{9v_2}{4_L} + - - - + \frac{1}{4\pi\epsilon} \frac{c_{VN}}{4_N}$

Behaviour of Conclustors in Electric field

) Net electric field inside a Conductor is always zero

2) Just outside the Surjace of a charged (modultur, electric field is normal (Pempendicular) to the surjace

51 clectric field is not perpendicular then it will have a transential Component along the surjace which will induce surjace current. But no such current exist. So electric field is normal to the Surjace.

3) Net change inside a conduction is always early any excess change always comes to the Surgare of the conductors.

4) Potential inside the Conductor & on the Surgare is always Constant.

we know $E = -\frac{dv}{dt}$ But inside (onductor E = 0dr So $-\frac{dv}{dt} = 0$ or $\frac{dv}{dt} = 0$

5) Electric field is zero in the Cavity of a hollow Conductor.

Relation 5/w electric field & Potential

Consider a charge of located cit point o. Let A B B be two points reported by distance du. Va= Potential at Point A = V VR = Potential at Point Bz V+dV Men Potential difference VB-VAZ V+dV-V = dV -1 How, funce applied on Test change (40) F = -que (minus because force & Electric field one Sphosite) Now work = force x displacement W = Fdx W = - 90 E d4 - 2 Also from aginition of potential difference VB-VA= W w= 90 (vB-VA) w= 90 dv (: from en 0) equating eqn (1) & (2) - que Edr = quo du

Ez - du

dr

hoints towards the decreasing Potential.

Equipotential Suryace

A Sury are that has some potential at every point on it is called equipotential sury are.

Puoperties:

No work is done in moving a charge over an equipotential surjoint we know $V_8 - V_A = W$ But at equipotential surjoint $V_A = V_B$ Thus $W = V_8 - V_8 = 0$

So w= 0

2) Electric field is always perpendicular to the equipotential Surface.

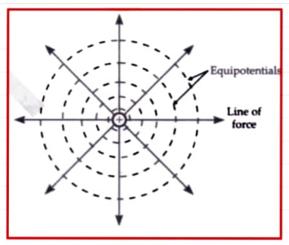
w= Fs (Ost

As w=0 for moving change at equipotential surface

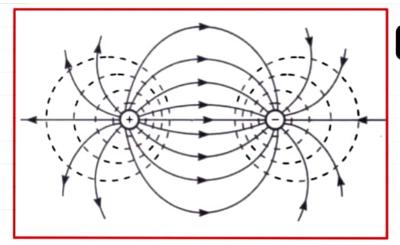


- 3) Equipotential surgare use closer together in surgions of strong field & forther apart in the surgions of weak field.
- 4) No two equipotential surgare con intersect each other.

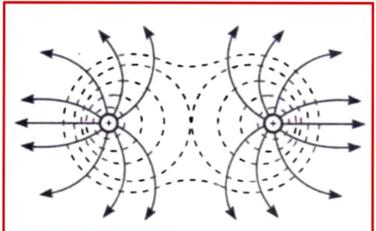
Equipotential Sunface



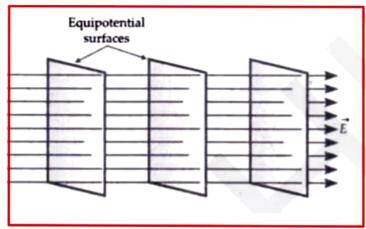
Point charge



Equipotential Surface due to a dipole



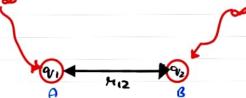
Equipotential Surgone due to Same type of charges



Equipotential surgare due to Uniform electric field

Potential enough due to a system of two changes

WI = WOUR done to bring of from infinity to point A (: Because no electric field is present) WIZO



w2 = work done to bring 9/2 from infinity to point

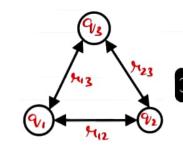
W2 = V1 9/2

here v, z Potential due to charge qui

Total wome 2 w, +w2

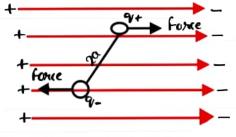
This work is converted into Potential energy

FON a system of 3 changes, Potential energy is (9192+ 9293+



Potential energy of a dipole in electric field

when a dipole is kept imide a uniform electric field, it experience a equal funce in upposite directions as shown in figure. Thus Net forme = 0 NOW



We know T= PESIND

where Pz dipole moment Ez Electric field

Now using :-

WOHK 2 TOrque & Angular displacement

FUR small displacement do, work will be dw. so

dw 2 T x do

dw =
$$\rho \in Sin0$$
 d0

Antegrating som Sides: $\int_{0}^{\omega} d\omega = \int_{0}^{0} \rho \in Sin0$ d0

$$\left[\omega\right]_{0}^{\omega} = \rho \in \left[-(0.50)_{0}^{0}\right]_{0}^{0} = -\rho \in \left[-(0.50)_{0}^{0}\right]_{0}^{0}$$

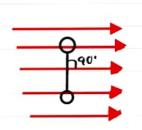
$$[\omega-0] z-\rho \in \int (0s\theta_z - (0s\theta_i))$$

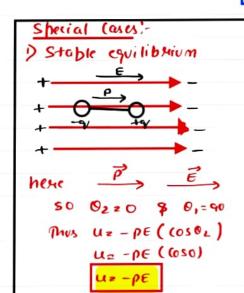
$$\omega = -\rho \in \int (0s\theta_z - (0s\theta_i))$$

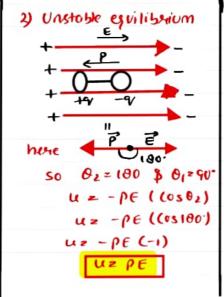
This work is converted into Potential energy Uz - PE[(0502 - (050,))

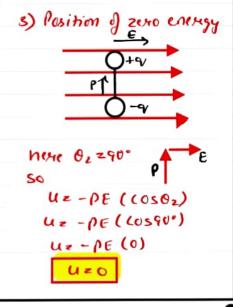
Now Let initially dipole is kept perpendicular to the electric field.

Then $0_1 = 90^{\circ}$ $u = -\rho \in \int (0.50_2 - (0.590)) = -\rho \in \int (0.592 - 0.590)$ $u = -\rho \in \int (0.50_2 - 0.590)$









(apositonce The electrical (apositance of a conductor is the caposity to hold

Copacitance = Charge Potential

ᆽ

 $C = \frac{Q}{V}$

02

(aparitance depends on :-

- 1) Size & shape of the Conductor
- 2) Nature of surrounding medium
- 3) Priesence of other Conductors near it.

SI unit of (apacitance is formed (f)

Parallel plate Copacitor

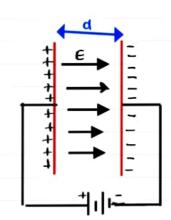
Let A = Amea of plate

d = distance blw plotes

T = Sumface change clessity

Q = change on each plate

Now capacitance = charge
Potential



Also,

Put 2,8 in () egn:

So Capacitance depends upon: 1) Asso of plate

- 2) Permittivity of me medium
- 3) distance 51w Motes

Capacitance in Sexies

when conocitous are aumanged in Series, charge on each capacitor is some = Q But Potential of each capacitor is different (V, almoss (1), (V2 conoss (2) & (V3 almoss (3)

Now using formula (= Q/V

for Conscitance 4:-

for copositance (2

For Capacitance Co

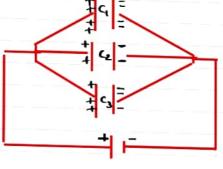
Total potential Une+ = VI+Vz+V3

$$\frac{Q}{Q} = \frac{C}{Q} + \frac{Q}{Q} + \frac{Q}{Q}$$

Capacitous in parallel

When Coparitures care consumped in ponallel voltage across each capacitus is some But change stored on each conacitor is different (Q, inc,), (Qz in (2) & (O3 in (3)

Now using formule C= 0



for Capacitance (:- for Capacitance (:-
$$C_{1} = \frac{\alpha_{1}}{V}$$

$$C_{1} = C_{2}$$

$$C_{2} = C_{2}$$

$$C_{3} = C_{4}$$

$$C_{4} = C_{4}$$

for Capacitance (2:-
$$\frac{C_2 = 0_2}{V}$$

$$0_2 = C_2 V$$

For Capacitance
$$C_3 = \frac{O_3}{V}$$

$$O_3 = C_3 V$$

Total charge, Onet = 01+0,+03 CNET V Z (IV + CZV+ GV

CHE+ = (+ C+ (3

Energy stored in a capacitor (No Perivotion, only formula in Syllabus)

Energy stored, $U = \frac{1}{2} CV^2$ on $U = \frac{1}{2} \frac{Q^2}{C}$ or $U = \frac{1}{2} QV$

Benaviour of Conductors in external field

When a Conclusion is placed inside an external electric field , the free electron procent inside the Constitute starts dufting towards the positive plate & the hositive ions of the conductor starts moving towards me negative plate. Due to which The electric field is set up inside the (modulary (Ei) This priviless continues till the internal electric field is equal to the external field. Now the two electric field (External field & internal electric field) Becomes equal inside the conductor. Thus Met electric field is zono.

Conductor No Hectric field Ene+ = Eo- Ei ENet = 0

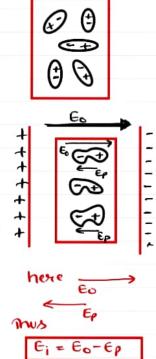
Behaviour of dielectric (Gasulatur) in external electric field

A cliefecturic is a type of gasulator which closs not have folian on non notion motionless which can be polarised in external electuric field.

When a dielectric is placed inside the external field the dipole present inside the dielectric starts motating in such a way, that -ve part of dipole points towards positive place & the part of dipole points towards negative place.

Due to the shifting of clipole, a small electric field is known cas Polanised Electric field (Ep). Nowever this electric field (Ep) however this electric field is never able to completely contends the external electric field.

Thus net electric field inside the dielectric



Dielectric Constant

Me leaste of extended electric field (6) to the Meduced electric field (9 mide Dielectric) is collect Cliclectric Contains (4) or sulprise permittivity.

 $K = \frac{\overrightarrow{E_o}}{\overrightarrow{E_i}} = \frac{\overrightarrow{E_o}}{\overrightarrow{E_o} - \overrightarrow{E_\rho}}$

Parallel plate Coparitor with dieletric

det A = Area of plate

d = distance blw plates

te thickness of dielectric

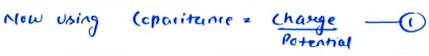
Ese External electric field

Ep = polarised electric field

Ei = Reduced electric field imide

Surgare change denity of Capacilon

Q > Change stored in plates.



we know surjuse charge density, $\sqrt{z} = \frac{Q}{A}$

Potential = Electric fixed x distance

$$V = (\text{ovside fixed x ovside distance}) + (\text{Smide field x 9mide distance})$$

 $V = (\text{Seo} \times (\text{d-t})) + (\text{Ei} \times \text{t})$

Putting eyn @ \$ 3 in eyn ()

here

Effect on Various hameters due to dielectric

Battery disconnected from the capacitor	Battery kept connected across the capacitor
$Q = Q_0$ (constant)	$Q = \kappa Q_0$
$V = \frac{V_0}{\kappa}$	$V = V_0$ (constant)
$E = \frac{E_0}{\kappa}$	$E = E_0$ (constant)
$C = \kappa C_0$	$C = \kappa C_0$
$U = \frac{U_0}{\kappa}$	$U = \kappa U_0$

here