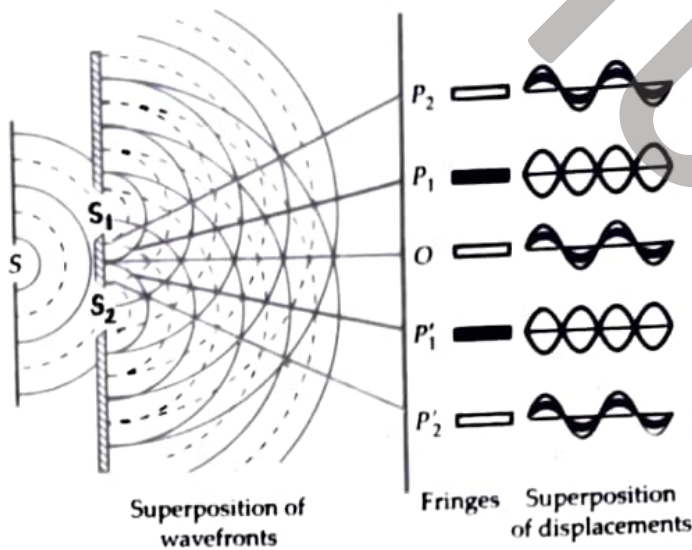
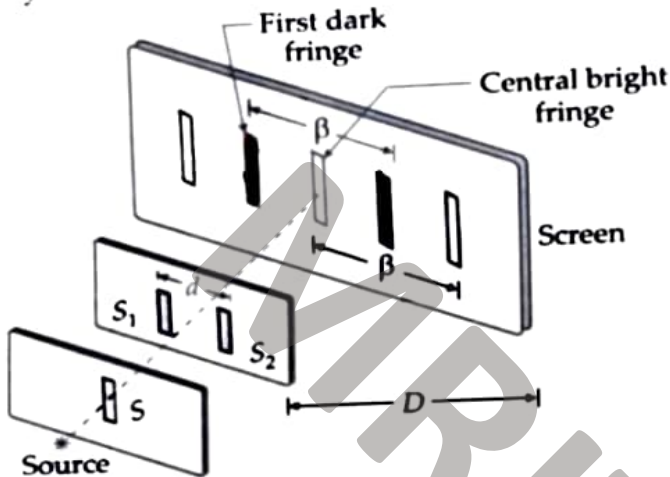


# WAVE OPTICS

## Young's Double Slit Experiment



Equation of light wave coming through  $S_1$   
 $y_1 = a_1 \sin \omega t$

Equation of light wave coming through  $S_2$   
 $y_2 = a_2 \sin(\omega t + \phi)$   
 where  $\phi$  is the phase difference.

Then, Resultant wave:-

$$y = y_1 + y_2$$

$$\rightarrow y = A \sin(\omega t + \theta)$$

where  $A$  = Amplitude of Resultant wave

$$\rightarrow A^2 = a_1^2 + a_2^2 + 2a_1a_2 \cos \phi$$

$A$  = Amplitude of Resultant wave  
 $a_1$  = Amplitude of wave through  $S_1$   
 $a_2$  = Amplitude of wave through  $S_2$   
 $\phi$  = phase difference

$$\rightarrow \text{Intensity} = k (\text{Amplitude})^2$$

$$I = kA^2$$

where  $k$  = constant

$$\rightarrow I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi$$

$I$  = Intensity of Resultant wave  
 $2\sqrt{I_1 I_2} \cos \phi$  = Interference term

## For constructive interference:-

phase difference,  $\phi = 0, 2\pi, 4\pi, \dots$

$$\phi = 2n\pi \quad \text{where } n = 0, 1, 2, \dots$$

path difference,  $p = 0, d, 2d, 3d, \dots$

$$p = n\lambda \quad \text{where } n = 0, 1, 2, \dots$$

## For destructive interference

phase difference,  $\phi = \pi, 3\pi, 5\pi, \dots$

$$\phi = (2n-1)\pi \quad \text{where } n = 1, 2, 3, \dots$$

path difference,  $p = \frac{\lambda}{2}, \frac{3\lambda}{2}, \frac{5\lambda}{2}, \dots$

$$p = (2n-1)\frac{\lambda}{2} \quad \text{where } n = 1, 2, 3, \dots$$

## Maximum and minimum amplitude

We know,  $A^2 = a_1^2 + a_2^2 + 2a_1a_2 \cos \phi$

Maximum amplitude:-

Amplitude will be maximum when  $\phi = 0, 2\pi, 4\pi \dots$  (Constructive Interference)

$$A^2 = a_1^2 + a_2^2 + 2a_1a_2 \cos 0$$

$$A^2 = a_1^2 + a_2^2 + 2a_1a_2 (1) \quad (\because \cos 0 = 1)$$

Now,

If  $a_1 = a$  &  $a_2 = a$  (Both slits produce light of same amplitude)

Then,

$$A^2 = a^2 + a^2 + 2aa = a^2 + a^2 + 2a^2$$

$$A^2 = 4a^2$$

$$A = \sqrt{4a^2} = 2a$$

$$A = 2a$$

(Total amplitude = 2 × Amplitude of any slit)

Minimum Amplitude:-

$$A^2 = a_1^2 + a_2^2 + 2a_1a_2 \cos \phi$$

Amplitude will be minimum when  $\phi = \pi, 3\pi, 5\pi \dots (2n-1)\pi$

So,

$$A^2 = a_1^2 + a_2^2 + 2a_1a_2 \cos \pi$$

$$A^2 = a_1^2 + a_2^2 + 2a_1a_2 (-1) = a_1^2 + a_2^2 - 2a_1a_2$$

If  $a_1 = a$  and  $a_2 = a$  (Both slits produce light of same amplitude)

Then

$$A = a^2 + a^2 - 2aa = 2a^2 - 2a^2$$

$$A = 0$$

(Total amplitude = 0)

## Maximum and minimum intensity

Maximum intensity.

$$I = I_1 + I_2 + 2\sqrt{I_1I_2} \cos \phi$$

Intensity will be maximum when  $\phi = 0, 2\pi, 4\pi \dots$  (Constructive Interference)

$$I = I_1 + I_2 + 2\sqrt{I_1I_2} \cos 0$$

$$I = I_1 + I_2 + 2\sqrt{I_1I_2} (1) \quad (\because \cos 0 = 1)$$

$$I = (\sqrt{I_1} + \sqrt{I_2})^2$$

Now

If  $I_1 = I'$  &  $I_2 = I'$  (Both slits produce light of same intensity)

$$I = I' + I' + 2\sqrt{I'I'}$$

$$I = 2I' + 2I'$$

$$I = 4I'$$

(So Intensity becomes 4 times)



## Minimum Intensity

$$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi$$

Intensity will be minimum when  $\phi = \pi, 3\pi, 5\pi, \dots$  (Destructive Interference)

$$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \pi$$

$$I = I_1 + I_2 + 2\sqrt{I_1 I_2} (-1) \quad (\because \cos \pi = -1)$$

Now

$$I = (\sqrt{I_1} - \sqrt{I_2})^2$$

eg  $I_1 = I'$  &  $I_2 = I'$  (Both slits produce light of same Intensity)

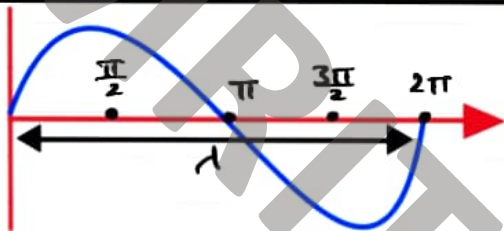
$$I = I' + I' + 2\sqrt{I'I'} (-1)$$

$$I = 2I' - 2I'$$

$$I = 0$$

(so Intensity becomes zero)

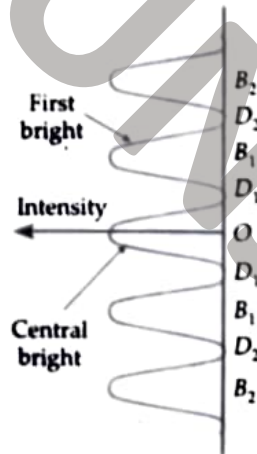
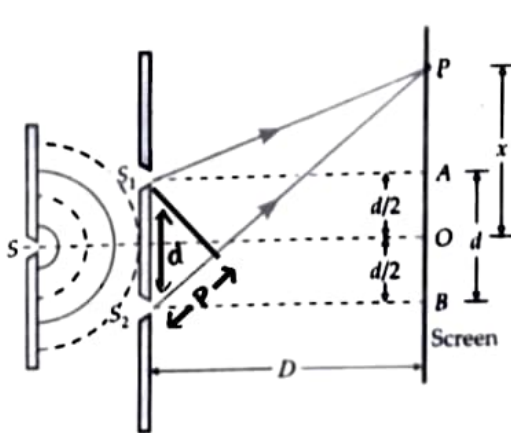
## Comparison b/w Phase and path difference



for a complete wave  
Path difference = phase difference

$$\lambda = 2\pi$$

## Distance of fringes from the center of screen



here

$p$  = path difference

$d$  = distance b/w slits

$D$  = distance b/w screen & slit

$n$  = no. of fringe

$\lambda$  = wavelength

for Bright fringe:-

$$p = \frac{x d}{D} = n \lambda$$

Then

$$x = \frac{n D \lambda}{d}$$

where  $x$  = Distance from centre of screen

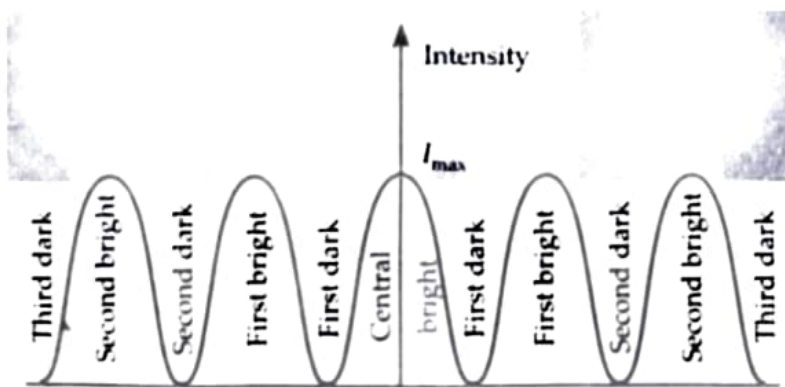
for Dark fringe:-

$$p = \frac{x d}{D} = (2n-1) \frac{\lambda}{2}$$

Then

$$x = (2n-1) \frac{D \lambda}{2d}$$

$x$  = Distance from center of screen.



Graph of Intensities

Fringe width:- It is the separation between two successive bright or dark fringe. It is denoted by  $\beta$ .

width of a dark fringe = separation b/w two consecutive bright fringe  
 $\beta = x_n - x_{n-1} = \frac{nDd}{d} - \frac{(n-1)Dd}{d}$

$$\beta = \frac{Dd}{d}$$

## Wavefront and Types of wavefront

A wavefront is defined as the continuous locus of all such particles of the medium which are vibrating in the same phase at any instant.

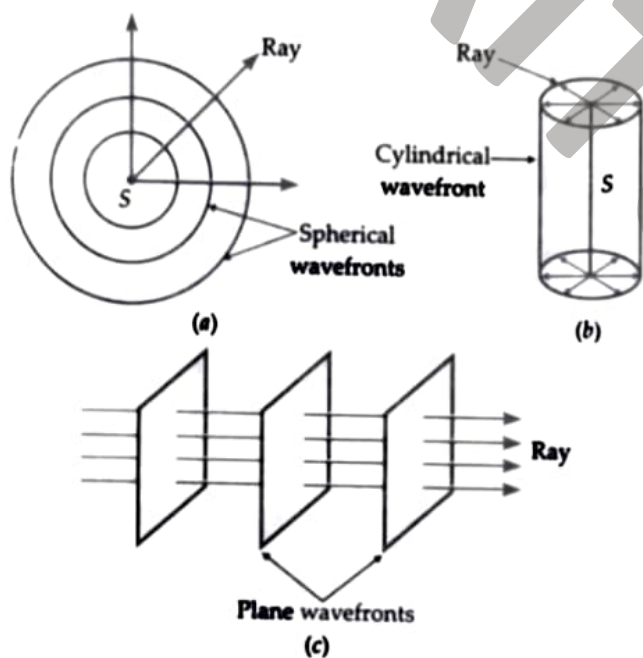


Fig. 9.1 Different types of wavefronts.

## Relation b/w Ray and wavefront

An arrow drawn perpendicular to a wavefront in the direction of propagation of a wave is called a ray.

A ray of light represents the path along which light travels.

This illustrates two general principles:

1. Rays are perpendicular to wavefronts.
2. The time taken for light to travel from one wavefront to another is the same along any ray.

In case of a plane wavefront, the rays are parallel [Fig. 9.2(a)]. A group of parallel rays is called a beam of light. In case of a spherical wavefront, the rays either converge to a point [Fig. 9.2(b)] or diverge from a point [Fig. 9.2(c)].

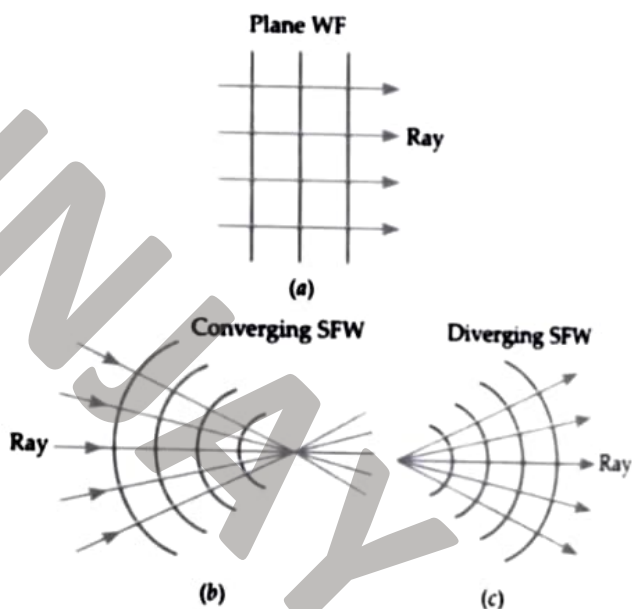


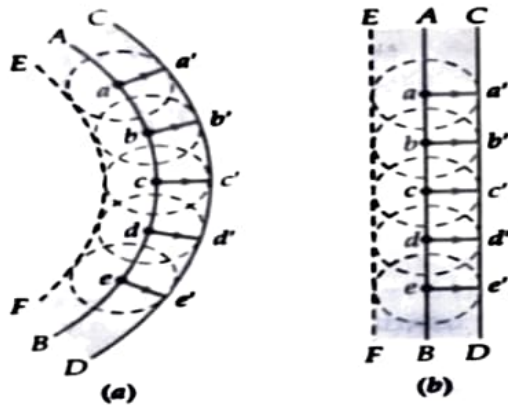
Fig. 9.2 Wavefronts and corresponding rays in three cases (a) plane, (b) converging spherical and (c) diverging spherical.

## Huygen's Principle

This principle is based on the following assumptions:

1. Each point on a wavefront acts as a fresh source of new disturbance, called secondary waves or wavelets.
2. The secondary wavelets spread out in all directions with the speed of light in the given medium.
3. The new wavefront at any later time is given by the forward envelope (tangential surface in the forward direction) of the secondary wavelets at that time.





## Reflection on the basis of Huygen's Theory

**Laws of reflection on the basis of Huygens' wave theory.** As shown in Fig. 9.4, consider a plane wavefront AB incident on the plane reflecting surface XY, both the wavefront and the reflecting surface being perpendicular to the plane of paper.

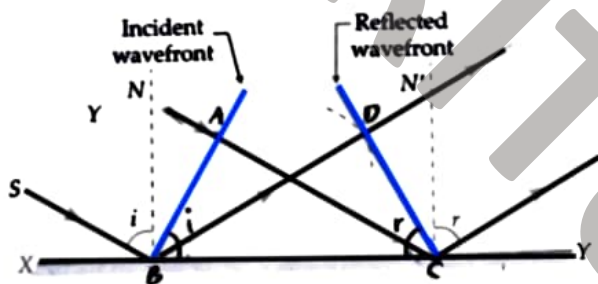


Fig. 9.4 Wavefronts and corresponding rays for reflection from a plane surface.

First the wavefront touches the reflecting surface at B and then at the successive points towards C. In accordance with Huygens' principle, from each point on BC, secondary wavelets start growing with the speed  $c$ . During the time the disturbance from A reaches the point C, the secondary wavelets from B must have spread over a hemisphere of radius  $BD = AC = ct$ , where  $t$  is the time taken by the disturbance to travel from A to C. The tangent plane CD drawn from the point C over this hemisphere of radius  $ct$  will be the new reflected wavefront.

Let angles of incidence and reflection be  $i$  and  $r$  respectively. In  $\triangle ABC$  and  $\triangle DCB$ , we have

$$\angle BAC = \angle CDB \quad [\text{Each is } 90^\circ]$$

$$BC = BC \quad [\text{Common}]$$

$$AC = BD \quad [\text{Each is equal to } ct]$$

$$\therefore \triangle ABC \cong \triangle DCB$$

$$\text{Hence } \angle ABC = \angle DCB$$

$$\text{or } \angle i = \angle r$$

i.e., the angle of incidence is equal to the angle of reflection.  
This proves the first law of reflection.

## Refraction on the basis of Huygen's

**theory.** Consider a plane wavefront AB incident on a plane surface XY, separating two media 1 and 2, as shown in Fig. 9.5. Let  $v_1$  and  $v_2$  be the velocities of light in the two media, with  $v_2 < v_1$ .

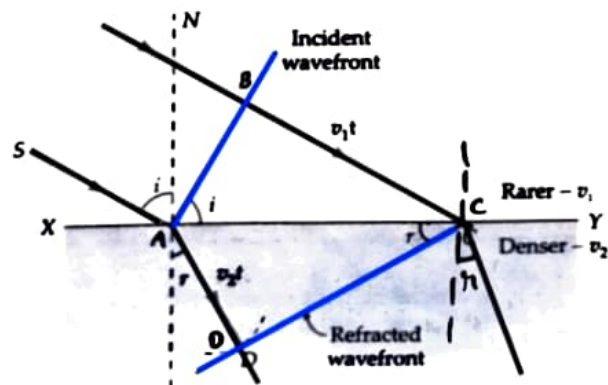


Fig. 9.5 Wavefronts and corresponding rays for refraction by a plane surface separating two media.

The wavefront first strikes at point A and then at the successive points towards C. According to Huygens' principle, from each point on AC, the secondary wavelets start growing in the second medium with speed  $v_2$ . Let the disturbance take time  $t$  to travel from B to C, then  $BC = v_1 t$ . During the time the disturbance from B reaches the point C, the secondary wavelets from point A must have spread over a hemisphere of radius  $AD = v_2 t$  in the second medium. The tangent plane CD drawn from point C over this hemisphere of radius  $v_2 t$  will be the new refracted wavefront.

Let the angles of incidence and refraction be  $i$  and  $r$  respectively.

From right  $\triangle ABC$ , we have

$$\sin \angle BAC = \sin i = \frac{BC}{AC}$$

From right  $\triangle ADC$ , we have

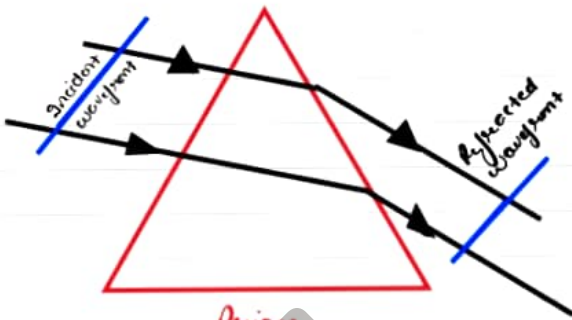
$$\sin \angle DCA = \sin r = \frac{AD}{AC}$$

$$\therefore \frac{\sin i}{\sin r} = \frac{BC}{AD} = \frac{v_1 t}{v_2 t}$$

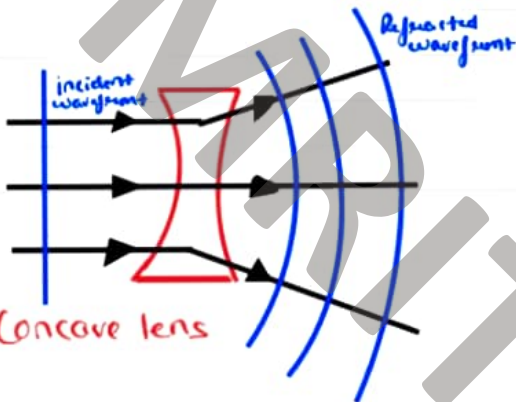
$$\text{or } \frac{\sin i}{\sin r} = \frac{v_1}{v_2} = {}^1\mu_2 \quad (\text{a constant})$$

This proves **Snell's law of refraction**. The constant  ${}^1\mu_2$  is called the **refractive index** of the second medium with respect to first medium.

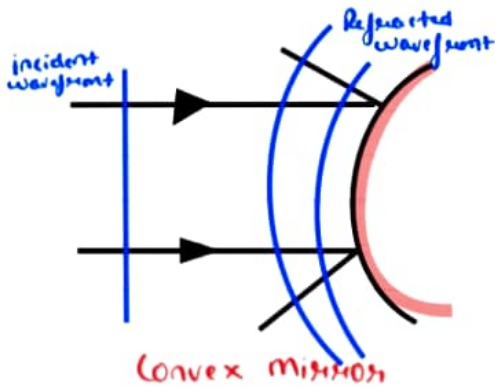
## Behaviour of lens, Prism and Mirror



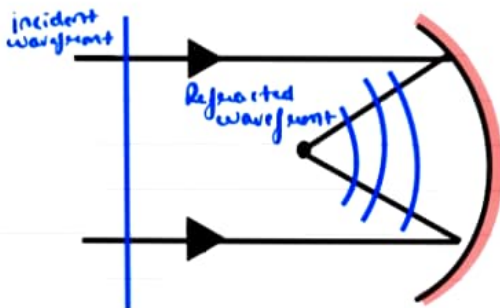
Prism



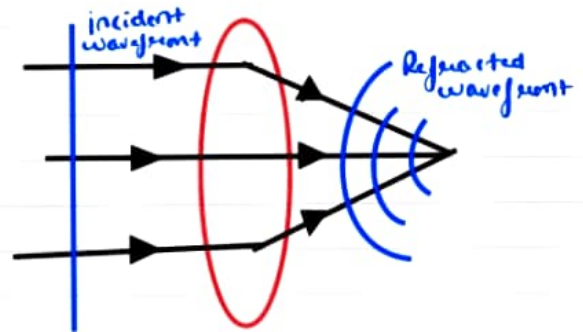
Concave lens



Convex mirror



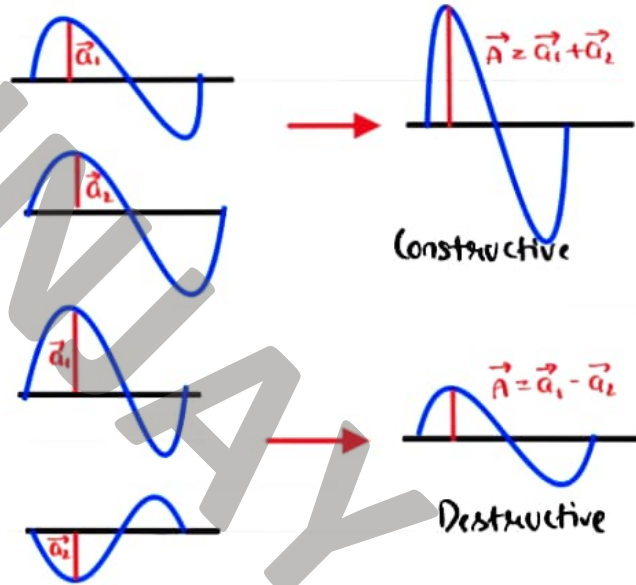
Concave mirror



Convex lens

## Principle of Superposition

When a number of waves travelling through a medium superpose on each other, the resultant displacement at any point at a given instant is equal to the vector sum of the displacements due to the individual waves at that point.



## Interference of light

Interference of light. When two light waves of the same frequency and having zero or constant phase difference travelling in the same direction superpose each other, the intensity in the region of superposition gets redistributed, becoming maximum at some points and minimum at others. This phenomenon is called interference of light.



## Coherent and Incoherent Sources

**Coherent and incoherent sources:** Two sources of light which continuously emit light waves of same frequency (or wavelength) with a zero or constant phase difference between them, are called **coherent sources**.

Two sources of light which do not emit light waves with a constant phase difference are called **incoherent sources**.

**Conditions for obtaining two coherent sources of light:**

1. The two sources of light must be obtained from a single source by some method. Then the relative phase difference between the two light waves from the sources will remain constant with time.

2. The two sources must give monochromatic light. Otherwise, different colours will produce different interference patterns and fringes of different colours will overlap.

3. The path difference between the waves arriving on the screen from the two sources must not be large. It should not exceed 30 cm. Then the phase difference produced due to path difference will not be constant. There will be general illumination on the screen.

## Sustained Interference

The interference pattern, in which the positions of maxima and minima of intensity on the observation screen do not change with time, is called a **sustained or permanent interference pattern**.

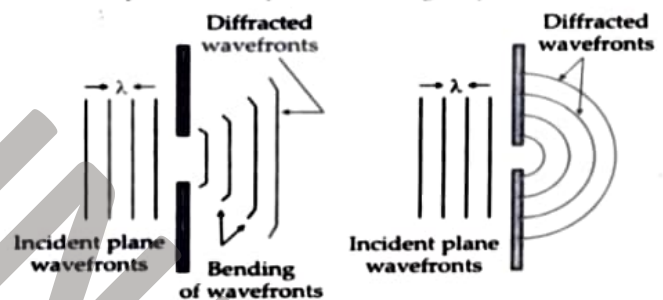
**Conditions for sustained interference:** The necessary conditions for obtaining a sustained and observable interference pattern of light are as follows:

1. The two sources should continuously emit waves of same frequency or wavelength.
2. The two sources of light should be **coherent**, i.e., they must vibrate either in the same phase or with a constant phase difference between them.
3. For a better contrast between maxima and minima of intensity, the amplitudes of the interfering waves should be equal.
4. The two sources should be narrow, otherwise interference will occur between waves of different parts of the same source and contrast will be poor.
5. The interfering waves must travel nearly along the same direction.
6. The sources should be **monochromatic**, otherwise fringes of different colours will overlap just to give a few observable fringes.

## Diffraction

The phenomenon of bending of light around the corners of small obstacles or apertures and its consequent spreading into the regions of geometrical shadow is called **diffraction of light**.

**Size of aperture or obstacle for observing diffraction.** Suppose plane waves are made to fall on a screen having a small aperture. The waves emerging out of the aperture are observed to be slightly curved at the edges. This is diffraction. If the size of the aperture is large compared to the wavelength of the waves, the amount of bending is small [Fig. 9.20(a)]. If the size of the aperture is small, comparable to the wavelength  $\lambda$  of the waves, then the diffracted waves are almost spherical [Fig. 9.20(b)]. Hence the diffraction effect is more pronounced if the size of the aperture or the obstacle is of the order of the wavelength of the waves.



## Diffraction due to single slit

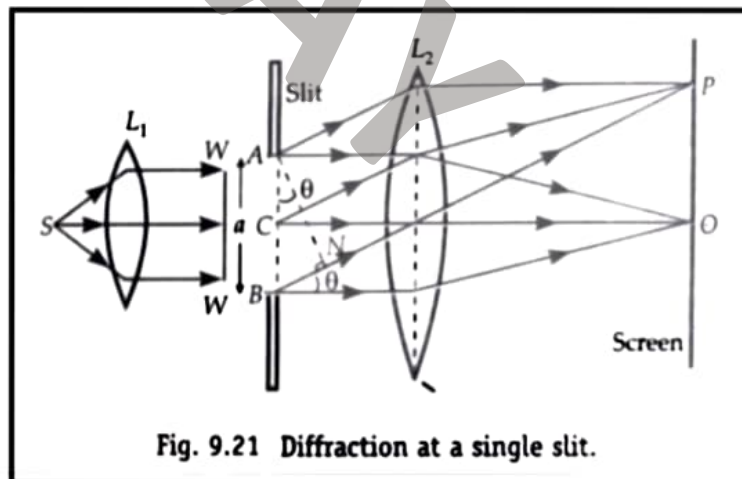


Fig. 9.21 Diffraction at a single slit.

## > Explanation of diffraction fringes

**Central maximum.** All the wavelengths going straight ( $\theta = 0^\circ$ ) across the slit are focussed at the central point O of the screen, as shown in Fig. 9.23. The wavelets from any two corresponding points such as (0, 12), (2, 10), (4, 8) etc. from the two halves of the slit have zero path difference. They undergo constructive interference to produce central bright fringe.

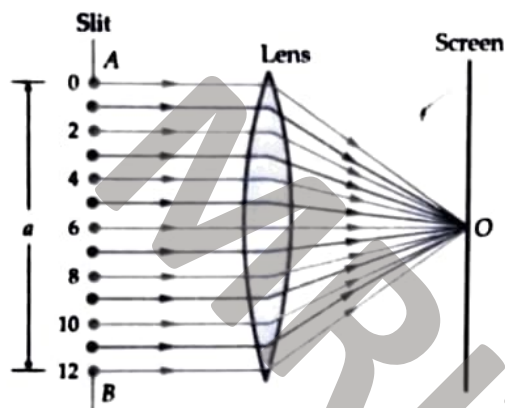
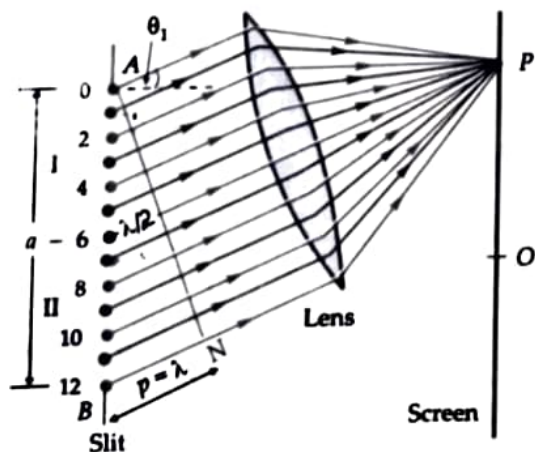


Fig. 9.23 Diffraction at angle  $\theta = 0^\circ$ .

**First dark fringe.** If angle  $\theta$  is such that the path difference,  $p = a \sin \theta = \lambda$ , then the path difference between the rays from A and B when they reach P is  $\lambda$ , as shown in Fig. 9.24. If we divide the slit into two halves I and II, of 6 parts each, then obviously the wavelets from 0 and 6 will have a path difference of  $\lambda/2$  or a phase difference of  $\pi$ . They interfere destructively. Similarly, the wavelet pairs (1, 7), (2, 8), (3, 9), (4, 10), (5, 11) and (6, 12) of the two halves will interfere destructively. Hence the condition for first dark fringe is

$$a \sin \theta = \lambda$$



**First secondary maximum.** Suppose the angle  $\theta$  is such that the path difference,  $p = a \sin \theta = 3\lambda/2$ .

We can divide the slit into three equal regions I, II and III, as shown in Fig. 9.25. The path difference between any two corresponding points of regions I and II will be  $\frac{\lambda}{2}$  or phase difference will be  $\pi$ . The wavelets from

these points will interfere destructively. The wavelets from III region of the slit will contribute to some intensity forming a secondary maximum. The intensity of this maximum is much less than the central maximum. The condition for the first secondary maximum can be written as

$$a \sin \theta = \frac{3}{2} \lambda$$

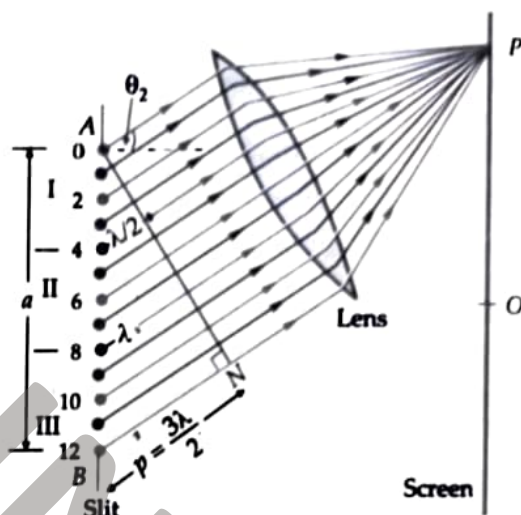


Fig. 9.25 Diffraction at an angle  $\theta$  given by  $a \sin \theta = 3/2 \lambda$ .

## Graph of Diffraction Pattern

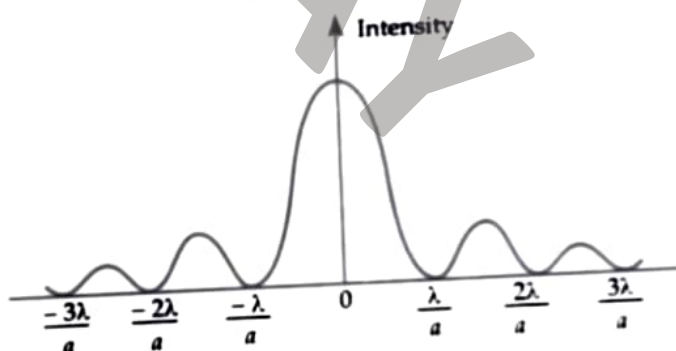


Fig. 9.22 Variation of intensity with angle  $\theta$  in single slit diffraction.



## Mathematical Expression of Diffraction

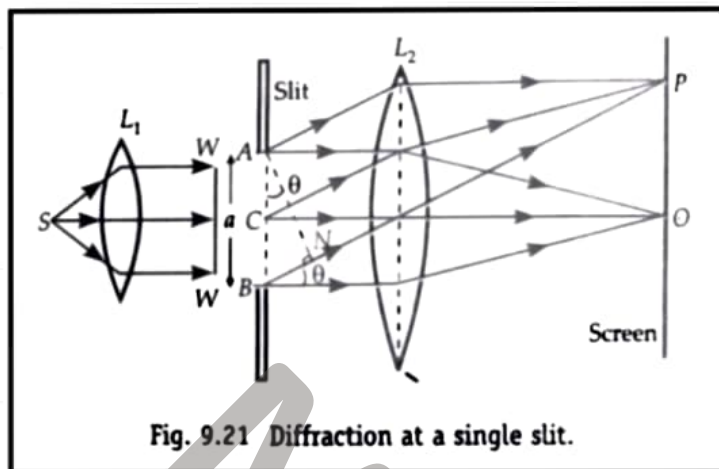


Fig. 9.21 Diffraction at a single slit.

From above diagram,  $BN = \text{Path difference}$   
In  $\triangle ABN$

$$\sin \theta = \frac{BN}{AB}$$

Then,  $BN = AB \sin \theta$

$$P = a \sin \theta \quad (\because BN = P)$$

Now, for first dark fringe ( $P = \lambda$ )

$$a \sin \theta = \lambda$$

for Second dark fringe ( $P = 2\lambda$ )

$$a \sin \theta = 2\lambda$$

So general formula for dark fringe

$$a \sin \theta = n\lambda \quad \text{where } n = 1, 2, 3, \dots$$

Angular position of dark fringe (minima)

As, for dark fringe

$$a \sin \theta = n\lambda$$

when  $\theta \approx \sin \theta$

$$\text{Then, } \theta = \frac{n\lambda}{a}$$

for Central maxima

There will be no path difference  $P = 0$

for first Secondary maxima ( $P = \frac{3}{2}\lambda$ )

$$a \sin \theta = \frac{3}{2}\lambda$$

for Second Secondary maxima  
( $P = \frac{5}{2}\lambda$ )

$$a \sin \theta = \frac{5}{2}\lambda$$

general formula for Secondary maxima

$$a \sin \theta = (2n+1) \frac{\lambda}{2}$$

Angular position of Secondary maxima

When  $\theta \approx \sin \theta$ . Then,  $\theta = (2n+1) \frac{\lambda}{2a}$

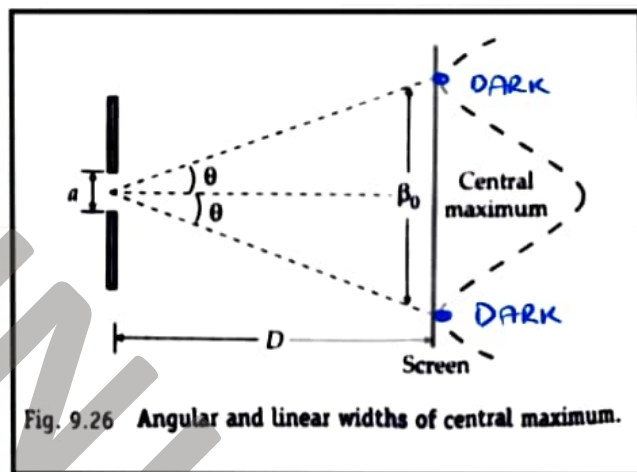


Fig. 9.26 Angular and linear widths of central maximum.

for first dark fringe ( $n=1$ )

$$a \sin \theta = n\lambda$$

we take  $\sin \theta \approx \theta$  and  $n=1$

$$a\theta = \lambda$$

Then

$$\theta = \frac{\lambda}{a}$$

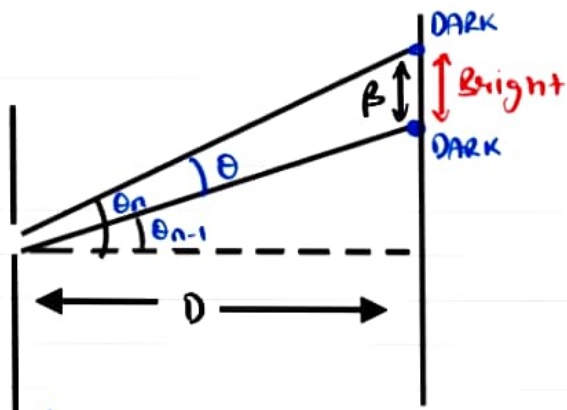
Angular width of central maxima =  $2\theta$

$$2\theta = \frac{2\lambda}{a}$$

Linear width of central maxima =  $P_0$

$$P_0 = D \times 2\theta$$

$$P_0 = \frac{2D\lambda}{a}$$



for Dark

$$\theta_n = \frac{n\lambda}{a} \quad \text{and} \quad \theta_{n-1} = \frac{(n-1)\lambda}{a}$$

Then  $\theta = \theta_n - \theta_{n-1}$

Angular width of any maxima

$$\theta = \theta_n - \theta_{n-1}$$

$$\theta = \frac{n\lambda}{a} - \frac{(n-1)\lambda}{a}$$

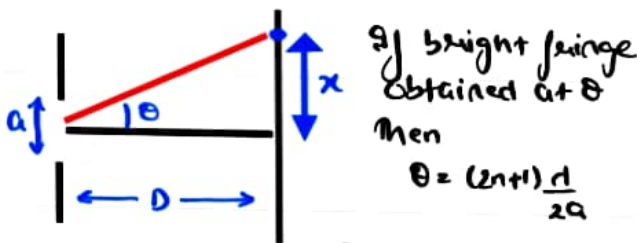
$$\theta = \frac{\lambda}{a}$$

Linear width of any maxima

$$\beta = D \times \theta$$

$$\beta = \frac{\lambda D}{a}$$

Distance from the centre



if bright fringe obtained at  $\theta$

then

$$\theta = (2n+1) \frac{\lambda}{2a}$$

Then, using  $\theta = \frac{x}{D}$

we get  $\theta = \frac{x}{D}$

for Bright fringe

$$x = \theta D = (2n+1) \frac{\lambda D}{2a}$$

if Dark fringe is obtained at  $\theta$ .

Then,  $\theta = \frac{n\lambda}{a}$  - Again by  $\theta = \frac{x}{D}$

for Dark fringe

$$x = \theta D = \frac{n\lambda D}{a}$$

## Diffraction vs Interference

Interference	Diffraction
1. Interference is the result of superposition of secondary waves starting from two different wavefronts originating from two coherent sources.	Diffraction is the result of superposition of secondary waves starting from different parts of the same wavefront.
2. All bright and dark fringes are of equal width.	The width of central bright fringe is twice the width of any secondary maximum.
3. All bright fringes are of same intensity.	Intensity of bright fringes decreases as we move away from central bright fringe on either side.
4. Regions of dark fringes are perfectly dark. So there is a good contrast between bright and dark fringes.	Regions of dark fringes are not perfectly dark. So there is a poor contrast between bright and dark fringes.
5. At an angle of $\lambda/d$ , we get a bright fringe in the interference pattern of two narrow slits separated by a distance $d$ .	At an angle of $\lambda/a$ , we get the first dark fringe in the diffraction pattern of a single slit of width $a$ .

## Fresnel and Fraunhofer Diffraction

**Two types of diffraction.** The diffraction phenomena can be divided into two categories :

1. **Fresnel's diffraction.** In Fresnel's diffraction, the source and screen are placed close to the aperture or the obstacle and light after diffraction appears

converging towards the screen and hence no lens is required to observe it. The incident wave fronts are either spherical or cylindrical.

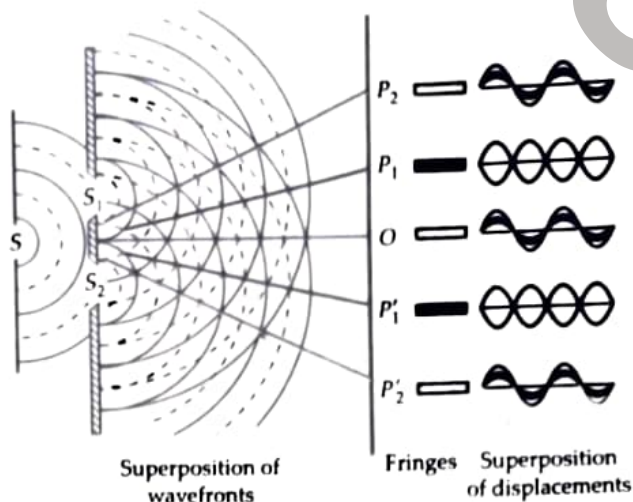
2. **Fraunhofer's diffraction.** In Fraunhofer's diffraction, the source and screen are placed at large distances (effectively at infinity) from the aperture or the obstacle and converging lens is used to observe the diffraction pattern. The incident wavefront is planar one.



## Young's Double Slit Experiment

In this experiment, a source of monochromatic light (e.g., a sodium vapour lamp) illuminates a rectangular narrow slit S, about 1 mm wide, as shown in Fig. 9.11.  $S_1$  and  $S_2$  are two parallel narrow slits which are arranged symmetrically and parallel to the slit S at a distance of about 10 cm from it. The separation between  $S_1$  and  $S_2$  is  $\approx 2$  mm and width of each slit is  $\approx 0.3$  mm. An observation screen is placed at a distance of  $\approx 2$  m from the two slits. **Alternate bright and dark bands appear on the observation screen. These are called *interference fringes*.** When one of the slits,  $S_1$  or  $S_2$  is closed, bright and dark fringes disappear and the **intensity of light becomes uniform.**

**Explanation.** Fig. 9.12 shows a section of Young's experiment in the plane of paper. According to Huygens' principle, cylindrical wavefronts emerge out from slit S, whose sections have been shown by circular arcs. The solid curves represent crests and the dotted curves represent troughs. As  $SS_1 = SS_2$ , these waves fall on the slits  $S_1$  and  $S_2$  simultaneously so that the waves spreading out from  $S_1$  and  $S_2$  are in the same phase. Thus  $S_1$  and  $S_2$  act as two *coherent sources* of monochromatic light. Interference takes place between the waves diverging from these sources.



At the lines leading to O,  $P_2$  and  $P_2'$ , the crest of one wave falls over the crest of other wave or the trough of one wave falls over the trough of other wave, the amplitudes of the two waves get added up and hence the intensity ( $I \propto a^2$ ) becomes maximum. This is called **constructive interference**. At the lines leading to  $P_1$  and  $P_1'$ , the crest of one wave falls over the trough of other or the trough of one wave falls over the crest of other wave, the amplitudes of the two waves get subtracted and hence the intensity becomes minimum. This is called **destructive interference**. So on the observation screen, we obtain a number of alternate bright and dark fringes, parallel to the two slits.

## Diffraction through Single Slit

Diffraction at a single slit. As shown in Fig. 9.21, a source S of monochromatic light is placed at the focus of a convex lens  $L_1$ . A parallel beam of light and hence a plane wavefront WW gets incident on a narrow rectangular slit AB of width  $a$ .

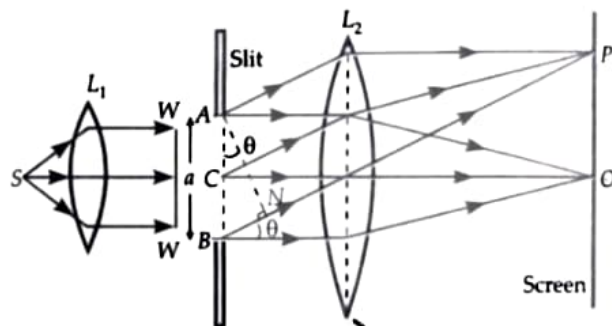


Fig. 9.21 Diffraction at a single slit.

**Central maximum.** All the secondary wavelets going straight across the slit AB are focussed at the central point O of the screen. The wavelets from any two corresponding points of the two halves of the slit reach the point O in the same phase, they add constructively to produce a *central bright fringe*. For detailed explanation of diffraction fringes, see *For Your Knowledge box* on page 9.32.

**Calculation of path difference.** Suppose the secondary wavelets diffracted at an angle  $\theta$  are focussed at point P. The secondary wavelets start from different parts of the slit in same phase but they reach the point P in different phases. Draw perpendicular AN from A on to the ray from B. Then the path difference between the wavelets from A and B will be

$$p = BP - AP = BN = AB \sin \theta = a \sin \theta.$$

**Positions of minima.** Let the point P be so located on the screen that the path difference,  $p = \lambda$  and angle  $\theta = \theta_1$ . Then from the above equation, we get

$$a \sin \theta_1 = \lambda$$

We can divide the slit AB into two halves AC and CB. Then the path difference between the wavelets from A and C will be  $\frac{\lambda}{2}$ . Similarly, corresponding to every point in the upper half AC, there is a point in the lower half CB for which the path difference is  $\frac{\lambda}{2}$ . Hence the wavelets from the two halves reach the point P always in opposite phases. They interfere destructively so as to produce a minimum.

Thus the condition for **first dark fringe** is

$$a \sin \theta_1 = \lambda$$

Similarly, the condition for **second dark fringe** will be

$$a \sin \theta_2 = 2\lambda$$

Hence the condition for  **$n$ th dark fringe** can be written as

$$a \sin \theta_n = n\lambda, \quad n = 1, 2, 3, \dots$$

The directions of various minima are given by

$$\theta_n \approx \sin \theta_n = n \frac{\lambda}{a}$$

[As  $\lambda \ll a$ , so  $\sin \theta_n \approx \theta_n$ ]

Positions of secondary maxima. Suppose the point  $P$  is so located that  $p = \frac{3\lambda}{2}$

$$\text{When } \theta = \theta'_1, \text{ then } a \sin \theta'_1 = \frac{3}{2} \lambda$$

We can divide the slit into three equal parts. The path difference between two corresponding points of the first two parts will be  $\frac{\lambda}{2}$ . The wavelets from these

points will interfere destructively. However, the wavelets from the third part of the slit will contribute to some intensity forming a secondary maximum. The intensity of this maximum is much less than that of the central maximum.

Thus the condition for the **first secondary maximum** is

$$a \sin \theta'_1 = \frac{3}{2} \lambda$$

Similarly, the condition for the **second secondary maximum** is

$$a \sin \theta'_2 = \frac{5}{2} \lambda$$

Hence the condition for  **$n$ th secondary maximum** can be written as

$$a \sin \theta'_n = (2n + 1) \frac{\lambda}{2}, \quad n = 1, 2, 3, \dots$$

The directions of secondary maxima are given by

$$\theta'_n \approx \sin \theta'_n = (2n + 1) \frac{\lambda}{2a}$$

The intensity of secondary maxima decreases as  $n$  increases.