# ELECTRIC CHARGES AND FIELD

Electric charge

Electric charge is an intrinsic property of handid of motter which give rise to electric force between muse particles

Electric charge is a scalar quantity.

A proton has (+) positive charge and an electron has (-) negative charge charge on min -> ez 1.6×10-19 womb

# Basic properties of charge.

1) Additivity = Additivity of electric charge means that the total charge of change of a system is the algebric sum of all the individual changes located at different points

Q = 91+92+93 - - - + 91

2) The total charge of a body is aways an Quantization = of charge integral multiple of a charge.

where 1=0/±1/±2--etc

1) The total charge of an isolated system rumains (onservation = of charge Contant 4) The electric change can neither be cheated non destroyed they can only be transferred from one body to another.

#### Couloms's law of ekithic force

The fourse of attraction on repulsion between two charges is directly proportional to the product of magnitude of changes

Fx q1xq2

inversly proportional to the square of clistance between them.

> FX 1/42 Combining 50th

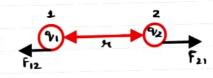
For gix que Now Fz 1 4180 412

Es & permittivity of free space

Let fel = force on change 2 due to change 1

fiz = force on change 1 due to change 2

Now from covoms's law



In vector form

F21 = 1 919/2

F21 = 1 9192 A12

here fire is a unit vector got tells the direction of force is from change 1 to 2

Similorly

UH F12 = 1 CV192 421

Phinciple of Supemposition

At states that when a number of charge are present, the total jurce on a given charge is the vector Sum of the jurce exerted on it due to an other charges.

The furice between two charges is not offected by the presence of other charges.

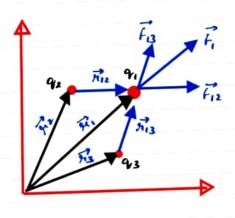
# furice between multiple changes

According to puinciple of superposition, the total force on change quis

F1 = F12 + F13 + F14 + FIN

here  $\overline{F}_{12}$  = funce on change 1 due to change 2  $\overline{F}_{13}$  = forme on change 1 due to change 3

Fin z force on charge 1 due to charge or



Now 90 vector form:

Fiz = 1 9192 412 -0

hem thingle law of adolition

Then This = This

Then eg 1 (1):-

F12 = 1 411 919/2 3 14- 1/2

Similarly 
$$\overrightarrow{F}_{13} = \underbrace{1}_{\text{UTIE}} \underbrace{9_{1}9_{3}}_{(\overrightarrow{F}_{1}-\overrightarrow{F}_{3})} \xrightarrow{\overrightarrow{F}_{1}} \overrightarrow{F}_{3} \longrightarrow 3$$

Total force on charge 1 is
$$\frac{F_1}{F_1} = F_{12} + F_{13} + F_{14} - - - + F_{10}$$
Using egn 2 & 1

$$\vec{F}_{1} = \left[\frac{1}{4\pi} \frac{c_{V_{1}}c_{V_{2}}}{|\vec{F}_{1}-\vec{F}_{2}|^{2}} \vec{F}_{1}-\vec{h}_{2}\right] + \left[\frac{1}{4\pi} \frac{c_{V_{1}}c_{V_{3}}}{|\vec{F}_{1}-\vec{F}_{1}|^{2}} \vec{F}_{1}-\vec{h}_{3}\right] + - - - + \left[\frac{1}{4\pi} \frac{c_{V_{1}}c_{V_{3}}}{|\vec{F}_{1}-\vec{F}_{1}|^{2}} \vec{F}_{1}-\vec{h}_{N}\right]^{3}$$

$$+ - - - + \left[\frac{c_{V_{1}}c_{V_{3}}}{4\pi} \vec{F}_{1}-\vec{h}_{N}\right]^{3} \vec{F}_{1}-\vec{h}_{N}\right]$$

$$+ - - - + \left[\frac{c_{V_{N}}}{|\vec{F}_{1}-\vec{F}_{1}|^{2}} \vec{F}_{1}-\vec{h}_{N}\right]^{3}$$

$$+ - - - + \left[\frac{c_{V_{N}}}{|\vec{F}_{1}-\vec{F}_{1}|^{2}} \vec{F}_{1}-\vec{h}_{N}\right]^{3}$$

$$\overrightarrow{F_{1}} = \frac{c_{V_{1}}}{c_{1}\pi\xi_{0}} \sum_{\lambda=2}^{\lambda=N} \frac{c_{V_{1}}}{|\overrightarrow{h_{1}}-\overrightarrow{h}_{\lambda}|^{3}} \overrightarrow{h_{1}} - \overrightarrow{h}_{\lambda}$$

Thus force on any at change:
$$\vec{F_{\alpha}} = \frac{c_{V\alpha}}{v_{ITI} \epsilon_{0}} \sum_{\substack{n=1 \\ n \neq \alpha}}^{\infty} \frac{c_{V\alpha}}{|\vec{H_{\alpha}} - \vec{H_{\alpha}}|^{2}} \vec{R_{\alpha}} \vec{$$

field The electric field at a point is elyined as the June experienced by a unit positive test change placed at that point.

It is a vector Quantity. Electric field is from the charge towards -ve.

## Electric field due to a point change

Consider a charge a is placed at Point 0 . We have to find electric field at point P. Let us put a test charge go on P:-NOW Force on go:

## Continuous charge distribution

- i) Linear change distribution (1) Change stoned pen unit length of a wine the
- Surface charge distribution (5) 2) charge stored ber unit Area.
- Volume change distribution (P) 3) change stored per unit volume



Electric dipole

A pain of equal and opposite changes separated by small distance is called electric dipole

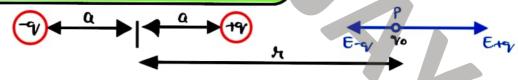
Dipole moment = 9t is equal to product of any charge with distance between the two charges. Que a q-

9+ is denoted

9+ is a vector aworkity.

9ts direction is from negative (-ve) to hasitive charge (+) 913 direction is opposite to that of electric field.

Electric field at Unial Point due to a dipole



Consider a test charge is kept at Point P. Etg z Electric field at Point P cheto to change Now E-y = Electric field at Point P dueto - y charge

$$\vec{E}_{axial} = \vec{E}_{tq} + \vec{E}_{-q}$$

$$= \frac{1}{4\pi\epsilon_0} \frac{+q_y}{(n-a)^2} + \frac{1}{4\pi\epsilon_0} \frac{-q_y}{(n+a)^2}$$

$$\vec{E}_{axial} = \frac{1}{4\pi\epsilon_0} q_y \left[ \frac{1}{(n-q)^2} - \frac{1}{(n+a)^2} \right]$$

$$\vec{E}_{axial} = \frac{1}{4\pi\epsilon_0} q_y \left[ \frac{(n+a)^2 - (n+a)^2}{(n+a)^2} \right]$$

Eaxial = 
$$\frac{1}{4\pi\epsilon_0} \gamma \left( \frac{H^2 + G^2 + 2a\pi - H^2 - G^2 + 2a\pi}{(H^2 - G^2)^2} \right)$$

=  $\frac{1}{4\pi\epsilon_0} \gamma \left( \frac{4G\pi}{(H^2 - G^2)^2} \right) = \frac{1}{4\pi\epsilon_0} \frac{(Gy \times 2G) \times 2\pi}{(H^2 - G^2)^2}$ 

Eaxial =  $\frac{1}{4\pi\epsilon_0} \frac{(P)(2\pi)}{(H^2 - G^2)^2}$  where  $P = Gy \times 2G = dipole$  moment

Eaxial =  $\frac{1}{4\pi\epsilon_0} \frac{(P^2 - G^2)^2}{(H^2 - G^2)^2}$  (towords light)

Net electric field at Point P is in the direction of dipole moment,

An vector form | Earial = 1 2pm p where p is a unit vector in it is towards right. & it is towards right.

Ety Coso

E-q(oso

# Electric field out equatorial point

Consider a test change is kept at Point P

Etg z Electric field at Point P clueto to thange E-y = Electric field at Point P clueto - q charge

NOW Both Etg, and E-g, will have two Components for Ery -> Ery (000 -> Ery Sind for E-q -> E-q (050 + E-q Sin 0

From diagram, Ety SIND & E-q SIND one in apposite direction. so they will concel each other out. Then net electric field at Print P will be



(050 = B = Q

Also by Phythagoras? 47 = 87+02 H= 1/ 52+02

$$E_{eqv} = E_{eqv} \cos \theta + E_{eqv} \cos \theta$$

$$E_{eqv} = 2E(\cos \theta)$$

$$E_{eqv} = 2 \times 1 \quad \text{(0s)}$$

$$UTE_{eqv} = h^{2}$$

Now Putting Volves of 42 \$ (050 Eegu = 2×1 9/ × 0/7  $= \frac{1}{4\pi\epsilon_0} \frac{c_V \times 2c_1}{(s^2 + c_1^2)} \frac{1}{\sqrt{s^2 + c_1^2}}$ 

41180 (S2+G2)312 here Pz dipuk moment PZ CVXZG

EtaySino

here electric field at P is opposite to that the dipole moment. so In vector form

Eequ = - 1 P 17720 (5+42)3/2 P

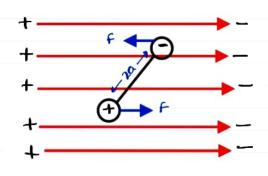
Here p is a unit vector it is toward left direction.

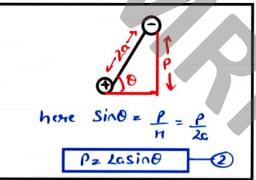
### Tunque on a Dipole la electric field

when a dipute is bept inside an electric field the dipute experience a force

But as funce expensioned by the positive charge is equal and opposite to the funce expensionced by a negative change. So a Tanque ask on the dipole:

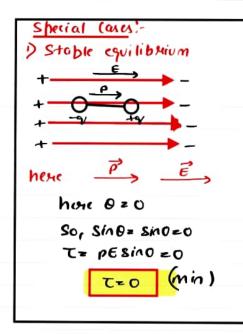
Torque = force x perpendicular

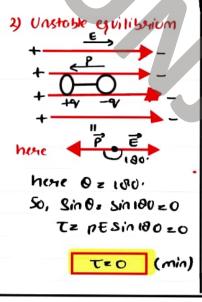


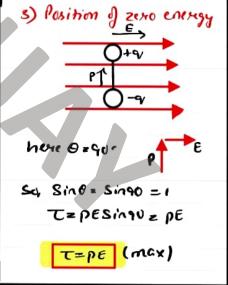


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Note: - gy dipole is placed in a uniform electric field, then it will have only subtational motion. (only Torque will act)

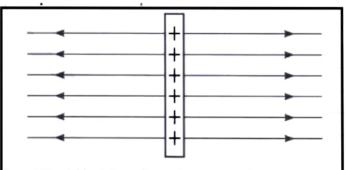
gy the dipole is placed in a non-uniform exertic field, men it will have both restational as well as Linear motion.

( Both Torque & forme will alt )

### Electric field lines

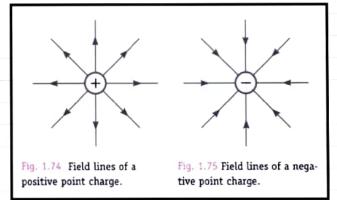
#### Properties of Electric Lines of Force

- The lines of force are continuous smooth curves without any breaks.
- The lines of force start at positive charges and end at negative charges – they cannot form closed loops. If there is a single charge, then the lines of force will start or end at infinity.
- The tangent to a line of force at any point gives the direction of the electric field at that point.
- 4. No two lines of force can cross each other.
- The lines of force are always normal to the surface of a conductor on which the charges are in equilibrium.
  - Reason. If the lines of force are not normal to the conductor, the component of the field  $\vec{E}$  parallel to the surface would cause the electrons to move and would set up a current on the surface. But no current flows in the equilibrium condition.
- The lines of force have a tendency to contract lengthwise. This explains attraction between two unlike charges.
- The lines of force have a tendency to expand laterally so as to exert a lateral pressure on neighbouring lines of force. This explains repulsion between two similar charges.
- The relative closeness of the lines of force gives a measure of the strength of the electric field in any region. The lines of force are
  - (i) close together in a strong field.
  - (ii) far apart in a weak field.
  - (iii) parallel and equally spaced in a uniform field.
- The lines of force do not pass through a conductor because the electric field inside a charged conductor is zero.

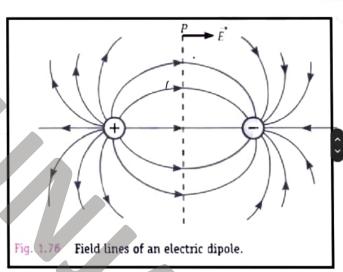


iig. 1.78 Field pattern of a positively charged plane conductor.

Uniform electric field.



# Electric field due to a point charge



Electric field elve to a dipole

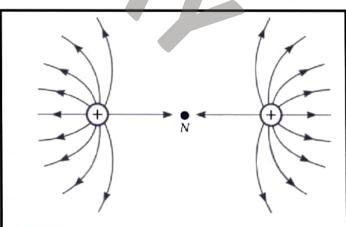
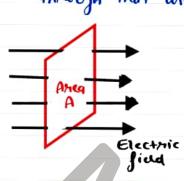


Fig. 1.77 Field lines of two equal positive charges.

Electric field due to 2 hositive changes

the total number of electric field lines pussing normally through that area.

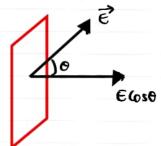


At is climbled by \$

det E= Electric field

A= Ameq

\$\$\delta = E(\color \color \color



here o is the angle between

electric field & Ameo vector

Note = Area vector is any vector which is perpendicular to

Φ= E.A

### houss hearn

a clused surjace is 1/80 times the net change enclosed by the clused surjace.

$$\phi = \oint \vec{\epsilon} \cdot d\vec{i} = 9/\epsilon_0$$

(Onsider a charge of is placed in the lenthe of the house an Surface. The value of electric field at a clistance of is

E = 1 cy



Now total electric field over whole houssian Surjace is given by. flux over whole Surjace

$$\phi = \oint E \cdot ds = E \oint ds = \frac{1}{4\pi\epsilon_0} \frac{4}{\lambda^2} \int ds$$

$$\phi = \oint E \cdot ds = \frac{1}{4\pi\epsilon_0} \frac{4}{\lambda^2} \left[ \text{Sunjoir area of shhore} \right]$$

$$\phi^2 \oint E \cdot ds = \frac{1}{4\pi\epsilon_0} \frac{4}{\lambda^2} \times \frac{4\pi x^2}{4\pi\epsilon_0}$$

# Electric field due to uniformly changed sheet

Consider an infinite changed sheet Now we want to find electric field due to mis changed sheet at a distance of from the sheet.

Now we alwaw a garssian surgare (cylindrical shape) as shown in the figure.

From Crows law :-

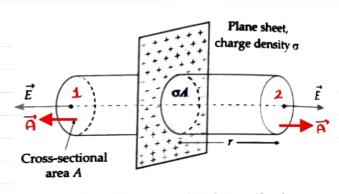


Fig. 1.98 Gaussian surface for a uniformly charged infinite plane sheet.

As there one two surjaces (surface 1 & surjace 2)

Just which the electric field is passing out. So gauss law will be  $\oint_1 E \cdot ds + \oint_2 E \cdot ds = 9/E_0$   $E \oint_1 ds + E \oint_2 ds = 9/E_0$   $E S + E S = 9/E_0$ here S = Surface Area of Circle

Now, we know, surface charge demity = charge Surface Arrea

More: The electric field due to a sheet.

More: The electric field due to a sheet does not depend upon the distance.

# Electric field due to two changed sheet

Electric field due to two positive

Sheet; 
Consider two sheets with charge density

T, and Tz. Now let T, > Tz.

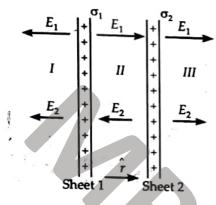


Fig. 1.99

An Megim I:-
$$\vec{\epsilon}_{Ne+} = -\frac{\sigma_1}{2\xi_0} - \frac{\sigma_2}{2\xi_0}$$

$$\vec{\epsilon}_{Ne+} = -\frac{\sigma_1}{2\xi_0} - \frac{\sigma_2}{2\xi_0}$$

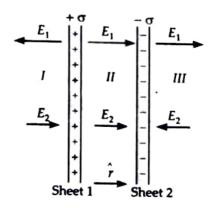
An Hegim II:
$$\frac{\overline{E}_{ner}}{\overline{E}_{ner}} = \frac{\overline{E}_{1}}{\overline{E}_{1}} - \frac{\overline{E}_{2}}{\overline{E}_{2}}$$

$$= \frac{\overline{V}_{1}}{2\overline{E}_{0}} - \frac{\overline{V}_{2}}{2\overline{E}_{0}}$$

$$\overline{E}_{Ner} = \frac{1}{2\overline{E}_{0}} (\overline{V}_{1} - \overline{V}_{2})$$

$$E_{net} = \frac{1}{25} (\sqrt{1+52})$$

Electric field due to one hositive and one negative plate Consider two sheets with change clemity + T and - T.



An Hegim T:-
$$\vec{E}_{Ne+} = (-\vec{E}_1) + (\vec{E}_2)$$

$$= -\frac{\tau}{2s_0} + \frac{\tau}{2s_0}$$

$$\vec{E}_{Ne+} = 0$$

An ucgim II;
$$\vec{E}_{Act} = \vec{E}_1 + \vec{E}_2$$

$$= \frac{T}{2S_0} + \frac{T}{2S_0}$$

$$= \frac{2T}{2S_0} = \frac{T}{S_0}$$

$$\vec{E}_{Nct} = \frac{T}{S_0}$$

An Megion 
$$\square > \overline{E}_{ne+} = \overline{E}_1' + (-\overline{E}_2')$$

$$= \frac{\sqrt{2}}{22} - \frac{\sqrt{2}}{22}$$

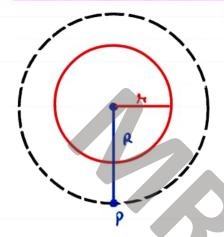
$$= \frac{\sqrt{2}}{22} - \frac{\sqrt{2}}{22}$$

So electric field only exist between the plater.

# Electric field due to uniformly charged thin sherical shell

Consider a spherical show of modius is with charge 'q' present on it. Now we have to find electric fixed at:-

## Doutside the shorical shell (A+ point P)

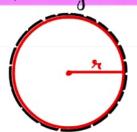


To find electric field at Point P, Let us drow o goussian rungue (sperical in shope) of madius R.

Now from yours law:

Ez 1 9/ 1/2

# 5) Electric field on the spenical sheet!



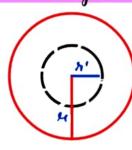
Now from gover low:

So E = 1 change Men,



here 9 2 change and, 4TH 22 Area Where T 2 Surgole change clemity T = change Area

## c) Electric field inside the spherical shell;



To find electric field inside the spherical shell let us draw a gaussian surjace of radius x'. Men Acc. to gauss law:-

But there is No charge inside the gaussian surgare so 920 Men, \$E. as 20 Men E=0

No electric field is present inside the shell