

Explanations

1. (c) The magnitude of electric field, $E = 9 \text{ N/C}$

At distance, $r = 4.0 \text{ m}$

$$\text{So, } F = \frac{1}{4\pi\epsilon_0} \times \frac{q}{(4)^2}$$

$$9 = \frac{1}{4\pi\epsilon_0} \times \frac{q}{16} \quad \dots (\text{i})$$

for $E = 16 \text{ N/C}$,

$$16 = \frac{1}{4\pi\epsilon_0} \times \frac{q}{x^2} \quad \dots (\text{ii})$$

Dividing Eqs. (i) and (ii),

$$\frac{9}{16} = \frac{\frac{1}{4\pi\epsilon_0} \times \frac{q}{4^2}}{\frac{1}{4\pi\epsilon_0} \times \frac{q}{x^2}}$$

$$\frac{9}{16} = \frac{x^2}{4^2} \Rightarrow \left(\frac{3}{4}\right)^2 = \frac{x^2}{4^2} \Rightarrow \frac{3}{4} = \frac{x}{4} \Rightarrow x = 3 \text{ m}$$

2. (c) Given that, dipole moment,

$$p = 2 \times 10^{-8} \text{ C-m}$$

Torque, $\tau = 6 \times 10^{-1} \text{ N-m}$

$$\tau_{\max} = pE$$

$$E = \frac{\tau_{\max}}{p} = \frac{6 \times 10^{-1}}{2 \times 10^{-8}} = 3 \times 10^7 \text{ Vm}^{-1}$$

3. (d) Electric field produced by charge particle at a distance of 3m

$$E = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r^2}$$

$$E = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{3^2} \quad [\text{Here, } r = 3 \text{ m}] \quad \dots (\text{i})$$

Let x be the distance from point charge where electric field is $\frac{E}{4}$.

$$\therefore \frac{E}{4} = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{x^2} \quad \dots (\text{ii})$$

Dividing Eq. (i) by Eq. (ii),

$$4 = \frac{x^2}{3^2}$$

$$x = 2 \times 3 = 6 \text{ m}$$

4. (b) Electron experience a force, $\mathbf{F} = 1.6 \times 10^{-16} \text{ N} \hat{\mathbf{i}}$

using, $\mathbf{F} = q \mathbf{E}$

$$\mathbf{E} = \frac{\mathbf{F}}{q} = \frac{1.6 \times 10^{-16} \hat{\mathbf{i}}}{-1.6 \times 10^{-19}}$$

$$= -\left(1.0 \times 10^3 \frac{\text{N}}{\text{C}}\right) \hat{\mathbf{i}}$$

5. (d) Given, surface charge density,

$$\sigma = 26.4 \times 10^{-12} \text{ C/m}^2$$

$$E = \frac{\sigma}{\epsilon_0} = \frac{26.4 \times 10^{-12}}{8.85 \times 10^{-12}} = 3 \text{ N/C}$$

$$(\because \epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N} \cdot \text{m}^2)$$



Common Mistake Sometime students think that, the electric field due to non-conducting sheet is $\frac{\sigma}{2\epsilon_0}$ but it is always $\frac{\sigma}{\epsilon_0}$ conducting sheet.

6. (b) According to Coulomb's law,

$$\mathbf{F}_{12} = -\mathbf{F}_{21}$$

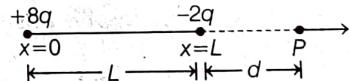
$$F = \frac{q_1 q_2}{4\pi\epsilon_0 r^2}$$

For attraction, $q_1 q_2 < 0$

$$q_1 = + \text{ and } q_2 = -$$

Thus, $q_1 q_2 < 0$

7. (c)



Let P is the observation point at a distance $(L+d)$ from $+8q$ and at d from $-2q$.

Then, \mathbf{E}_1 = Electric field intensity at P due to $+8q$

\mathbf{E}_2 = Electric field intensity at P due to $-2q$

$$|\mathbf{E}_1| = |\mathbf{E}_2|$$

$$\therefore \frac{K(8q)}{(L+d)^2} = \frac{K(2q)}{d^2}$$

$$\Rightarrow \frac{4}{(L+d)^2} = \frac{1}{d^2}$$

$$\Rightarrow 4d^2 = (L+d)^2$$

$$2d = L + d \Rightarrow d = L$$

$$\therefore P \text{ is at } x = L + L = 2L$$

8. (a) As we know,

$$F = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q_1 Q_2}{r^2}$$

Charges placed in a medium,

$$F_m = \frac{1}{4\pi\epsilon_0 k} \cdot \frac{Q_1 Q_2}{r^2} \quad \dots \text{(i)}$$

Force in the charges in the air is

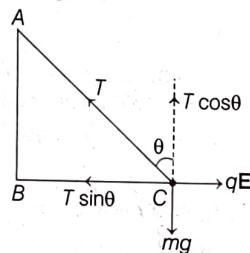
$$F_{\text{air}} = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q_1 Q_2}{r^2} \quad \dots \text{(ii)}$$

Thus, from Eqs. (i) and (ii), we have

$$\frac{F_m}{F_{\text{air}}} = \frac{1}{K}$$

$$\Rightarrow F_{\text{air}} = K F_m = K F = 5 F$$

9. (b) From given figure,



$$F_e = mg \times \tan \theta$$

$$qE = mg \tan \theta$$

$$q = \left(\frac{mg}{E} \right) \tan \theta$$

$$\tan \theta = \frac{F_e}{mg}$$

Hence, the sign and magnitude of q positive with magnitude $(mg/E) \tan \theta$.

10. (c) Since X is repelled by Y . So, object Y is positively charged. As object Z is attracted to object Y . So, it must either be neutral or positively charged.

11. (b) Since charge is quantised in a system, so total charge $= q_1 + q_2 + q_3 = +3e + 5e - 3e = +5e$

Among given options, only option (b) gives this value i.e. $+6e + 6e - 7e = +5e$

Therefore, the possible values for the final charge on the spheres are $+6e, +6e, -7e$.

12. (c) The force on charge q_0 due to $-q$ is

$$F_1 = K \frac{(-q)(q_0)}{a^2}, \text{ towards } +Y\text{-axis}$$

$\dots \text{(i)}$

Force on q_0 due to q is

$$F_2 = K \frac{(q)(q_0)}{a^2}, \text{ towards } -X\text{-axis} \quad \dots \text{(ii)}$$

So, the resultant or net force on the charge at O is

$$F_{\text{net}} = \sqrt{F_1^2 + F_2^2 + 2F_1 F_2 \cos \theta}$$

Since, $F_1 = -F_2$

$$\begin{aligned} \therefore F_{\text{net}} &= \sqrt{F_2^2 + F_2^2 + 2(-F_2)(F_2) \cos 90^\circ} = \sqrt{2} F_2 \\ &= \frac{\sqrt{2} Kqq_0}{a^2} \end{aligned}$$

13. (d) Given, charge, $q = 1 \text{ C}$

Number of electrons gained,

$$n = 5 \times 10^{18}$$

\therefore Total charge gained,

$$q' = ne = 5 \times 10^{18} \times 1.6 \times 10^{-19}$$

$$= 8 \times 10^{-1} = 0.80 \text{ C}$$

Since, electron is negatively charged, so net charge on the object becomes

$$q_{\text{net}} = q - q' = 1 - 0.8 = +0.20 \text{ C}$$

14. (a) An electric dipole placed in non-uniform electric field experiences both torque and force.

15. (d) A negative charge in an electric field moves in the direction opposite to the electric field as the force acting on it is in opposite direction to the field. So, A is false and R is also false.

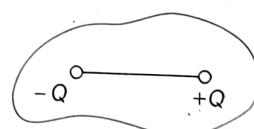
16. (b) Charge is always conserved but energy is lost in the form of heat.

17. (d) Gravitational force is the dominating force in nature. It is the weakest force.

Also, Coulomb's force \gg gravitational force.

18. (d) At the centre of the line joining two equal and opposite charge, $E \neq 0$. For similar charge, $E = 0$.

19. (a) If a dipole is enclosed by a surface as shown in figure, then



$$Q_{\text{enclosed}} = 0$$

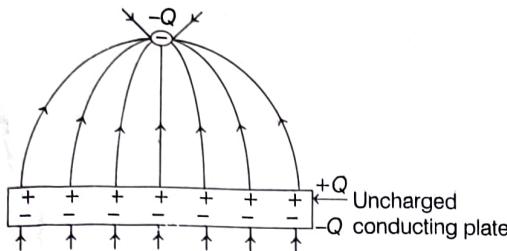
$$\therefore \phi = 0$$

(from Gauss' law)

20. 4 : 1

21. 90°

22.



23. Refer to diagram on page 3 (Electric Field Lines).

24. Refer to diagram on page 3 (Electric Field Lines).

25. The electrostatic field lines do not form closed loop because no electric field lines exist inside the charged body.

26. According to the question, both the balls have same charge q . Let the balls are separated by a distance r . Hence, according to Coulomb's law, if F and F' are the force of attraction between balls in air and in medium respectively.

$$\text{Then, } F = \frac{1}{4\pi\epsilon_0} \frac{q^2}{r^2}$$

$$\text{In medium, } F' = \frac{1}{4\pi K\epsilon_0} \frac{q^2}{r^2}$$

$$\therefore F' = F/K$$

where, K is dielectric constant of material and $K > 1$ for insulators, hence the force is reduced, when a plastic sheet is inserted.

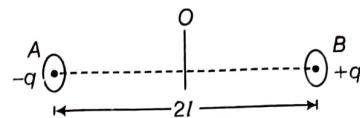
27. If electric field lines cross each other, then there would be two tangents drawn at the point of intersection and hence two directions of electric field at that point which is not possible. So, lines of forces never cross each other.

28. As, electric field inside a conductor is always zero. The electric lines of forces exert lateral pressure on each other which leads to repulsion between like charges. Thus, in order to stabilize spacing, the electric field lines are normal to the surface.

29. As per the condition given in question, two conclusions that can be drawn are as follows

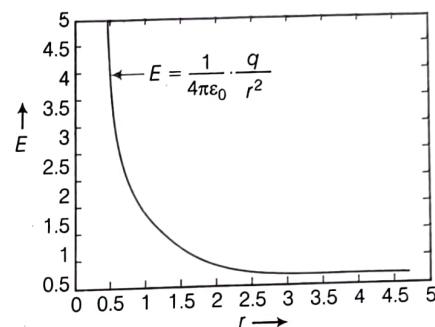
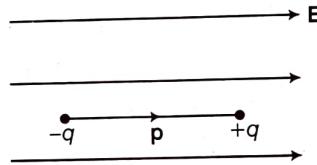
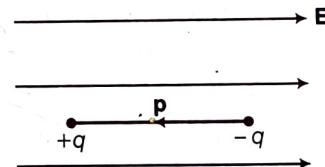
(i) The two point charges (q_1 and q_2) should be of opposite nature.(ii) The magnitude of charge q_1 must be greater than the magnitude of charge q_2 .

30. Electric dipole moment of an electric dipole is equal to the product of the magnitude of its either charge and the length of the electric dipole.

It is denoted by \mathbf{p} . Its SI unit is coulomb-metre.

$$|\mathbf{p}| = q \times 2l$$

It is a vector quantity and its direction is from negative charge to positive charge.

31. The plot showing the variation of electric field with distance r due to a point charge q is shown as below32. (i) For stable equilibrium, the angle between \mathbf{p} and \mathbf{E} is 0° i.e. it should be placed parallel to electric field.(ii) For unstable equilibrium, the angle between \mathbf{p} and \mathbf{E} is 180° i.e. it should be placed antiparallel to electric field.33. Path d is followed by electric field lines because electric field intensity inside the metallic sphere will be zero. Therefore, no electric lines of force exist inside the sphere. Also, electric field lines are always perpendicular to the surface of the conductor.

34. Right, because mutual force acting between two point charges is proportional to the product of magnitude of charges and inversely proportional to the square of the distance between them i.e. independent of the other charges.

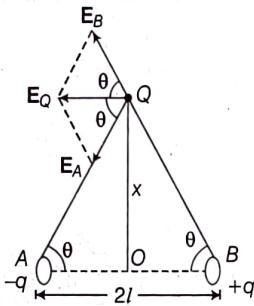
35. (i) Refer to text on page 4 (Torque on an electric dipole placed in a uniform electric field).

(ii) Refer to text on page 4 (Torque on an electric dipole placed in a uniform electric field).

36. Refer to text on page 4 (Torque on an electric dipole placed in a uniform electric field).

37. Electric field at a point on the equatorial line of an electric dipole.

Consider an electric dipole consisting of two point charges $+q$ and $-q$ separated by a small distance $AB = 2l$ with centre at O and dipole moment, $\mathbf{p} = q(2l)$ as shown in the figure.



Resultant electric field intensity at the point Q ,

$$\mathbf{E}_Q = \mathbf{E}_A + \mathbf{E}_B$$

$$\text{Here, } E_A = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{(x^2 + l^2)}$$

$$\text{and } E_B = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{(x^2 + l^2)}$$

On resolving \mathbf{E}_A and \mathbf{E}_B into two rectangular components, the vectors $E_A \sin \theta$ and $E_B \sin \theta$ are equal in magnitude and opposite to each other and hence, cancel out.

The vectors $E_A \cos \theta$ and $E_B \cos \theta$ are acting along the same direction and hence, add up.

$$\begin{aligned} \therefore E_Q &= E_A \cos \theta + E_B \cos \theta \\ &= 2E_A \cos \theta \quad [\because E_A = E_B] \\ &= \frac{2}{4\pi\epsilon_0} \cdot \frac{q}{(x^2 + l^2)} \cdot \frac{l}{(x^2 + l^2)^{1/2}} \\ &\quad \left[\because \cos \theta = \frac{l}{(x^2 + l^2)^{1/2}} \right] \\ &= \frac{1}{4\pi\epsilon_0} \cdot \frac{2ql}{(x^2 + l^2)^{3/2}} \end{aligned}$$

But, the dipole moment $|\mathbf{p}| = q \times 2l$

$$\therefore E_Q = \frac{1}{4\pi\epsilon_0} \cdot \frac{|\mathbf{p}|}{(x^2 + l^2)^{3/2}}$$

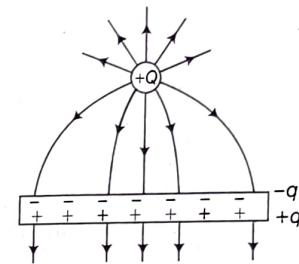
The direction of \mathbf{E} is along E_Q that is parallel to BA , i.e. opposite to AB . In vector form, we can rewrite as, $\mathbf{E}_Q = \frac{-\mathbf{p}}{4\pi\epsilon_0(x^2 + l^2)^{3/2}}$

38. We know that, $\tau = pE \sin \theta$

If $\theta = \pi/2$, then τ is maximum

$$\text{i.e. } \tau = pE \sin \frac{\pi}{2} \Rightarrow \tau = pE \text{ (maximum)}$$

39. Equal charge of opposite nature induces on the surface of conductor nearer to the source charge.

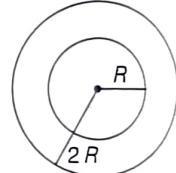


Electric lines of forces should fall normally on the surface of conductor, i.e. at 90° on the conducting plate.

40. Surface charge density,

$$\sigma = \frac{Q}{4\pi R^2}$$

According to the question, surface charge density, $\sigma = \text{constant}$



Let Q_1 and Q_2 are two charges
Hence, Charge, $Q_1 = 4\pi R^2 \sigma$... (i)

Charge, $Q_2 = 4\pi(2R)^2 \sigma$... (ii)

On dividing Eq. (i) with Eq. (ii), we get

$$\therefore \frac{Q_1}{Q_2} = \frac{4\pi R^2 \sigma}{4\pi(2R)^2 \sigma} = \frac{1}{4}$$

41. When two identical conducting charged spheres are brought in contact, then redistribution of charge takes place, i.e. the charge is equally divided on both the spheres.

When C and A are placed in contact, charge of A equally divides in two spheres. Therefore, charges on each spherical shell A and C = $+2Q$.

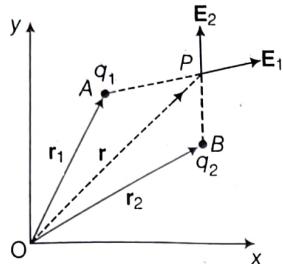
Now, C is placed in contact with B , then charge on each spherical shell B and C becomes

$$\frac{2Q + (-10Q)}{2} = -4Q$$

When A and B are placed in contact, then charge on each A and B becomes

$$\frac{2Q + (-4Q)}{2} = -Q$$

42. Let two point charges q_1 and q_2 are situated at points A and B have position vectors \mathbf{r}_1 and \mathbf{r}_2 .



$$\therefore \mathbf{AP} = \mathbf{r} - \mathbf{r}_1$$

$$\text{and } \mathbf{BP} = \mathbf{r} - \mathbf{r}_2$$

Electric field intensity at point P due to q_1 ,

$$\mathbf{E}_1 = \frac{1}{4\pi\epsilon_0} \cdot \frac{q_1}{|\mathbf{AP}|^3} \mathbf{AP}$$

$$\text{Similarly, } \mathbf{E}_2 = \frac{1}{4\pi\epsilon_0} \cdot \frac{q_2}{|\mathbf{BP}|^3} \mathbf{BP}$$

\therefore Net electric field intensity at point P ,

$$\mathbf{E} = \mathbf{E}_1 + \mathbf{E}_2$$

$$= \frac{1}{4\pi\epsilon_0} \left[\frac{q_1}{|\mathbf{r} - \mathbf{r}_1|^3} (\mathbf{r} - \mathbf{r}_1) + \frac{q_2}{|\mathbf{r} - \mathbf{r}_2|^3} (\mathbf{r} - \mathbf{r}_2) \right]$$

43. (i) p_1 is in stable equilibrium

p_2 is in unstable equilibrium because, the electric field, on either side is directed towards the negatively charged sheet and its magnitude is independent of the distance of the field point from the sheet. For position p_1 , dipole moment and electric field are parallel. For position p_2 , they are anti-parallel.

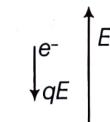
- (ii) The dipole will not be in equilibrium in any of the two positions. The electric field due to an infinite straight charged wire is non-uniform. Hence, there will be a net non-zero force on the dipole in each case.

44. (i) An electron falls through distance 1.5 cm, if electric field is 2×10^4 N/C.

So, net force on electron $F = q_e E$

$$m_e a = q_e E$$

$$a = \frac{q_e E}{m_e}$$



$$[\because F = ma]$$

where, $q_e = 1.6 \times 10^{-19}$ C,

$$m_e = 9.1 \times 10^{-31}$$
 kg

and $E = 2 \times 10^4$ N/C

$$\text{so, } a = \frac{1.6 \times 10^{-19} \times 2 \times 10^4}{9.1 \times 10^{-31}} \\ = 3.5 \times 10^{15} \text{ m/s}^2$$

$$\text{As we know, } s = ut + \frac{1}{2} at^2$$

$$\text{So, } 1.5 \times 10^{-2} = 0 \times t + \frac{1}{2} \times 3.5 \times 10^{15} \times t^2$$

$$t = \sqrt{\frac{2 \times 1.5 \times 10^{-2}}{3.5 \times 10^{15}}}$$

$$= \sqrt{8.57 \times 10^{-8}} = 2.92 \text{ ms}$$

- (ii) Similarly, time of fall of proton if direction of field is reversed

$$t_p = \sqrt{\frac{2s}{a_p}} = \sqrt{\frac{2sm_p}{q_p E}} \quad \left(\because a_p = \frac{q_p E}{m_p} \right)$$

$$\text{where, } m_p = 1.6 \times 10^{-27} \text{ kg, } q_p = 1.6 \times 10^{-19} \text{ C}$$

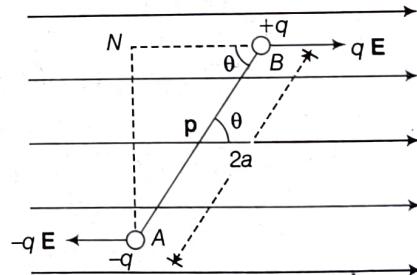
$$\text{and } s = 1.5 \text{ cm}$$

$$t_p = \sqrt{\frac{2 \times 1.5 \times 10^{-2} \times 1.6 \times 10^{-27}}{1.6 \times 10^{-19} \times 2 \times 10^4}} \\ = \sqrt{15 \times 10^{-14}} \\ t_p = 122 \times 10^{-7} \text{ s}$$

45. (i) Refer to Sol. 37 on page 12.

- (ii) Refer to Sol. 32 on page 11.

46. (i) Dipole in a uniform electric field



According to the figure, if we consider an electric dipole consisting of charges $-q$ and $+q$ of length $2a$ placed in a uniform electric field \mathbf{E} making an angle θ with electric field, then force exerted on charge $-q$ at $A = -q \mathbf{E}$ (opposite to \mathbf{E})

Force exerted on charge $+q$ at $B = q \mathbf{E}$ (along \mathbf{E})

Hence, the net translating force on a dipole in a uniform electric field is zero. But the two equal and opposite forces act at different points and form couple which exerts a torque τ .

$\tau = \text{Force} \times \text{Perpendicular distance between the two forces}$

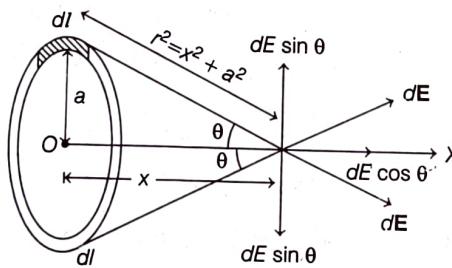
$$\tau = qE(AN) = qE(2a \sin \theta)$$

$$\tau = q(2a)E \sin \theta$$

$$\Rightarrow \tau = pE \sin \theta \Rightarrow \tau = \mathbf{p} \times \mathbf{E}$$

(ii) When the dipole is placed in a non-uniform electric field, it experiences both net force and net torque.

47. According to the question, suppose that the ring is placed with its plane perpendicular to the X -axis as shown in figure. Consider small element dl of the ring.



Let the total charge q is uniformly distributed, so the charge dq on element dl is $dq = \frac{q}{2\pi a} \times dl$.

$$\Rightarrow \frac{dq}{dl} = \lambda = \frac{q}{2\pi a} \quad \dots \text{(i)}$$

$$\text{or} \quad dq = \lambda \cdot dl$$

Since, only the axial component gives the net E at point P due to charge on ring.

$$\begin{aligned} \text{So, } \int_0^E d\mathbf{E} &= \int_0^{2\pi a} dE \cos \theta = \int_0^{2\pi a} K \cdot \lambda \cdot \frac{dl}{r^2} \times \frac{x}{r} \\ &\quad \left[\text{where, } \cos \theta = \frac{x}{r}, K = \frac{1}{4\pi \epsilon_0} \right] \\ &= Kx \lambda \frac{1}{r^3} \int_0^{2\pi a} dl = Kx \lambda \cdot \frac{1}{r^3} [l]_0^{2\pi a} \\ &= K \lambda x \cdot \frac{1}{(x^2 + a^2)^{3/2}} \cdot 2\pi a \quad [\because r^2 = x^2 + a^2] \\ \therefore E &= \frac{Kqx}{(x^2 + a^2)^{3/2}} \quad [\text{using Eq. (i)}] \end{aligned}$$

Now, for points at large distances from the ring $x \gg a$.

$$\therefore E = \frac{Kq}{x^2} = \frac{1}{4\pi \epsilon_0} \frac{q}{x^2}$$

This is same as the field due to a point charge and indicating that for far-off axial point from the centre of a ring, the charged ring behaves as a point charge.

48. Refer to text on page 4 (Torque on an electric dipole placed in a uniform electric field).

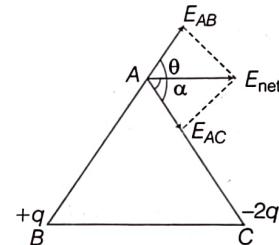
Pairs of perpendicular vectors

$$(a) (\tau, \mathbf{p}) \quad (b) (\tau, \mathbf{E})$$

49. (i) The magnitude,

$$|\mathbf{E}_{AB}| = \frac{1}{4\pi \epsilon_0} \times \frac{q}{a^2} = E$$

$$|\mathbf{E}_{AC}| = \frac{1}{4\pi \epsilon_0} \times \frac{2q}{a^2} = 2E$$



$$\begin{aligned} E_{\text{net}} &= \sqrt{E_{AB}^2 + E_{AC}^2 + 2E_{AB}E_{AC} \cos \theta} \\ &= \sqrt{(2E)^2 + E^2 + 2 \times 2E \times E \times \left(-\frac{1}{2}\right)} \\ &= \sqrt{4E^2 + E^2 - 2E^2} = E\sqrt{3} \end{aligned}$$

We know that, $E = q/4\pi \epsilon_0 a^2$

$$\text{So, } E_{\text{net}} = q\sqrt{3}/4\pi \epsilon_0 a^2$$

- (ii) Direction of resultant electric field at vertex,

$$\tan \alpha = \frac{E_{AB} \sin 120^\circ}{E_{AC} + E_{AB} \cos 120^\circ} = \frac{E \times \sqrt{3}/2}{2E + E \times (-1/2)}$$

$$\tan \alpha = \frac{1}{\sqrt{3}} \Rightarrow \alpha = \tan^{-1} \left(\frac{1}{\sqrt{3}} \right)$$

$$\alpha = 30^\circ \quad (\text{with side } AC)$$

50. Refer to text on page 4 (Electric dipole moment).

For derivation of E

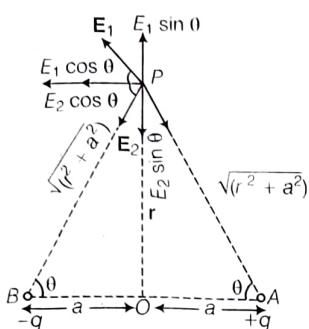
Consider an electric dipole AB consists of two charges $+q$ and $-q$ separated by a distance $2a$. We have to find electric field at point P on equipotential line separated by a distance r .

Electric field at point P due to charge $+q$

$$\mathbf{E}_1 = \frac{1}{4\pi \epsilon_0} \times \frac{q}{[\sqrt{(r^2 + a^2)}]^2}$$

$$= \frac{1}{4\pi\epsilon_0} \times \frac{q}{(r^2 + a^2)}$$

Along AP,



Electric field at point P due to charge $-q$,

$$\mathbf{E}_2 = \frac{1}{4\pi\epsilon_0} \times \frac{q}{r^2 + a^2} \text{ along } PB$$

On resolving \mathbf{E}_1 and \mathbf{E}_2 into rectangular components, we get resultant electric field at point P.

$$E = E_1 \cos \theta + E_2 \cos \theta$$

$$\begin{aligned} &= \frac{1}{4\pi\epsilon_0} \times \frac{q}{(r^2 + a^2)} \cos \theta + \frac{1}{4\pi\epsilon_0} \times \frac{q}{(r^2 + a^2)} \cos \theta \\ &= 2 \times \frac{1}{4\pi\epsilon_0} \times \frac{q}{(r^2 + a^2)} \times \frac{a}{\sqrt{(r^2 + a^2)}} \end{aligned}$$

$$= \frac{1}{4\pi\epsilon_0} \times \frac{q \cdot 2a}{(r^2 + a^2)^{3/2}} \quad [\text{But } q \times 2a = p]$$

$$\therefore E = \frac{1}{4\pi\epsilon_0} \times \frac{p}{(r^2 + a^2)^{3/2}}$$

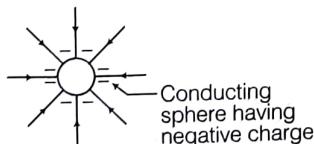
$$\text{If } r \gg a, \text{ then } E = \frac{1}{4\pi\epsilon_0} \times \frac{p}{r^3}$$

51. Refer to text on page 4 (Torque on an electric dipole placed in a uniform electric field).

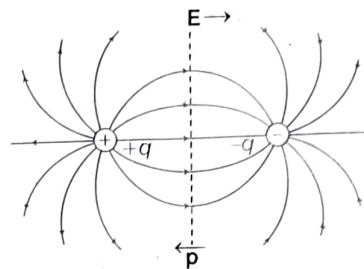
Conditions

- (i) When $\theta = 0^\circ$; $\tau = 0$, then \mathbf{p} and \mathbf{E} are parallel and the dipole is in a position of stable equilibrium.
- (ii) When $\theta = 180^\circ$, $\tau = 0$, then \mathbf{p} and \mathbf{E} are anti-parallel and the dipole is in a position of unstable equilibrium.

52. (i) Electric field lines due to a conducting sphere are shown in figure.



- (ii) Electric field lines due to an electric dipole are shown in figure.



53. (i) An ideal electric dipole consists of two very large charges $+q$ and $-q$ separated by very small distance.

Example- H_2O , HCl , N_2O etc.

(ii) Refer to text on page 4. (Torque on an electric dipole placed in a uniform electric field)

$$(iii) \tau = p E \sin \theta = q (2a) E \sin \theta$$

Putting values,

$$8\sqrt{3} = q \times 0.02 \times 10^5 \times \sin 60^\circ$$

$$q = 8 \times 10^{-3} \text{ C}$$

Potential energy

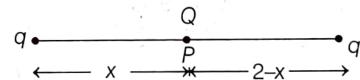
$$\begin{aligned} PE &= -p \mathbf{E} \cos \theta \\ &= -q(2a) \times \mathbf{E} \cos \theta \\ &= -8 \times 10^{-3} \times 0.02 \times 10^5 \times \cos 60^\circ \end{aligned}$$

$$\text{Thus, } PE = -8 \text{ J}$$

54. (i) Refer to Sol. 37 on page 12.

(ii) Let P be the point at which the system of charges as shown in the figure below is in equilibrium, then

$$F(x) = F(2-x)$$



$$\frac{1}{4\pi\epsilon_0} \cdot \frac{qQ}{x^2} = \frac{1}{4\pi\epsilon_0} \cdot \frac{qQ}{(2-x)^2} \quad (\text{from figure})$$

$$\Rightarrow \frac{1}{x^2} = \frac{1}{(2-x)^2}$$

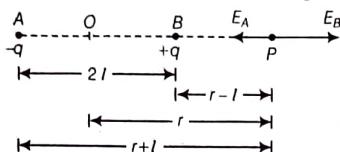
$$\Rightarrow x = (2-x)$$

$$\Rightarrow x = 1 \text{ m}$$

Thus, the charge Q should be placed at the centre of the line joining two given charges. Also, the two given charges are identical i.e. having same nature. So, the third charge could be of any nature (positive or negative), as the forces on it at the centre are equal and opposite.

55. (i) Electric field due to dipole at axial point

We have to calculate the field intensity E at a point P on the axial line of the dipole at distance $OP = r$ from the centre O of the dipole.



Resultant electric field intensity at the point P is $\mathbf{E}_P = \mathbf{E}_A + \mathbf{E}_B$

The vectors \mathbf{E}_A and \mathbf{E}_B are collinear and opposite.
 $\therefore \mathbf{E}_P = \mathbf{E}_B - \mathbf{E}_A$

$$\text{Here, } E_A = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{(r+l)^2}, \quad E_B = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{(r-l)^2}$$

$$\therefore E_P = \frac{1}{4\pi\epsilon_0} \left[\frac{q}{(r-l)^2} - \frac{q}{(r+l)^2} \right] \\ = \frac{1}{4\pi\epsilon_0} \cdot \frac{4q \times l}{(r^2 - l^2)^2}$$

$$\therefore E_P = \frac{1}{4\pi\epsilon_0} \cdot \frac{2p}{(r^2 - l^2)^2}$$

If the length of dipole is short i.e. $2l \ll r$, then

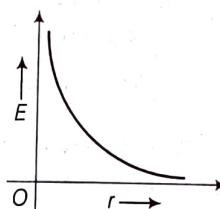
$$E_P = \frac{2p}{4\pi\epsilon_0 \cdot r^3}$$

The direction of E_P is along BP produced.

$$\text{So, } E_P \propto \frac{1}{r^3}$$

$$(ii) E \propto \frac{1}{r^3}. \text{ As } r \text{ increases, } E$$

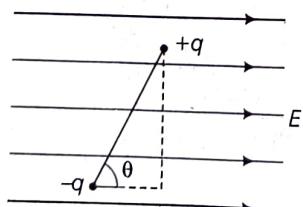
will sharply decrease. The shape of the graph will be as given in the figure.



$$(iii) \text{ When the dipole were kept in a uniform electric field } E_0.$$

The torque acting on dipole is

$$\tau = |\mathbf{p} \times \mathbf{E}| \\ = pE \sin \theta$$



$$(a) \text{ If } \theta = 0^\circ, \text{ then } \tau = 0, \mathbf{p} \parallel \mathbf{E} \text{ and the dipole is in stable equilibrium.}$$

For diagram Refer to Sol. 32 (i) on page 11.

$$(b) \text{ If } \theta = 180^\circ, \text{ then } \tau = 0, \mathbf{p} \parallel -\mathbf{E} \text{ and the dipole is in unstable equilibrium.}$$

For diagrams Refer to Sol. 32 (ii) on page 11.

$$56. (i) \text{ Torque, } \tau = pE \sin \theta$$

$$\text{In vector notation, } \tau = \mathbf{p} \times \mathbf{E}$$

SI unit of torque is newton-metre (N-m) and its dimensional formula is $[ML^2 T^{-2}]$. Torque is always directed in plane perpendicular to the plane of dipole movement and electric field.

$$\text{Case 1} \quad \text{If } \theta = 0^\circ, \text{ then } \tau = 0$$

The dipole is in **stable equilibrium**.

$$\text{Case 2} \quad \text{If } \theta = 90^\circ, \text{ then } \tau = pE \text{ (maximum value)}$$

The torque acting on dipole will be **maximum**.

$$\text{Case 3} \quad \text{If } \theta = 180^\circ, \text{ then } \tau = 0$$

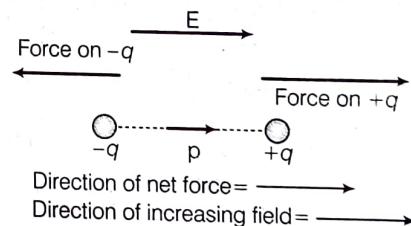
The dipole is in **unstable equilibrium**.

$$(ii) \text{ If the field is non-uniform, then there would be a net force acting on the dipole in addition to the net torque and the resulting motion would be a combination of translation and rotation.}$$

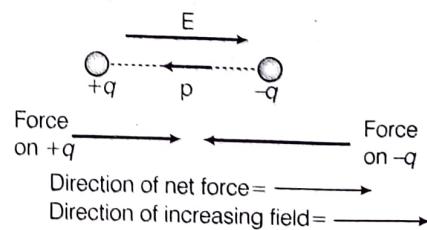
$$\tau = \mathbf{p} \times \mathbf{E} (\mathbf{r})$$

Net torque acts on the dipole depending on the location, where \mathbf{r} is the position vector of the centre of the dipole.

$$(iii) (a) \mathbf{E} \text{ is increasing parallel to } \mathbf{p}, \text{ then } \theta = 0^\circ. \text{ So, torque becomes zero but the net force on the dipole will be in the direction of increasing electric field and hence, it will have linear motion along the dipole moment.}$$



$$(b) \mathbf{E} \text{ is increasing anti-parallel to } \mathbf{p}. \text{ So, the torque still remains zero, but the net force on the dipole will be in the direction of increasing electric field which is opposite to the dipole moment. Hence, it will have linear motion opposite to the dipole moment.}$$



Explanations

1. (b) The charge at the centre of the cube is Q , then electric flux through each surface is same,
Using Gauss' law

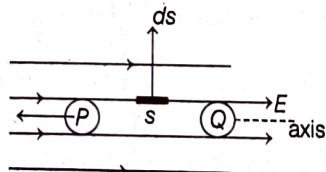
$$\phi_E = Q \times \frac{1}{\epsilon_0}$$

There are 6 faces of cube,

so $\phi_E = \frac{Q}{6\epsilon_0}$

Concept Enhancer To determine electric field in such cases, we have to imagine a symmetrical Gaussian surface and find the flux linked with the Gaussian surface.

2. (a)



Flux through surface P ,

$$\phi_P = E \times \pi R^2$$

Similarly, for flux through surface Q ,

$$\phi_Q = E \times \pi R^2$$

Flux through curved surface S , $= \int \mathbf{E} \cdot d\mathbf{s}$

$$= \int Eds \cos 90^\circ = 0$$

\therefore Total flux through cylinder

$$= \phi_P + \phi_Q + \phi_s = 0$$

3. (d) The electric field over the Gaussian surface remains continuous and uniform at every point.

4. (c) The electric field due to a point charge $2q$ at a distance r is

$$E = K \frac{(2q)}{r^2} \quad \dots (i)$$

The electric field due to a uniformly charged thin sphere shell of charge q and of radius R at distance $\frac{r}{2}$ ($r \gg R$) is

$$E' = K \frac{q}{(r/2)^2} = \frac{4Kq}{r^2} \quad \dots (ii)$$

From Eqs. (i) and (ii), we get

$$E' = 2E$$

5. (a) Given, $\mathbf{E} = cz^2 \hat{\mathbf{k}}$

As, electric flux, $\phi = \int_S \mathbf{E} \cdot d\mathbf{s}$

$$= \int_S cz^2 \hat{\mathbf{k}} dx dy \hat{\mathbf{k}}$$

$$= \int_S cz^2 dx dy = cz^2 \int_0^a dx \int_0^a dy$$

$$= cz^2 \times a^2$$

Here, $z = a$ so, $\phi = ca^4$

6. (a) The total electric flux passes through the cube $= \frac{q}{\epsilon_0}$

As we know, there are 6 faces in a cube so,

Electric flux will be $\phi = \frac{q}{6\epsilon_0}$

Correct option is (a), $\frac{q}{6\epsilon_0}$.

7. (a) According to the Gauss' law, the net electric flux through any closed Gaussian surface is equal to the net charge enclosed by it divided by permittivity of the medium.

$$\text{Mathematically, } \phi_E = \oint_S \mathbf{E} \cdot d\mathbf{S} = \frac{q}{\epsilon_0}$$

This law is true for any closed surface, no matter what is its shape or size.

8. (a) Flux, $\phi_{\text{net}} = \frac{q_{\text{in}}}{\epsilon_0}$

If a closed body is placed in an electric field (either uniform or non-uniform), total flux linked with it will be zero.

i.e. $\phi_{\text{net}} = 0$

$$\Rightarrow q_{\text{in}} = 0$$

9. (d) With the help of Gauss's theorem, we can find electric flux at any point and it is true that Gauss's theorem can be applied for any symmetric of charge distribution.

10. According to question, electric flux ϕ due to a point charge enclosed by a spherical Gaussian surface is given by

$$\phi = \mathbf{E} \cdot \mathbf{A}$$

Electric Charges and Fields

$$\phi = \frac{\mathbf{K}q}{r^2} \cdot 4\pi r^2 = \mathbf{K}q \cdot 4\pi$$

$$\left(\because E = \frac{\mathbf{K}q}{r^2} \text{ and } A = 4\pi r^2 \right)$$

So, there is no effect of change in radius on the electric flux.

11. According to the Gauss' law of electrostatics, electric flux through any closed surface is given by

$$\phi_E = q/\epsilon_0 \quad \dots(i)$$

So, in the given case, cube encloses an electric dipole. Therefore, the total charge enclosed by the cube is zero. i.e. $q = 0$.

Therefore, from Eq. (i), we have

$$\phi_E = q/\epsilon_0 = 0$$

i.e. electric flux is zero.

12. According to the question, $\mathbf{E} = 3 \times 10^3 \hat{i} \text{ NC}^{-1}$.

Side of square (S) = 10 cm = 0.1 m.

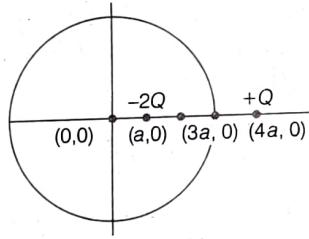
$$\text{Area of square } (A) = (\text{side})^2 = (0.1)^2 = 1 \times 10^{-2} \text{ m}^2$$

Hence, electric flux through the square,

$$\phi = \mathbf{E} \cdot \mathbf{A} = (3 \times 10^3) \cdot 10^{-2} = 30 \text{ Nm}^2 \text{ C}^{-1}$$

13. Gauss' theorem states that the total electric flux linked with closed surface S is $\phi_E = q/\epsilon_0$

where, q is the total charge enclosed by the closed Gaussian (imaginary) surface.



Charge enclosed by the sphere = $-2Q$

Therefore, $\phi = 2Q/\epsilon_0$ (inwards)

14. By Gauss' theorem, total electric flux linked with a closed surface is given by $\phi = q/\epsilon_0$
where, q is the total charge enclosed by the closed surface.

∴ Total electric flux linked with cube, $\phi = q/\epsilon_0$

As charge is at centre. Therefore, electric flux is symmetrically distributed through all 6 faces.

$$\text{Flux linked with each face} = \frac{1}{6}\phi = \frac{1}{6} \times \frac{q}{\epsilon_0} = \frac{q}{6\epsilon_0}$$

15. Electric flux through the closed surface S is

$$\begin{aligned} \phi_S &= \frac{\Sigma q}{\epsilon_0} = \frac{+2q - q}{\epsilon_0} \\ &= \frac{q}{\epsilon_0} \Rightarrow \phi_S = \frac{q}{\epsilon_0} \end{aligned}$$

Charge $+3q$ is outside the closed surface S . Therefore, it would not be taken into consideration in applying Gauss' theorem.

16. Given, electric field intensity

$$\mathbf{E} = 5 \times 10^3 \hat{i} \text{ NC}^{-1}$$

Magnitude of electric field intensity

$$|\mathbf{E}| = 5 \times 10^3 \text{ NC}^{-1}$$

Side of square, $S = 10 \text{ cm} = 0.1 \text{ m}$

$$\text{Area of square, } A = (0.1)^2 = 0.01 \text{ m}^2$$

The plane of the square is parallel to the YZ -plane.
Hence, the angle between the unit vector normal to the plane and electric field is zero.

i.e., $\theta = 0^\circ$

∴ Flux through the plane,

$$\phi = |\mathbf{E}| \times A \cos \theta$$

$$\Rightarrow \phi = 5 \times 10^3 \times 0.01 \cos 0^\circ$$

$$\phi = 50 \text{ Nm}^2 \text{ C}^{-1}$$

If the plane makes an angle of 30° with the X -axis, then $\theta = 60^\circ$

∴ Flux through the plane,

$$\phi = |\mathbf{E}| \times A \times \cos 60^\circ$$

$$= 5 \times 10^3 \times 0.01 \times \cos 60^\circ$$

$$= 25 \text{ Nm}^2 \text{ C}^{-1}$$

17. $40 \text{ Nm}^2 \text{ C}^{-1}$ and $20 \text{ Nm}^2 \text{ C}^{-1}$

Refer to Sol. 16 on page 25.

18. $200 \text{ Nm}^2 \text{ C}^{-1}$ and $100 \text{ Nm}^2 \text{ C}^{-1}$

Refer to Sol. 16 on page 25.

19. According to Gauss' law,

$$\text{Flux through } S_1, \phi_1 = \frac{Q}{\epsilon_0} \quad \dots(i)$$

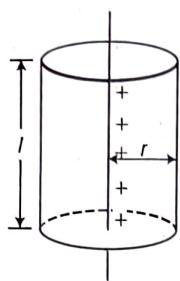
$$\text{Flux through } S_2, \phi_2 = \frac{Q + 2Q}{\epsilon_0} = \frac{3Q}{\epsilon_0} \quad \dots(ii)$$

On dividing Eq. (i) by Eq. (ii), we get

$$\phi_1/\phi_2 = 1/3$$

There is no change in the flux through S_1 with dielectric medium is introduced inside the sphere S_2 .

20. A thin straight conducting wire will be a uniform linear charge distribution.



Let q charge be enclosed by the cylindrical surface.

$$\therefore \text{Linear charge density, } \lambda = \frac{q}{l}$$

$$\therefore q = \lambda l \quad \dots(i)$$

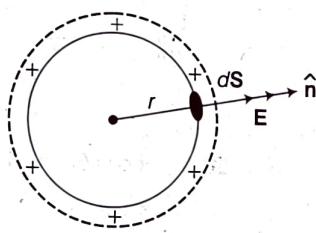
By Gauss' theorem,

\therefore Total electric flux through the surface of cylinder

$$\phi = \frac{q}{\epsilon_0} \quad [\text{Gauss' theorem}]$$

$$\therefore \phi = \frac{\lambda l}{\epsilon_0} \quad [\text{from Eq. (i)}]$$

21. Let q charge be uniformly distributed over the spherical shell of radius r .



\therefore Surface charge density on spherical shell

$$\sigma = \frac{q}{4\pi r^2} \quad \dots(ii)$$

\therefore Electric field intensity on the surface of spherical shell

$$E = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r^2} \hat{n}$$

$[\because E$ acts along radially outward and along \hat{n}]

$$E = \frac{(q/4\pi r^2)}{\epsilon_0} \hat{n} \Rightarrow E = \frac{\sigma}{\epsilon_0} \hat{n} \quad \dots(ii)$$

22. (i) According to Gauss' theorem,

$$\phi = \frac{\Sigma q}{\epsilon_0} \propto \Sigma q$$

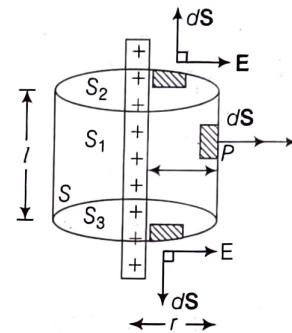
$$\Rightarrow \frac{\phi_{S_1}}{\phi_{S_2}} = \frac{2Q}{2Q + 4Q} = \frac{1}{3}$$

- (ii) If the medium is filled in S_1 , then electric flux through spheres is

$$\phi_{S_1} = \frac{\Sigma q}{\epsilon_0 \epsilon_r} = \frac{2Q}{\epsilon_0 \epsilon_r}$$

23. Electric field intensity due to an infinitely long uniformly charged wire at point P at distance r from it is obtained as follows

Consider a thin cylindrical Gaussian surface S with charged wire on its axis and point P on its surface, then net electric flux through surface S is



$$\phi = \oint_S \mathbf{E} \cdot d\mathbf{S}$$

$$= \int_{\text{Upper plane face}} EdS \cos 90^\circ + \int_{\text{Curved surface}} EdS \cos 0^\circ + \int_{\text{Lower plane face}} EdS \cos 90^\circ$$

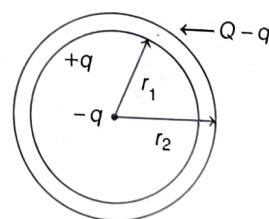
$$\phi = 0 + EA + 0 \text{ or } \phi = E \cdot 2\pi rl$$

But, by Gauss' theorem, $\phi = q/\epsilon_0 = \lambda l/\epsilon_0$, where, q is the charge on length l of wire enclosed by cylindrical surface S and λ is uniform linear charge density of wire.

$$\therefore E \times 2\pi rl = \frac{\lambda l}{\epsilon_0} \Rightarrow E = \frac{\lambda}{2\pi\epsilon_0 r}$$

Thus, electric field of a line charge is inversely proportional to distance directed normal to the surface of charged wire.

24. (i) When a charge $-q$ is placed at the centre of the hollow conducting sphere, then the charge induced on the inner surface is $+q$ and on outer surface is $-q$. But charge Q is already present on its outer surface. So, net charge on outer surface is $(Q - q)$ as shown.



Therefore, surface charge density on

$$(a) \text{ inner surface is } \frac{q}{4\pi r_1^2}$$

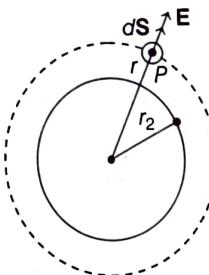
$$(b) \text{ and on outer surface is } \frac{Q-q}{4\pi r_2^2}.$$

- (ii) By Gauss's law, at a point lying outside the sphere the electric flux is given by

$$\phi_E = \oint_S \mathbf{E} \cdot d\mathbf{S} = \frac{q}{\epsilon_0}$$

where, q is the net charge enclosed.

As \mathbf{E} and $d\mathbf{S}$ are in same direction as shown.



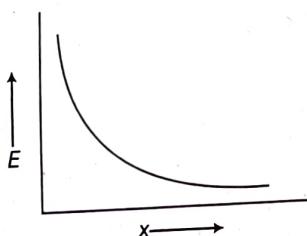
$$\therefore E (4\pi r^2) = \frac{Q-q}{\epsilon_0}$$

$$\Rightarrow \text{Electric field, } E = \frac{Q-q}{4\pi \epsilon_0 r^2}$$

25. (i) Refer to Sol. 23 on pages 26.

(Replacing r by x).

- (ii) Electric field E due to the linear charge is inversely proportional to the distance x from the linear charge. The variation of electric field E with distance x is shown in figure.



26. (i) As the electrostatic field inside a conductor is zero.

By using Gauss's law,

Charge $-Q$ is induced on the inner surface and $+Q$ is induced on the outer surface of the hollow spherical conductor.

\therefore Surface charge density on the inner surface

$$= \frac{-Q}{4\pi a^2}$$

Surface charge density on the outer surface

$$= \frac{+Q}{4\pi b^2}$$

$$(ii) \text{ Using } \mathbf{F} = \frac{1}{4\pi \epsilon_0} \times \frac{Q}{r^2}$$

$$(a) \text{ For } r = a/2,$$

$$F = \frac{1}{4\pi \epsilon_0} \times \frac{Q}{(a/2)^2} = \frac{1}{4\pi \epsilon_0} \times \frac{4Q}{a^2}$$

$$(ii) \text{ For } r = 2b,$$

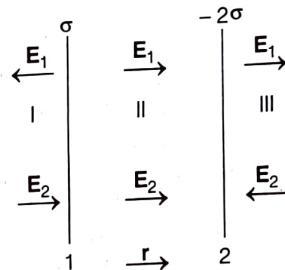
$$F = \frac{1}{4\pi \epsilon_0} \times \frac{Q}{(2b)^2} = \frac{1}{4\pi \epsilon_0} \times \frac{Q}{4b^2}$$

$$= \frac{1}{16\pi \epsilon_0} \frac{Q}{b^2}$$

27. (i) Electric field to the left of first sheet (region I)

$$\mathbf{E}_I = \mathbf{E}_1 + \mathbf{E}_2 = \frac{2\sigma}{2\epsilon_0} \mathbf{r} - \frac{\sigma}{2\epsilon_0} \mathbf{r}$$

where \mathbf{r} be the unit vector in the direction from first sheet (+ve sheet) to second sheet (-ve sheet)



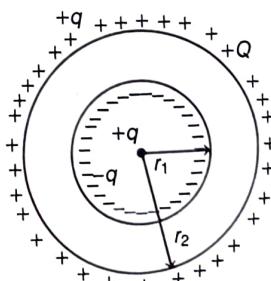
- (ii) Electric field to the right of second sheet (region III)

$$\mathbf{E}_{III} = \frac{\sigma}{2\epsilon_0} \mathbf{r} - \frac{2\sigma}{2\epsilon_0} \mathbf{r}$$

- (iii) Electric field between two sheets (region II)

$$\mathbf{E}_{II} = \frac{\sigma}{2\epsilon_0} \mathbf{r} + \frac{2\sigma}{2\epsilon_0} \mathbf{r}$$

28. (i) When a charge $+q$ is placed at the centre of spherical cavity as shown in the figure, then the charge induced on the inner surface of a shell is $-q$ and the charge induced on the outer surface of shell is $+q$. So,



(a) Outer surface charge density = $\frac{Q+q}{4\pi r_2^2}$

(b) Inner surface charge density = $\frac{-q}{4\pi r_1^2}$

- (ii) Yes, the electric field inside a cavity is zero irrespective of shape because the cavity has enclosed zero net charge.

29. Refer to text on page 17 (Electric flux).

Since, the electric field is only an x component for face perpendicular to x direction.

The flux, $\phi = E\Delta s$ is separately zero for each face of the cube except the two faces i.e. front and its opposite ones.

Now, the magnitude of electric field at the left face is $E_L = \alpha x = \alpha a$ ($\because x = a$ at the left face)

$$\text{So, } \phi = E_L \Delta s \cos \theta = \alpha a [a^2 \cos 180^\circ] = -\alpha a^3$$

$(\because \theta = 180^\circ)$

Field at right face, i.e. $x = 2a$

$$\begin{aligned} E_R &= \alpha x = \alpha 2a \\ \Rightarrow \phi &= E_R \Delta s \cos \theta = 2a \alpha [a^2 \cos 0^\circ] = 2\alpha a^3 \\ \therefore \phi_{\text{net}} &= 2\alpha a^3 - \alpha a^3 = \alpha a^3 \quad (\because \theta = 0^\circ) \end{aligned}$$

According to Gauss' law

$$\begin{aligned} \phi_{\text{net}} &= \frac{Q}{\epsilon_0} \Rightarrow Q = \epsilon_0 \phi_{\text{net}} \\ &= 8.85 \times 10^{-12} \times 100 \times (0.1)^3 = 8.85 \times 10^{-13} \text{ C} \end{aligned}$$

30. (i) At point C inside the shell.

The electric field inside a spherical shell is zero. Thus, the force experienced by charge at the centre C will also be zero.

$$\begin{aligned} \therefore F_C &= qE \quad (E_{\text{inside the shell}} = 0) \\ \therefore F_C &= 0 \end{aligned}$$

$$\text{At point } A, |F_A| = 2Q \left(\frac{1}{4\pi\epsilon_0} \frac{3Q/2}{x^2} \right)$$

$$F = \frac{3Q^2}{4\pi\epsilon_0 x^2} \text{ away from shell}$$

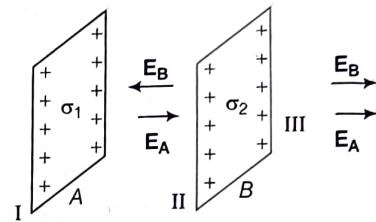
(ii) Electric flux through the shell,

$$\begin{aligned} \phi &= \frac{1}{\epsilon_0} \times \text{Magnitude of the charge enclosed by the shell} \\ \Rightarrow \phi &= 1/\epsilon_0 \times Q/2 = Q/2\epsilon_0 \end{aligned}$$

- 31.** According to the figure, A and B are two thin parallel plane sheets of charge having uniform densities σ_1 and σ_2 with $\sigma_1 > \sigma_2$.

$\phi = E \times \text{area of the end faces of the Gaussian cylinder}$

$$E \times 2A = \frac{\sigma A}{\epsilon_0} \Rightarrow E = \frac{\sigma}{2\epsilon_0}$$



In region II

The electric field due to the sheet of charge A will be from left to right (along the positive direction) and that due to the sheet of charge B will be from right to left (along the negative direction).

Therefore, in region II, we have

$$\begin{aligned} E &= \frac{\sigma_1}{2\epsilon_0} + \left(-\frac{\sigma_2}{2\epsilon_0} \right) \\ \Rightarrow E &= \frac{1}{2\epsilon_0} (\sigma_1 - \sigma_2) \quad (\text{along positive direction}) \end{aligned}$$

In region III

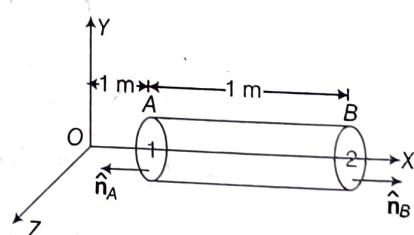
The electric fields due to both the charged sheets will be from left to right, i.e. along the positive direction. Therefore, in region III, we have

$$E = \frac{\sigma_1}{2\epsilon_0} + \frac{\sigma_2}{2\epsilon_0}$$

$$E = \frac{1}{\epsilon_0} (\sigma_1 + \sigma_2) \quad (\text{along positive direction})$$

32. (i) Given, $\mathbf{E} = 50x \hat{\mathbf{i}}$

$$\text{and } \Delta S = 25 \text{ cm}^2 = 25 \times 10^{-4} \text{ m}^2$$



As the electric field is only along the X -axis, so flux will pass only through the cross-section of the cylinder.

Magnitude of electric field at cross-section A,

$$E_A = 50 \times 1 = 50 \text{ NC}^{-1}$$

Magnitude of electric field at cross-section B,

$$E_B = 50 \times 2 = 100 \text{ NC}^{-1}$$

The corresponding electric fluxes are

$$\begin{aligned}\phi_A &= \mathbf{E}_A \cdot d\mathbf{S} = 50 \times 25 \times 10^{-4} \times \cos 180^\circ \\ &= -0.125 \text{ Nm}^2 \text{ C}^{-1}\end{aligned}$$

$$\begin{aligned}\phi_B &= \mathbf{E}_B \cdot d\mathbf{S} = 100 \times 25 \times 10^{-4} \times \cos 0^\circ \\ &= 0.25 \text{ Nm}^2 \text{ C}^{-1}\end{aligned}$$

So, the net flux through the cylinder,

$$\begin{aligned}\phi &= \phi_A + \phi_B = -0.125 + 0.25 \\ &= 0.125 \text{ Nm}^2 \text{ C}^{-1}\end{aligned}$$

(ii) Using Gauss' law, $\phi = \oint \mathbf{E} \cdot d\mathbf{l} = \frac{q}{\epsilon_0}$

$$\Rightarrow 0.125 = \frac{q}{8.85 \times 10^{-12}}$$

$$\Rightarrow q = 8.85 \times 0.125 \times 10^{-12} \Rightarrow q = 1.1 \times 10^{-12} \text{ C}$$

So, the charge enclosed by the cylinder is

$$1.1 \times 10^{-12} \text{ C.}$$

33. (i) **Gauss' law** states that the total flux through a closed surface is $\frac{1}{\epsilon_0}$ times the net charge enclosed by the closed surface. Mathematically,

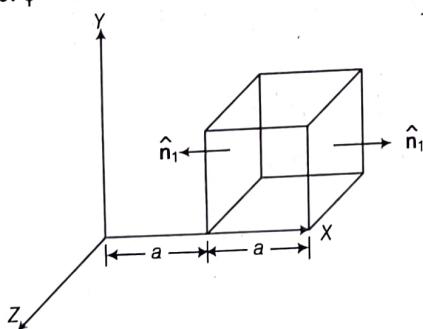
$$\phi_E = \oint_S \mathbf{E} \cdot d\mathbf{S} = \frac{q}{\epsilon_0}.$$

Here, ϵ_0 is the absolute permittivity of the free space, q is the total charge enclosed the closed surface and \mathbf{E} is the electric field at the area element $d\mathbf{S}$.

(ii) Refer to Sol. 23 on Page 26.

34. Refer to text on page 17 (Gauss's theorem)

Now, the electric field $\mathbf{E} = Cx \hat{i}$ is in X -direction only. So, the faces of the cube with surface normal vector perpendicular to this field would give zero electric flux, i.e. $\phi = E dS \cos 90^\circ = 0$ through it.



So, flux would be across only two surfaces.

Magnitude of E at left face,

$$E_L = Cx = Ca \quad [x = a \text{ at left face}]$$

Magnitude of E at right face

$$E_R = Cx = C2a = 2aC \quad [x = 2a \text{ at right face}]$$

Thus, corresponding fluxes are

$$\begin{aligned}\phi_L &= \mathbf{E}_L \cdot d\mathbf{S} = E_L dS \cos \theta \\ &= -aC \times a^2 \quad [\text{As, } \theta = 180^\circ]\end{aligned}$$

$$\begin{aligned}\phi_R &= \mathbf{E}_R \cdot d\mathbf{S} = 2aC dS \cos \theta \quad [\because \theta = 0^\circ] \\ &= 2aCa^2 = 2a^3C\end{aligned}$$

(i) Now, net electric flux through the cube is

$$\begin{aligned}&= \phi_L + \phi_R = -a^3C + 2a^3C \\ &= a^3C \text{ Nm}^2 \text{ C}^{-1}\end{aligned}$$

(ii) Net charge inside the cube

Again, we can use Gauss' law to find total charge q inside the cube.

We have $\phi = \frac{q}{\epsilon_0}$

or $q = \phi \epsilon_0 \quad q = a^3C\epsilon_0 \text{ coulomb}$

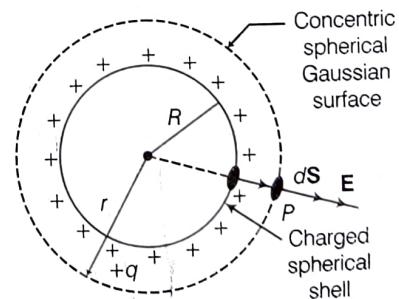


Common Mistake Students think that, the flux $\phi = E \cdot d\mathbf{S}$ is zero here for all faces of the cube but electric flux is zero for each face of the cube except the two faces, i.e. front and opposite others.

35. Let us consider charge $+q$ be uniformly distributed over a spherical shell of radius R . Let E is to be obtained at P lying outside of spherical shell.

$\therefore E$ at any point is radially outward (if charge q is positive) and has same magnitude at all points which lie at the same distance r from centre of spherical shell such that $r > R$.

Therefore, Gaussian surface is concentric sphere of radius r such that $r > R$.



By Gauss' theorem,

$$\oint \mathbf{E} \cdot d\mathbf{S} = \frac{q}{\epsilon_0}$$

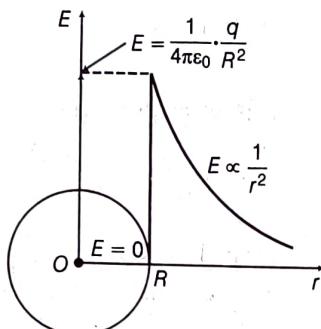
$$\Rightarrow \oint E dS \cos 0^\circ = \frac{q}{\epsilon_0}$$

[$\because E$ and dS are along the same direction]

$$E \cdot \oint dS = \frac{q}{\epsilon_0} \quad [\because \text{Magnitude of } E \text{ is same at every point on Gaussian surface}]$$

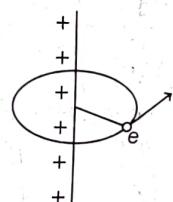
$$E \times 4\pi r^2 = \frac{q}{\epsilon_0} \Rightarrow E = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r^2}$$

Now, graph



36. (i) Refer to solution 23 on page 26.

(ii) For infinitely long positive charged straight wire,



$$E = \frac{\lambda}{2\pi\epsilon_0 r} \quad \dots (i)$$

The electron revolving, experience an electrostatic force and centripetal force,

$$\text{So, } eE = \frac{mv^2}{r} \quad \dots (ii)$$

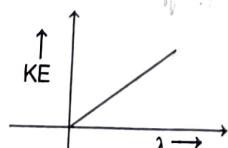
For Eq. (i),

$$\frac{e\lambda}{2\pi\epsilon_0 r} = \frac{mv^2}{r} \Rightarrow mv^2 = \frac{e\lambda}{2\pi\epsilon_0}$$

Kinetic energy of the revolving electron,

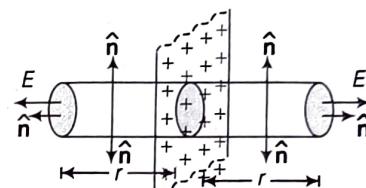
$$KE = \frac{1}{2}mv^2 = \frac{e\lambda}{4\pi\epsilon_0}$$

(iii) Graph of kinetic energy and linear charge density λ .



37. (i) Refer to text on page 17 (Electric flux)

(ii) According to the question, σ is the surface charge density of the sheet. From symmetry, E on either side of the sheet must be perpendicular to the plane of the sheet having same magnitude at all equidistant points from the sheet. We take a cylinder of cross-sectional area A and length $2r$ as the Gaussian surface. On the curved surface of the cylinder, E and \hat{n} are perpendicular to each other. Therefore, the flux through the curved surface of the cylinder = 0.



Flux through the flat surfaces = $EA + EA = 2EA$
The total electric flux over the entire surface of cylinder

$$\phi_E = 2EA$$

Total charge enclosed by the cylinder, $q = \sigma A$

According to Gauss's law,

$$\phi_E = \frac{q}{\epsilon_0} \Rightarrow 2AE = \frac{\sigma A}{\epsilon_0} \text{ or } E = \frac{\sigma}{2\epsilon_0}$$

E is independent of r i.e. the distance of the point from the plane charged sheet. E at any point is directed away from the sheet for positive charge and directed towards the sheet in case of negative charge.

$$(iii) \text{ Given, } \mathbf{E} = (Ax + B) \hat{i} \frac{\mathbf{N}}{C}$$

$$\mathbf{E} \cdot \Delta \mathbf{S} = (Ax + B) \hat{i} \cdot L^2 (-\hat{i})$$

Here, $x = 0$

$$\therefore E \cdot \Delta s = B \hat{i} \cdot L^2 (-\hat{i})$$

$$\phi_L = -BL^2 \quad \dots (i)$$

For right side,

$$\mathbf{E} \cdot \Delta \mathbf{S} = (Ax + B) \hat{i} \cdot L^2 \hat{i} = AL^2 x + BL^2$$

Here, $x = L$

$$\text{then, } \phi_R = AL^3 + BL^2 \quad \dots (ii)$$

From Eqs. (i) and (ii),

$$\begin{aligned} \phi_{\text{net}} &= 3\phi_R + \phi_L \\ &= AL^3 + BL^2 + (-BL^2) \end{aligned}$$

$$\phi_{\text{net}} = AL^3$$

38. (i) Refer to text on page 17 (Gauss' Theorem).

As we know, $d\phi = \mathbf{E} \cdot d\mathbf{s}$

$$= \frac{Kq}{r^2} \hat{\mathbf{r}} \cdot d\mathbf{s} \quad (\because \hat{\mathbf{r}} \cdot d\mathbf{s} = \hat{\mathbf{r}} \cdot d\mathbf{s} \cdot \hat{\mathbf{s}})$$

$$\therefore \int_S d\phi = \int_S Kq \left(\frac{ds}{r^2} \right) \hat{\mathbf{r}} \cdot d\hat{\mathbf{s}}$$

$$\phi = \int_S Kq \left(\frac{ds}{r^2} \right) \cdot 1$$

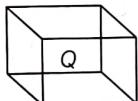
$$\text{As, } (\hat{\mathbf{r}} \cdot d\hat{\mathbf{s}} = |\hat{\mathbf{r}}| |d\hat{\mathbf{s}}| \cos 0^\circ = 1)$$

$$\text{Now, } \phi = Kq \int_S \frac{ds}{r^2} = Kq \frac{4\pi r^2}{r^2} = Kq \cdot 4\pi$$

$$\text{Then, } \phi = \frac{1}{4\pi\epsilon_0} q : 4\pi$$

$$\phi = \frac{q}{\epsilon_0} \text{ (i.e. independent of shape and size)}$$

Figures are



Flux through both the closed surfaces will be same.

(ii) Electric field to the left of sheet of charge density $+2\sigma$,

$$\mathbf{E}_A = \frac{2\sigma}{2\epsilon_0} (-\hat{\mathbf{i}}) + \frac{2\sigma}{2\epsilon_0} (\hat{\mathbf{i}}) + \frac{\sigma}{2\epsilon_0} (-\hat{\mathbf{i}}) \quad \dots (i)$$

Now for the right of sheet of charge density $+\sigma$,

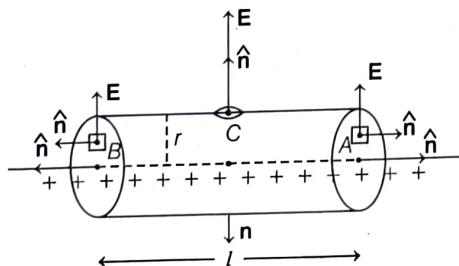
$$\mathbf{E}_D = \frac{\sigma}{2\epsilon_0} (\hat{\mathbf{i}}) - \frac{2\sigma}{2\epsilon_0} (\hat{\mathbf{i}}) + \frac{2\sigma}{2\epsilon_0} (\hat{\mathbf{i}}) \quad \dots (ii)$$

From Eq. (i), we get

$$\mathbf{E}_A = \frac{\sigma}{2\epsilon_0} (-\hat{\mathbf{i}})$$

$$\text{and from Eq. (ii)} \mathbf{E}_D = \frac{\sigma}{2\epsilon_0} (\hat{\mathbf{i}})$$

39. (i) Consider an infinitely long thin straight wire with uniform linear charge density (λ).



From symmetry, the electric field is everywhere radial in the plane cutting the wire normally and its magnitude only depends on the radial distance (r).

$$\text{From Gauss' law } \phi_E = \oint_S \mathbf{E} \cdot d\mathbf{S} = \frac{q}{\epsilon_0}$$

$$\text{Now, } \phi_E = \oint_S \mathbf{E} \cdot d\mathbf{S} = \oint_S \mathbf{E} \cdot \hat{\mathbf{n}} d\mathbf{S}$$

$$= \oint_A \mathbf{E} \cdot \hat{\mathbf{n}} d\mathbf{S} + \oint_B \mathbf{E} \cdot \hat{\mathbf{n}} d\mathbf{S} + \oint_C \mathbf{E} \cdot \hat{\mathbf{n}} d\mathbf{S}$$

$$\therefore \oint_S \mathbf{E} \cdot d\mathbf{S} = \oint_A \mathbf{E} \cdot d\mathbf{S} \cos 90^\circ$$

$$+ \oint_B \mathbf{E} \cdot d\mathbf{S} \cos 90^\circ + \oint_C \mathbf{E} \cdot d\mathbf{S} \cos 0^\circ$$

$$= \oint_S \mathbf{E} \cdot d\mathbf{S} = E (2\pi rl)$$

Charge enclosed in the cylinder, $q = \lambda l$

$$\therefore E (2\pi rl) = \frac{\lambda l}{\epsilon_0} \text{ or } E = \frac{\lambda}{2\pi\epsilon_0 r}$$

(ii) (a) Given, $E_x = \alpha x$, $E_y = 0$, $E_z = 0$

$$\alpha = 400 \text{ N/cm} \quad a = 0.1 \text{ m}, \phi = ? \quad q = ?$$

As the electric field has only x -component, therefore $\mathbf{E} \cdot \Delta \mathbf{s} = \phi_E = 0$ for each of four faces of cube perpendicular to Y -axis and Z -axis.

Flux is there only for left face L and right face R of the cube.

At the left face, $x = a$

$$E_L = \alpha a$$

Flux for left face of cube,

$$\phi_L = \mathbf{E} \cdot \Delta \mathbf{s} = \alpha a \cdot (a^2) \cos 180^\circ = -\alpha a^3 \quad \dots (i)$$

Similarly, at right face,

$$x = a + a = 2a$$

$$E_R = \alpha (2a)$$

$$\phi_R = \mathbf{E} \cdot \Delta \mathbf{s} = \alpha (2a) (a^2) \cos 0^\circ$$

$$= \alpha (2a) a^2 \quad \dots (ii)$$

From Eqs. (i) and (ii),

The net flux through the cube,

$$\phi_{\text{net}} = \phi_R + \phi_L = \alpha (2a) a^2 - \alpha a^3$$

$$= 400 \times 2a^3 - 400 a^3$$

$$= 800 a^3 - 400 a^3$$

$$= 400 (a)^3 = 400 (0.1)^3$$

$$\phi_{\text{net}} = 0.4 \text{ Nm}^2 \text{C}^{-1}$$

- (b) Applying Gauss' theorem and the charge within the cube,

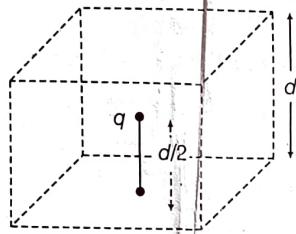
$$\begin{aligned} q &= \epsilon_0 \times \phi \\ &= 8.85 \times 10^{-12} \times 0.4 \\ &= 3.540 \times 10^{-12} \text{ C} \end{aligned}$$

40. (i) **Electric flux** It is defined as the total number of electric field lines that are normally pass through that surface.

Total electric flux ϕ over the whole surface S due to an electric field E is given as

$$\phi = \oint_S \mathbf{E} \cdot d\mathbf{S} = \oint_S E dS \cos \theta$$

It is a scalar quantity.



From the given problem, q is the point charge at a distance of $\frac{d}{2}$ directly above the centre of the square side.

Now, construct a Gaussian surface in form of a cube of side d to evaluate the amount of electric flux.

\therefore We can calculate the amount of electric flux for six surfaces by using Gauss' law,

$$\phi_E = \oint_S \mathbf{E} \cdot d\mathbf{S} = \frac{q}{\epsilon_0}$$

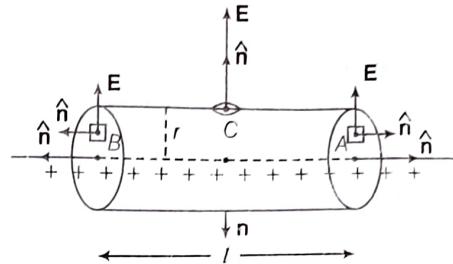
\therefore For one surface of the cube, amount of electric flux is given as $\phi_{E'} = \frac{q}{6\epsilon_0}$

(ii) Even if the point charge is moved to a distance d from the centre of the square and side of the square is doubled, but amount of charge enclosed into the Gaussian surface does not change.

\therefore The amount of electric flux remains same.

41. (i) **Field due to an infinitely long thin straight charged line**

Consider an infinitely long thin straight line with uniform linear charge density (λ).



From symmetry, the electric field is everywhere in the radial direction and its magnitude only depends on the radial distance (r).

From Gauss' law,

$$\phi_E = \oint_S \mathbf{E} \cdot d\mathbf{S} = \frac{q}{\epsilon_0}$$

$$\begin{aligned} \text{Now, } \phi_E &= \oint_S \mathbf{E} \cdot d\mathbf{S} = \oint_S \mathbf{E} \cdot \hat{n} dS \\ &= \oint_A \mathbf{E} \cdot \hat{n} dS + \oint_B \mathbf{E} \cdot \hat{n} dS + \oint_C \mathbf{E} \cdot \hat{n} dS \\ \therefore \oint_S \mathbf{E} \cdot d\mathbf{S} &= \oint_A \mathbf{E} dS \cos 90^\circ + \oint_B \mathbf{E} dS \cos 90^\circ \\ &\quad + \oint_C \mathbf{E} dS \cos 0^\circ \\ &= \oint_C \mathbf{E} dS = E(2\pi rl) \end{aligned}$$

Charge enclosed in the cylinder, $q = \lambda l$

$$\therefore E(2\pi rl) = \frac{\lambda l}{\epsilon_0}$$

$$\text{or } E = \frac{\lambda}{2\pi\epsilon_0 r}$$

The direction of the electric field is radially outward from the positive line charge. For negative line charge, it will be radially inward.

- (ii) Refer to sol 25 (ii) on page 27 (Replacing x by r)

$$\begin{aligned} (\text{iii}) V &= \int \mathbf{E} \cdot d\mathbf{r} = \int_{r_1}^{r_2} \frac{\lambda}{2\pi\epsilon_0 r} dr = \frac{\lambda}{2\pi\epsilon_0} \cdot \int_{r_1}^{r_2} \frac{1}{r} dr \\ &= \frac{\lambda}{2\pi\epsilon_0} \left[\log \frac{r_2}{r_1} \right] \end{aligned}$$

$$\text{Work done} = qV = q \left[\frac{\lambda}{2\pi\epsilon_0} \left(\log \frac{r_2}{r_1} \right) \right]$$

Concept Enhancer The electric field due to infinitely long line charge depends upon the distance of the observation point from the line charge.

42. (i) Refer to Sol. 37 (ii) on Page 30.

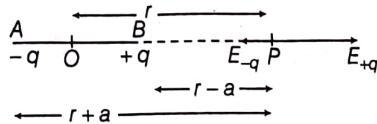
- (ii) Surface charge density of the uniform plane sheet which is infinitely large $= +\sigma$. The electric potential (V) due to infinite sheet of uniform charge density $+\sigma$

$$V = -\frac{\sigma r}{2\epsilon_0}$$

The amount of work done in bringing a point charge q from infinite to point of distance r in front of the charged plane sheet.

$$W = q \times V = q \cdot \frac{-\sigma r}{2\epsilon_0} = -\frac{\sigma r \cdot q}{2\epsilon_0} \text{ J}$$

43. (i) Electric field on an axial line of an electric dipole



Let P be the point at distance r from the centre of the dipole on the side of charge $+q$.

Then, the electric field at point P due to charge $-q$ of the dipole is given by,

$$\mathbf{E}_{-q} = -\frac{q}{4\pi\epsilon_0(r+a)^2} \hat{\mathbf{p}}$$

where, $\hat{\mathbf{p}}$ is the unit vector along the dipole axis (from $-q$ to $+q$).

Also, the electric field at point P due to charge $+q$ of the dipole is given by, $\mathbf{E}_{+q} = \frac{q}{4\pi\epsilon_0(r-a)^2} \hat{\mathbf{p}}$

The total field at point P is

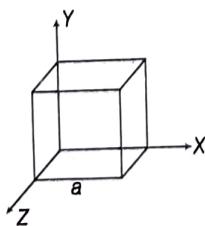
$$\mathbf{E} = \mathbf{E}_{+q} + \mathbf{E}_{-q} = \frac{q}{4\pi\epsilon_0} \left[\frac{1}{(r-a)^2} - \frac{1}{(r+a)^2} \right] \hat{\mathbf{p}}$$

$$\Rightarrow \mathbf{E} = \frac{q}{4\pi\epsilon_0} \cdot \frac{4ar}{(r^2 - a^2)^2} \hat{\mathbf{p}} \quad [:: r=x] \text{ (given)}$$

$$\mathbf{E} = \frac{q}{4\pi\epsilon_0} \frac{4ax}{(x^2 - a^2)^2} \hat{\mathbf{p}}$$

$$\text{For } x \gg a, \quad \mathbf{E} = \frac{4qa}{4\pi\epsilon_0 x^3} \hat{\mathbf{p}} \Rightarrow \mathbf{E} = \frac{2\mathbf{p}}{4\pi\epsilon_0 x^3} \quad [:: p = 2qa]$$

(ii)



Since, the electric field has only x component. For faces normal to X -direction the angle between E and ΔS is 0° . Therefore, the flux is separately zero for each of the cube except the surface perpendicular to X -axis.

The magnitude of the electric field at the left face is

$$E_L = 0 \quad (\text{as, } x=0 \text{ at the left face}).$$

The magnitude of the electric field at the right face is $E_R = 2a$ (as, $x=a$ at the right face).

The corresponding fluxes are

$$\begin{aligned} \phi_L &= \mathbf{E}_L \cdot \Delta \mathbf{S} = 0 \\ \phi_R &= \mathbf{E}_R \cdot \Delta \mathbf{S} \\ &= E_R \Delta S \cos \theta = E_R \Delta S \quad (\because \theta = 0^\circ) \\ \Rightarrow \phi_R &= E_R a^2 \end{aligned}$$

Net flux through the cube

$$\begin{aligned} \phi &= \phi_L + \phi_R \\ &= 0 + E_R a^2 = E_R a^2 \\ \Rightarrow \phi &= 2a(a)^2 = 2a^3 \end{aligned}$$

We can use Gauss' law to find the total charge q inside the cube.

$$\phi = q/\epsilon_0$$

$$\therefore \phi = \phi \epsilon_0 = 2a^3 \epsilon_0$$

44. (i) Refer to text on page 17 (Electric flux).

The SI unit of electric flux is $\text{N}\cdot\text{m}^2\text{C}^{-1}$.

According to Gauss' law in electrostatics, the surface integral of electrostatic field \mathbf{E} produced by any sources over any closed surface S enclosing a volume V in vacuum is $\frac{q}{\epsilon_0}$ i.e. total electric flux

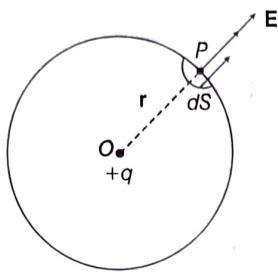
over the closed surface S in vacuum is $1/\epsilon_0$ times the total charge (q) contained inside S , i.e.

$$\phi_E = \oint_S \mathbf{E} \cdot d\mathbf{S} = \frac{q}{\epsilon_0}$$

Gauss' law in electrostatics is true for an closed surface, no matter what its shape or size is. In order to justify the above statement, consider an isolated positive charge q situated at the centre O of a sphere of radius r .

According to Coulomb's law, electric field intensity at any point P on the surface of the sphere is

$$\mathbf{E} = \frac{q}{4\pi\epsilon_0 r^2} \hat{\mathbf{r}}$$



where, \hat{r} is unit vector directed from O to P .

Consider a small area element dS of the sphere around P . Let it be represented by the vector $d\mathbf{S}$ or $\hat{n} \cdot dS$.

where, \hat{n} is unit vector along normal to the area element.

\therefore Electric flux over the area element,

$$\begin{aligned}d\phi_E &= \mathbf{E} \cdot d\mathbf{S} \\&= (q/4\pi\epsilon_0 \cdot \hat{r}/r^2) \cdot (\hat{n} \cdot dS) \\&= \mathbf{E} \cdot d\mathbf{S} = q/4\pi\epsilon_0 \cdot dS/r^2 \cdot \hat{r} \cdot \hat{n}\end{aligned}$$

As normal to a surface of every point is along the radius vector at that point. Therefore, $\hat{r} \cdot \hat{n} = 1$

$$\mathbf{E} \cdot d\mathbf{S} = q/4\pi\epsilon_0 \cdot dS/r^2$$

Integrating over the closed surface area of the sphere, we get total normal electric flux over the entire sphere,

$$\begin{aligned}\phi_E &= \oint_S \mathbf{E} \cdot d\mathbf{S} = \frac{q}{4\pi\epsilon_0 r^2} \oint_S dS \\&= \frac{q}{4\pi\epsilon_0 r^2} \times \text{total area of surface of sphere} \\&= \frac{q}{4\pi\epsilon_0 r^2} (4\pi r^2) = \frac{q}{\epsilon_0}\end{aligned}$$

Hence, $\oint_S \mathbf{E} \cdot d\mathbf{S} = q/\epsilon_0$, which proves Gauss' theorem.

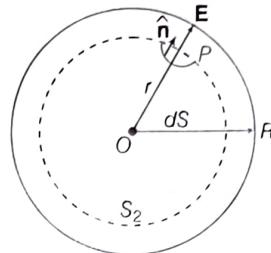
(ii) Electric field inside a uniformly charged spherical shell

According to Gauss' theorem

$$\begin{aligned}\oint_S \mathbf{E} \cdot d\mathbf{S} &= \oint_S \mathbf{E} \cdot \hat{n} \cdot dS = \frac{q}{\epsilon_0} \\ \text{or } E \oint_S dS &= \frac{q}{\epsilon_0} \\ \therefore E \cdot 4\pi r^2 &= q/\epsilon_0 \\ \Rightarrow E &= q/4\pi\epsilon_0 r^2\end{aligned} \quad \dots(i)$$

In the given figure, the point P where we have to find the electric field intensity is inside the shell. The Gaussian surface is the surface of a sphere S_2

S_2 passing through P and with the centre at O . The radius of the sphere S_2 is $r < R$.



The electric flux through the Gaussian surface, as calculated in Eq. (i), i.e. $E \times 4\pi r^2$. As, charge inside a spherical shell is zero. So, the Gaussian surface encloses no charge. The Gauss' theorem gives

$$E \times 4\pi r^2 = \frac{q}{\epsilon_0} = 0$$

$$\therefore E = 0 \text{ for } r < R.$$

Hence, the field due to a uniformly charged spherical shell is zero at all points inside the shell.

45. (i) Refer to text on page 4 (Torque on an electric dipole placed in a uniform electric field).
(ii) Refer to Sol. 22 on page 26.
46. (i) Refer to Sol. 35 on pages 29, 30 and refer to Sol. 44 (ii) on page 34.
(ii) Refer to Sol. 37 (ii) on page 30.
47. (i) Refer to text on page 17 (Electric flux).
(ii) Refer to Sol. 37 (ii) on page 30.

$$E = \frac{\sigma}{2\epsilon_0}$$

Hence, electric field at a point is independent of distance from the sheet.

- (a) Normally away from the sheet when sheet is positively charged.
(b) Normally inward towards the sheet when plane sheet is negatively charged.

48. (i) (c) Copper
(ii) (a) Car
(iii) (c) Zero
(iv) (c) Its surface have charge equal to $-q$.
(v) (b) $q = 2 \mu\text{C}$

$$\phi = \frac{q}{\epsilon_0} = \frac{2 \times 10^{-6}}{8.85 \times 10^{-12}}$$

$$\phi = 225 \times 10^5 \text{ Nm}^2/\text{C} \text{ leaving the surface}$$