

# ADABOOST Report

## Introduction to Adaboost and algorithm used:

Adaboost is defined as a booster and it works in a number of rounds. At round the 't' booster defines a distribution of weights over training examples, and the weak learner produces a weak hypothesis this implementation can be defined using an algorithm.

### Algorithm:

input:

training set  $S = (x_1, y_1), \dots, (x_m, y_m)$

weak learner WL

number of rounds T

initialize  $D(1) = (1/m, \dots, 1/m)$ .

for  $t = 1, \dots, T$ :

invoke weak learner  $h_t = \text{WL}(D(t), S)$

compute  $\text{error}_t = \sum_{i=1}^m D_i(t) \cdot 1[y_i \neq h_t(x_i)]$

let  $\text{weight}_t = 1/2 \cdot \log(1/\text{error}_t)$

update  $D_{t+1}(i) = D_t(i) \cdot \exp(-\text{weight}_t \cdot y_i \cdot h_t(x_i)) / \sum_{j=1}^m D_t(j) \cdot \exp(-\text{weight}_t \cdot y_j \cdot h_t(x_j))$  for all  $i = 1, \dots, m$

output the hypothesis  $h_s(x) = \text{sign}(\sum_{t=1}^T \text{weight}_t \cdot h_t(x))$ .

By using the above defined algorithm, to calculate the error and update the weight, weak learners can be used in adaboost to produce a much better hypothesis.

## Implementation of Code:

1. In the code defined I have defined a class which contains the different methods used for fitting the model and predicting the output of the defined model.
2. Used Decision tree classifiers as weak classifiers at each iteration to create appropriate decision stumps.
3. Created a function named `plot_adaboost_in2D` to plot the decision boundary of the adaboost classifier.
4. Used `make_gaussian_quantiles` to create a random data set of defined data points.
5. **For different values of data points change the value of variable 'n' and for different numbers of weak classifiers change the value of variable 'i'**
6. **For checking the value of error and weights, set `iteration_information` to True during model creation, otherwise set False.**
7. **Finally a plot is provided for minimum train and test error in which the maximum number of weak classifiers to get minimum train and test error is used.**

## Experiments Conducted and Observations:

1. **Comparison with AdaBoostClassifier defined in sklearn.ensemble:** By comparing the two models for constant value of data points and iterations. It is observed that both the models have the same performance.
2. **Different Values of Iterations:** While using different values of iterations or weak learners it is observed that with a constant data points the number of weak learners can vary but they are mostly less than  $n/2$  where  $n$  is the number of data points.

Example:

1. For  $n = 160$  the number of weak learners for 100% accuracy is around 47.
2. For  $n = 50$  the number of weak learners for highest accuracy is around 14.
3. **Plotting the Decision boundary for Different values of Data points and iterations:** It is observed that when try to plot decision boundary or even calculating error without plotting the boundary, as the number of data points increases the time taken by program for different number of iterations/weak classifiers is increased gradually the machine is not able to handle large values of data points and weak classifiers.

**Note:**

1. For very large data points above 100 the machine could not produce the plots for different iterations hence for data points above 100 plots are not plotted.
2. Even for data points less than 100 the plots are only checked and plotted for  $n/2$  iterations as the minimum number of iterations can be found out in  $n/2$  iterations for minimum train and test error.