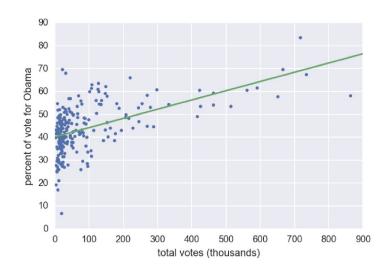
Formulating and simulating a hypothesis

2008 US swing state election results



¹ Data retrieved from Data.gov (https://www.data.gov/)



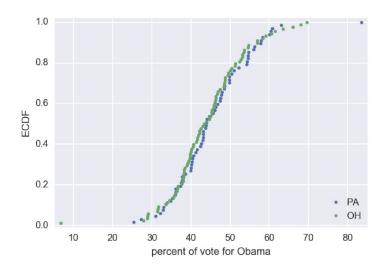
Hypothesis testing

• Assessment of how reasonable the observed data are assuming a hypothesis is true

Null hypothesis

Another name for the hypothesis you are testing

ECDFs of swing state election results



¹ Data retrieved from Data.gov (https://www.data.gov/)

Percent vote for Obama

	PA	ОН	PA — OH difference
mean	45.5%	44.3%	1.2%
median	44.0%	43.7%	0.4%
standard deviation	9.8%	9.9%	-0.1%

¹ Data retrieved from Data.gov (https://www.data.gov/)

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60.08, 40.64, 36.07, 41.21, 31.04, 43.78, 44.08, 46.85,
44.71, 46.15, 63.10, 52.20, 43.18, 40.24, 39.92, 47.87,
37.77, 40.11, 49.85, 48.61, 38.62, 54.25, 34.84, 47.75,
43.82, 55.97, 58.23, 42.97, 42.38, 36.11, 37.53, 42.65,
                                                          Pennsylvania
50.96, 47.43, 56.24, 45.60, 46.39, 35.22, 48.56, 32.97,
57.88, 36.05, 37.72, 50.36, 32.12, 41.55, 54.66, 57.81,
54.58, 32.88, 54.37, 40.45, 47.61, 60.49, 43.11, 27.32,
44.03, 33.56, 37.26, 54.64, 43.12, 25.34, 49.79, 83.56,
40.09, 60.81, 49.81, 56.94, 50.46, 65.99, 45.88, 42.23
45.26, 57.01, 53.61, 59.10, 61.48, 43.43, 44.69, 54.59
48.36, 45.89, 48.62, 43.92, 38.23, 28.79, 63.57, 38.07
40.18, 43.05, 41.56, 42.49, 36.06, 52.76, 46.07, 39.43,
39.26, 47.47, 27.92, 38.01, 45.45, 29.07, 28.94, 51.28,
50.10, 39.84, 36.43, 35.71, 31.47, 47.01, 40.10, 48.76,
                                                          Ohio
31.56, 39.86, 45.31, 35.47, 51.38, 46.33, 48.73, 41.77,
41.32, 48.46, 53.14, 34.01, 54.74, 40.67, 38.96, 46.29
38.25, 6.80, 31.75, 46.33, 44.90, 33.57, 38.10, 39.67,
40.47, 49.44, 37.62, 36.71, 46.73, 42.20, 53.16, 52.40,
58.36, 68.02, 38.53, 34.58, 69.64, 60.50, 53.53, 36.54,
49.58, 41.97, 38.11
```

¹ Data retrieved from Data.gov (https://www.data.gov/)

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60.08, 40.64, 36.07, 41.21, 31.04, 43.78, 44.08, 46.85,
44.71, 46.15, 63.10, 52.20, 43.18, 40.24, 39.92, 47.87,
37.77, 40.11, 49.85, 48.61, 38.62, 54.25, 34.84, 47.75,
43.82, 55.97, 58.23, 42.97, 42.38, 36.11, 37.53, 42.65,
50.96, 47.43, 56.24, 45.60, 46.39, 35.22, 48.56, 32.97,
57.88, 36.05, 37.72, 50.36, 32.12, 41.55, 54.66, 57.81,
54.58, 32.88, 54.37, 40.45, 47.61, 60.49, 43.11, 27.32,
44.03, 33.56, 37.26, 54.64, 43.12, 25.34, 49.79, 83.56,
40.09, 60.81, 49.81, 56.94, 50.46, 65.99, 45.88, 42.23,
45.26, 57.01, 53.61, 59.10, 61.48, 43.43, 44.69, 54.59,
48.36, 45.89, 48.62, 43.92, 38.23, 28.79, 63.57, 38.07,
40.18, 43.05, 41.56, 42.49, 36.06, 52.76, 46.07, 39.43,
39.26, 47.47, 27.92, 38.01, 45.45, 29.07, 28.94, 51.28,
50.10, 39.84, 36.43, 35.71, 31.47, 47.01, 40.10, 48.76,
31.56, 39.86, 45.31, 35.47, 51.38, 46.33, 48.73, 41.77,
41.32, 48.46, 53.14, 34.01, 54.74, 40.67, 38.96, 46.29,
38.25, 6.80, 31.75, 46.33, 44.90, 33.57, 38.10, 39.67,
40.47, 49.44, 37.62, 36.71, 46.73, 42.20, 53.16, 52.40,
58.36, 68.02, 38.53, 34.58, 69.64, 60.50, 53.53, 36.54,
49.58, 41.97, 38.11
```

¹ Data retrieved from Data.gov (https://www.data.gov/)

```
59.10, 38.62, 51.38, 60.49, 6.80, 41.97, 48.56, 37.77,
48.36, 54.59, 40.11, 57.81, 45.89, 83.56, 40.64, 46.07,
28.79, 55.97, 33.57, 42.23, 48.61, 44.69, 39.67, 57.88,
48.62, 54.66, 54.74, 48.46, 36.07, 43.92, 49.85, 53.53,
48.76, 41.77, 36.54, 47.01, 52.76, 49.44, 34.58, 40.24,
44.08, 46.29, 49.81, 69.64, 60.50, 27.32, 45.60, 63.10,
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25.34, 46.73, 44.90, 56.94, 58.23, 39.84, 36.05, 43.05,
38.25, 40.47, 31.04, 54.25, 46.15, 57.01, 52.20, 47.75,
36.06, 47.61, 51.28, 43.43, 42.97, 38.01, 54.64, 45.26,
47.47, 34.84, 49.58, 48.73, 29.07, 54.58, 27.92, 34.01,
38.07, 31.47, 36.11, 39.26, 41.56, 52.40, 40.18, 47.87,
46.33, 46.39, 43.11, 38.53, 33.56, 42.65, 68.02, 35.47,
40.09, 36.43, 36.71, 60.08, 50.36, 39.43, 28.94, 58.36,
42.20, 47.43, 44.71, 43.78, 39.92, 37.62, 63.57, 53.61,
40.10, 46.33, 53.16, 32.88, 38.96, 41.55, 56.24, 38.11,
42.38, 38.10, 43.82, 45.31, 60.81, 54.37, 53.14, 32.97,
61.48, 50.10, 31.75
```

¹ Data retrieved from Data.gov (https://www.data.gov/)

```
59.10, 38.62, 51.38, 60.49, 6.80, 41.97, 48.56, 37.77,
48.36, 54.59, 40.11, 57.81, 45.89, 83.56, 40.64, 46.07,
28.79, 55.97, 33.57, 42.23, 48.61, 44.69, 39.67, 57.88,
48.62, 54.66, 54.74, 48.46, 36.07, 43.92, 49.85, 53.53,
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44.08, 46.29, 49.81, 69.64, 60.50, 27.32, 45.60, 63.10,
35.71, 39.86, 40.67, 65.99, 50.46, 37.72, 50.96, 42.49,
31.56, 38.23, 37.26, 41.21, 37.53, 46.85, 44.03, 41.32,
45.88, 40.45, 32.12, 35.22, 49.79, 43.12, 43.18, 45.45,
25.34, 46.73, 44.90, 56.94, 58.23, 39.84, 36.05, 43.05,
38.25, 40.47, 31.04, 54.25, 46.15, 57.01, 52.20, 47.75,
36.06, 47.61, 51.28, 43.43, 42.97, 38.01, 54.64, 45.26,
47.47, 34.84, 49.58, 48.73, 29.07, 54.58, 27.92, 34.01,
38.07, 31.47, 36.11, 39.26, 41.56, 52.40, 40.18, 47.87,
46.33, 46.39, 43.11, 38.53, 33.56, 42.65, 68.02, 35.47,
40.09, 36.43, 36.71, 60.08, 50.36, 39.43, 28.94, 58.36,
42.20, 47.43, 44.71, 43.78, 39.92, 37.62, 63.57, 53.61,
40.10, 46.33, 53.16, 32.88, 38.96, 41.55, 56.24, 38.11,
42.38, 38.10, 43.82, 45.31, 60.81, 54.37, 53.14, 32.97,
61.48, 50.10, 31.75
```

"Pennsylvania"

"Ohio"

Permutation

Random reordering of entries in an array

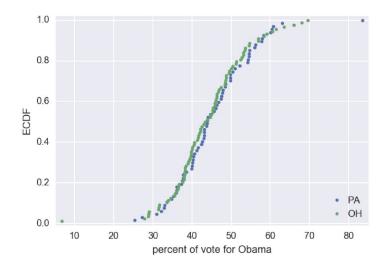
Generating a permutation sample

Let's practice!



Test statistics and p-values

Are OH and PA different?



¹ Data retrieved from Data.gov (https://www.data.gov/)

Hypothesis testing

• Assessment of how reasonable the observed data are assuming a hypothesis is true

Test statistic

- A single number that can be computed from observed data and from data you simulate under the null hypothesis
- It serves as a basis of comparison between the two

Permutation replicate

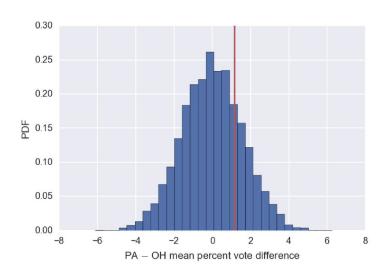
```
np.mean(perm_sample_PA) - np.mean(perm_sample_OH)
```

1.122220149253728

```
np.mean(dem_share_PA) - np.mean(dem_share_OH) # orig. data
```

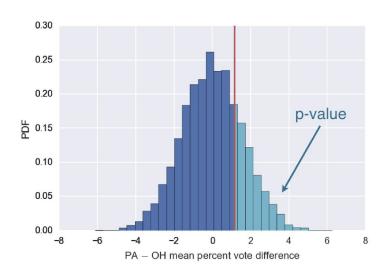
1.1582360922659518

Mean vote difference under null hypothesis



¹ Data retrieved from Data.gov (https://www.data.gov/)

Mean vote difference under null hypothesis



¹ Data retrieved from Data.gov (https://www.data.gov/)

p-value

- The probability of obtaining a value of your test statistic that is at least as extreme as what was observed, under the assumption the null hypothesis is true
- NOT the probability that the null hypothesis is true

Statistical significance

Determined by the smallness of a p-value