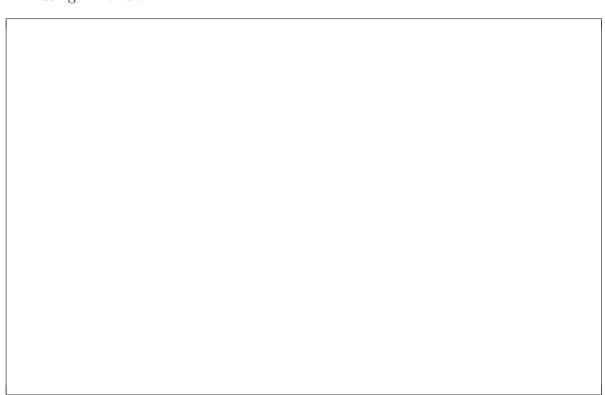
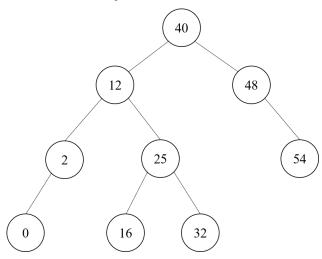
- 1. Prove that $T(n) = 3n^3 + 2n^2 + n + 90$ is both $O(n^3)$ and $O(n^4)$.
 - Determine the asymptotic relationship between $f(n) = n \ln(3n)$ and $g(n) = 3n^2$ using limit rule.



2. Let T(n) = f(n)g(n) + h(n) be a function defined on three running time functions, where f(n) is $\Theta(\sqrt{n})$; g(n) is $\Omega(\log n^n)$ and h(n) is $O(n^3)$. Show that T(n) is $\Omega(n^{3/2} \log n)$.

| ning 23, 20, 6, 17, 13, 25, 14, assume |
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| he pivot. |
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| 0, 37, 18, 6, 32, 13, 3, 14. |
| 9, 97, 10, 0, 92, 19, 9, 14. |
| |
| evious step. |
| |

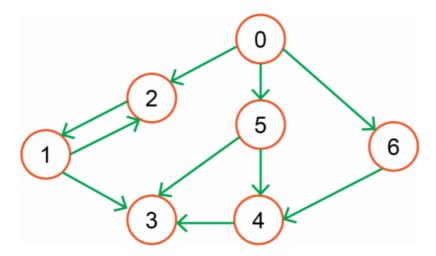
6. Given the binary search tree below:



Describe the process and the outcome of the following deletion operations on the above BST.

- 1. Delete node 48 in the tree.
- 2. Delete node 16 in the tree.
- 3. Delete node 12 in the tree by using the minimum key in the right subtree.
- 4. Delete node 12 in the tree by using the maximum key in the left subtree.

7. Consider the following digraph G:



- 1. What is the order and size of G?
- 2. Identify all sources and sinks in G.
- 3. Write down the adjacency matrix representation of G.
- 4. Consider the vertex sequence 0, 2, 1, 3, 4, 5, is it a walk, path or cycle?
- 5. Give the distance of the following pairs of nodes, d(0,1), d(0,3) and d(5,6)

| 8. | Consider the adjacency list of a digraph G below: |
|----|---|
| | 0: 1 2 |
| | 1: 2 |
| | 2: 1 3 4 |
| | 3: 4 |
| | 4: |
| | 1. Draw the digraph G. |
| | 2. Draw the sub-digraph induced by {1, 2, 3}. |
| | 3. Draw the underlying graph of G. |
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