Graph Properties

Instructor: Meng-Fen Chiang

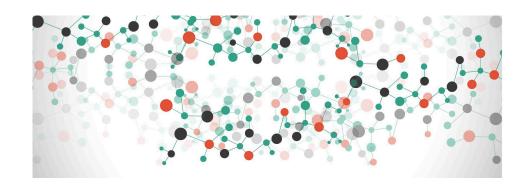
COMPCSI220: WEEK 11





OUTLINE

- Distance
- Eccentricity
- Diameter
- Radius
- Periphery and Center





Distance

- Let u and v be two vertices in a graph G, then the distance between u and v, denoted as d(u,v) is the length of shortest path between u and v in G.
- If G is disconnected and u and v are in different components then $d(u,v)=\infty$

$$d(1,1) = 0$$
 $d(1,2) = 1$
 $d(1,3) = 2$
3

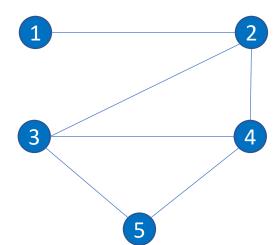


Eccentricity

• The eccentricity of a vertex v in V(G), denoted as e(v), is the maximum of the distances between v and any other vertex u in V(G).

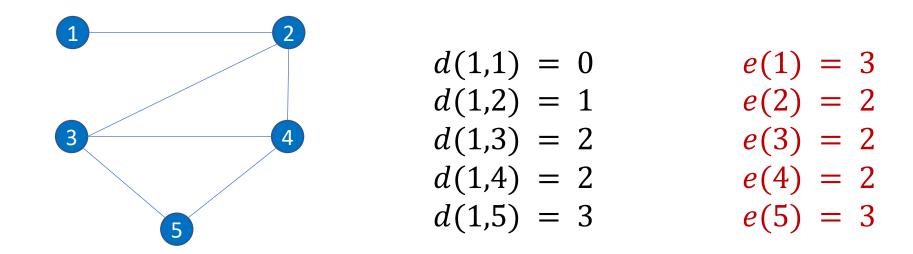
$$d(1,1) = 0$$

 $d(1,2) = 1$
 $d(1,3) = 2$
 $d(1,4) = 2$
 $d(1,5) = 3$





Eccentricity (Contd.)

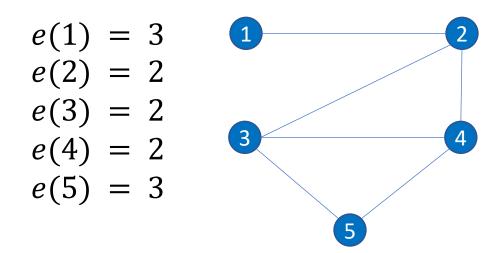


Note: Distance is defined on two vertices while eccentricity is defined on a vertex



Diameter

• The diameter of a graph (or strongly connected digraph) G, denoted as diam(G), is the maximum eccentricity of the vertices in V(G).

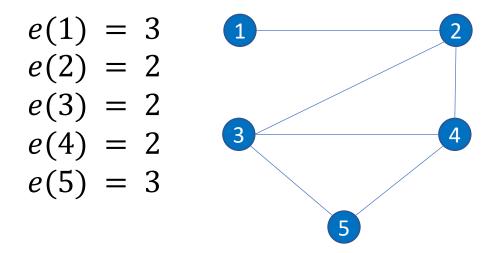


The diameter of this graph is 3



Radius

• The radius of a graph (or strongly connected digraph) G, denoted as rad(G), is the minimum eccentricity of the vertices in V(G).



The radius of this graph is 2



Periphery and Centre in Graph

- A vertex v of a graph G with eccentricity equals to the diameter of G is said to be a peripheral vertex
- The set of all peripheral vertices in the graph is called the periphery of the graph

$$e(1) = 3$$
 $e(2) = 2$
 $e(3) = 2$
 $e(4) = 2$
 $e(5) = 3$

Node 1 and Node 5 form the periphery of the graph



Periphery and Centre in Graph

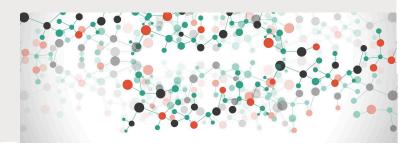
- A vertex v of a graph G with eccentricity equals to the radius of G is said to be a central vertex
- The set of all central vertices in the graph is called the centre of the graph

$$e(1) = 3$$
 $e(2) = 2$
 $e(3) = 2$
 $e(4) = 2$
 $e(5) = 3$

Nodes 2, 3 and 4 form the centre of the graph



SUMMARY



- The **eccentricity** of a vertex v in V(G), denoted as e(v), is the maximum of the distances between v and any other vertex u in V(G).
- The diameter of a graph (or strongly connected digraph) G, denoted as diam(G), is the maximum eccentricity of the vertices in V(G).
- The **radius** of a graph (or strongly connected digraph) G, denoted as rad(G), is the **minimum eccentricity** of the vertices in V(G).
- A vertex v of a graph G with eccentricity equals to the diameter of G is said to be a peripheral vertex
- A vertex v of a graph G with eccentricity equals to the radius of G is said to be a central vertex