

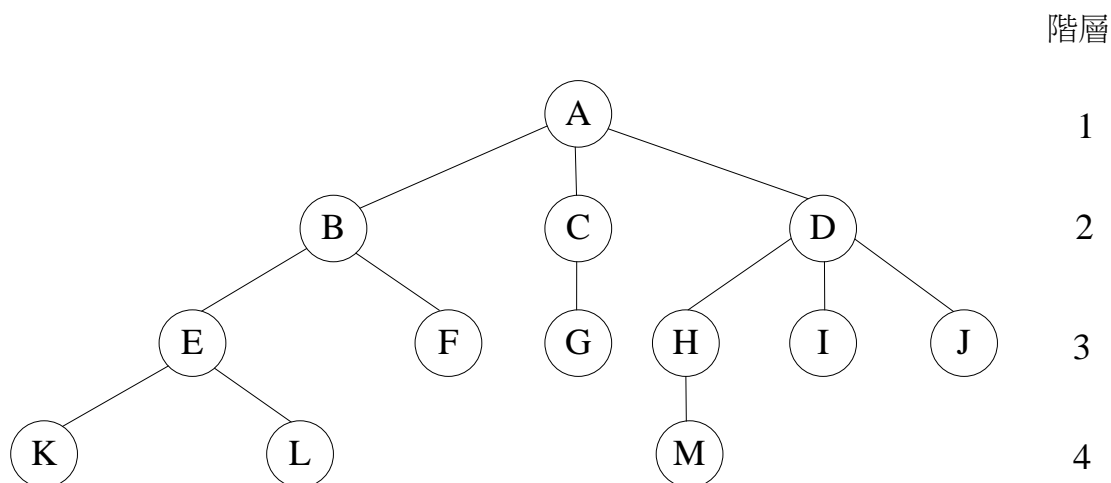
EECS2040 Data Structure Hw #4 (Chapter 5 Tree)

due date 5/16/2022, 23:59

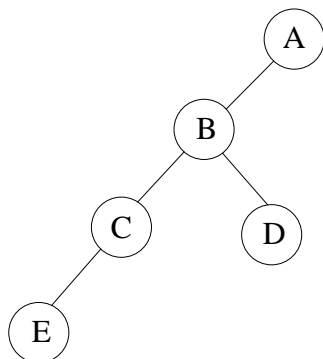
by 108011235 陳昭維

Part 1 (2% of final Grade)

- (4%) What is the maximum number of nodes in a k -ary tree of height h ? Prove your answer.
- (16%) For a simple tree shown below,
 - Draw a list representation of this tree using a node structure with three fields: tag, data/down, and next.
 - Write down a generalized list expression form for this tree.
 - Convert the tree into a left-child and right-sibling tree representation
 - Draw a corresponding binary tree for this tree based on (c).
 - What is the depth of node L? What is the height of node B? What is the height of the tree?
 - Write out the preorder traversal of this tree.
 - Write out the postorder traversal of this tree.
 - Write out the level order traversal of this tree.



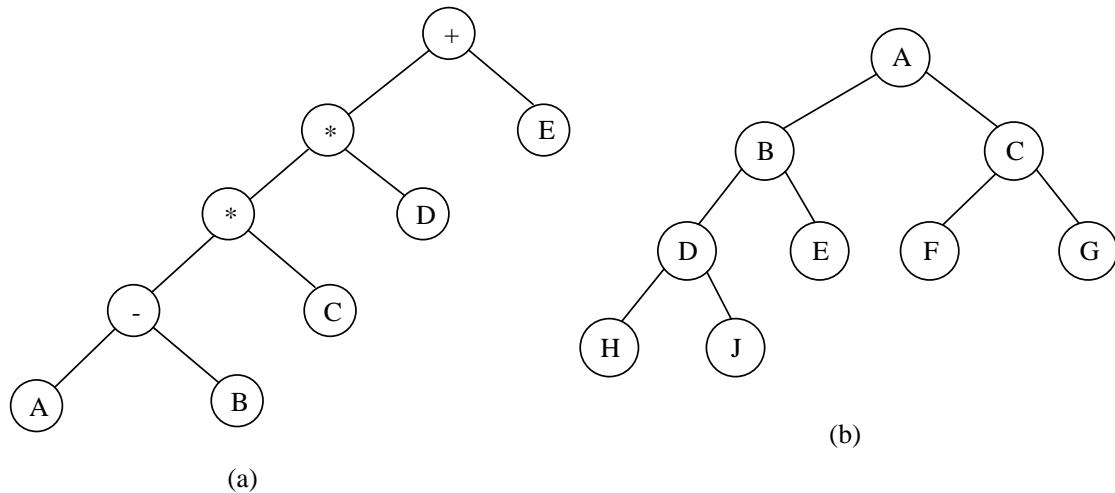
- (10%) Draw the internal memory representation of the binary tree below using (a) sequential and (b) linked representations.



- (4%) Extend the array representation of a complete binary tree to the case of complete trees

whose degree is d , $d > 1$. Develop formulas for the parent and children of the node stored in position i of the array.

5. (16%) Write out the inorder, preorder, postorder, and levelorder traversals for the following binary trees.



6. (16%) Given a sequence of 13 integer number: 50, 5, 30, 40, 80, 35, 2, 20, 15, 60, 70, 8, 10.

- (a) Assume a **max heap** tree is **initialize** with these 13 numbers placed into nodes of the tree according to node numbering of complete binary tree by using the **bottom up heap construction initialization** process. Please draw the final Max heap tree after initialization process.
- (b) Construct a max heap by **inserting** the given 13 numbers one by one according to the sequence order into an initially empty max heap tree, instead of bottom up heap construction.
- (c) Repeat (a) for min Heap.
- (d) Repeat (b) for min Heap.

7. (4%) For initializing a max heap from n key values stored in an array, instead of inserting key value one by one, assume that

The height of heap = h ,

Number of subtrees with root at level j is $\leq 2^{j-1}$,

Time for each subtree is $O(h-j)$. (# of bubbling down),

Time for level j subtrees is $\leq 2^{j-1}(h-j) = t(j)$,

Then total time is $t(1) + t(2) + \dots + t(h-1) = O(n)$.

Please prove the above argument.

8. (20%) Binary Search Tree

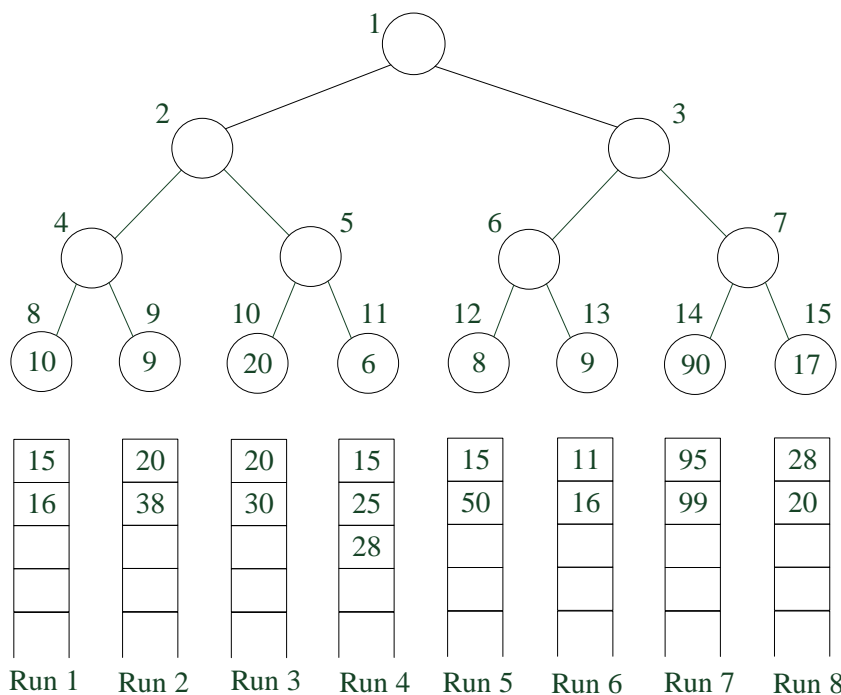
(a) How many different binary search trees can store the keys $\{1,2,3\}$?

(b) If we insert the entries $(1,A)$, $(2,B)$, $(3,C)$, $(4,D)$, and $(5,E)$, where the number denotes the key

value of the node, in this order, into an initially empty binary search tree, what will it look like? Please draw this BST.

- (c) John claims that the order in which a fixed set of entries is inserted into a binary search tree does not matter—the same tree results every time. Give a small example that proves he is wrong.
- (d) Given a sequence of 13 integer number: 50, 5, 30, 40, 80, 35, 2, 20, 15, 60, 70, 8, 10, use the BST Insert function (manually) to insert the 13 number sequentially to construct a binary search tree. Draw the final 13-node BST.
- (e) A binary search tree produces the following preorder traversal, where “null” indicates an empty subtree (i.e. the left/right child is the null pointer).
 9,5,3,1,null,null,4,null,null,8,6,null,null,null,20,12,10,null,11,null,null,null,30,21,null,null,31,null,null
 Draw the tree that produced this preorder traversal.

9. (10%) An 8-run with total of 25 numbers are to be merged using Winner tree and Loser tree, respectively. The numbers of the 8 runs are shown below. The first numbers from each of the 8 runs have been placed in the leaf nodes of the tree as shown. Then these eight numbers enter the tournament to get the overall winner.



- (a) Draw the winner tree and indicate the overall winner of **this tournament**.
- (b) Draw the loser tree and indicate (draw) the overall winner of **this tournament**.