

Preparation of Papers for IEEE Sponsored Conferences & Symposia*

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Abstract—Write an abstract here.

I. INTRODUCTION

Write the introduction here.

II. RELATED WORK

A. Model predictive control

List some literature with information about model predictive control (MPC).

B. Solving optimization problems

Many Algorithms which use primal dual methods to solve several optimization problems and give solutions with high accuracy are described in literature. For application as MPC optimization often do not necessarily has to find such exact solutions, therefor in [1] a primal barrier method with focus of getting fast sufficiently exact solutions of quadratic programs is described, where of the special MPC problem structure is made use of. This paper's contribution is mainly based on the algorithm in [1], which has been extended by some numerical robustness approaches and for application to more general optimization problems, especially QPQCs and SOCPs.

III. PROBLEM STATEMENT

A. Description of a Quadratic Program

Introduce the unchanged problem statement of [1]

B. Quadratic Constrained Quadratic Program

If linear constraints as bounds for state and control variable are not sufficient it can be necessary to use nonlinear constraints such as quadratic constraints.

$$z^T \Gamma z + \beta^T z \leq \alpha \quad (1)$$

C. Second Order Cone Program

A more general form of constraints are second order cone constraints. An Optimization problem using this type of constraints is called second order cone program. Constraints are described as a second order cone as following: {Description as Cone Definition K:=...} as following inequality:

$$\|Az + b\|_2 \leq c^T z + d \quad (2)$$

D. Soft Constraints

IV. EXTENDED ALGORITHM

A. Generalized Constraints

In the described primal barrier method the gradient and the Hessian of the logarithmic barrier function are necessary. SOCCs in the above mentioned form are not continuously differentiable. Therefor SOCCs in Generalized form [2] can be used.

$$\|Az + b\|_2^2 \leq (c^T z + d)^2 \quad (3)$$

B. Extended Problem Statement

The algorithm of [1] shall still be used, therefor its general form is not changed. Only the constant matrix P and the vector h, also constant regarding the optimization variable z, are expended with p rows belonging to the p new quadratic constraints and q rows for the conic constraints. Different from the extended vector \hat{h} the extended matrix $\hat{P}(z)$ is not constant regarding z anymore.

$$\hat{P}(z) = \begin{bmatrix} P & & \\ \beta_1^T + z^T \Gamma_1 & & \\ \vdots & & \\ \beta_p^T + z^T \Gamma_p & & \\ -(c_1^T z + 2d_1) c_1^T + (z^T A_1^T + 2b_1^T) A_1 & & \\ \vdots & & \\ -(c_q^T z + 2d_q) c_q^T + (z^T A_q^T + 2b_q^T) A_q \end{bmatrix} \quad (4)$$

$$\hat{h} = \begin{bmatrix} h \\ \alpha_1^T \\ \vdots \\ \alpha_p^T \\ d_1^2 - b_1^T b_1 \\ \vdots \\ d_q^2 - b_q^T b_q \end{bmatrix} \quad (5)$$

Expending P and h does not change the structure of Φ exploited in [1]. So we have not to worry go on with its algorithm. With new \hat{h} and $\hat{P}(z)$ the logarithmic barrier function looks like

$$\phi(z) = \sum_{i=1}^{lT+l_f+p+q} -\log(\hat{h}_i - \hat{p}_i^T(z)z) \quad (6)$$

where $\hat{p}_i^T(z)$ is the i-th rows of $\hat{P}(z)$ depending on z. The gradient of the logarithmic barrier function $\nabla \phi(z)$ necessary to calculate the residual is derived simply by forming \hat{P} with argument 2z multiplied by \hat{d} .

$$\nabla \phi(z) = \hat{P}^T(2z) \hat{d} \quad (7)$$

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with

$$\hat{d}_i = \frac{1}{\hat{h}_i - \hat{p}_i^T(z)z} \quad (8)$$

To obtain Φ in the resulting system of linear equations two additional terms have to be added to the Hessian of $\phi(z)$.

$$\begin{aligned} \nabla^2 \phi(z) = & \hat{P}(2z) \text{diag}(\hat{d})^2 \hat{P}(2z) \\ & + \sum_{i=lT+lf+1}^{lT+lf+p} \left(\hat{d}_i 2\Gamma_i \right) \\ & + \sum_{j=lT+lf+p+1}^{lT+lf+p+q} \left(\hat{d}_j - 2(c_j c_j^T - A_j^T A_j) \right) \end{aligned} \quad (9)$$

C. Selecting κ

In [1] the use of a fixed kappa is proposed. But it is difficult to find one. Eventually it should be considered to calculate a new κ once every time step, not every inner step, to have the effect of the barrier function to the cost in same magnitude as the effect of weighting terms like in [4] for linear programs. Adopted for quadratic programs a good κ can be estimated by

$$\kappa = \frac{z^T H z + g^T z}{T(n+m)} \quad (10)$$

D. Numerical Improvements

V. RESULTS

A. Test QPs

Results of Solving Test QPs by [3]

B. Application Example

VI. CONCLUSIONS

What are the conclusions?

ACKNOWLEDGMENT

Acknowledgment.

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