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# Counterfactual Multi-Agent Policy Gradients

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*Severance*

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## Counterfactual Multi-Agent Policy Gradients

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## Counterfactual Multi-Agent Policy Gradients

J Foerster 저술 · 2018 · 1315회 인용 — To this end, we propose a r

# Contents

- 1. Introduction & Background**
- 2. Related Work**
- 3. Methods**
- 4. Experimental Setup**
- 5. Results**
- 6. Conclusion & Future Work**

# 1. Introduction & Background

## Basic Backgrounds

### *Single Agent Policy Gradient*

Expected Discounted Total Reward

REINFORCE policy gradient

$$J = \mathbb{E}_{\pi}[R_0]$$

$$g = \mathbb{E}_{s_{0:\infty}, u_{0:\infty}} [\sum_{t=0}^T R_t \nabla_{\theta} \log \pi(u_t | s_t)]$$

### *Actor-critic approaches*

Actor, i.e., the policy, is trained by following a gradient that depends on a critic, estimates a value function.

### *Advantage Function*

$A(s_t, u_t) = R_t - b(s_t)$  : Reward function with baseline to reduce variance

$b(s_t) = V(s_t)$  : Common Choice

### *Temporal Difference (TD) error*

$r_t + \gamma V(s_{t+1}) - V(s_t)$  : Unbiased Estimate of  $A(s_t, u_t)$

# 1. Introduction & Background

## Basic Backgrounds

### *Reward Functions*

$$R_t = \sum_{l=0}^{\infty} \gamma^l r_{(t+l)} \quad : \text{discounted return}$$

$$V^{\pi}(s_t) = \mathbb{E}_{s_{t+1:\infty}, u_{t:\infty}} [R_t | s_t] \quad : \text{State-Value Function}$$

$$Q^{\pi}(s_t) = \mathbb{E}_{s_{t+1:\infty}, u_{t+1:\infty}} [R_t | s_t, u_t] \quad : \text{Action-Value Function}$$

$$A^{\pi}(s_t, u_t) = Q^{\pi}(s_t, u_t) - V^{\pi}(s_t) \quad : \text{Advantage Function}$$

# 1. Introduction & Background

## Basic Backgrounds

*Train critics*  $f^c(\cdot, \theta^c)$

Adapt TD( $\lambda$ )

- Mixture of n-step returns  $G_t^{(n)} = \sum_{l=1}^n \gamma^{l-1} r_{t+l} + \gamma^n f^c(\cdot_{t+n}, \theta^c)$ 
  - $\theta^c$  : critic parameter
    - Updated by minibatch gradient descent to minimize the loss

*Loss Function*

$$\mathcal{L}_t(\theta^c) = \left( y^{(\lambda)} - f^c(\cdot_t, \theta^c) \right)^2$$

$$y^{(\lambda)} = (1 - \lambda) \sum_{n=1}^{\infty} \lambda^{n-1} G_t^{(n)}$$

$G_t^{(n)}$  : calculated with bootstrapped values estimated by a target network with parameters copied periodically from  $\theta^c$

# 1. Introduction & Background

## Basic Backgrounds

### *Joint-Action*

$a : \text{agent } (1, 2, \dots, n)$

$P(\mathbb{U}|s_t) = P(u^1|s^1) \cdot \dots \cdot P(u^n|s^n) : \text{joint-action}$

### *Credit Assignment Problem*

Scalar Global reward

- Allocating which actions each agent has received rewards should be included in the learning process.  
(Makes confuse to figure out which agent is good for training)
- Allocating reward to each agent could be disturbed by the others

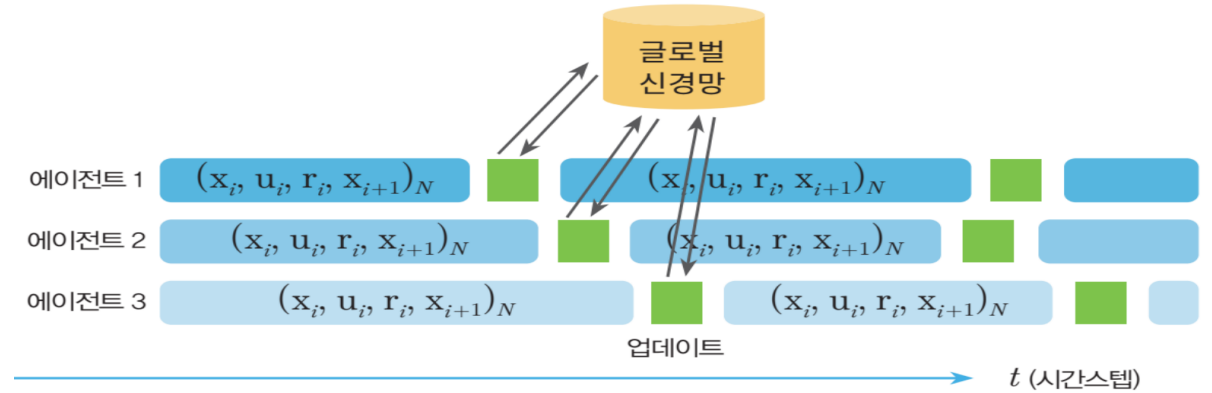


그림 5.6 비동기적 A2C

# 1. Introduction & Background

## Notations

$$G = \langle S, U, P, r, Z, O, n, \gamma \rangle$$

- G : Stochastic Game
- U : Action
- P : State Transition Function
- r : Reward Function,  $r(s, u): S \times U \rightarrow \mathbb{R}$
- Z : Observations, agents draw observations  $z \in Z$
- O : Observation Function,  $O(s, a): S \times A \rightarrow Z$
- n : Number of Agents
- $\gamma$  : Discount Factor,  $\gamma \in [0, 1)$
- a : Agents,  $a \in A \equiv \{1, 2, \dots, n\}$
- s : True State of Environment,  $s \in S$
- $u^a$  : Action Chosen by Agent at Each Time Step,  $u^a \in U$
- $\mathbb{u}$  : Joint Action,  $\mathbb{u} \in \mathbb{U} \equiv U^n$
- $\tau^a$  : Action Observation History of Agent a,  $\tau^a \in T$
- $\pi$  : Stochastic Policy,  $\pi^a(u^a | \tau^a): T \times U \rightarrow [0, 1]$
- $u^{-a}$  : agents except a



# 1. Introduction & Background

## Introduction

Reinforcement Learning Problems are naturally modelled as cooperative multi-agent systems.

- Autonomous Vehicles (Cao et al. 2013)
- Network Packet Delivery (Ye, Zhang, and Yang 2015)
- Distributed Logistics (Ying and Dayong 2005)

RL methods designed for single agents typically fare poorly on such tasks (autonomous vehicles ...), since the joint action space of the agents grows exponentially with the number of agents

# 1. Introduction & Background

## Centralized training of Decentralized policies

### *Centralized Training of Decentralized Policies*

To cope with such complexity,

It is often necessary to resort to decentralized policies,  
in which each agent selects its own action only on its local action-observation history.

∴ Agent may make use of RNN (LSTM, GRU, etc...)

Learning can take place in a simulator or a laboratory

in which extra state information is available and agents can communicate freely

### *Centralized*

$\pi^C(\mathbb{U}|s_t) : \mathbb{U} \times S \rightarrow [0,1]$  : One centralized policy with given state  $s_t$

### *Decentralized*

$\pi^a(u^a|s_t)$  : local policy of agent  $a$

$P(\mathbb{U}|s_t) = \prod_a \pi^a(u^a|s_t)$  : joint-action ( product of prob. of each agent with given)

# 1. Introduction & Background

## Limitations

Multi-agent *credit assignment*

- Joint Action generate only global rewards
- Each agent to deduce its own contribution to the team's success
- [Individual Reward Function] not generally available in cooperative settings and often fail

➔ ***C*ounterfactual Multi-Agent(COMA) policy gradients & actor-critic**

# 1. Introduction & Background

## 3 Main Ideas of COMA

### 1. COMA uses a centralized critic

- **Critic**
  - Centralized
  - Only used during learning
  - Critic conditions on the joint action and all available state information
- **Actor**
  - Decentralized
  - Needed during execution
  - Policy conditions only on its own action-observation history

# 1. Introduction & Background

## 3 Main Ideas of COMA

### 2. Counterfactual baseline

- Inspired by *difference rewards*
  - Use *Aristocrat utility*

=> *Advantage function*

Computes separate baseline for each agent that relies on the centralized critic to reason about counterfactuals in which only that agent's action changes

# 1. Introduction & Background

## 3 Main Ideas of COMA

### 3. Critic representation

- the counterfactual baseline to be computed efficiently.
- In a single forward pass,  
it computes the Q-values for all the different actions of a given agent,  
conditioned on the actions of all the other agents

# 1. Introduction & Background

## Evaluation



# 1. Introduction & Background

## Evaluation

### StarCraft unit micromanagement

- high stochasticity
- large state-action space
- delayed rewards



**Previous works** have made use of a centralized control policy

### COMA

- Massively reduces each agent's field-of-view
- Removes access to macro-actions (combined move and attack)
- Significantly improve performance over other multi-agent actor-critic methods
- Almost SOTA performance of centralized controllers



## 2. Related Work

### **Tabular Data**

- Busoniu, Babuska, and De Schutter 2008;
- Yang and Gu 2004
- VS ; We used CV data

### **DQN with independent Q-learning**

- Tampuu et al. (2015) : two player pong
- Leibo et al. (2017) : Emergence of collaboration and defection in sequential social dilemmas
- VS ; We used Actor-Critic Method

### **Emergence of Communication between agents, learned by gradient descent**

- centralized training (passing gradients between agents during training and sharing parameters)
  - Das et al. (2017)
  - Mordatch and Abbeel (2017)
  - Lazaridou, Peysakhovich, and Baroni (2016)
  - Foerster et al. (2016)
  - Sukhbaatar, Fergus, and others (2016)
- VS ; We used extra state Information during learning and addressed multi-agent credit assignment problem

## 2. Related Work

### **Actor-critic methods for decentralized execution with centralized training**

- Gupta, Egorov, and Kochenderfer (2017)
- VS; They used hand-crafted local rewards

### **StarCraft micromanagement**

- centralized controller
  - Access to full state, control of all units
  - VS; We used Multi-agent
- Greedy MDP, sequentially choose actions for agents given all previous actions
  - Usunier et al. (2016)
- Actor-critic method that relies on RNNs to exchange information between the agents.
  - Peng et al. (2017)
- Multi-Agent representation and decentralized policies with experience replay
  - Foerster et al. (2017)

# 3. Methods

## Independent Actor-Critic (IAC)

### *Independent Q-Learning*

apply policy gradients to multiple agents is learn each agent independently, with its own action-observation history.

### *Independent Actor-Critic (Baseline)*

Actor-critic in place of Q-learning

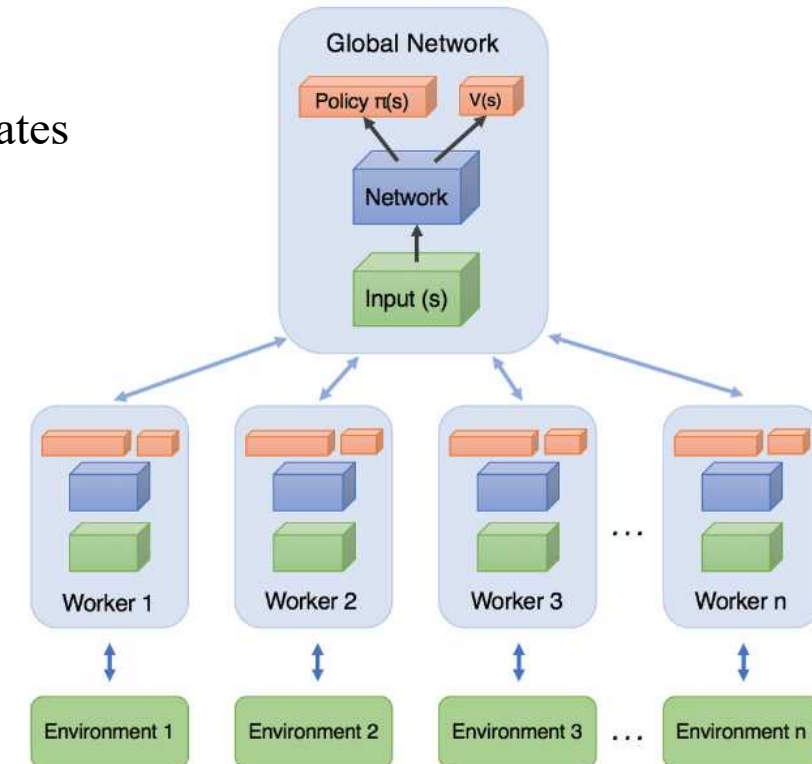
- Agents can behave differently due to its different observations and hidden states
- Learning remains independent in the sense that each agent
- each actor  $\pi(u^a | \tau^a)$  and each critic  $Q(\tau^a, u^a)$  or  $V(\tau^a)$  only on the agent's own action-observation history  $\tau^a$

### *IAC-V*

- Critic estimates  $V(\tau^a)$ , follows a gradient based TD error

### *IAC-Q*

- Critic estimates  $Q(\tau^a, u^a)$ , follows gradient based advantage
- $A(\tau^a, u^a) = Q(\tau^a, u^a) - V(\tau^a), V(\tau^a) = \sum_{u^a} \pi(u^a | \tau^a) Q(\tau^a, u^a)$



### 3. Methods

#### Counterfactual Multi-Agent Policy Gradients

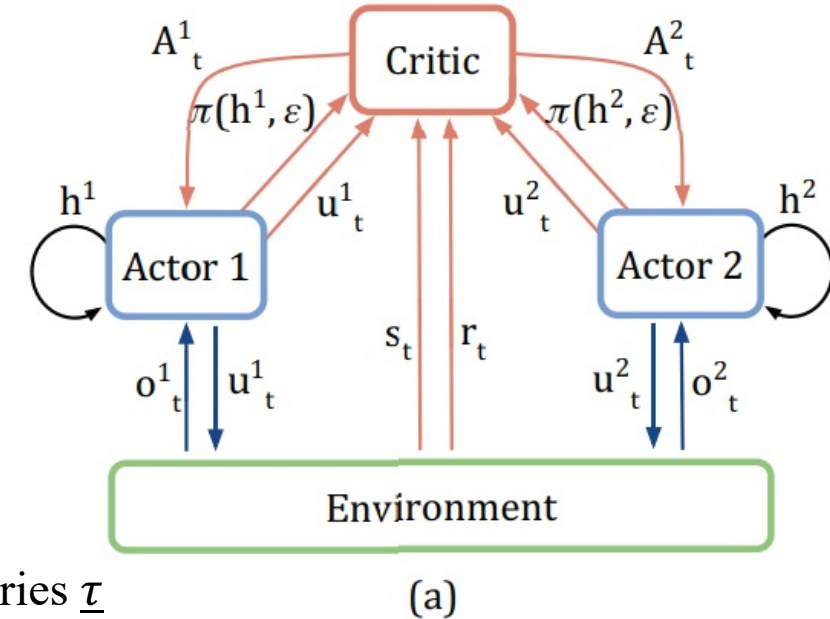
*A centralized critic*

COMA

- Critic is used only during learning and the actor is needed during execution
- Critic use true global state  $s$  if available, or the joint action-observation histories  $\underline{\tau}$
- Actor use own action-observation histories  $\tau^a$
- Centralized critic would be for each actor to follow a gradient based on the TD error

$$g = \nabla_{\theta} \pi \log \pi(u | \tau_t^a) (r + \gamma V(s_{t+1}) - V(s_t))$$

- This TD error considers only global rewards, the Gradient computed for each actor does not explicitly reason about how that particular agent's actions contribute to that global reward.



### 3. Methods

#### Counterfactual Multi-Agent Policy Gradients

##### *Counterfactual Baseline*

Difference rewards

- Shaped reward

$$D^a = r(s, \mathbb{u}) - r(s, (\mathbb{u}^{-a}, c^a))$$

$r(s, \mathbb{u})$  : global reward with joint action  $\mathbb{u}$

$r(s, (\mathbb{u}^{-a}, c^a))$  : action of agent  $a$  is replaced with a *default action*  $c^a$

$\therefore$  true global reward – reward that not depend on agent  $a$ 's actions

Aristocrat Utility

- avoids the problem of a recursive interdependence between the policy and utility function

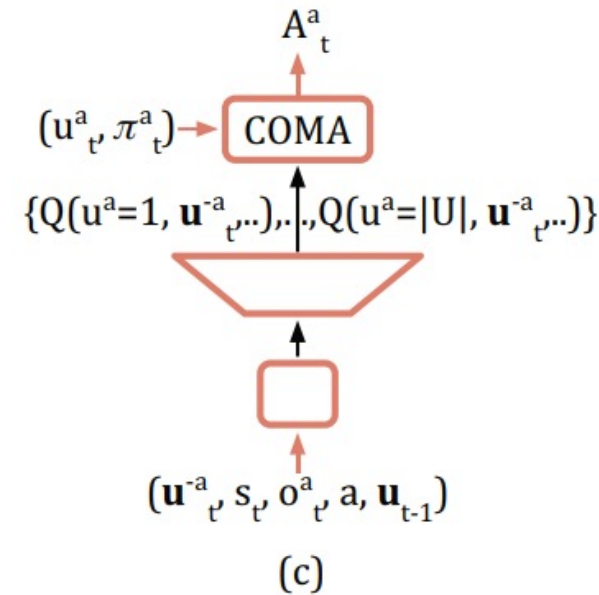
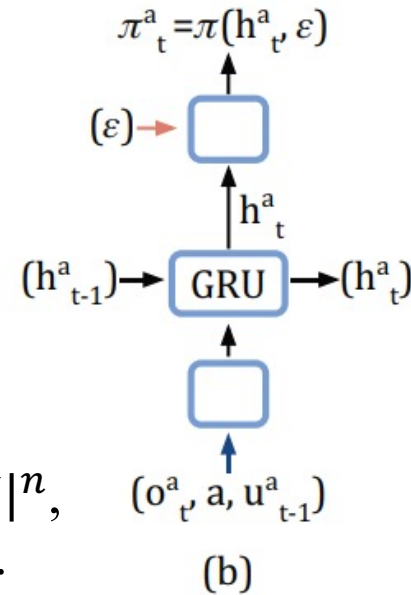
$$A^a(s, \mathbb{u}) = Q(s, \mathbb{u}) - \sum_{u'^a} \pi^a(u'^a | \tau^a) Q(s, (u^{-a}, u'^a))$$

### 3. Methods

#### Counterfactual Multi-Agent Policy Gradients

##### *Single Forward Pass*

The number of output nodes of such a network would equal  $|U|^n$ ,  
the size of the joint action space, making it impractical to train.



COMA uses a critic representation that allows for efficient evaluation of the baseline.

The number of outputs is only  $|U|$  instead of  $(|U|^n)$

- Large input space that scales linearly in the number of agents and actions

### 3. Methods

#### Convergence Proof of COMA to a locally optimal policy

$$g_k = \mathbb{E}_\pi[\sum_a \nabla_{\theta_k} \log \pi^a(u^a | \tau^a) A^a(s, u)] \quad \text{TD}(1)$$

$$g = \mathbb{E}_\pi[\sum_a \nabla_{\theta} \log \pi^a(u^a | \tau^a) A^a(s, \mathbb{U})]$$

$$A^a(s, \mathbb{U}) = Q(s, \mathbb{U}) - b(s, \mathbb{U}^{-a})$$



$$\liminf_k \|\nabla J\| = 0 \quad w.p. 1.$$

$$A^a(s, \mathbb{U}) = Q(s, \mathbb{U}) - \sum_{u'^a} \pi^a(u'^a | \tau^a) Q(s, (u^{-a}, u'^a))$$

$$g_b = - \mathbb{E}_\pi[\sum_a \nabla_{\theta_k} \log \pi^a(u^a | \tau^a) b^a(s, \mathbb{U}^{-a})]$$

### 3. Methods

#### Convergence Proof of COMA to a locally optimal policy

$$\begin{aligned}
 g_b &= -\mathbb{E}_\pi \left[ \sum_a \nabla_{\theta_k} \log \pi^a(u^a | \tau^a) b(s, \mathbb{U}^{-a}) \right] \\
 &= -\sum_s d^\pi(s) \sum_a \sum_{\mathbb{U}^{-a}} \pi(\mathbb{U}^{-a} | \boldsymbol{\tau} - a) \cdot \sum_{u^a} \pi^a(u^a | \tau^a) \nabla_\theta \log \pi^a(u^a | \tau^a) b(s, \mathbb{U}^{-a}) \\
 &= -\sum_s d^\pi(s) \sum_a \sum_{\mathbb{U}^{-a}} \pi(\mathbb{U}^{-a} | \boldsymbol{\tau} - a) \cdot \sum_{u^a} \nabla_\theta \pi^a(u^a | \tau^a) b(s, \mathbb{U}^{-a}) \\
 &= -\sum_s d^\pi(s) \sum_a \sum_{\mathbb{U}^{-a}} \pi(\mathbb{U}^{-a} | \boldsymbol{\tau} - a) \cdot b(s, \mathbb{U}^{-a}) \nabla_\theta 1 \\
 &= 0
 \end{aligned}$$

$d^\pi(s)$  : discounted ergodic state distribution  
 + Chain Rule  
 $\nabla_\theta \log \pi(s, a)$   
 $= \frac{\nabla_\theta \pi_\theta(s, a)}{\pi(s, a)}$   
 $b(s, \mathbb{U}^{-a})$  is not relevant to  $u^a$   
 $\sum_{u^a} \nabla_\theta \pi^a(u^a | \tau^a) = 1$  by definition  
 $\nabla_\theta 1 = 0$

$\therefore$  the per-agent baseline does not change the expected gradient and not affect the convergence of COMA



### 3. Methods

#### Reminder of the expected policy gradient

$$g_k = \mathbb{E}_\pi \left[ \sum_a \nabla_{\theta_k} \log \pi^a(u^a | \tau^a) A^a(s, u) \right]$$

$$g = \mathbb{E}_\pi \left[ \sum_a \nabla_\theta \log \pi^a(u^a | \tau^a) A^a(s, \mathbb{u}) \right]$$

$$A^a(s, \mathbb{u}) = Q(s, \mathbb{u}) - b(s, \mathbb{u}^{-a})$$

$$A^a(s, \mathbb{u}) = Q(s, \mathbb{u}) - \sum_{u'^a} \pi^a(u'^a | \tau^a) Q(s, (u^{-a}, u'^a))$$


$$g = \mathbb{E}_\pi [\nabla_\theta \log \pi(\mathbb{u} | s) Q(s, \mathbb{u})]$$

### 3. Methods

#### Reminder of the expected policy gradient

Single-agent actor-critic policy gradient  $g$

$$\begin{aligned}
 g &= \mathbb{E}_{\pi}[\nabla_{\theta} \log \pi(\mathbb{u}|s) Q(s, \mathbb{u})] \\
 &= \mathbb{E}_{\pi}[\nabla_{\theta} \log \Pi_a \pi^a(u^a | \tau^a) Q(s, \mathbb{u})] \\
 &= \mathbb{E}_{\pi}[\nabla_{\theta} \log \pi(\mathbb{u}|s) Q(s, \mathbb{u})]
 \end{aligned}$$


 $\pi(\mathbb{u}|s) = \Pi_a \pi^a(u^a | \tau^a)$

Actor-critic following this gradient converges to a local maximum of the expected return  $J^{\pi}$ , given

1. Policy is differentiable
2. Update timescales for  $Q$  and  $\pi$  are sufficiently slow, and that  $\pi$  is updated sufficiently slower than  $Q$
3.  $Q$  uses a representation compatible with  $\pi$

## 4. Experimental Setup

### Decentralized StarCraft Micromanagement

Low-level control of individual units' positioning and attack commands as the fight enemies.

#### *Environment*

Symmetric teams formed of

- 3 marines (3m)
- 5 marines (5m)
- 5 wraiths (5w)
- 2 dragoons with 3 zealots (2d\_3z)

Enemy team is controlled by the StarCraft AI

## 4. Experimental Setup

### Decentralized StarCraft Micromanagement

#### *Discrete Actions*

- Move[direction]
- Attack[enemy\_id]
  - Originally, moves into attack range before firing using the game's built-in pathfinding route
  - However, Restricted field of view on the agents, equal to the firing range of ranged units' weapons
- Stop
- Noop
  - Invalid Action choice, such as attack to died enemy

## 4. Experimental Setup

### Decentralized StarCraft Micromanagement

#### *Effect of Restricted field of view on the agents*

1. Significant partial observability
2. Units can only attack when they are in range or enemies
3. Agents cannot distinguish between enemies who are dead and who are out of range that can issue invalid attack commands at such enemies, which results in no action being taken.

Increased the average size of the action space, increases the difficulty of both exploration and control.

Before this setting, run forward and attack one enemy instruct achieves 98% win, but 66% in this setting.



Figure 2: Starting position with example local field of view for the 2d\_3z map.

## 4. Experimental Setup

### Decentralized StarCraft Micromanagement

#### *Reward Setting*

All agents receive the same global reward at each time step,

R =

$$\sum(\text{damage on the opponent}) - \frac{1}{2} \sum(\text{damage taken}) + 10 * (\text{enemy killed}) + (\text{remaining health} + 200 \text{ if win})$$

## 4. Experimental Setup

### State Features

#### *Actor Input Features*

- Local observations
- Distance
- Relative x
- Relative y
- Unit type
- Shield

map	Local Field of View (FoV)							Full FoV, Central Control		
	heur.	IAC- <i>V</i>	IAC- <i>Q</i>	cnt- <i>V</i>	cnt- <i>QV</i>	COMA		heur.	DQN	GMEZO
						mean	best			
3m	35	47 (3)	56 (6)	83 (3)	83 (5)	<b>87</b> (3)	98	74	-	-
5m	66	63 (2)	58 (3)	67 (5)	71 (9)	<b>81</b> (5)	95	98	99	100
5w	70	18 (5)	57 (5)	65 (3)	76 (1)	<b>82</b> (3)	98	82	70	74 <sup>3</sup>
2d_3z	<b>63</b>	27 (9)	19 (21)	36 (6)	39 (5)	47 (5)	65	68	61	90

#### *Critic Input Features*

- Global state
  - X-y locations relative to the center of the map
  - Health points
  - Cooldown
- Local observations of agents
  - Same but egocentric distances relative to that agent

## 4. Experimental Setup

### Architecture & Training

#### *Actor*

- 128-bit gated recurrent units (GRUs)
  - Use fc layers both to process the input and to produce output values
- Action probabilities are produced from the final layer,  $z$ 
  - Bounded softmax distribution
    - Lower-bounds :  $\epsilon/|U| : P(u) = (1 - \epsilon)\text{softmax}(z)_u + \frac{\epsilon}{|U|}$
    - $\epsilon$  : linearly from 0.5 to 0.02 across 750 training episodes
  - TD( $\lambda$ )
    - $\lambda = 0.8$  worked best

#### *Critic*

- Factored at the agent level and further exploit internal parameter sharing



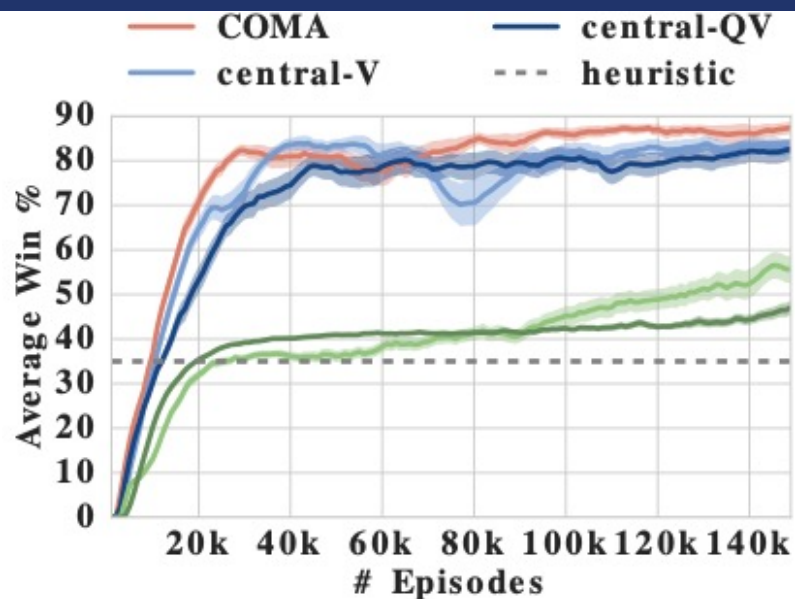
## 4. Experimental Setup

### Ablations

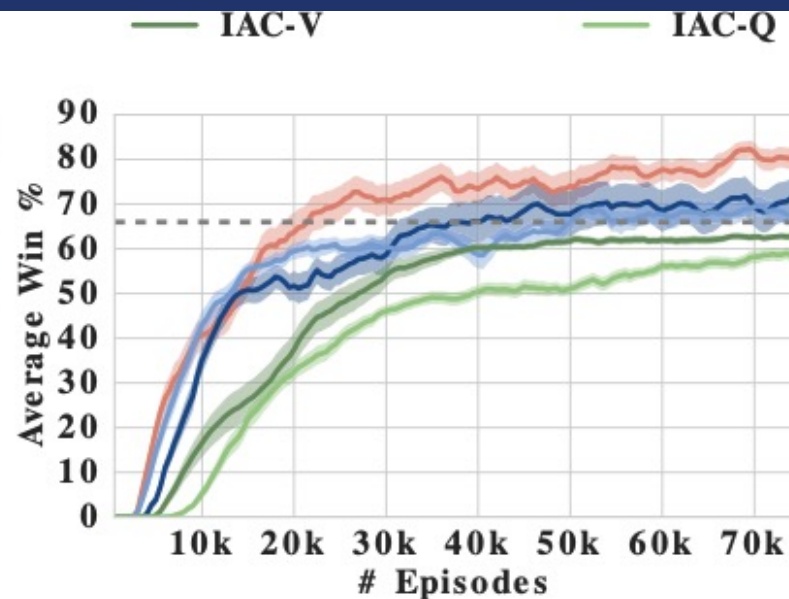
Ablation experiments to validate three key elements of COMA

1. Importance of centralizing the critic by comparing against two IAC variants, IAC-Q, IAC-V
  - IAC-Q : outputs  $|U|$   $Q$ -values, one for each action
  - IAC-V : outputs single state-value
2. Significance of learning  $Q$  instead of  $V$ 
  - *central* –  $V$  uses a central state for the critic, but learns  $V(s)$
  - Uses the TD Error to estimate the advantage for policy gradient updates
3. Utility of counterfactual baseline
  - *central* –  $QV$  learns both  $Q$  and  $V$  simultaneously and estimates the advantage as  $Q - V$

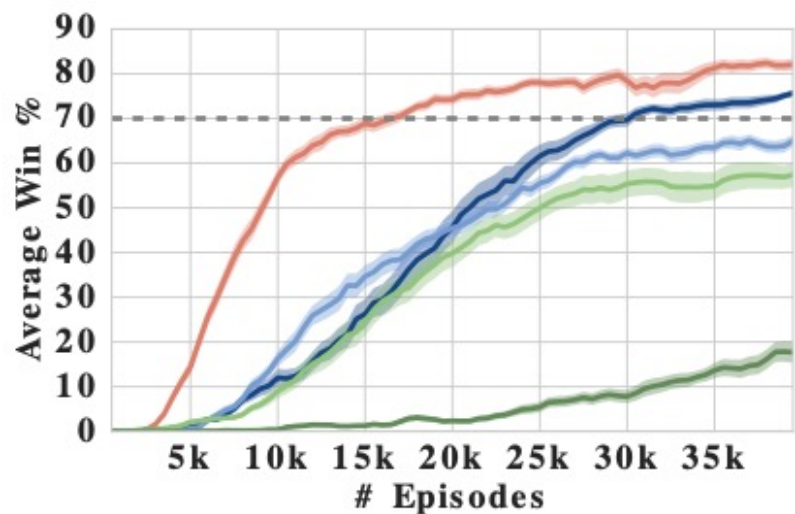
## 5. Results



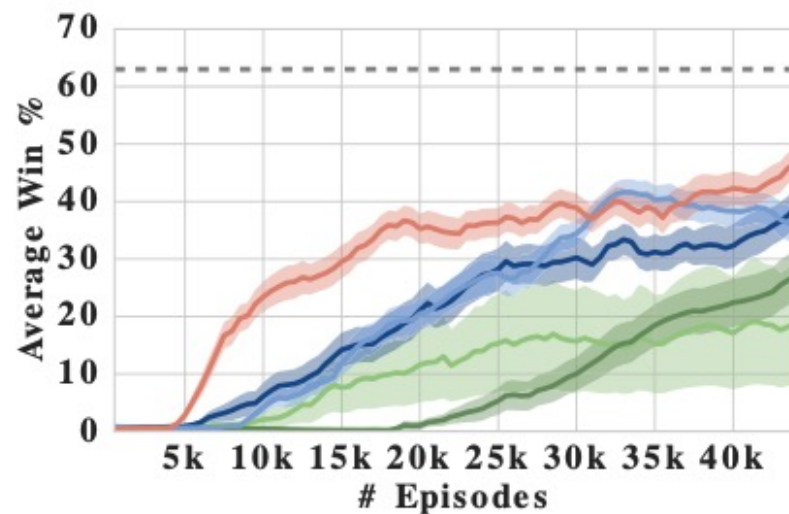
(a) 3m



(b) 5m



(c) 5w



(d) 2d\_3z

## 6. Conclusions & Future Work

### *Conclusions*

centralized critic in order to estimate a counterfactual advantage for decentralized policies in multi-agent RL

Multi-agent credit assignment by using a counterfactual baseline

- Marginalizes out a single agent's action
- Keeping the other agents' actions fixed

improves final performance and training speed

### *Future Work*

Scenarios with large numbers of agents

Centralized critics are more difficult to train

Exploration is harder to coordinate

More sample-efficient variants such as self-driving cars

# THANKS FOR LISTENING

## Q&A