250A_HW8_A59017531

November 29, 2022

```
[1]: import numpy as np
     from collections import defaultdict
     from tqdm.notebook import tqdm
     from prettytable import PrettyTable
    0.1 Q1
    0.1.1 Importing data
[2]: users = np.loadtxt("hw8_ids.txt",dtype=str)
     items = np.loadtxt("hw8_movies.txt",dtype=str)
     tmpRatings = np.loadtxt("hw8 ratings.txt",dtype=str)
    0.1.2 Preprocessing
[3]: ratings = np.zeros((tmpRatings.shape[0],tmpRatings.shape[1]))
     for i in range(len(tmpRatings)):
       for j in range(len(tmpRatings[0])):
         try:
           ratings[i][j] = int(tmpRatings[i,j])
         except:
           ratings[i,j] = -1
[4]: ratings
[4]: array([[ 1., 1., -1., ..., 1., -1., -1.],
            [1., -1., 0., ..., 0., -1., -1.],
            [1., 1., -1., ..., 0., -1., -1.],
            [1., -1., -1., ..., -1., -1., -1.]
            [-1., 0., -1., ..., -1., -1., -1.]
            [ 1., -1., -1., ..., -1., 1., 1.]])
[5]: np.unique(ratings)
[5]: array([-1., 0., 1.])
```

[6]: UIR = []

```
[7]: for i in range(len(ratings)):
        user = users[i]
        for j in range(len(ratings[0])):
          item = items[j]
          UIR.append([user,item,ratings[i,j]])
 [8]: UIR[:10]
 [8]: [['\ufeffA12614795', 'Inception', 1.0],
       ['\ufeffA12614795', 'The_Social_Network', 1.0],
       ['\ufeffA12614795', 'Black_Swan', -1.0],
       ['\ufeffA12614795', 'Shutter_Island', 1.0],
       ['\ufeffA12614795', 'The_Last_Airbender', 0.0],
       ['\ufeffA12614795', 'Harry_Potter_and_the_Deathly_Hallows:_Part_1', -1.0],
       ['\ufeffA12614795', 'Iron_Man_2', 1.0],
       ['\ufeffA12614795', 'Toy Story 3', 1.0],
       ['\ufeffA12614795', 'Fast_Five', 1.0],
       ['\ufeffA12614795', 'Thor', 1.0]]
 [9]: ratingsPerUser = defaultdict(list)
      ratingsPerItem = defaultdict(list)
      for u,b,r in UIR:
          ratingsPerUser[u].append((b,r))
          ratingsPerItem[b].append((u,r))
[10]: usersPerItem = defaultdict(set) # Maps an item to the users who rated it
      itemsPerUser = defaultdict(set) # Maps a user to the items that they rated
[11]: ratingDict = {} # To retrieve a rating for a specific user/item pair
[12]: for i in UIR:
        itemsPerUser[i[0]].add(i[1])
        usersPerItem[i[1]].add(i[0])
        ratingDict[(i[0],i[1])] = i[2]
[13]: ratingsPerUser["A59017531"][:10]
[13]: [('Inception', 1.0),
       ('The_Social_Network', -1.0),
       ('Black_Swan', -1.0),
       ('Shutter_Island', -1.0),
       ('The_Last_Airbender', 1.0),
       ('Harry_Potter_and_the_Deathly_Hallows:_Part_1', 1.0),
       ('Iron_Man_2', 1.0),
       ('Toy_Story_3', 1.0),
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('Fast_Five', 1.0), ('Thor', 1.0)]
```

0.1.3 Q1A

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[]: popDict = {}
for item in ratingsPerItem:
    recN = 0
    sawN = 0
    for user in ratingsPerUser:
        rat = ratingDict[(user,item)]
        if rat == -1:
            continue
        if rat == 1:
            recN+=1
        sawN+=1
        if sawN!=0:
            popDict[item] = recN/sawN
        else:
            popDict[item] = -1
```

```
[]: popDict = dict(sorted(popDict.items(),key=lambda item:item[1]))
```

[]: popDict.keys()

```
[]: dict_keys(['Chappaquidick', 'The_Last_Airbender', 'I_Feel_Pretty',
     'Fifty_Shades_of_Grey', 'Fast_&_Furious:_Hobbs_&_Shaw', 'Hustlers',
     'Magic_Mike', 'Bridemaids', 'World_War_Z', 'The_Shape_of_Water', 'Good_Boys',
     'Prometheus', 'Pokemon_Detective_Pikachu', 'American_Hustle',
     'Terminator: Dark_Fate', 'The_Farewell', 'Man_of_Steel', 'Fast_Five',
     'The_Hateful_Eight', 'Star_Wars:_The_Force_Awakens', 'The_Help', 'Rocketman',
     'Drive', 'The_Girls_with_the_Dragon_Tattoo', 'Thor', 'Avengers:_Age_of_Ultron',
     'Phantom_Thread', 'Us', 'The_Revenant', 'X-Men:_First_Class', 'Pitch_Perfect',
     'Dunkirk', 'Ready_Player_One', 'Room', 'Jurassic_World', 'Mad_Max:_Fury_Road',
     'Once_Upon_a_Time_in_Hollywood', 'Manchester_by_the_Sea',
     'The_Perks_of_Being_a_Wallflower', 'Spiderman:_Far_From_Home', 'Her',
     'Captain_America: The_First_Avenger', 'Frozen', 'Hidden_Figures',
     'The_Hunger_Games', 'Iron_Man_2', 'Les_Miserables', 'Toy_Story_3',
     'Three_Billboards_Outside_Ebbing', 'Darkest_Hour', 'Ex_Machina', 'Gone_Girl',
     'Black_Swan', '12_Years_a_Slave', 'Avengers:_Endgame', 'The_Avengers',
     'Midnight_in_Paris', 'The_Great_Gatsby', 'La_La_Land', 'Avengers:_Infinity_War',
     'The_Theory_of_Everything', 'Now_You_See_Me', '21_Jump_Street',
     'Django_Unchained', 'The_Martian',
     'Harry Potter and the Deathly Hallows: Part 1', 'Joker', 'Wolf of Wall Street',
     'The_Lion_King', 'Harry_Potter_and_the_Deathly_Hallows:_Part_2', 'Parasite',
     'The_Social_Network', 'The_Dark_Knight_Rises', 'Shutter_Island', 'Interstellar',
     'Inception'])
```

[]: popDict.items()

```
[]: dict_items([('Chappaquidick', 0.34285714285714286), ('The_Last_Airbender',
    0.460431654676259), ('I_Feel_Pretty', 0.4878048780487805),
    ('Fifty Shades of Grey', 0.4975124378109453), ('Fast & Furious: Hobbs & Shaw',
    0.5181347150259067), ('Hustlers', 0.5185185185185), ('Magic_Mike',
    0.533333333333333), ('Bridemaids', 0.5384615384615384), ('World_War_Z',
    0.5774647887323944), ('The_Shape_of_Water', 0.57954545454546), ('Good_Boys',
    0.6), ('Prometheus', 0.6017699115044248), ('Pokemon_Detective_Pikachu',
    0.6020942408376964), ('American_Hustle', 0.6052631578947368),
    ('Terminator:_Dark_Fate', 0.6052631578947368), ('The_Farewell',
    0.611111111111111), ('Man_of_Steel', 0.625), ('Fast_Five', 0.6256684491978609),
    ('The_Hateful_Eight', 0.6282051282051282), ('Star_Wars:_The_Force_Awakens',
    0.6495726495726496), ('The Help', 0.65151515151515), ('Rocketman',
    0.6515151515151515), ('Drive', 0.6623376623376623),
    ('The Girls with the Dragon Tattoo', 0.67777777777778), ('Thor',
    0.6804123711340206), ('Avengers: _Age_of_Ultron', 0.6928104575163399),
    ('Phantom Thread', 0.6976744186046512), ('Us', 0.6976744186046512),
    ('The_Revenant', 0.7007874015748031), ('X-Men:_First_Class', 0.701195219123506),
    ('Pitch Perfect', 0.7086614173228346), ('Dunkirk', 0.713541666666666),
    ('Ready_Player_One', 0.7142857142857143), ('Room', 0.7162162162162162),
     ('Jurassic_World', 0.71717171717171), ('Mad_Max:_Fury_Road',
    0.7243589743589743), ('Once_Upon_a_Time_in_Hollywood', 0.725925925925926),
    ('Manchester_by_the_Sea', 0.7272727272727273),
     ('The_Perks_of_Being_a_Wallflower', 0.7346938775510204),
    ('Spiderman:_Far_From_Home', 0.7450331125827815), ('Her', 0.75),
    ('Captain_America: The First_Avenger', 0.7523510971786834), ('Frozen',
    0.7552447552447552), ('Hidden_Figures', 0.7590361445783133),
     ('The Hunger_Games', 0.7676767676767676), ('Iron_Man_2', 0.770392749244713),
    ('Les Miserables', 0.7737226277372263), ('Toy_Story_3', 0.77777777777777),
    ('Three Billboards Outside Ebbing', 0.7804878048780488), ('Darkest Hour',
    0.78125), ('Ex_Machina', 0.7863247863247863), ('Gone_Girl', 0.7938931297709924),
    ('Black_Swan', 0.7981651376146789), ('12_Years_a_Slave', 0.811965811965812),
    ('Avengers: Endgame', 0.8136645962732919), ('The_Avengers', 0.8147058823529412),
    ('Midnight_in_Paris', 0.8170731707317073), ('The_Great_Gatsby',
    0.8178137651821862), ('La_La_Land', 0.8235294117647058),
    ('Avengers:_Infinity_War', 0.826625386996904), ('The_Theory_of_Everything',
    0.8294117647058824), ('Now_You_See_Me', 0.836), ('21_Jump_Street',
    0.837037037037), ('Django Unchained', 0.84472049689441), ('The Martian',
    0.861244019138756), ('Harry_Potter_and_the_Deathly_Hallows:_Part_1',
    0.8628048780487805), ('Joker', 0.8647686832740213), ('Wolf_of_Wall_Street',
    0.8669064748201439), ('The_Lion_King', 0.8717948717948718),
    ('Harry_Potter_and_the_Deathly_Hallows:_Part_2', 0.871875), ('Parasite',
    0.8878923766816144), ('The_Social_Network', 0.8960396039603961),
    ('The_Dark_Knight_Rises', 0.8982456140350877), ('Shutter_Island',
    0.933333333333333), ('Interstellar', 0.946843853820598), ('Inception',
    0.9605263157894737)])
```

0.1.4 The rankings are somewhat in line with what I would vote, but not all are matching

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0.1.5 \quad Q1)E)
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[]: pz = np.loadtxt("hw8_probZ_init.txt")
     prz = np.loadtxt("hw8_probR_init.txt")
[ ]: k = 4
     N = 256
     postProb = np.zeros((k,len(users)))
[]: def loglikeli(user):
      sumi = 0
      rec, = np.where(ratings[user,:] == 1)
      notRec, = np.where(ratings[user,:] == 0)
       for i in range(k):
         sumi+=(pz[i])*(np.prod(prz[rec,i]))*(np.prod(1-prz[notRec,i]))
       return np.log(sumi)
[]: def e_step(i,user):
      rec, = np.where(ratings[user,:] == 1)
      notRec, = np.where(ratings[user,:] == 0)
      numi = pz[i]*np.prod(prz[rec,i])*(np.prod(1-prz[notRec,i]))
       deno = 0
       for ind in range(k):
         deno+=pz[ind]*np.prod(prz[rec,ind])*(np.prod(1-prz[notRec,ind]))
       return numi/deno
[]: def m_step(i,item):
       seen, = np.where(ratings[:,item] == 1)
      nSeen, = np.where(ratings[:,item] == -1)
       sumi = (np.sum(postProb[i,seen])+prz[item,i]*np.sum(postProb[i,nSeen]))/np.
      ⇒sum(postProb[i,:])
       return sumi
[]: logliklii = []
     for i in tqdm(range(N+1)):
       logli = 0
      pzTmp = np.zeros(k)
      przTmp = np.zeros((len(items),k))
      for user in range(len(users)):
         logli += loglikeli(user)
         for i in range(k):
           postProb[i,user] = e_step(i,user)
       for i in range(k):
         pzTmp[i] = np.sum(postProb[i,:])/len(users)
```

```
for item in range(len(items)):
          przTmp[item,i] = m_step(i,item)
      logliklii.append(logli/len(users))
      pz = pzTmp
      prz = przTmp
                   | 0/257 [00:00<?, ?it/s]
      0%1
[]: indi = [0]
    11 = [logliklii[0]]
    for i in range(9):
      indi.append(2**i)
      ll.append(logliklii[int(2**i)])
[]:
[]: print("Table:")
    x = PrettyTable()
    x.add_column("Iteration", indi)
    x.add_column("LogLikelihood", 11)
    print(x)
    Table:
    | Iteration |
                    LogLikelihood
      ------
                | -28.627324487337628 |
                | -19.350314946503318 |
               | -17.90956481801792 |
               | -17.081155562337017 |
         8
               | -16.629824767528113 |
          16
               | -16.287828721915584 |
          32
               | -15.80153795397027 |
               | -15.749887678844283 |
          64
         128
                | -15.735940712575664 |
                | -15.728520329683299 |
         256
    0.1.6 Yes the loglikelihood becomes less and less negative, as we expected.
    0.1.7 Q1F
[]: ratingsPerUser["A59017531"][:10]
[]: [('Inception', 1.0),
     ('The_Social_Network', -1.0),
      ('Black_Swan', -1.0),
      ('Shutter_Island', -1.0),
```

```
('The_Last_Airbender', 1.0),
      ('Harry_Potter_and_the_Deathly_Hallows:_Part_1', 1.0),
      ('Iron_Man_2', 1.0),
      ('Toy_Story_3', 1.0),
      ('Fast_Five', 1.0),
      ('Thor', 1.0)]
[]:
[]: (array([9]),)
[]: user = "A59017531"
     userId = np.where(users == user)[0][0]
     recommendations = {}
     for me in ratingsPerUser[user]:
       if me[1] == -1: #unseen
         sumi = 0
         movieIdx = np.where(items==me[0])[0][0]
         for i in range(k):
           estep = e_step(i,userId)
           mstep = m step(i,movieIdx)
           sumi += estep*mstep
         recommendations[me[0]] = sumi
[]: dict(sorted(recommendations.items(),key=lambda item:item[1],reverse=True))
[]: {'The_Theory_of_Everything': 0.9810400408235112,
      'Shutter_Island': 0.9745852668879414,
      'Django_Unchained': 0.9731063931312587,
      '21 Jump Street': 0.9729138079741417,
      'Midnight_in_Paris': 0.9700705368973399,
      'Parasite': 0.9697855734535975,
      'Hidden Figures': 0.9648232899695831,
      'The_Hunger_Games': 0.9631952084894266,
      'The_Perks_of_Being_a_Wallflower': 0.9618823785178835,
      'Phantom_Thread': 0.9568020557602742,
      '12_Years_a_Slave': 0.9549226481950793,
      'Gone_Girl': 0.9533566794438127,
      'The_Help': 0.9532991684985187,
      'Her': 0.9487601164156515,
      'The_Social_Network': 0.947674353086089,
      'Prometheus': 0.9431487813732097,
      'Black_Swan': 0.9403008886436867,
      'Drive': 0.9389080698290413,
      'The_Farewell': 0.9364692582778592,
      'Good_Boys': 0.9316805551144837,
      'The_Martian': 0.9243198446314408,
```

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'Hustlers': 0.9230392263890211,
'I_Feel_Pretty': 0.9198683449177839,
'Darkest_Hour': 0.9188775043021438,
'Three_Billboards_Outside_Ebbing': 0.9166413870517898,
'La_La_Land': 0.9075400177503928,
'Les_Miserables': 0.898955453530586,
'The_Girls_with_the_Dragon_Tattoo': 0.894674775604871,
'The_Great_Gatsby': 0.887310662485786,
'Dunkirk': 0.8799365619470496,
'The Revenant': 0.8793113974336506,
'Ex Machina': 0.8778101088513737,
'Manchester_by_the_Sea': 0.8740733188278312,
'Pitch_Perfect': 0.8623469324170651,
'World_War_Z': 0.8553481123564523,
'Mad_Max:_Fury_Road': 0.848810825704276,
'Room': 0.8367003390062016,
'Bridemaids': 0.8340954026340719,
'Once_Upon_a_Time_in_Hollywood': 0.8315862756962407,
'The_Hateful_Eight': 0.8268013366459704,
'American_Hustle': 0.8140761941342205,
'Rocketman': 0.8126156038813724,
'Us': 0.7974269241726685,
'The_Shape_of_Water': 0.7931415651194657,
'Star Wars: The Force Awakens': 0.7873841266943339,
'Chappaquidick': 0.763837402223503,
'Terminator: Dark Fate': 0.7487409431505707,
'Magic_Mike': 0.7146949155178426,
'Fifty_Shades_of_Grey': 0.6712659458102751}
```

0.1.8 Yup, these recommendations are wayy more accurate than the mean ones.

[]: