

# STATISTICS

$$\bar{V}_J = \sum_{i=1}^{N_J} A_{RING_i} \frac{N_{iJ}}{N_i}$$

$$SD_J = \sqrt{\sum_{i=1}^{N_J} A_{RING_i} \underbrace{\frac{N_{iJ}}{N_i}}_{P_{iJ}} \underbrace{\left(1 - \frac{N_{iJ}}{N_i}\right)}_{1-P_{iJ}} \frac{A_{RING_i}}{N_i}}$$

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$$\bar{V}_J = (\pi b^2) P_J = \int_0^{2\pi} \int_0^{\infty} \tilde{b} \tilde{p}_J d\tilde{b} d\theta =$$

$$= 2\pi \int_0^{b_1} b p_J db + \int_{b_1}^{b_2} b p_J db + \dots$$

$$\approx \pi b_1^2 \frac{N_{1J}}{N_1} + \pi (b_2^2 - b_1^2) \frac{N_{2J}}{N_2} + \dots$$

$$\approx \sum_{i=1}^{\infty} \pi (b_i - b_{i-1}) \frac{N_{iJ}}{N_i} \quad (b_0 = 0)$$

$$VAR(\bar{V}_J) \stackrel{MC}{=} \frac{V^2}{N^2} VAR(P_J) \approx$$

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$$= \sum_i \frac{A_{RING_i}^2}{N_i} P_{iJ} (1 - P_{iJ})$$

$$SD_g = \sqrt{\sum_i \frac{V_i \bar{V}_i}{N_i}} \quad \begin{array}{l} \nearrow \text{COMPLEMENTARY} \\ \text{PROCESSES} \end{array}$$