

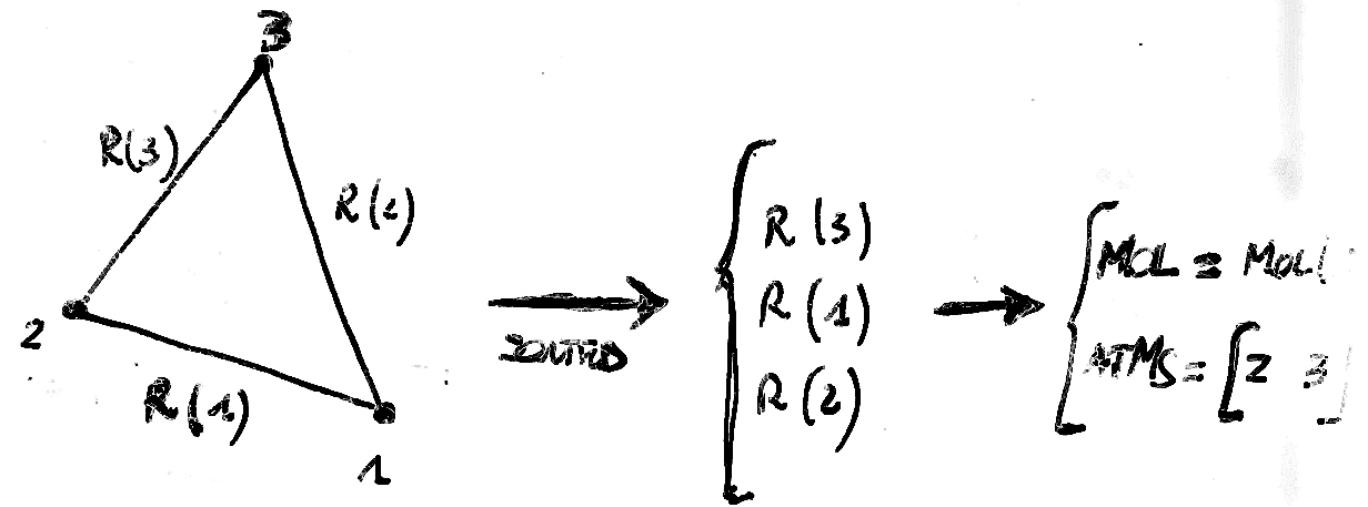
$\leftarrow$  ATOMS  $\rightarrow$

$$\vec{x} = \begin{bmatrix} PAQ(7) & PAQ(10) & -\frac{m_1}{m_3} PAQ(7) - \frac{m_2}{m_3} PAQ(10) \\ PAQ(8) & PAQ(11) & -\frac{m_1}{m_3} PAQ(8) - \frac{m_2}{m_3} PAQ(11) \\ PAQ(9) & PAQ(12) & -\frac{m_1}{m_3} PAQ(9) - \frac{m_2}{m_3} PAQ(12) \end{bmatrix}$$

$$\dot{\vec{x}} = \begin{bmatrix} PAQ(1) & PAQ(4) & -\frac{m_1}{m_3} PAQ(1) - \frac{m_2}{m_3} PAQ(4) \\ PAQ(2) & PAQ(5) & -\frac{m_1}{m_3} PAQ(2) - \frac{m_2}{m_3} PAQ(5) \\ PAQ(3) & PAQ(6) & -\frac{m_1}{m_3} PAQ(3) - \frac{m_2}{m_3} PAQ(6) \end{bmatrix}$$



COMPUTE COORD AND VELOC



WITH PIAGORA'S THEOREM

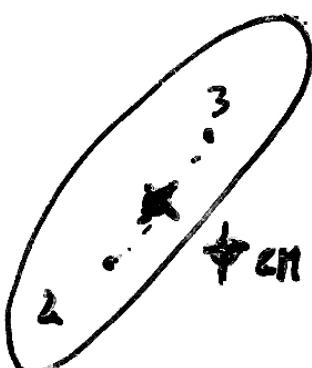
### SETPAIRS

$$CM = \left[ \begin{array}{l} \frac{m_2 x_{12} + m_3 x_{13}}{m_2 + m_3} \\ \frac{m_2 x_{22} + m_3 x_{23}}{m_2 + m_3} \\ \frac{m_2 x_{32} + m_3 x_{33}}{m_2 + m_3} \end{array} \right]$$

$$\begin{array}{l} \frac{m_1 x_{11}}{m_1} \\ \frac{m_1 x_{21}}{m_1} \\ \frac{m_1 x_{31}}{m_1} \end{array}$$

$$\dot{CM} = \frac{d(CM)}{dt}$$

TRANSIT



PROJECTILE



3  
2  
1

$\vec{K}_1 - \vec{x}_{rel}$   
 $\vec{v}_{rel} = \vec{x}_{rel}$

$$dist = \sqrt{x_{relx}^2 + x_{rely}^2 + x_{relz}^2}$$

$$\sqrt{V_{relx}^2 + V_{rely}^2 + V_{relz}^2}$$

$$t = \frac{x_{relx} v_{relx} + x_{rely} v_{rely} + x_{relz} v_{relz}}{V_{relx}^2 + V_{rely}^2 + V_{relz}^2}$$

$$b = \sqrt{(x_{relx} + t v_{relx})^2 + (x_{rely} + t v_{rely})^2 + (x_{relz} + t v_{relz})^2}$$

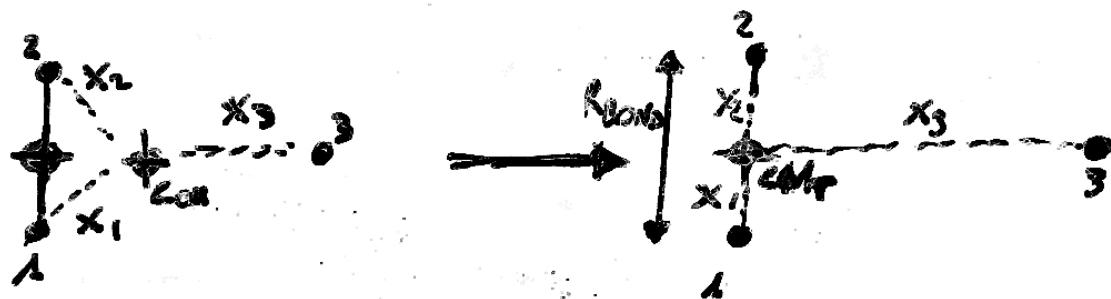
$$E_{kin} = \sum_{i=1}^3 \left( \frac{1}{2} (m_2 + m_3) c_{i,1}^2 + \frac{1}{2} (m_1) c_{i,2}^2 \right)$$

$$\vec{x}_g = (\vec{c}_{M_T} \times \dot{\vec{c}}_{M_T} + \vec{c}_{M_P} \times \dot{\vec{c}}_{M_P}) M_T.$$

$$f_a = \frac{m_a}{m_a + m_b}$$

$$f_b = \frac{m_b}{m_a + m_b}$$

$$\begin{cases} \vec{x}_{a_4} = f_a \vec{x}_a + f_b \vec{x}_b \\ \dot{\vec{x}}_{a_4} = f_a \dot{\vec{x}}_a + f_b \dot{\vec{x}}_b \end{cases}$$



$$E_{INT_K} = \sum_{i=1}^3 \frac{1}{2} (m_a \dot{x}_{i1}^2 + m_b \dot{x}_{i2}^2)$$

$$Ang\text{M}_K = \parallel (\vec{x}_1 \times \dot{\vec{x}}_1) m_1 + (\vec{x}_2 \times \dot{\vec{x}}_2) m_2 \parallel$$

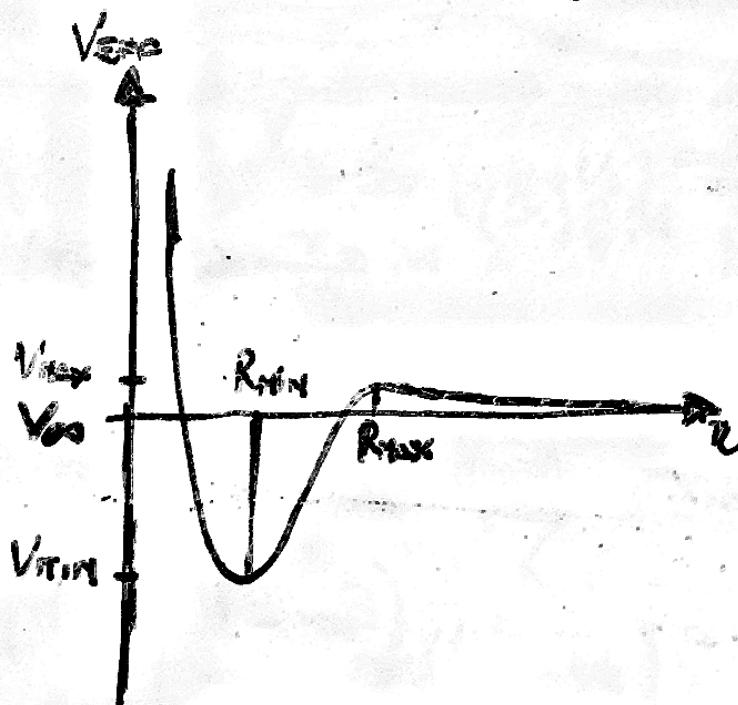
$$M = \frac{m_a m_b}{m_a + m_b}$$

$$V_c = \frac{1}{2} \frac{\text{Ang}^2 M R^2}{\mu R^2} = \frac{1}{2} \frac{(J + \frac{1}{2})^2}{\mu R^2}$$

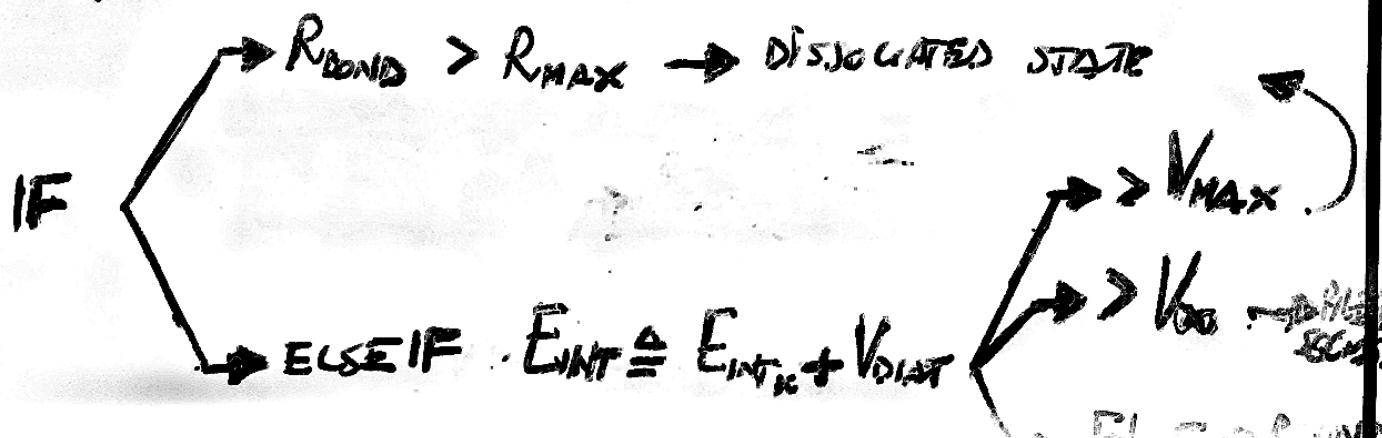
CENTRIFUGAL  
POTENTIAL

$$V_{\text{eff}} = V_{\text{int}} + V_c$$

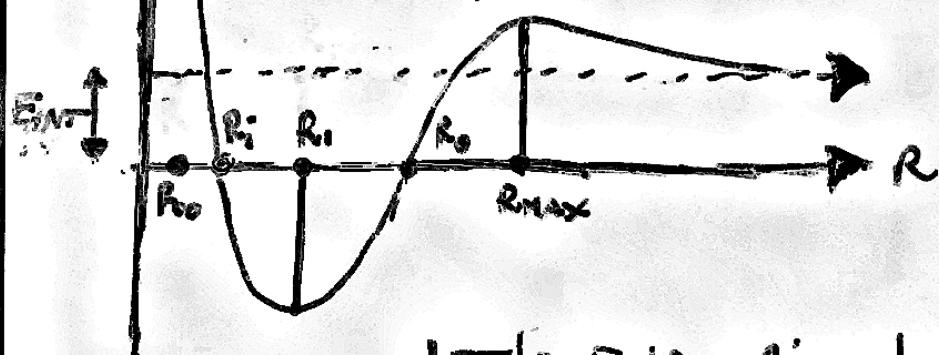
$$\begin{cases} R_{\min} \\ V_{\min} \end{cases} \quad \text{and} \quad \begin{cases} R_{\max} \\ V_{\max} \end{cases}$$



LET'S FIND  $R_{\min}$  AND  
THROUGH FIND  $E_{\text{INT}}$



$$V_{DIAT} = \underbrace{(E_{INTk} + V_{DIAT}(R_{S0}))}_{E_{INT}}$$



LET'S FIND  $R_i$  AND  $R_o$  THROUGH  
TURNING POINT

CHEBYSHEV-GAUSS INTEGRAL FOR ACTION INTEGRAL:

$$\int_{-1}^{+1} \sqrt{1-x^2} g(x) dx \approx \sum_{i=1}^{N_{GAUSS}} w_i g(x_i) \quad x_i = \cos\left(\frac{i}{m+1}\pi\right) \\ w_i = \frac{\pi}{m+1} m^2 \left(\frac{i}{m+1}\pi\right)$$

$$\pi(N+1/2) = 2 \cdot \sqrt{2\mu} \cdot \sum_{i=2}^{N_{GAUSS}} \sqrt{(E_{INT} - V_{ext}(R_i))} w_i$$

$$R_p = \frac{R_o + R_i}{2} + \underbrace{\frac{R_o - R_i}{2} x_{i+1}}_{R_M}$$

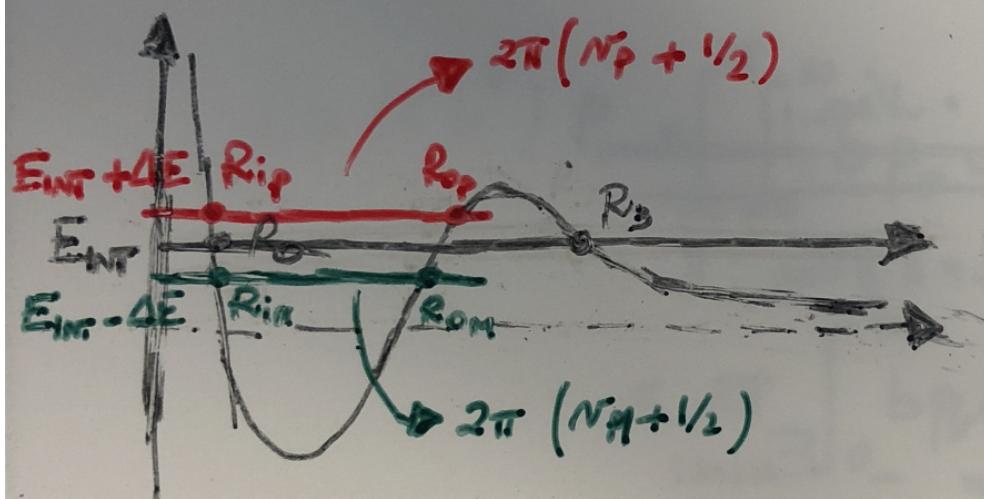
ACTION INTEGRAL.

For solving the EBK QUANTIZATION condition:

$$2\sqrt{2m} \int_{R_1}^{R_0} \sqrt{(\epsilon_{VR} - V_{DAR} - V_c)} dR = \hbar(v + \frac{1}{2})$$

$\frac{1}{2\pi\hbar}$

IF  $E_{INT} > V_{DD}$



$$\Delta E = \begin{cases} (\text{run down}) \\ V_{MAX} - E_{INT} \end{cases} \frac{2}{2}$$

$$\frac{dn}{dE} = \frac{(N_p + \cancel{\chi}_2) - (N_{in} + \cancel{\chi}_2)}{2\Delta E}$$

$$\left. \frac{R_o}{R_{in}} \right] \rightarrow 2\pi \left( \frac{N_p + \cancel{\chi}_2}{2} \right)$$

$$\Gamma \triangleq \frac{e^{-2\pi \left( \frac{N_p + \cancel{\chi}_2}{2} \right)}}{\frac{dn}{dE}}$$

$$t_{LIFE} = \frac{1}{\Gamma}$$

NB:  $t_{LIFE} > t_{MIN}$   
MUST

$$\Delta N_{\text{tot}} = \left[ \Gamma_{\text{tot}} \left( N_{\text{tot}} \right) - N_{\text{tot}} \left( \log \left( \frac{N_{\text{tot}}}{N_{\text{tot}} + 1} \right) - 1 \right) \right] \rho_{\text{gas}}$$

↑  
FINAL

$$\text{dot}_3 = \frac{v_{\text{rel f}} \cdot v_{\text{rel i}}}{\sqrt{\|v_{\text{rel f}}\| \|v_{\text{rel i}}\|}}$$

$$\Delta E_{\text{kin}} = E_{\text{kin f}} - E_{\text{kin i}}$$