

quollr: An R Package for Visualizing 2D Models from Nonlinear Dimension Reduction in High Dimensional Space

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Abstract An abstract of less than 150 words.

1 Introduction

2 Methodology

3 Implementation

The package can be installed from CRAN:

```
install.packages("quollr")
```

The development version can be installed from GitHub:

```
devtools::install_github("JayaniLakshika/quollr")
```

The following demonstration of the package's functionality assumes `quollr` has been loaded. We also want to load the built-in data sets `s_curve_noise_training` and `s_curve_noise_umap`.

The mains steps for the algorithm can be executed by the main function `fit_highd_model()`, or can be run separately for more flexibility. When constructing the 2D model, the user can choose either to fir the 2D model with hexagonal bin centroids or bin means using `is_bin_centroid` argument.

Constructing the 2D model

Preprocessing

The function `gen_scaled_data()` is used to prepare the NLDR data to fit within the bounds required for regular hexagonal binning, ensuring effective visualization.

Binning data

The mains steps for the hexagonal binning algorithm can be executed by the main function `hex_binning()`, or can be run separately for more flexibility.

Step 1: Compute hexagonal grid configurations

Step 2: Generate the hexagonal bin centroids

Step 3: Create the hexagonal grid

Step 4: Assign NLDR data to hexagons

Obtain bin centroids/ means

To obtain hexagonal bin centroids, `extract_hexbin_centroids()` is used. The function `extract_hexbin_mean()` is used to obtain average within each hexagon.

Triangulate bin centroids/ means

The `tri_bin_centroids()` is used to do triangulate bin centroids/ bin means. Then, `gen_edges()` compute the edges to obtain the triangular mesh which is the 2D model.

Lifting the model into high dimensions

The p -D model is generated by `avg_highd_data()` by passing the p -D data.

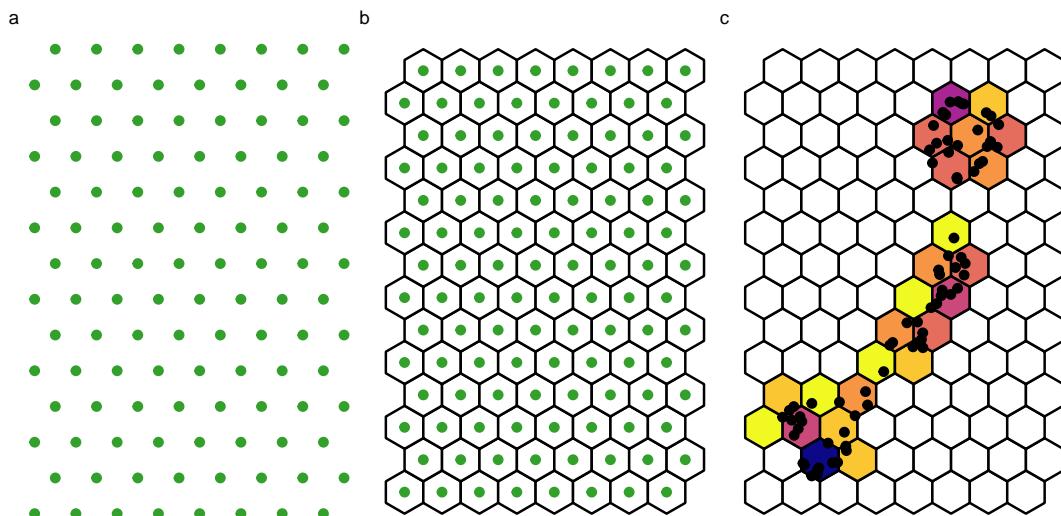


Figure 1: Illustration of key steps of the hexagonal binning algorithm: (a) first, all hexagonal bin centroids are created; (b) second, full hexagon grid is created; and (c) finally, assign the data to hexagons. The centroids are used to generate hexagonal coordinates. Once the full hexagonal grid is generated, by computing the 2D euclidean distance from each NLDR points to hexagonal bin centroids, the nearest NLDR points are allocated to the nearest hexagoanl bin.

Tuning model parameters

Mainly there are two model parameter need to consider: benchmark value to remove the low-density hexagons, and benchmark value to remove the long edges. `find_low_dens_hex()` is used to find the hexagons which contains less number of points by considering the density of their neighboring points as well. In here, user can first decide which are the low-density hexagons and pass them to this function to check whether these removal of low-density hexagons can affect the model fit by looking at the the neighbors. On the other hand, `find_lg_benchmark()` function is used to compute the threshold for removing long edges.

Prediction

`predict_emb()` function is used to predict 2D embedding for a new p -D data point using the fitted model. This function is useful to predict 2D embedding irrespective of the NLDR technique.

Compute residuals and Mean Square Error (MSE)

As a Goodness of fit statistics for the model, `gen_summary()` is used to compute residuals and MSE. For the fitted model, how residuals and MSE is changing is shown in Figure 2.

Visualizations

The package provides four basic visualizations which includes three visualizations regarding 2D model (static vis) and one is regrading p -D model (dynamic vis). Each visualization can be done their own functions which describes in this section.

2D model visualization

To visualize the 2D model, mainly three functions are used. As shown in Figure 1, `geom_trimesh()` to visualize the triangular mesh by adding a new layer to `ggplot()`. After identifying benchmark value to remove long edge, `vis_lg_mesh()` is used to visualize the triangular mesh by coloring the small and long edges. As shown in Figure 1, the small and long edges are colored by black and red respectively. Following this, `vis_rmlg_mesh()` is used to visualize smoothed 2D model which is the 2D model after removing the long edges (see Figure 1). In `vis_lg_mesh()` and `vis_rmlg_mesh()`, `benchmark_value` argument controls the edge removal in 2D.

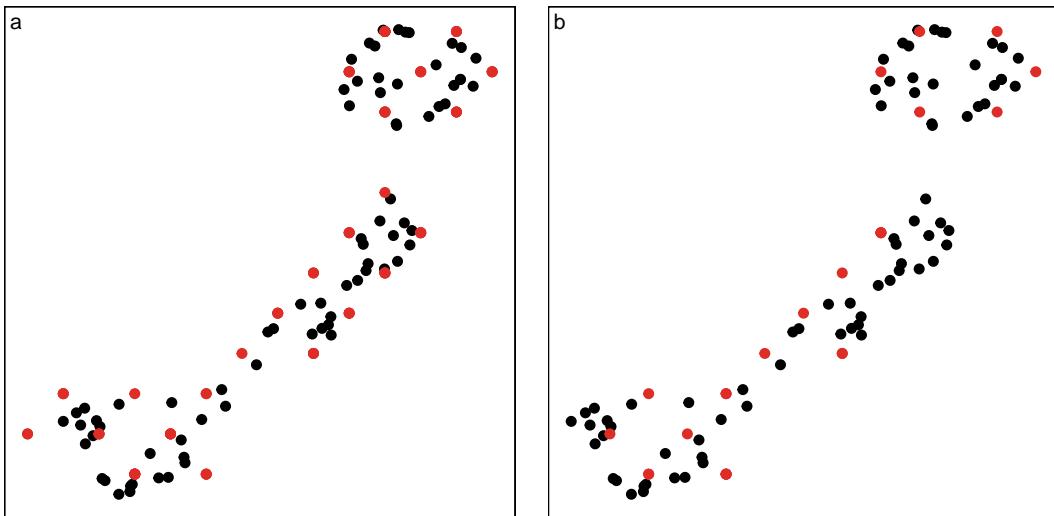


Figure 2: Predicted 2D embedding overlaid with S-curve training UMAP data: (a) Prediction of 2D embeddings for S-curve training data, and (b) Prediction of 2D embeddings for S-curve test data. Once the high-D model is generated, first, for the new data points the nearest high-D mappings of hexagonal bin centroids find by computing Euclidean distance. Then, mapping back the 2D hexagonal bin centroids gives the prediction for the new data points.

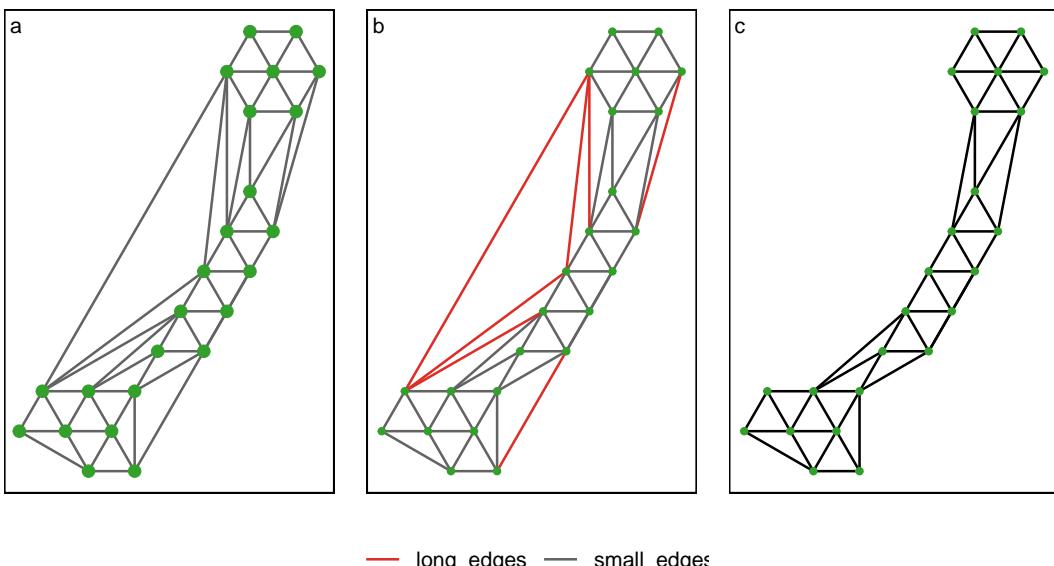


Figure 3: Visualization of model generated for UMAP embedding for S-curve data in 2D space: (a) triangular mesh, (b), triangular mesh colored by edge type, and (c) triangular mesh after removing the long edges. The edges which has the length greater than 0.5 are assigned as long edges. To obtain smooth representation in 2D space, the long edges are removed.

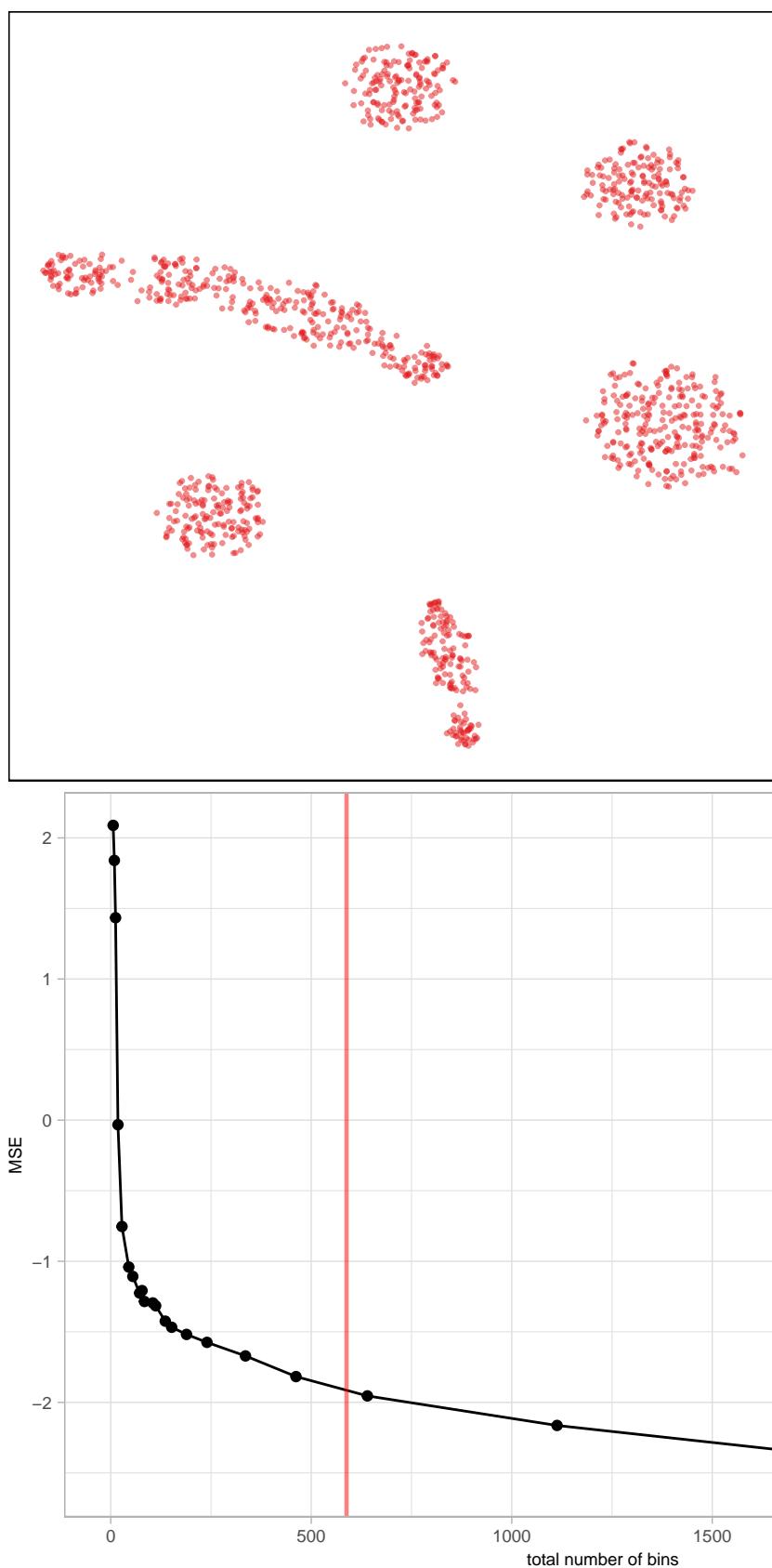
p-D model visualization

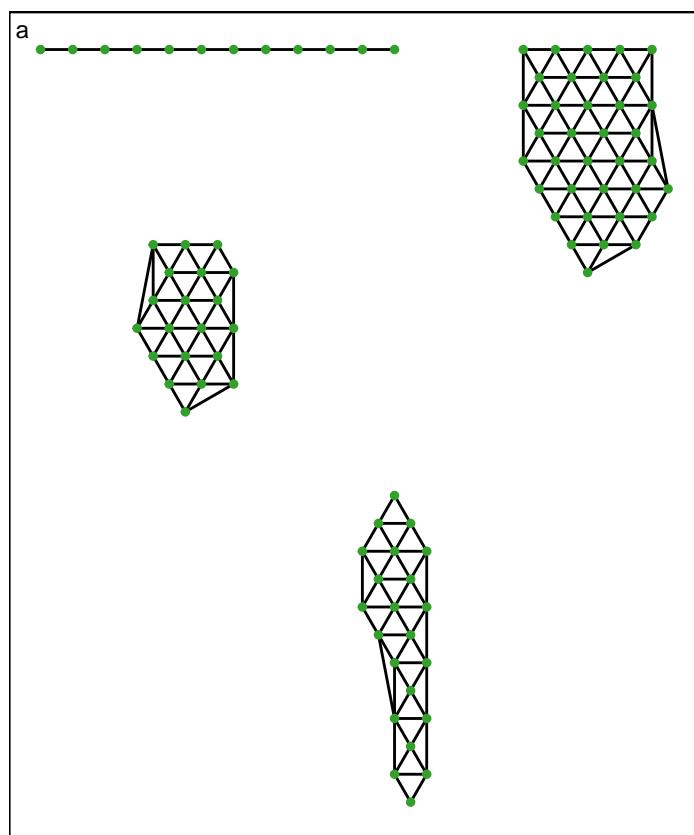
The *p*-D model overlaid on data is visualized by the function `show_langevitour()`. This is a useful dynamic visualization result to validate visually whether the model fits the data well or not.

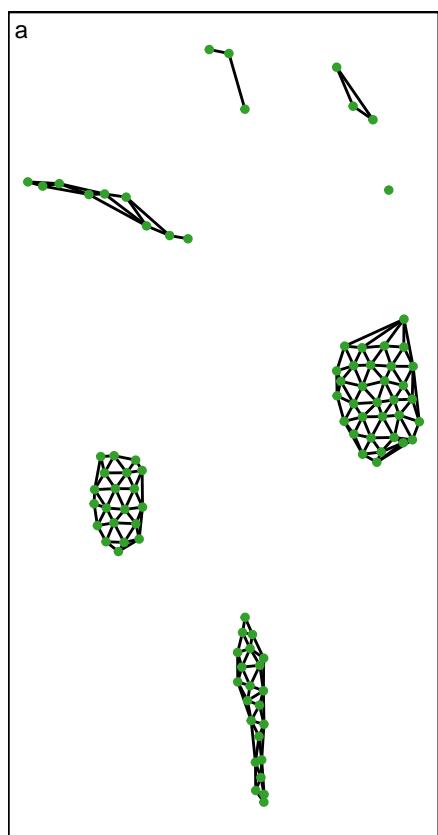
Tests

All functions have tests written and implemented using the `testthat` (Wickham 2011) in R.

4 Application







5 Conclusion

6 Acknowledgements

This article is created using `knitr` (Xie 2015) and `rmarkdown` (Xie, Allaire, and Grolemund 2018) in R with the `rjtools::rjournal_article` template. The source code for reproducing this paper can be found at: <https://github.com/JayaniLakshika/paper-quollr>.

References

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