

LAB EXERCISE 3

Name: Jayannthan P T

Dept: CSE 'A'

Roll No.: 205001049

1. Use import matplotlib.pyplot as plt and plot the graph for n and complexity for the following recurrence relations:

a. $T(n)=T(n-1)+n$

Code:

```
import matplotlib.pyplot as plt
import math
import numpy as np

xpoints = np.array(range(900))

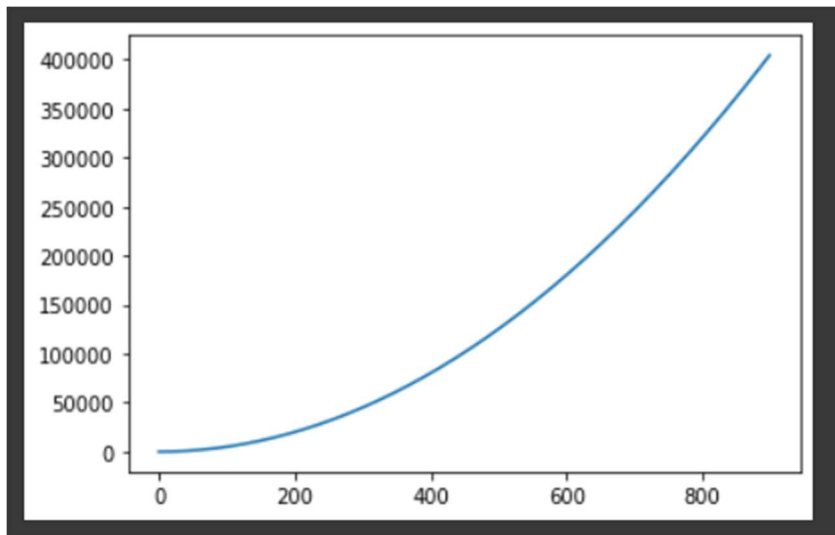
def yarray(k):
    if(k <= 1):
        return 1
    else:
        return yarray(k-1)+k

ypoints = []

for i in xpoints:
    # print(i)
    ypoints.append(yarray(i))

plt.plot(xpoints, ypoints)
plt.show()
```

Output:



b. $T(n) = T(n-1) + n^2$

Code:

```
# T(n) = T(n-1) + n^2

xpoints = np.array(range(900))

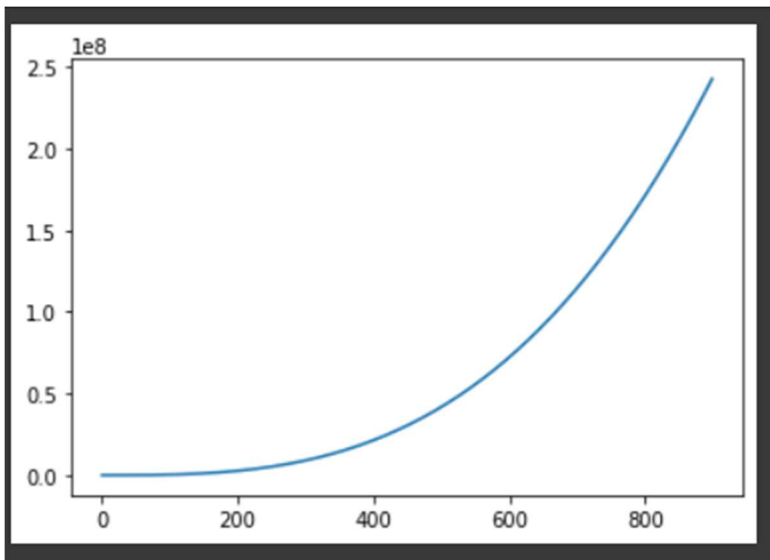
def yarray(k):
    if(k <= 1):
        return 1
    else:
        return yarray(k-1) + (k*k)

ypoints = []

for i in xpoints:
    ypoints.append(yarray(i))

plt.plot(xpoints, ypoints)
plt.show()
```

Output:



c. $T(n) = T(n-1) + \log n$

Code:

```
# T(n)=T(n-1)+log n

xpoints = np.array(range(100))

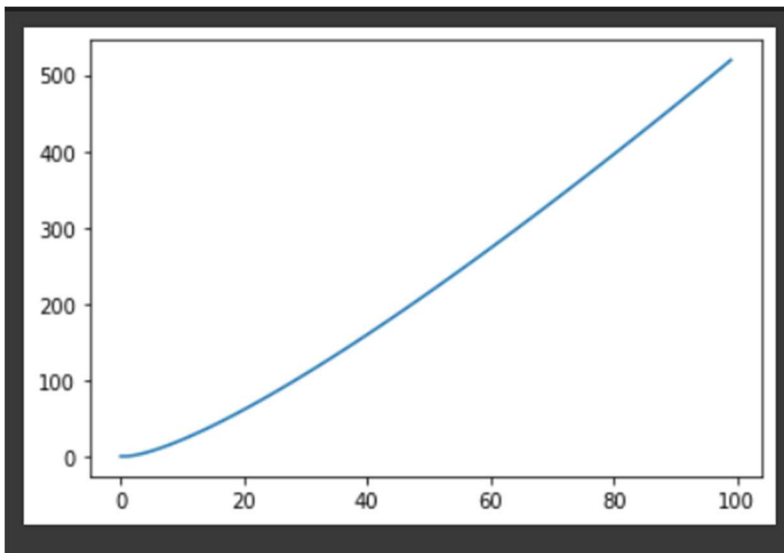
def yarray(k):
    if(k <= 1):
        return 1
    else:
        return yarray(k-1)+math.log(k, 2)

ypoints = []

for i in xpoints:
    ypoints.append(yarray(i))

plt.plot(xpoints, ypoints)
plt.show()
```

Output:



d. $T(n) = T(n/2) + \log n$

Code:

```
#  $T(n) = T(n/2) + \log n$ 

xpoints = np.array(range(100))

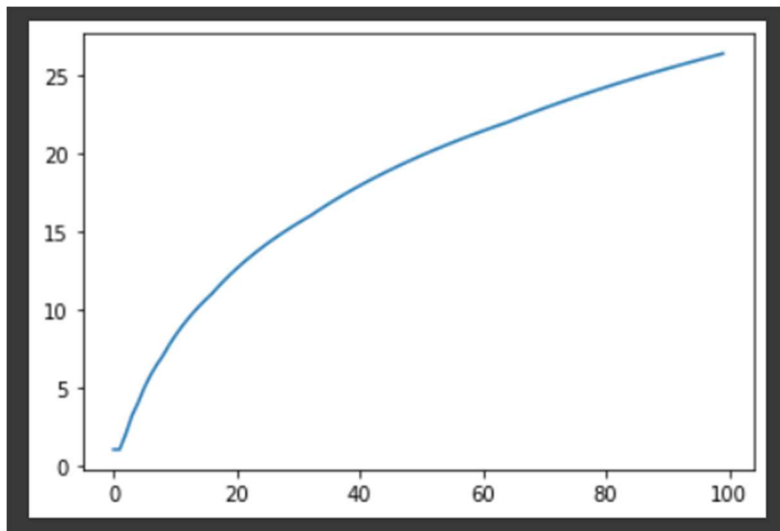
def yarray(k):
    if(k <= 1):
        return 1
    else:
        return yarray(k/2)+math.log(k, 2)

ypoints = []

for i in xpoints:
    ypoints.append(yarray(i))

plt.plot(xpoints, ypoints)
plt.show()
```

Output:



e. $T(n) = T(\sqrt{n}) + \log n$

Code:

```
# T(n) = T(sqrt(n)) + log n

xpoints = np.array(range(100))

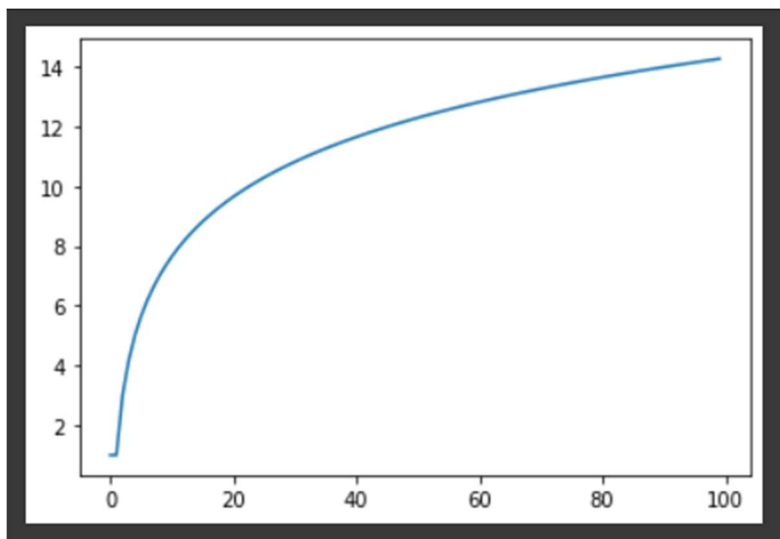
def yarray(k):
    if(k <= 1):
        return 1
    else:
        return yarray(math.sqrt(k))+math.log(k, 2)

ypoints = []

for i in xpoints:
    ypoints.append(yarray(i))

plt.plot(xpoints, ypoints)
plt.show()
```

Output:



2. Implement Strassen Matrix multiplication

Code:

```
import numpy as np

def split(mat):
    r, c = mat.shape
    r2, c2 = r // 2, c // 2
    return mat[: r2, : c2], mat[: r2, c2:], mat[r2:, : c2], mat[r2:, c2:]

def strassen(x, y):
    if len(x) == 1:
        return x * y
    a, b, c, d = split(x)
    e, f, g, h = split(y)

    p1 = strassen(a, f - h)
    p2 = strassen(a + b, h)
    p3 = strassen(c + d, e)
    p4 = strassen(d, g - e)
    p5 = strassen(a + d, e + h)
    p6 = strassen(b - d, g + h)
    p7 = strassen(a - c, e + f)
    c11 = p5 + p4 - p2 + p6
    c12 = p1 + p2
    c21 = p3 + p4
    c22 = p1 + p5 - p3 - p7

    c = np.vstack((np.hstack((c11, c12)), np.hstack((c21, c22))))

    return c

strassen(np.array([[1, 2], [3, 4]]), np.array([[1, 2], [3, 4]]))
```

Output:

```
array([[ 7, 10],  
       [15, 22]])
```