



Higher Normalization - 5NF

Overview

- Join Dependencies [JD]
- Fifth Normal Form – 5NF

Join Dependency

- There exists relvars that can be nonloss-decomposed into three or more – *n-decomposable*.
- Consider relvar SHIPMENTS from the supplier-parts-projects.
- The relvar is all key and involves no nontrivial FDs or MVDs, hence in 4NF.

SHIPMENTS

| SUPPLIER_NUMBER | PART_NUMBER | PROJECT_NUMBER |
|-----------------|-------------|----------------|
| S1 | P1 | J2 |
| S1 | P2 | J1 |
| S2 | P1 | J1 |
| S1 | P1 | J1 |

Join Dependency

- SP

| SUPPLIER_ NUMBER | PART_ NUMBER |
|---------------------|-----------------|
| ----- | |
| S1 | P1 |
| S1 | P2 |
| S2 | P1 |

PJ

| PART_ NUMBER | PROJECT_ NUMBER |
|-----------------|--------------------|
| ----- | |
| P1 | J2 |
| P2 | J1 |
| P1 | J1 |

JS

| PROJECT_ NUMBER | SUPPLIER_ NUMBER |
|--------------------|---------------------|
| ----- | |
| J2 | S1 |
| J1 | S1 |
| J1 | S2 |

Join Dependency

- SP **Join** PJ over PART_NUMBER

| SUPPLIER_ NUMBER | PART_ NUMBER | PROJECT_ NUMBER |
|---------------------|-----------------|--------------------|
| S1 | P1 | J2 |
| S1 | P2 | J1 |
| S2 | P1 | J1 |
| S2 | P1 | J2 |
| S1 | P1 | J1 |

Spurious
tuple

JS

| PROJECT_ NUMBER | SUPPLIER_ NUMBER |
|--------------------|---------------------|
| J2 | S1 |
| J1 | S1 |
| J1 | S2 |

Join over
PROJECT_NUMBER,
SUPPLIER_NUMBER

SHIPMENTS

Join Dependency

- SHIPMENTS is equal to the join of its three projections SP, PJ, and JS is equivalent to:

If the pair (s1,p1) appears in SP
and the pair (p1,j1) appears in PJ
and the pair (j1,s1) appears in JS
then the triple (s1,p1,j1) certainly appears in
join of {SP,PJ,JS} = SHIPMENTS

- A relvar will be n-decomposable for some $n > 2$ if and only if it satisfies some such (n-way) cyclic constraint.

Join Dependency

- JD is equal to the following constraints. If,
 - $\langle s1, p1, z \rangle$: a supplier $s1$ supplies part $p1$ to some project, and
 - $\langle x, p1, j1 \rangle$: a project $j1$ uses part $p1$ supplied by some supplier, and
 - $\langle s1, y, j1 \rangle$: the supplier $s1$ supplies *at least one* part to project $j1$, then
 - $\langle s1, p1, j1 \rangle$: supplier $s1$ will also be supplying part $p1$ to project $j1$
- Constraint 3-decomposable [3D] is satisfied if and only if the relvar is equal to the join of certain of its projections – refer to that constraint as a *join-dependency* (JD)

Join Dependency

- Let R be a relvar, and let A, B, \dots, Z be subsets of the attributes of R . Then we say that R satisfies the JD

$$* \{ A, B, \dots, Z \} \quad [\text{star } A, B, \dots, Z]$$

if and only if **every legal value of R** is equal to the join of its projections on A, B, \dots, Z .

- For example, the set of attributes of SP, PJ and JS , then relvar $\text{SHIPMENTS}(S,P,J)$ satisfies the JD $*\{SP, PJ, JS\}$

JDs and Fifth NF

Figure 11.4

Fourth and fifth normal forms.

- (a) SUPPLY in 4NF, with JD(R1,R2,R3) – not in 5NF
- (b) Decomposing into 5NF relations R1, R2, R3

(c) SUPPLY

| <u>Sname</u> | <u>Part_name</u> | <u>Proj_name</u> |
|--------------|------------------|------------------|
| Smith | Bolt | ProjX |
| Smith | Nut | ProjY |
| Adamsky | Bolt | ProjY |
| Walton | Nut | ProjZ |
| Adamsky | Nail | ProjX |
| Adamsky | Bolt | ProjX |
| Smith | Bolt | ProjY |

(d) R_1

| <u>Sname</u> | <u>Part_name</u> |
|--------------|------------------|
| Smith | Bolt |
| Smith | Nut |
| Adamsky | Bolt |
| Walton | Nut |
| Adamsky | Nail |

R_2

| <u>Sname</u> | <u>Proj_name</u> |
|--------------|------------------|
| Smith | ProjX |
| Smith | ProjY |
| Adamsky | ProjY |
| Walton | ProjZ |
| Adamsky | ProjX |

R_3

| <u>Part_name</u> | <u>Proj_name</u> |
|------------------|------------------|
| Bolt | ProjX |
| Nut | ProjY |
| Bolt | ProjY |
| Nut | ProjZ |
| Nail | ProjX |

Fifth Normal Form – 5NF

Fifth Normal Form:

Relvar R is in 5NF – also called **projection-join** normal form – if and only if every non-trivial join dependency that is satisfied by R is implied by the candidate key(s) of R, where

- a) the JD * {A, B, ..., Z} on R is **trivial** if and only if at least one of A, B, ..., Z is the set of all attributes of R.
- b) the JD * {A, B, ..., Z} on R is **implied by the candidate key(s)** of R if and only if each of A, B, ..., Z is a superkey for R.

References

- *Chapter 11: Functional Dependencies*
An introduction to database systems, *CJ. Date*

