

Tutorial T0

Partha Pratir Das

Tutorial Reca

Outline

Jpdate UD'

Fraction UDT friend Operato

Template
Mixed Format

Int<N> UD7

Wraparound Binary Ops

Mixed UDT App
Fraction <int:
Fraction
<Int<4>>
Poly<Int<4>>

.

Tutorial Summan

Programming in Modern C++

Tutorial T09: How to design a UDT like built-in types?: Part 3: Updates and Mixes of UDTs

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All url's in this module have been accessed in September, 2021 and found to be functional



Tutorial Recap

Tutorial TC

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Tutorial Recap

Outline

lpdate UD

friend Operation

Wraparound

Fraction <int Fraction <Int<4>> Poly<Int<4>> Poly <Fraction

Caveat

- Presented the design, implementation and test for Int<N> and Poly<T> types
- Showed how Poly<int> as well as Poly<Fraction> works
- Outlined several practice UDTs for homework

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Tutorial Objectives

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Objective & Outline

Update UE

Fraction UDT friend Operato Template

Mixed Format

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Ripary Opr

Fraction <int
Fraction
<Int<4>>
Poly<Int<4>>
Poly <Fractic
<Int<N>>
>

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• To update UDTs: Fraction, Int<N> and Poly<T>

• To test mix of UDTs





Tutorial Outline

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Objective &

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Fraction UDT friend Operator Template

Int<N> UDT

Wraparound

Fraction <int: Fraction <Int<4> > Poly<Int<4> > Poly <Fraction

Cavea

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 Programming in Modern C++



Update UDTs

Update UDTs



Update UDTs



Update UDTs

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Update UDTs

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Mixed UDT Apps
Fraction <int>
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Poly<Int<4> >
Poly <Fraction
<Int<N> >

Tutorial Summa

• Fraction

- Change binary arithmetic and comparison operators to <u>friend</u> functions from non-static member functions
- Parameterize Fraction with type T = int
- Provide mixed format support

• Int<N>

- In the constructor of Int<N>, allow out-of-range values to wrap around instead of assert
- o Implement operator*(), operator/(), and operator%()

Mixed UDT Apps

- o Test Fraction<int>
- o Test Fraction<Int<4> >
- o Test Poly<Int<4> >
- o Test Polv<Fraction<Int<4> > >



Fraction UDT: Update

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Fraction UDT: Update: Agenda

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Fraction UDT

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Mixed UDT App Fraction <int Fraction <Int<4>>

Caveat

Tutorial Summary

- We have the following update agenda for Fraction
 - Change binary arithmetic and comparison operators to <u>friend</u> functions from non-static member functions
 - Parameterize Fraction with type T = int
 - Provide mixed format support



Fraction: friend Operators

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Mixed UDT App:
Fraction <int:
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Poly<Int<4> >
Poly <Fraction
<Int<N> > >

Tutorial Summa

```
    To facilitate the power of friend operators, we make the constructor non-explicit
    /* explicit */ Fraction(int n = 1, int d = 1): // Three overloads
        n_(d < 0 ? -n : n), d_(d < 0 ? -d : d) // d_ cannot be -ve
    { *(*this); } // Reduces the fraction by operator*()</li>
```

Binary Arithmetic Operations: Add, Subtract, Multiply, Divide, and Modulus friend Fraction operator+(const Fraction&, const Fraction&); // Add() friend Fraction operator-(const Fraction&, const Fraction&); // Subtract() friend Fraction operator*(const Fraction&, const Fraction&); // Multiply() friend Fraction operator/(const Fraction&, const Fraction&); // Divide() friend Fraction operator/(const Fraction&, const Fraction&); // Residue()

```
• Binary Relational Operations: Less, LessEq, More, MoreEq, Eq, NotEq friend bool operator==(const Fraction& f1, const Fraction& f2); // Eq() friend bool operator!=(const Fraction& f1, const Fraction& f2); // NotEq() friend bool operator<(const Fraction& f1, const Fraction& f2); // Less() friend bool operator<=(const Fraction& f1, const Fraction& f2); // LessEq() friend bool operator>(const Fraction& f1, const Fraction& f2); // More() friend bool operator>=(const Fraction& f1, const Fraction& f2); // MoreEq()
```



Fraction: Template

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Poly <Fraction
<Int<N>>
Poly <Fraction

Tutorial Summary

- To provide an underlying type for Fraction, we introduce type variable T with int as default
- T could be any integral type like int, short, char, long, or Int<N> etc.
- We also change the name of the type from Fraction to Fraction not to clutter the user name space

In the application, add:

typedef Fraction_<int> Fraction; // Fraction is used in the application



Fraction: Template

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```
template<typename T = int> class Fraction_ { public: // Parameterized Fraction_ with T = int
                  Fraction_(T n = 1, T d = 1); Fraction_(const Fraction_& f);
                                                                                         // Ctor. C-Ctor. C=. Dtor
                   "Fraction_(); Fraction_& operator=(const Fraction_& f);
                  friend ostream& operator << (ostream& os. const Fraction & f):
                                                                                         // Streaming ops
                  friend istream& operator>>(istream& is, Fraction & f);
                  Fraction operator-() const: Fraction operator+() const:
                                                                                         // Unary arithmetic ops
                  Fraction & operator++(): Fraction operator++(int):
                  Fraction_& operator--(); Fraction_ operator--(int);
                  friend Fraction operator+(const Fraction & f1. const Fraction & f2): // Binary arithmetic ops
                  friend Fraction operator-(const Fraction & f1, const Fraction & f2):
                  friend Fraction operator*(const Fraction & f1, const Fraction & f2);
                  friend Fraction_ operator/(const Fraction_& f1, const Fraction_& f2);
Template
                  friend Fraction operator% (const Fraction & f1. const Fraction & f2);
                  friend bool operator == (const Fraction & f1, const Fraction & f2);
                                                                                         // Comparison ops
                  friend bool operator!=(const Fraction & f1, const Fraction & f2):
                  friend bool operator (const Fraction & f1, const Fraction & f2);
                  friend bool operator <= (const Fraction & f1. const Fraction & f2):
                  friend bool operator>(const Fraction_& f1, const Fraction_& f2);
                  friend bool operator>=(const Fraction_& f1, const Fraction_& f2);
                  Fraction_& operator+=(const Fraction_& f);
                                                                                         // Advanced assignment ops
                  Fraction & operator == (const Fraction_& f); Fraction_& operator == (const Fraction_& f);
                  Fraction_& operator/=(const Fraction_& f); Fraction_& operator%=(const Fraction_& f);
                  Fraction_ operator!() const; operator double() const;
                                                                                         // Special ops
              private: static T gcd(T a, T b); static T lcm(T a, T b); Fraction_& operator*(); // Support functions
```

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Fraction: Mixed Format Support

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Poly <Fraction
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Tutorial Summar

• Irrespective of whether a fraction is in *simple format* like $\frac{n}{d}$ ($\frac{2}{3}$ or $\frac{17}{5}$) or in *mixed format* like $w\frac{n}{d}$ ($\frac{2}{3}$ or $3\frac{2}{5}$), its *internal representation is always simple* $w\frac{n}{d} \equiv \frac{w*d+n}{d}$

Hence, mixed format support is limited to:

Fraction construction

```
explicit Fraction_(T w, T n, T d) : // Mixed format fraction constructor n_{(d < 0? w * -d - n : w * d + n), d_{(d < 0? -d : d)} // d must by non-negative { *(*this); } // Reduces the fraction
```

Fraction output operator
 friend ostream& operator<<(ostream& os, const Fraction_& f);

Fraction input operator
 friend istream& operator>>(istream& is, Fraction_& f);

While the constructor can be distinguished by the distinct signature, the streaming operators
have the same signature for simple as well as mixed format. Hence, we need a way to tell these
operators about the format



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Tutorial Summar

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• To design for the mixed format i/o, we recall the support for writing integers in multiple bases using <iomanip> component in standard library

```
#include <iostream>
#include <iomanip>
int main() { int i = 76;
    std::cout << std::oct << i << std::endl; // Set octal format. Prints 114
    std::cout << std::hex << i << std::endl; // Set hexadecimal format. Prints 4c
    std::cout << std::dec << i << std::endl; // Set decimal format. Prints 76
}</pre>
```

- Using <iomanip>, the format flag is set in ostream (cout). We cannot do that as ostream (or istream) cannot be changed. So, we need to keep the format option in the Fraction_ class
- We add a static bool bMixedFormat_ (true for mixed format, false for simple format)
- In the streaming operators, we can check this flag and adopt the appropriate formatting
- But how do we set / reset this flag? Using SetFormat(bool) spoils the built-in type-like syntax
 Easy
 Desired

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```
Fraction f(17,5);
Fraction::SetFormat(false);
cout << f; // 17/5
Fraction::SetFormat(true);
cout << f; // 3+2/5</pre>
Fraction f(17,5);
cout << Fraction::simple;
cout << f; // 17/5
cout << f; // 17/5
cout << Fraction::mixed;
cout << f; // 3+2/5</pre>
```



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Tutorial Recap

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Tutorial Summa

```
    For cout << Fraction::simple (cout << Fraction::mixed), we observe the following:</li>
    Fraction::simple (Fraction::mixed) needs to have an appropriate type, say Format, different
```

O Fraction::simple (Fraction::mixed) needs to have an appropriate type, say Format, different from Fraction_, yet encapsulated by Fraction_. So we choose nested class Format in Fraction_ class Format { bool bFormat_; public: Format(bool b): bFormat_(b) { } /* ... */ }; // Wraps bool

```
O Fraction::simple and Fraction::mixed must be constants in Fraction_
static const Format mixed; // bMixedFormat_ = true
static const Format simple; // bMixedFormat_ = false
```

Output streaming Fraction::simple (Fraction::mixed) in Fraction::Format should print nothing and set Fraction::bMixedFormat_appropriately friend ostream& operator<<(ostream& os, const Format& m) { // writes nothing // sets / resets mixed format flag bMixedFormat_ = m.bFormat_; // error: operator<< is friend of Format, not of Fraction_return os; }
 So we use a wrapper in Format

```
void SetMixedFormat(bool b) const { bMixedFormat_ = b; } // access private member of Fraction_
friend ostream& operator<<(ostream& os, const Format& m) { // writes nothing
    m.SetMixedFormat(m.bFormat_); // sets / resets mixed format flag
    return os;</pre>
```

class Format { // ...



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Poly <Fraction
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Caveat

Futorial Summar

• We use Fraction_::bMixedFormat_ to decide the format in the streaming operators:

```
friend ostream& operator << (ostream& os. const Fraction & f) {
       T w = 0, n = f.n_{-}, d = f.d_{-};
       if (f.bMixedFormat_) { // Mixed format support
           w = n / d: // Whole part = 3 in 17/5
                             // Fraction part = 2/5 in 17/5
           n %= d:
           if (n < 0) \{ -w; n += d; \} // Negative: -17/5 = -4+3/5 = (-17/5 -1)+(-17%5+5)/5
           if (w) os << w << "+": // w+ to be suppressed if 0
       os << n; if ((n != 0) && (d != 1)) os << "/" << d; // To print the fraction part in both formats
       return os:
   friend istream& operator>>(istream& is, Fraction & f) {
       if (f.bMixedFormat ) { // Mixed format support - reads 3 numbers: w. n. d
           cout << "Input fraction in mixed Format" << endl;</pre>
           Tw.n:
           is \gg w \gg n \gg f.d :
           f.n_{-} = w * f.d_{-} + n:
       else // Simple format support - reads 2 numbers: n, d
           is >> f.n_ >> f.d_:
       *f; // Reduces the fraction
       return is:
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                                                                                                     T09 15
```



Mixed Format

• Finally, we put together Fraction_::Format class:

```
template<typename T = int> class Fraction_ { public: // ...
  private: /* ... */ // Support for Mixed Format
      class Format { private: // Wraps bool so that special IO operators can be defined
          bool bFormat_: // Truthvalue for Format object
          void SetMixedFormat(bool b) const; // Sets Fraction_::bMixedFormat_
          Format(bool b): bFormat (b) { } // Ctor is private - used only by friend class Fraction
          friend ostream& operator << (ostream& os. const Format& m): // Called to set bMixedFormat
          friend istream& operator>>(istream& is, const Format& m); // Called to set bMixedFormat_
          friend class Fraction; // Since ctor of Format is private, Fraction must be a friend
      };
  public:
      // Format markers
      static const Format mixed: // Denotes bMixedFormat = true
      static const Format simple: // Denotes bMixedFormat = false

    Instantiations of Format markers are:
```

```
const Fraction::Format Fraction::mixed(true);  // Denotes bMixedFormat_ = true
   const Fraction::Format Fraction::simple(false): // Denotes bMixedFormat = false
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```



Int<N> UDT: Update

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Fraction
<Int<4>>

<Int<4>>
Poly<Int<4>>

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Int<N> UDT: Update: Agenda

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Mixed UDT App Fraction <int Fraction <Int<4>> Poly<Int<4>> Poly <Fractio

Caveat

We have the following update agenda for Int<N>

- In the constructor of Int<N>, allow out-of-range values to wrap around instead of assert
- o Implement operator*(), operator/(), and operator%()



Int<N>: Constructor with Wraparound

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Fraction <int>
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Poly <Fraction
<Int<N>>>

Caveat

Futorial Summary

For wraparound, we remove asserts and overload operator*()
template<typename T = int, unsigned int N = 4>
class Int_ { public: // ...
 explicit Int_<T, N>(int v = 1): v_(v) // Two overloads of Constructor
 { *(*this); }
 Int_<T, N> operator*() { // Wraparound operator
 v_ = v_ % TwoPowerN_T;
 if (v_ > MaxInt_T) v_ -= TwoPowerN_T;
 else if (v_ < MinInt_T) v_ += TwoPowerN_T;
 return *this;
 } // ...
}</pre>

• With this we get the following wraparound:

```
cout << Int_<>(5) << ' ' << Int_<>(77) << ' ' << Int_<>(-43) << endl; // 5 -3 5
```



Int<N>: Binary Operators

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VIXED UD1 Apps
Fraction
<Int<4> >
Poly<Int<4> >
Poly <Fraction
<Int<1> >

Tutorial Summa

```
• With the wraparound, it becomes straightforward to implement binary operators with overflow
   template<typename T = int, unsigned int N = 4>class Int { public: // ...
       friend Int_<T, N> operator+(const Int_<T, N>& i1, const Int_<T, N>& i2) {
            return Int <T, N>(i1.v + i2.v ); }
       friend Int <T. N> operator-(const Int <T. N>& i1. const Int <T. N>& i2) {
            return i1 + (-i2); } // return Int_<T, N>(i1.v_ - i2.v_); is also okay
       friend Int <T. N> operator*(const Int <T. N>& i1. const Int <T. N>& i2) {
            return Int_<T, N>(i1.v_ * i2.v_);}
       friend Int_<T, N> operator/(const Int <T, N>& i1, const Int_<T, N>& i2) {
            return Int <T. N>(i1.v / i2.v ); }
       friend Int_<T, N> operator%(const Int_<T, N>& i1, const Int_<T, N>& i2) {
           return Int_<T, N>(i1.v_ % i2.v_); } // ...
   };
• With this we get the following:
   cout << "Binary Plus: Int(2) + Int(3) = " << (Int(2) + Int(3)) << endl;
                                                                                       // 5
   cout << "Binary Plus: Int(-6) + Int(-7) = " << (Int(-6) + Int(-7)) << endl:
                                                                                       // 3
   cout \lt\lt "Binary Minus: Int(2) - Int(3) = " \lt\lt (Int(2) - Int(3)) \lt\lt end1:
                                                                                      // -1
   cout \leq "Binary Minus: Int(-6) - Int(-7) = " \leq (Int(-6) - Int(-7)) \leq end1:
                                                                                      // 1
   cout << "Binary Multiply: Int(3) * Int(2) = " << (Int(3) * Int(2)) << endl:</pre>
                                                                                      // 6
   cout << "Binary Multiply: Int(7) * Int(5) = " << (Int(7) * Int(5)) << endl:
                                                                                       // 3
   cout \leq "Binary Multiply: Int(-8) * Int(-8) = " \leq (Int(-8) * Int(-8)) \leq endl: // 0
   cout \leq "Binary Divide: Int(3) / Int(2) = " \leq (Int(3) / Int(2)) \leq end1:
                                                                                       // 1
   cout << "Binary Divide: Int(7) / Int(-5) = " << (Int(7) / Int(-5)) << endl:
                                                                                       // -1
   cout << "Binary Residue: Int(3) % Int(2) = " << (Int(3) % Int(2)) << endl:
                                                                                       // 1
cout << "Binary Residue: Int(-6) % Int(2) = " << (Int(-6) % Int(2)) << endl;
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                                                                                       // 0
```



Int<N>: Binary Operators: Properties

Binary Ops

 Try to prove the usual arithmetic properties of the Int<N> binary operators for addition, subtraction, multiplication, and division under wraparound:

• Are all operators *Associative*? For example,

$$\triangleright$$
 a + b + c = (a + b) + c = a + (b + c)

• Are addition and multiplication *Commutative*? For example,

$$\triangleright$$
 a + b = b + a

Do multiplication and division Distribute over addition and subtraction? For example,

$$\triangleright$$
 a * (b + c) = a * b + a * c

• Especially, check for the boundary conditions under wraparound:

 Consider exception and / or assert support in the constructors and / or operators if some specific values can break the properties



Mixed UDT Apps

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Mixed UDT Apps: Agenda

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Poly <Fraction

Caveat

We have the following agenda for Mixed UDT Apps

- o Test Fraction<int>
- o Test Fraction<Int<4> >
- Test Poly<int>: Done in Tutorial 08
- Test Poly<Fraction<int > >: Done in Tutorial 08 actually using the non-template version of Fraction
- o Test Poly<Int<4> >
- o Test Poly<Fraction<Int<4>>>



Fraction<int>: Application

Fraction fb(7, 9) = 7/9 = 7/9 fa + fb = 2+4/9 = 22/9 fa - fb = 8/9 = 8/9 fa * fb = 1+8/27 = 35/27 fa / fb = 2+1/7 = 15/7 Programming in Modern C++

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Poly <Fraction

Caveat

utorial Summar

```
#include <iostream>
using namespace std:
#include "Frac.h"
typedef Fraction <int> Fraction:
const Fraction Fraction::UNITY = Fraction(1). Fraction::ZERO = Fraction(0):
bool Fraction::bMixedFormat = false:
const Fraction::Format Fraction::mixed(true). Fraction::simple(false):
int main() {
   Fraction fa(5, 3):
    cout << "Fraction fa(5, 3) = " << Fraction::mixed << fa << " = " << Fraction::simple << fa:
   Fraction fb(7, 9);
    cout << "Fraction fb(7, 9) = " << Fraction::mixed << fb << " = " << Fraction::simple << fb:
    cout << "fa + fb = " << Fraction::mixed << (fa + fb) << " = " << Fraction::simple << (fa + fb);
    cout << "fa - fb = " << Fraction::mixed << (fa - fb) << " = " << Fraction::simple << (fa - fb);
    cout << "fa * fb = " << Fraction::mixed << (fa * fb) << " = " << Fraction::simple << (fa * fb):
    cout << "fa / fb = " << Fraction::mixed << (fa / fb) << " = " << Fraction::simple << (fa / fb):
Fraction fa(5, 3) = 1+2/3 = 5/3
```



Fraction<Int<4> >: Application

<Int<4> >

```
#include <iostream>
using namespace std:
#include "Frac.h"
#include "../Int/Int.h"
typedef Int <int. 4> Int: typedef Fraction <Int> Fraction:
const Fraction Fraction::UNITY = Fraction(1). Fraction::ZERO = Fraction(0):
bool Fraction::bMixedFormat = false:
const Fraction::Format Fraction::mixed(true). Fraction::simple(false):
int main() {
   Fraction fa(5, 3):
    cout << "Fraction fa(5, 3) = " << Fraction::mixed << fa << " = " << Fraction::simple << fa:
   Fraction fb(7, 10);
    cout << "Fraction fb(7, 10) = " << Fraction::mixed << fb << " = " << Fraction::simple << fb:
    cout << "fa + fb = " << Fraction::mixed << (fa + fb) << " = " << Fraction::simple << (fa + fb);
    cout << "fa - fb = " << Fraction::mixed << (fa - fb) << " = " << Fraction::simple << (fa - fb);
    cout << "fa * fb = " << Fraction::mixed << (fa * fb) << " = " << Fraction::simple << (fa * fb):
    cout << "fa / fb = " << Fraction::mixed << (fa / fb) << " = " << Fraction::simple << (fa / fb):
Fraction fa(5, 3) = 1+2/3 = 5/3
Fraction fb(7, 10) = -2+5/6 = -7/6
fa + fb = 1/2 = 1/2
fa - fb = 1/6 = 1/6
fa * fb = -2+1/2 = -3/2
fa / fb = 2/5 = 2/5
Programming in Modern C++
```



Poly<Int<4> >: Application

```
#include <iostream>
              using namespace std;
              #include "../Int/Int.h"
              #include "Polv.h"
              typedef Int <int. 4> Int:
              const int Int::MaxInt_T = (1 << (N-1))-1; /* 2^{(N-1)}-1 */ Int::MinInt_T = -(1 << (N-1)); // -2^{(N-1)}
              const Int Int::MaxInt = Int(Int::pow() - 1). Int::MinInt = Int(-Int::pow()):
              void main() { vector\langle Int \rangle vf = { 2, 15, 7 }:
                  Polv < Int > pf1(vf) : cout << "pf1(x): " << pf1 << " pf1(2) = " << pf1(2) << end1:
                  Poly<Int> pf2; cout << "pf2(x): " << pf2 << " pf2(2) = " << pf2(2) << end1;
                  cin >> pf2; /* 3 9 7 2 -11 */ cout << "pf2(x): " << pf2 << " pf2(2) = " << pf2(2) << endl;
                  Poly(Int) pf3 = pf1 + pf2: cout << "pf3(x): " << pf3 << " pf3(2) = " << pf3(2) << end1:
                  Poly<Int> pf4 = pf1 - pf2; cout << "pf4(x): " << pf4 << " pf4(2) = " << pf4(2) << end1 << end1;
              pf1(x): 7x^2 + -1x^1 + 2, pf1(2) = -4 // 2 = 2, 15 = -1, 7 = 7, pf1(2) = 7*4 + -1*2 + 2 = 28-2+2 = 28 = -4
              pf2(x): 1. pf2(2) = 1
              Enter degree of the polynomial 3
              Enter all the coefficients like a0+a1*x+a2*x^2+....an*x^n
Poly<Int<4>>
              9 7 2 -11 // -7 7 2 5
              pf2(x): 5x^3 + 2x^2 + 7x^1 + -7. pf2(2) = 7 // pf2(2) = 5*8 + 2*4 + 7*2 + -7 = 56+8+14-7 = 71 = 71-64 = 7
              pf3(x): 5x^3 + -7x^2 + 6x^1 + -5. pf3(2) = 3
              pf4(x): -5x^3 + 5x^2 + -8x^1 + -7. pf4(2) = 5
              Programming in Modern C++
                                                                   Partha Pratim Das
```

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Poly<Fraction<Int<4>> >: Application

```
#include <iostream>
                using namespace std:
                #include "../Fraction/Frac.h"
                #include "../Int/Int.h"
                #include "Polv.h"
                const int N = 4: typedef Int <int. 4> Int: const int Int::TwoPowerN T = 1 << N: // 2^N
                const int Int::MaxInt_T = (1 << (N-1))-1; /* 2^(N-1)-1 */ Int::MinInt_T = -(1 << (N-1)); // -2^(N-1)
                const Int Int::MaxInt = Int(Int::pow() - 1). Int::MinInt = Int(-Int::pow()):
                typedef Fraction <Int> Fraction: bool Fraction::bMixedFormat = false:
                const Fraction Fraction::UNITY = Fraction(1), Fraction::ZERO = Fraction(0);
                const Fraction::Format Fraction::mixed(true). Fraction::simple(false):
                void main() {
                    vector<Fraction> vf1 = { Fraction(1, 2), Fraction(-3, 5), Fraction(2, 4) };
                    Poly<Fraction> pf1(vf1); cout << "pf1(x): "<< pf1 << " pf1(Fraction(2)) = "<< pf1(Fraction(2)) << endl;
                    vector<Fraction> vf2 = { Fraction(1, 2), Fraction(2, 3) };
                    Poly<Fraction> pf2(vf2); cout << "pf2(x): "<< pf2 << "pf2(Fraction(2)) = "<< pf2(Fraction(2))<< endl;
                    Polv < Fraction > pf3 = pf1 + pf2:
                    cout << "pf3(x): " << pf3 << " pf3(Fraction(2)) = " << pf3(Fraction(2)) << endl;</pre>
                    Polv<Fraction> pf4 = pf1 - pf2:
                    cout \lt "pf4(x): " \lt pf4 \lt "pf4(Fraction(2)) = " \lt pf4(Fraction(2)) \lt endl < endl:
                pf1(x): \frac{1}{2}x^2 + \frac{-3}{5}x^1 + \frac{1}{2}. pf1(Fraction(2)) = \frac{7}{6} \frac{1}{2}pf1(\frac{2}{1}) = \frac{1}{2}*4 - \frac{3}{5}*2 + \frac{1}{2} = \frac{7}{6}
Poly <Fraction
<Int<N>>>
                pf2(x): 2/3x^1 + 1/2. pf2(Fraction(2)) = -5/6 // pf2(2/1) = 2/3*2/1 + 1/2 = 4/3 + 1/2 = 11/6 = -5/6
                pf3(x): 1/2x^2 + 1. pf3(Fraction(2)) = 3 // pf4(2/1) = 1/2*4/1 + 1 = 3
                pf4(x): 1/2x^2. pf4(Fraction(2)) = 2 // <math>pf4(2/1) = 1/2*4/1 = 2
                Programming in Modern C++
                                                                         Partha Pratim Das
                                                                                                                          T09 27
```



Caveat: Mixes may fail

Tutorial T

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Tutorial Reca

Objective &

Update UE

Fraction UDT

friend Operato

Template

Mixed Format

Int<N> UDT

Wraparound Binary Ops

Fraction <int: Fraction <Int<4>> Poly<Int<4>>

Poly<Int<4>
Poly <Fracti
<Int<N>>>

Caveat

Tutorial Summar

Caveat: Mixes may fail



Caveat in mixing UDTs

Tutorial T0

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Tutorial Reca

Objective &

Update UD

friend Operato

Int<N> UDT
Wraparound
Binary Ops

Mixed UDT App
Fraction <int
Fraction
<Int<4>>
Poly<Int<4>>
Poly <Fraction
<Int<N>>>

Caveat

utorial Summar

- While Fraction<int>, Poly<int>, Int<N>, or Poly<Fraction<int> > work perfectly fine, Fraction<Int<N> > or Poly<Fraction<Int<N> > > may have some surprise
- This is due to the T gcd(T, T) algorithm in the context of Int<N>. Normally, we invoke gcd() for
 positive numbers only (that's how the Euler's Algorithm is designed to work)
- However, for MinInt in Int<N>, we have -MinInt = MinInt. Hence, if one of the gcd() parameters is
 MinInt we are perpetually in the realm of negative numbers. This leads to an infinite loop in the code
 below:

```
static T gcd(T a, T b) { // Finds the gcd for two +ve integers
   while (a != b) if (a > b) a = a - b; else b = b - a; // N = 4. (-8,3) => (-8,-5) => (-8,3) => ...
   return a;
}
```

• So we choose to throw (and eventually assert in the constructor) when one of the gcd() arguments is negative (eventually MinInt)

```
static T gcd(T a, T b) { // Finds the gcd for two +ve integers
  if (a < 0) throw "Negative first arg in gcd";
  if (b < 0) throw "Negative second arg in gcd";
  while (a != b) if (a > b) a = a - b; else b = b - a; // For N = 4, a = -8 is an infinite loop
  return a;
}
```

How to fix?



Tutorial Summary

Tutorial T0

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Tutorial Reca

Objective &

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Fraction UDT friend Operato

Template Mixed Format

Int<N> UDT
Wraparound

Mixed UDT App Fraction <int Fraction <Int<4> > Poly<Int<4> >

Cave

Tutorial Summary

- UDTs Fraction, Int and Poly have been updated with various features
- Mixed applications involving multiple UDTs have been checked
- Caveat or loophole has been identified