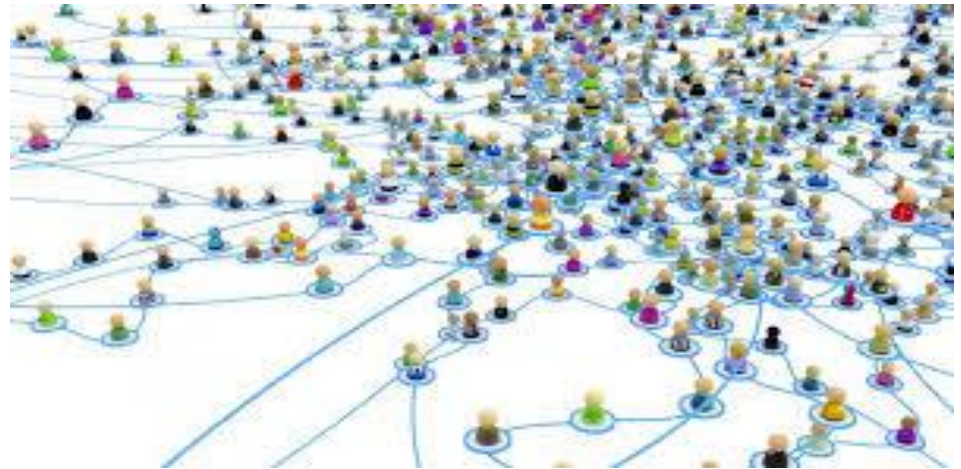


# Social Network Analysis

**NOTATIONS FOR SOCIAL  
NETWORK DATA**



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- Social network data can be represented mathematically in different ways
- Three different notational schemes
- Based on its appropriateness, clarity, or efficiency any one is used
- Graph theoretic
- Sociometric
- Algebraic

## **Graph theoretic notation**

It is most useful for centrality and prestige methods, cohesive subgroup ideas and as dyadic and triadic methods

## **Sociometric notation**

It is often used for the study of structural equivalence and block models.

## **Algebraic notation**

It is most appropriate for role and positional analyses and relational algebras.

$$N = \{n_1, n_2, n_3 \dots n_g\}$$

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## Graph Notations

It is viewed as an elementary way to represent actors and relations

It views is as a graph, consisting of nodes joined by lines  $N = \{n_1, n_2, n_3 \dots n_g\}$

Set N contains g actors

Example:

$$N = \{Alex, George, Alan, Bob, michael, Harris\}$$

Here we infer,  $n_1 = Alex, n_2 = George, n_3 = Alan \dots$

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## Single Relation

Single relation records whether each actor in  $N$  relates to every other actor on this relation

The relation be dichotomous and directional

If a tie is present between pair of actors  $n_i$  and  $n_j$  then the ordered pair belongs to set  $L$

Maximum element in the  $L$  is  $g(g-1)$  and the minimum can be 0

*If the ordered pair  $\langle n_i, n_j \rangle$  has tie between them it is represented by  $n_i \rightarrow n_j$*

*$L = \{l_1, l_2, l_3 \dots l_l\}$ , here each  $l$  represents ordered pairs*

*$L$  can be represented graphically by drawing line from first actor in the element to second actor*

*The graph is called as directed graph and directed lines are called arcs*

*Graph  $g$  consists of set of nodes  $N$  and set of lines  $L$ , mathematically represented as  $(N, L)$*

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*In some relation, individual actor don't relate to itself, here self choices are not considered*

*In non – directional no distinguish between the line  $n_i$  and  $n_j$  and  $n_j$  and  $n_i$*

*Example: set of actors live near each other*

*L contains  $\frac{g(g-1)}{2}$  pairs for undirected graph*

*L can be  $l1 = \langle \text{Ross, Alan} \rangle, l2 = \langle \text{Alex, michael} \rangle, \dots, l8 = \langle \text{Sarah, Drew} \rangle$*

*Here friendship is not reciprocal, so it can be  $n_i \nrightarrow n_j$*

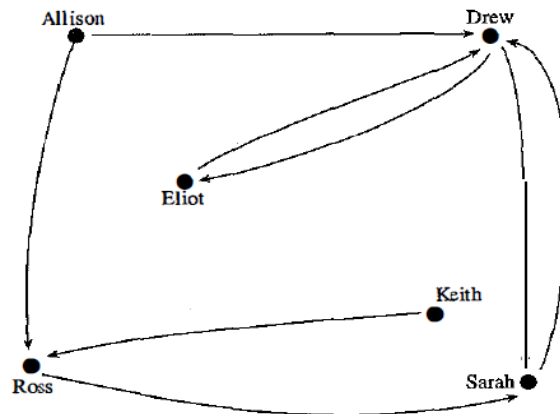
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A graph represented as diagram where, nodes are represented as points in 2D space and arcs are represented by directed arrows between points

Location of points in two-dimensional space is irrelevant

Example:





## Multirelational

Graph theoretic notation can be generalized to multirelational networks

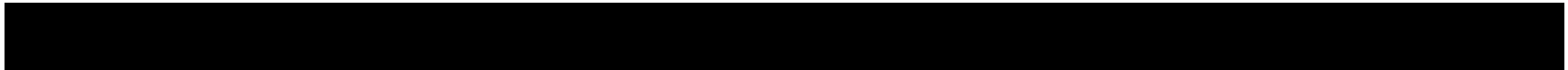
It could include both directional and nondirectional relations

Example:

Between 2 persons, two types of relationship: friendship and marital tie

Each relation has a corresponding set of arcs  $L_r$  in  $\mathbf{L}_r$  which contains ordered pairs of actors as elements

Where  $r$  ranges from 1 to  $R$ , the total number of relations



each relation is defined on the same set of nodes, but each has a different set of arcs  
Example: relation1: friendship, relation2: classmate, relation3: neighborhood

# Social Network Analysis



For each relations, the directed graphs can be viewed in one or more figures

each relation is defined on the same set of nodes, but each has a different set of arcs

Example: relation1: friendship, relation2: classmate, relation3: neighborhood

## Single Relation

single relation measured on one set of factors in

Define  $x_{ij}$  as the value of the tie from the  $i^{\text{th}}$  actor to the  $j^{\text{th}}$  actor on the single relation

Place these measurements into a sociomatrix

Rows and columns of this sociomatrix index the individual actors.

Since there are  $g$  actors, the matrix is of size  $g \times g$

# Social Network Analysis



Sociometric notation uses such matrices to denote measurements on ties

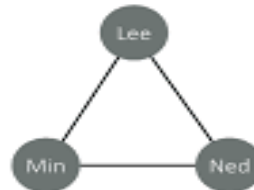
For the relation  $X$ , we define  $\mathbf{X}$  as the associated sociomatrix. The entries are defined as:

$X_{ij}$  = the value of tie from  $n_i$  to  $n_j$  where  $i$  and  $j$  ( $i \neq j$ ) range over all integers from 1 to  $g$   
|  
pairs listing same actor twice ( $n_i, n_i$ ),  $i = 1, 2, \dots, g$  are called self choices

Self choices are usually undefined, lie along diagonal of sociomatrix

Sociomatrix

	Lee	Min	Ned
Lee	0	1	1
Min	1	0	1
Ned	1	1	0



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The possible values of the relation  $C$ , if it is dichotomous  $C=2$  or if relation is valued and discrete can take no. of different values

Example, if the relation can take on the values  $-1, 0, 1$ ,

Then map  $-1$  to  $0$ ,  $0$  to  $1$ , and  $+1$  to  $2$  (so that  $C=3$ )

Single relation is just a special case of the multirelational

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## Multiple relations

Suppose  $R$  relations  $X_1, X_2, X_3, \dots$  measured on a single set of actors where  $r = 1, 2, 3, \dots R$ .

Relations are valued and come from the set  $\{0, 1, 2, \dots, C - 1\}$

$X_{ijr}$  is the strength of the tie from  $i$ th actor to  $j$ th actor on  $r$ th relation

It is placed in the collection of sociomatrices, one for each relation

Example:

<i>Friendship at Beginning of Year</i>						
	Allison	Drew	Eliot	Keith	Ross	Sarah
Allison	-	1	0	0	1	0
Drew	0	-	1	0	0	1
Eliot	0	1	-	0	0	0
Keith	0	0	0	-	1	0
Ross	0	0	0	0	-	1
Sarah	0	1	0	0	0	-

# Social Network Analysis



There are  $R$ ,  $g \times g$  sociomatrices, one for each relation defined for the actors in  $N$

$R$  sociomatrices viewed as the layers in a three-dimensional matrix of size  $g \times g \times R$

The rows index the sending actors, the columns index the receiving actors, and the layers index the relations

Also referred to as a **super sociomatrix** as represents information in a multirelational network.

## Example:

Consider of a collection of  $g = 6$  children and  $R = 3$  relations:

- 1) Friendship at beginning of the school year
- 2) Friendship at end of the school year
- 3) Lives near

# Social Network Analysis



*Friendship at Beginning of Year*

	Allison	Drew	Eliot	Keith	Ross	Sarah
Allison	-	1	0	0	1	0
Drew	0	-	1	0	0	1
Eliot	0	1	-	0	0	0
Keith	0	0	0	-	1	0
Ross	0	0	0	0	-	1
Sarah	0	1	0	0	0	-

*Friendship at End of Year*

	Allison	Drew	Eliot	Keith	Ross	Sarah
Allison	-	1	0	0	1	0
Drew	0	-	1	0	1	1
Eliot	0	0	-	0	1	0
Keith	0	1	0	-	1	0
Ross	0	0	0	1	-	1
Sarah	0	1	0	0	0	-

*Lives Near*

	Allison	Drew	Eliot	Keith	Ross	Sarah
Allison	-	0	0	0	1	1
Drew	0	-	1	0	0	0
Eliot	0	1	-	0	0	0
Keith	0	0	0	-	1	1
Ross	1	0	0	1	-	1
Sarah	1	0	0	1	1	-

$X_{121}$  = the value of tie from  $n_1$  to  $n_2$  on the relation  $X_1$

$X_{211} = 0$ , no friendship between two

|



## Summary

- Social network data can be represented mathematically in 3 notations
  - Graph theoretic
  - Sociometric
  - Algebraic
- Graph theoretic notation used in centrality and prestige methods, subgroups
- Sociometric notation used in structural equivalence and block models
- Algebraic notation used in role and positional analyses and relational algebras