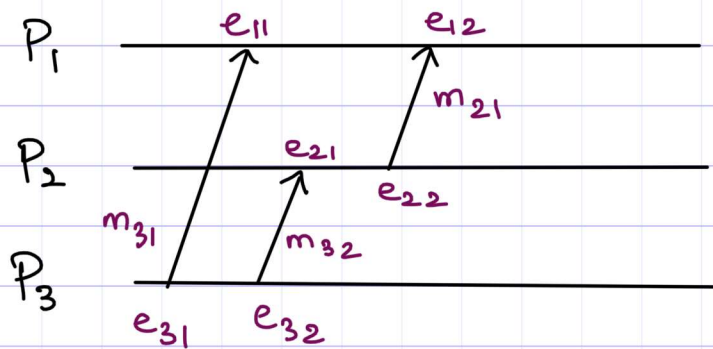


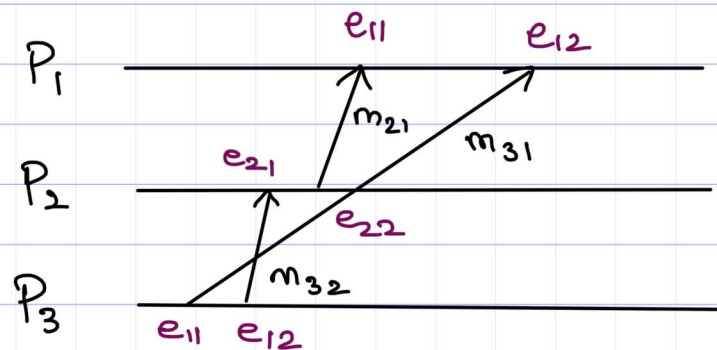
## Causal Ordering of Messages - Non Broadcast



$\text{send}(m_{31}) \rightarrow \text{send}(m_{32})$   
 $\text{send}(m_{32}) \rightarrow \text{rec}(m_{32})$   
 $\text{rec}(m_{32}) \rightarrow \text{send}(m_{21})$   
 $\text{send}(m_{21}) \rightarrow \text{rec}(m_{21})$

Conclusion  $\} \Rightarrow \text{rec}(m_{31}) \rightarrow \text{rec}(m_{21})$

Delivery is causal.

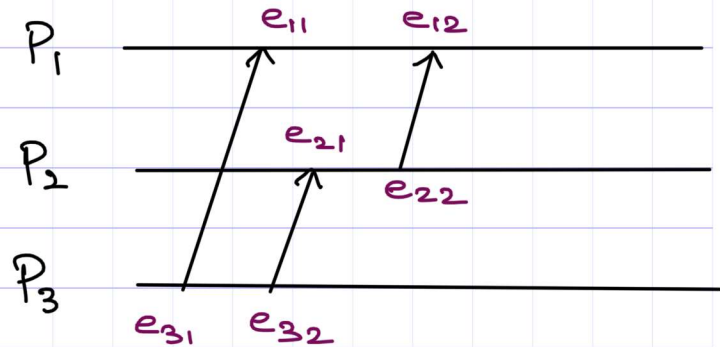


Non-causal delivery.

$m_{21}$  should be delivered after  $m_{31}$ .

# Schipper - Eggli - Sandoz Protocol

$e_{31}$   
 $C(0, 0, 1)$   
 $V_3(x, x, x)$   
 Send  $t, V_3$ .



Update  $V_3$ .  
 $V_3(0, 0, 1, x, x)$

$t$  - timestamp  
 $V_m$  - message vector

$e_{32}$   
 $C(0, 0, 2)$   $V_3(0, 0, 1, x, x)$   
 Send  $t, V_3$ .  
 Update  $V_3$ .  
 $V_3(0, 0, 1, (0, 0, 2), x)$

$e_{11}$   
 $C(0, 0, 0)$   $V_1(x, x, x)$   
 $t(0, 0, 1)$   $V_m(x, x, x)$  } ← received.  
 → Both null.  
 ⇒ nothing has happened yet.

Accept the message.

$V_1(x, x, (0, 0, 1))$

copied here ✓  
 because message received  
 from  $P_3$ .

Merge the vectors  
 & copy the  
 timestamp to the  
 vector.

$C(0, 0, 1)$

e<sub>21</sub>

$C(0,0,0)$      $V_2(x, \textcircled{x}, x)$   
 $t(0,0,2)$      $V_m((0,0,1), \textcircled{x}, x)$

no conflict

$V_2((0,0,1), x, (0,0,2))$      $C(0,0,2)$

e<sub>22</sub>

$C(0,1,2)$      $V_2((0,0,1), x, (0,0,2))$

Send  $C, V_2$ .

Update  $V_2$ .

$V_2((0,1,2), x, (0,0,2))$

e<sub>12</sub>

$C(0,0,1)$      $V_1(x, x, (0,0,1))$   
 $t(0,1,2)$      $V_m((0,0,1), x, (0,0,2))$

---

$e_{31}$

Send event

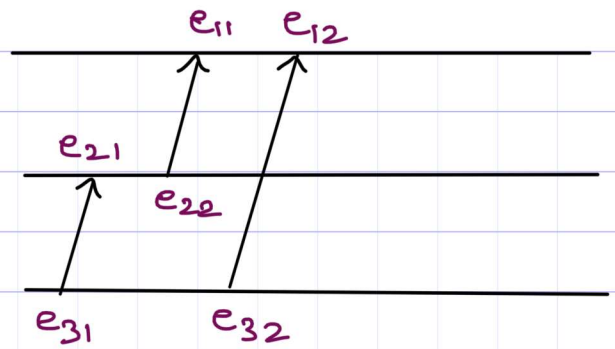
$C_3(0, 0, 1)$

$V_3(x, x, x)$

$P_1$

$P_2$

$P_3$



Send  $C_3, V_3$ .

Update  $V_3$ .

$V_3(x, (0, 0, 1), x)$ .

$e_{32}$

Send event

$C_3(0, 0, 2)$

$V_3(x, (0, 0, 1), x)$

Send  $C_3, V_3$ .

Update  $V_3$ .

$V_3((0, 0, 2), (0, 0, 1), x)$ .

$e_{21}$

$C_2(0, 0, 0)$

$V_2(0, 0, 0)$

Receive

$C_m(0, 0, 1)$  &

$V_m(x, x, x)$ .

⇒ First msg.  
from sender.

Accept the message.

Update  $V_2$ .

$V_2(x, x, (0, 0, 1))$

Merge Clock Values.

$C_2(0, 0, 1)$

e<sub>22</sub>

Send event

$C_2(0, 1, 1)$

$V_2(x, x, (0, 0, 1))$

Send  $C_2$  &  $V_2$ .

Update  $V_2$ .

$V_2((0, 1, 1), x, (0, 0, 1))$

e<sub>11</sub>

$C_1(0, 0, 0)$

$V_1(\textcircled{x}, x, x)$

Receive

$C_m(0, 1, 1)$

$V_m(\textcircled{x}, x, (0, 0, 1))$

no conflict.

Accept the message.

Update  $C_1$ .

$C_1(0, 1, 1)$

Update  $V_1$ .

$V_1(x, \underbrace{(0, 1, 1)}, \underbrace{(0, 0, 1)})$

↓  
timestamp copied to  
sender's location.  
+ merged  $V_m$  &  $V_1$ .

now  $P_1$  is aware  
that  $P_3$  has sent a msg. to  $P_2$ .

$e_{12}$

$C_1 (0, 1, 1)$

$V_1 (\textcircled{x}, (0, 1, 1), (0, 0, 1))$

Receive

$C_m (0, 0, 2)$

$V_m (\textcircled{x}, (0, 0, 1), x)$

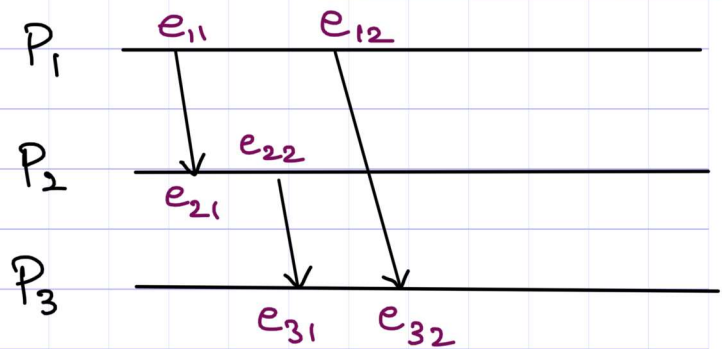
no conflict

Accept the message.

Update/merge  $C_1$  &  $V_1$ .

$V_1 (x, (0, 1, 1), (0, 0, 2))$

$C_1 (0, 1, 2)$



Try.



## Example

$e_{31}$

$C_3 [0 \ 0 \ 0]$   
 $V_3 [x \ x \ x]$

send  $C_3 [0 \ 0 \ 1]$  ;  $V_3 [x \ x \ x]$  to  $e_{12}$ .  
 update  $C_3 [0 \ 0 \ 1]$  ;  $V_3 [(0 \ 0 \ 1) \ x \ x]$

$e_{32}$

$C_3 [0 \ 0 \ 1]$   
 $V_3 [(0 \ 0 \ 1) \ x \ x]$

send  $C_3 [0 \ 0 \ 2]$  ;  $V_3 [(0 \ 0 \ 1) \ x \ x]$  to  $e_{21}$ .  
 update  $C_3 [0 \ 0 \ 2]$  ;  $V_3 [(0 \ 0 \ 1) (0 \ 0 \ 2) \ x]$

$e_{21}$

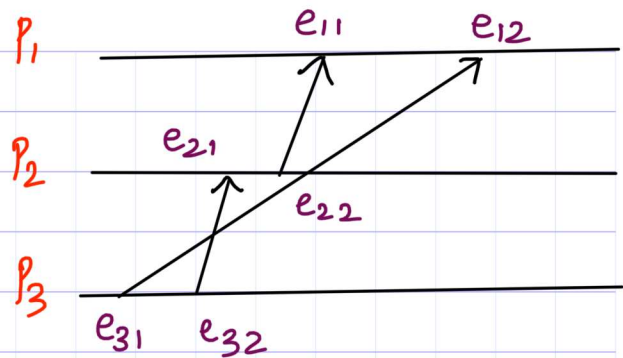
$C_2 [0 \ 0 \ 0]$      $V_2 [x \ x \ x]$   
 rec  $[0 \ 0 \ 2]$  ;  $V_m [(0 \ 0 \ 1) \ x \ x]$   
 update  $C_2 [0 \ 0 \ 2]$  ;  $V_2 [(0 \ 0 \ 1) (0 \ 0 \ 2) \ x]$

$e_{22}$

$C_2 [0 \ 0 \ 2]$  ;  $V_2 [(0 \ 0 \ 1) (0 \ 0 \ 2) \ x]$   
 send  $C_2 [0 \ 1 \ 2]$  ;  $V_2 [(0 \ 0 \ 1) (0 \ 0 \ 2) \ x]$   
 update  $C_2 [0 \ 1 \ 2]$  ;  $V_2 [(0 \ 1 \ 2) (0 \ 0 \ 2) \ x]$

$e_{11}$

$C_1 [0 \ 0 \ 0]$      $V_1 [x \ x \ x]$   
 rec  $C_1 [0 \ 1 \ 2]$      $V_m [(0 \ 0 \ 1) (0 \ 0 \ 2) \ x]$   
 send  $C_1 [0 \ 1 \ 2]$      $V_m [(0 \ 0 \ 1) (0 \ 0 \ 2) \ x]$   
                                  to buffer.



e<sub>12</sub>

C<sub>1</sub> [0 0 0] V<sub>1</sub> [x x x]

recw. [0 0 1] V<sub>m</sub> [x x x]

update C<sub>1</sub> [0 0 1] V<sub>1</sub> [(0 0 1) x x]

since clock C<sub>1</sub> is updated, check buffer.

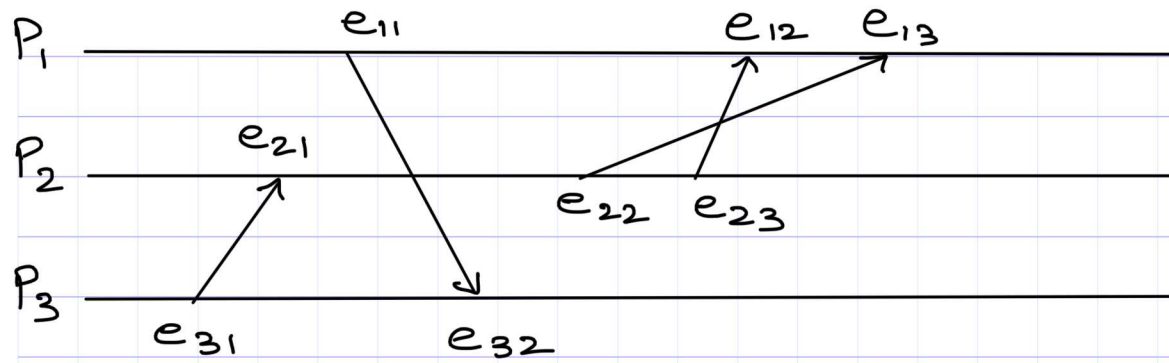
e<sub>11</sub>'

C<sub>1</sub> [0 0 1] V<sub>1</sub> [(0 0 1) x x]

recw. [0 1 2] V<sub>m</sub> [(0 0 1) (0 0 2) x]

update C<sub>1</sub> [0 1 2] V<sub>1</sub> [(0 0 1) (0 0 2) x]





e31 (send)

$C_3[0, 0, 0]$        $V_3[x, x, x]$

$C_3[0, 0, 1]$        $V_3[x, x, x]$

send to e21

$V_3[x, [0, 0, 1], x]$

e21 (receive)

$C_2[0, 0, 0]$        $V_2[x, \textcircled{x}, x]$

→  $C_m[0, 0, 1]$        $V_m[x, \textcircled{x}, x]$

unset

Accept delivery.

$C_2[0, 0, 1]$        $C_2[x, [0, 0, 1], x]$

e11 (send)

$C_1[0, 0, 0]$        $V_1[x, x, x]$

$C_1[1, 0, 0]$        $V_1[x, x, x]$

send to e32

$V_1[x, x, [1, 0, 0]]$

e<sub>32</sub> (receive)

$C_3 [0, 0, 1]$   $V_3 [x, [0, 0, 1], \textcircled{x}]$   
 $C_m [1, 0, 0]$   $V_m [x, x, \textcircled{x}]$   
unset

Accept delivery

$C_3 [1, 0, 1]$   
 $V_3 [x, [0, 0, 1], [1, 0, 0]]$

e<sub>22</sub> (send)

$C_2 [0, 0, 1]$   $V_2 [x, [0, 0, 1], x]$   
 $C_2 [0, 1, 1]$   $V_2 [x, [0, 0, 1], x]$   
send to e<sub>13</sub>

$V_2 [[0, 1, 1], [0, 0, 1], x]$

e<sub>23</sub> (send)

$C_2 [0, 2, 1]$   $V_2 [[0, 1, 1], [0, 0, 1], x]$   
send to e<sub>12</sub>

$V_2 [[0, 2, 1], [0, 0, 1], x]$

e<sub>12</sub> (receive)

$C_1 [1, 0, 0]$   $V_1 [\textcircled{x}, x, [1, 0, 0]]$   
 $C_m [0, 2, 1]$   $V_m [\textcircled{[0, 1, 1]}, [0, 0, 1], x]$

buffer it.

e<sub>13</sub> (receive)

$C_1 [1, 0, 0]$   $V_1 [\textcircled{x}, x, [1, 0, 0]]$   
 $C_m [0, 1, 1]$   $V_m [\textcircled{x}, [0, 0, 1], x]$   
accept delivery

$C_1 [1, 1, 1]$   $V_1 [[0, 1, 1], x, [1, 0, 0]]$

$e_{12}'$  (redelivery)

$C_1 [1, 1, 1]$	$V_1 [0, 1, 1],$	$x$	$[1, 0, 0]$
$C_m [0, 2, 1]$	$V_m [0, 1, 1],$	$x$	$[x]$

accept delivery

$C_1 [1, 2, 1] \quad V_1 [0, 2, 1], \quad x, [1, 0, 0]$