```
> with(combinat);
 [Chi, bell, binomial, cartprod, character, choose, composition, conjpart, decodepart,
                                                                                                                                                                                                                                                                                                                          (1)
              encodepart, eulerian1, eulerian2, fibonacci, firstcomb, firstpart, firstperm, graycode,
              inttovec, lastcomb, lastpart, lastperm, multinomial, nextcomb, nextpart, nextperm,
              numbcomb, numbcomp, numbpart, numbperm, partition, permute, powerset, prevcomb,
             prevpart, prevperm, randcomb, randpart, randperm, rankcomb, rankperm, setpartition,
              stirling1, stirling2, subsets, unrankcomb, unrankperm, vectoint]
> ?permute;
> permute(4);
[[1, 2, 3, 4], [1, 2, 4, 3], [1, 3, 2, 4], [1, 3, 4, 2], [1, 4, 2, 3], [1, 4, 3, 2], [2, 1, 3, 4], [2, 1, 4, 4], [2, 1, 4, 4], [2, 1, 4, 4], [2, 1, 4, 4], [2, 1, 4, 4], [2, 1, 4, 4], [2, 1, 4, 4], [2, 1, 4, 4], [2, 1, 4, 4], [2, 1, 4, 4], [2, 1, 4, 4], [2, 1, 4, 4], [2, 1, 4, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2, 1, 4], [2,
                                                                                                                                                                                                                                                                                                                         (2)
              3], [2, 3, 1, 4], [2, 3, 4, 1], [2, 4, 1, 3], [2, 4, 3, 1], [3, 1, 2, 4], [3, 1, 4, 2], [3, 2, 1, 4],
              [1, 2], [4, 3, 2, 1]
> numbperm(4, 4);
                                                                                                                                                   24
                                                                                                                                                                                                                                                                                                                          (3)
> permute(5, 2);
[[1, 2], [1, 3], [1, 4], [1, 5], [2, 1], [2, 3], [2, 4], [2, 5], [3, 1], [3, 2], [3, 4], [3, 5], [4, 1],
                                                                                                                                                                                                                                                                                                                          (4)
              [4, 2], [4, 3], [4, 5], [5, 1], [5, 2], [5, 3], [5, 4]]
> numbperm(5, 2);
                                                                                                                                                   20
                                                                                                                                                                                                                                                                                                                          (5)
\rightarrow permute([a, a, c, d], 3);
 [a, a, c], [a, a, d], [a, c, a], [a, c, d], [a, d, a], [a, d, c], [c, a, a], [c, a, d], [c, d, a], [d, a], [
                                                                                                                                                                                                                                                                                                                          (6)
              a], [d, a, c], [d, c, a]]
> numbperm([a, a, c, d], 3);
                                                                                                                                                   12
                                                                                                                                                                                                                                                                                                                          (7)
\rightarrow permute([a, b, f]);
                                                              [[a, b, f], [a, f, b], [b, a, f], [b, f, a], [f, a, b], [f, b, a]]
                                                                                                                                                                                                                                                                                                                          (8)
> permute([a, b, c, d], 2);
                [[a, b], [a, c], [a, d], [b, a], [b, c], [b, d], [c, a], [c, b], [c, d], [d, a], [d, b], [d, c]]
                                                                                                                                                                                                                                                                                                                          (9)
\rightarrow choose([a, b, f]);
                                                                        [[], [a], [b], [a, b], [f], [a, f], [b, f], [a, b, f]]
                                                                                                                                                                                                                                                                                                                      (10)
> choose([a, b, c, d], 2);
                                                                                   [[a, b], [a, c], [a, d], [b, c], [b, d], [c, d]]
                                                                                                                                                                                                                                                                                                                     (11)
\rightarrow nops(choose([a, b, c, d], 2));
                                                                                                                                                      6
                                                                                                                                                                                                                                                                                                                      (12)
\rightarrow orderedLists := proc(S, k)
          local i, L : L := NULL :
          for i from 1 to nops(S) do
         L := L, seq(S[i], j = 1..k)
            od: RETURN(permute([L], k)) end;
orderedLists := proc(S, k)
                                                                                                                                                                                                                                                                                                                      (13)
              local i, L;
              L := NULL;
```

```
for i to nops(S) do L := L, seq(S[i], j = 1..k) end do;
        RETURN(combinat:-permute([L], k))
end proc
\rightarrow orderedLists([a, b, c, d], 2);
[a, a], [a, b], [a, c], [a, d], [b, a], [b, b], [b, c], [b, d], [c, a], [c, b], [c, c], [c, d], [d, a],
                                                                                                                                                                                                             (14)
         [d, b], [d, c], [d, d]
\rightarrow orderedLists([a, b, c, d, e, f, g, h, i, j], 2);
[[a, a], [a, b], [a, c], [a, d], [a, e], [a, f], [a, g], [a, h], [a, i], [a, j], [b, a], [b, b], [b, c],
                                                                                                                                                                                                            (15)
        [b,d], [b,e], [b,f], [b,g], [b,h], [b,i], [b,j], [c,a], [c,b], [c,c], [c,d], [c,e], [c,f],
        [c,g], [c,h], [c,i], [c,j], [d,a], [d,b], [d,c], [d,d], [d,e], [d,f], [d,g], [d,h], [d,i],
        [d, j], [e, a], [e, b], [e, c], [e, d], [e, e], [e, f], [e, g], [e, h], [e, i], [e, j], [f, a], [f, b],
        [f, c], [f, d], [f, e], [f, f], [f, g], [f, h], [f, i], [f, j], [g, a], [g, b], [g, c], [g, d], [g, e],
        [g, f], [g, g], [g, h], [g, i], [g, j], [h, a], [h, b], [h, c], [h, d], [h, e], [h, f], [h, g], [h, h],
        [h, i], [h, j], [i, a], [i, b], [i, c], [i, d], [i, e], [i, f], [i, g], [i, h], [i, i], [i, j], [j, a], [j, b],
        [j, c], [j, d], [j, e], [j, f], [j, g], [j, h], [j, i], [j, j]
\rightarrow permute(3, 2);
                                                     [[1, 2], [1, 3], [2, 1], [2, 3], [3, 1], [3, 2]]
                                                                                                                                                                                                             (16)
\rightarrow nops(permute(3, 0));
                                                                                                   1
                                                                                                                                                                                                             (17)
\rightarrow nops(permute(3, 1));
                                                                                                   3
                                                                                                                                                                                                             (18)
> nops(permute(3, 2));
                                                                                                   6
                                                                                                                                                                                                             (19)
> nops(permute(3,3));
                                                                                                   6
                                                                                                                                                                                                             (20)
> nops(choose(3,0));
                                                                                                   1
                                                                                                                                                                                                             (21)
> nops(choose(3, 1));
                                                                                                   3
                                                                                                                                                                                                             (22)
> nops(choose(3,2));
                                                                                                   3
                                                                                                                                                                                                             (23)
> nops(choose(3,3));
                                                                                                   1
                                                                                                                                                                                                             (24)
> permute([H, H, H, H, T, T], 5);
[H, H, H, H, T], [H, H, H, T, H], [H, H, H, T, T], [H, H, T, H, H], [H, H, T, H, T], [H, H, T, T]
                                                                                                                                                                                                             (25)
        H], [H, T, H, H, H], [H, T, H, H, T], [H, T, H, T, H], [H, T, T, H, H], [T, H, H, H, H], [T, H, H], [
        H, H, T, [T, H, H, T, H], [T, H, T, H, H], [T, T, H, H, H]
\rightarrow nops(permute(4,0));
                                                                                                   1
                                                                                                                                                                                                             (26)
> nops(permute(4, 1));
                                                                                                   4
                                                                                                                                                                                                             (27)
> nops(permute(4, 2));
                                                                                                  12
                                                                                                                                                                                                             (28)
```

```
> nops(permute(4, 3));
                                                 24
                                                                                                        (29)
> nops(permute(4, 4));
                                                 24
                                                                                                        (30)
\rightarrow nops(choose(4, 0));
                                                  1
                                                                                                        (31)
> nops(choose(4, 1));
                                                  4
                                                                                                        (32)
\rightarrow nops(choose(4, 2));
                                                  6
                                                                                                        (33)
\rightarrow nops(choose(4, 3));
                                                                                                        (34)
                                                  4
\rightarrow nops(choose(4, 4));
                                                  1
                                                                                                        (35)
> for i from 0 to 3 do
   S := choose(3, i);
   print(S);
   od
                                             S := [[]]
                                                [[]]
                                       S := [[1], [2], [3]]
                                          [[1], [2], [3]]
                                    S := [[1, 2], [1, 3], [2, 3]]
                                      [[1, 2], [1, 3], [2, 3]]
                                          S := [[1, 2, 3]]
                                                                                                        (36)
                                             [[1, 2, 3]]
                                                 10
                                                                                                        (37)
\rightarrow for i from 0 to 3 do
   S := numbperm(3, i);
   print(S);
   od:
                                                  1
                                                  3
                                                  6
                                                  6
                                                                                                        (38)
```